

#### RADIATION THERAPY

An Application of Linear Optimization

15.071x – The Analytics Edge

#### Cancer

- Cancer is the second leading cause of death in the United States, with an estimated **570,000 deaths** in 2013
- Over **1.6 million new cases** of cancer will be diagnosed in the United States in 2013
- In the world, cancer is also a leading cause of death –
   8.2 million deaths in 2012

### Radiation Therapy

- Cancer can be treated using radiation therapy (RT)
- In RT, beams of high energy photons are fired into the patient that are able to kill cancerous cells
- In the United States, about half of all cancer
   patients undergo some form of radiation therapy

## History of Radiation Therapy

- X-rays were discovered by Wilhelm Röntgen in 1895 (awarded the first Nobel Prize in Physics in 1901)
  - Shortly after, x-rays started being used to treat skin cancers
- Radium discovered by Marie and Pierre Curie in 1898 (Nobel Prize in Chemistry in 1911)
  - Began to be used to treat cancer, as well as other diseases



### History of Radiation Therapy

- First radiation delivery machines (linear accelerators) developed in 1940
- Computed tomography (CT) invented in 1971
- Invention of intensitymodulated radiation therapy (IMRT) in early 1980s







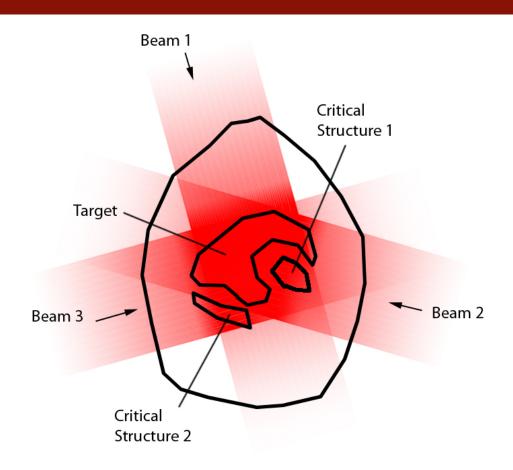
#### **IMRT**

- To reach the tumor, radiation passes through healthy tissue, and damages both healthy and cancerous tissue
- Damage to healthy tissue can lead to undesirable side effects that reduce post-treatment quality of life
- We want the dose to "fit" the tumor as closely as possible, to reduce the dose to healthy tissues

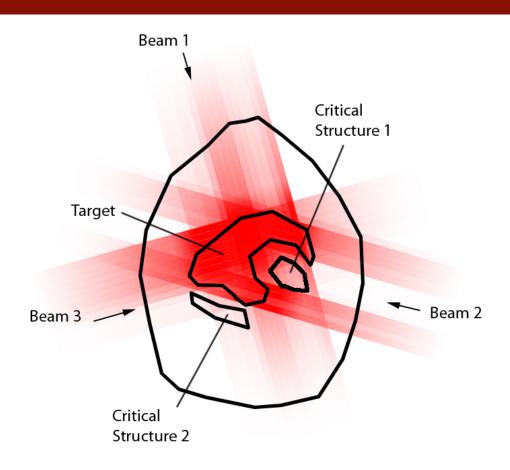
#### **IMRT**

- In IMRT, the intensity profile of each beam is non-uniform
- By using non-uniform intensity profiles, the threedimensional shape of the dose can better fit the tumor
- Let's see what this looks like

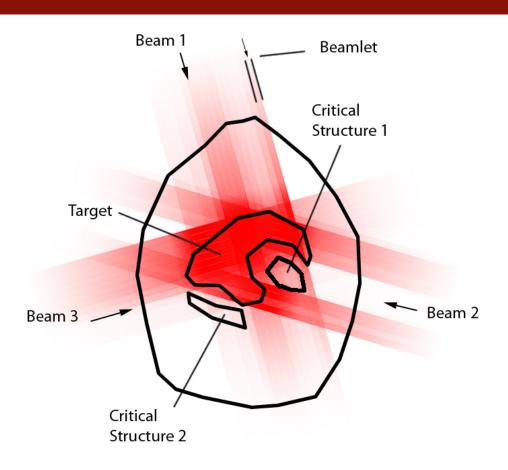
## Using Traditional Radiation Therapy



# Using IMRT



# Using IMRT



## Designing an IMRT Treatment

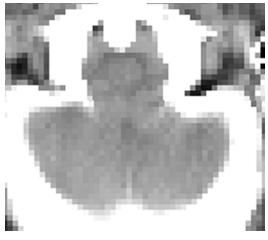
- Fundamental problem:
  - How should the beamlet intensities be selected to deliver a therapeutic dose to the tumor *and* to minimize damage to healthy tissue?

#### The Data

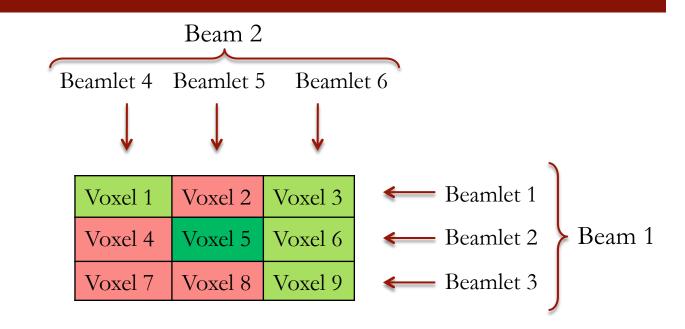
- Treatment planning starts from a CT scan
  - A radiation oncologist contours (draws outlines) around the tumor and various critical structures
  - Each structure is discretized into voxels (volume elements) – typically 4 mm x 4 mm x 4 mm
- From CT scan, can compute how much dose each beamlet delivers to every voxel







### Small Example – 9 Voxels, 6 Beamlets



Tumor

Spinal Cord

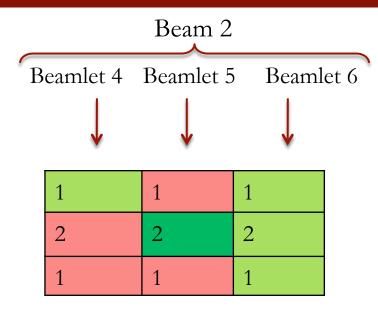
Other healthy tissue

- Minimize total dose to healthy tissue (spinal + other)
- Constraints: tumor voxels at least 7Gy (Gray), spinal cord voxel at most 5Gy

### Dose to Each Voxel – Beamlets 1, 2, 3

1	2	2	Beamlet 1	
1	2	2.5	← Beamlet 2	Beam 1
1.5	1.5	2.5	Beamlet 3	

### Dose to Each Voxel – Beamlets 4, 5, 6



## Small Example – The Model

1	2	2	← Beamlet 1
1	2	2.5	← Beamlet 2
1.5	1.5	2.5	← Beamlet 3

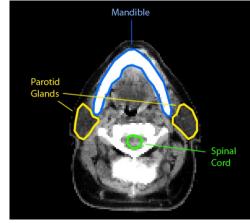
В	eamlet 4	Beamlet 5	Beaml	et 6
	1	1	1	
	2	2	2	
	1	1	1	

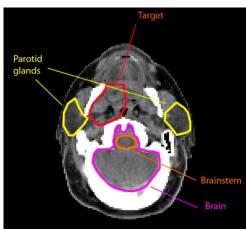
Decisions: X1, X2, X3, X4, X5, X6

Minimize 
$$(1+2)X_1 + (2+2.5)X_2 + 2.5X_3 + X_4 + 2X_5 + (1+2+1)X_6$$
  
 $2X_1 + X_5 \ge 7$   
 $X_2 + 2X_4 \ge 7$   
 $1.5X_3 + X_4 \ge 7$   
 $1.5X_3 + X_5 \ge 7$   
 $2X_2 + 2X_5 \le 5$   
 $X_1, X_2, X_3, X_4, Y_5, X_6 \ge 0$ 

## A Head and Neck Example

- We will test out this approach on a head-and-neck case
  - Total of 132,878 voxels
  - One target volume (9,777 voxels)
  - Five critical structures: spinal cord, brain, brain stem, parotid glands, mandible (jaw)
  - 5 beams; each beam ~60 beamlets (1cm x 1cm) for a total of 328 beamlets





#### Treatment Plan Criteria

- Dose to whole tumor between 70Gy and 77Gy
- Maximum spinal cord dose at most 45Gy
  - Significant damage to any voxel will result in loss of function
- Maximum brain stem dose at most 54Gy
- Maximum mandible dose at most 70Gy
- Mean parotid gland dose at most 26Gy
  - Parotid gland is a parallel structure: significant damage to any voxel does not jeopardize function of entire organ

### The Optimization Problem

minimize Total healthy tissue dose

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subject to 70\text{Gy} \leq \text{Dose} to voxel v \leq 77\text{Gy}, for all tumor voxels v,

Dose to voxel v \leq 45\text{Gy}, for all spinal cord voxels v,

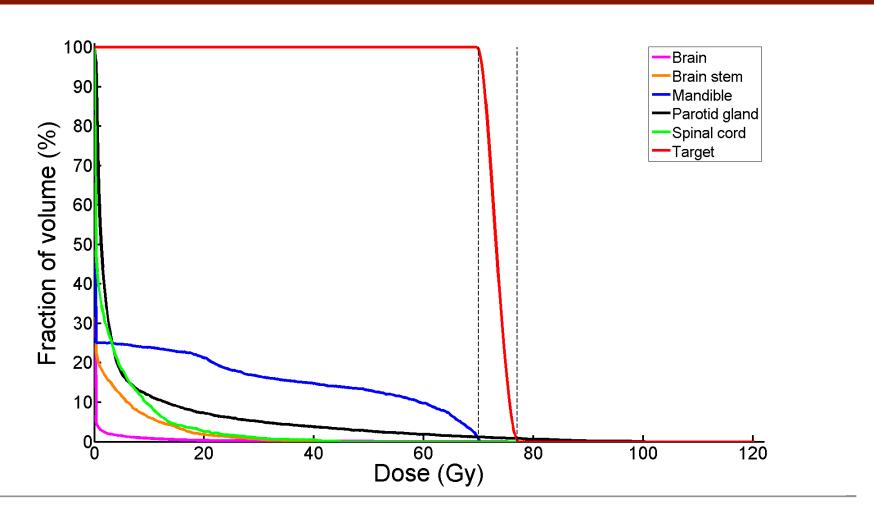
Dose to voxel v \leq 54\text{Gy}, for all brain stem voxels v,

Dose to voxel v \leq 70\text{Gy}, for all mandible voxels v,

\frac{\text{Total parotid dose}}{\text{Num. parotid voxels}} \leq 26\text{Gy},

w_b \geq 0, for all beamlets b.
```

#### Solution



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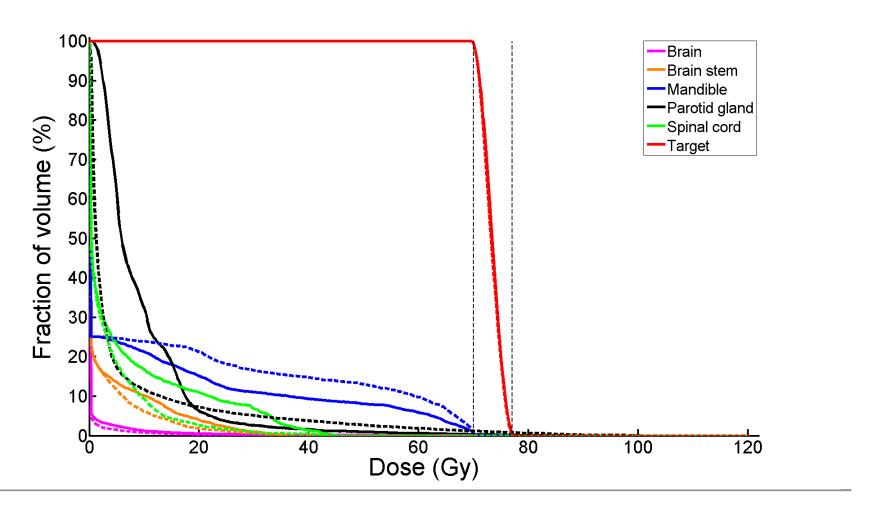
## Exploring Different Solutions

- Mean mandible dose was 11.3Gy how can we reduce this?
- One approach: modify objective function
  - Current objective is the sum of the total dose  $T_{\rm B} + T_{\rm BS} + T_{\rm SC} + T_{\rm PG} + T_{\rm M}$
  - Change objective to

$$T_{\rm B} + T_{\rm BS} + T_{\rm SC} + T_{\rm PG} + 10 \times T_{\rm M}$$

• Set mandible weight from 1 (current solution) to 10

#### New Solution



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### Sensitivity

- Another way to explore tradeoffs is to modify constraints
  - For example: by relaxing the mandible maximum dose constraint, we may improve our total healthy tissue dose
  - How much does the objective change for different constraints?

#### Shadow Prices

Organ	Highest shadow price
Parotid gland	0
Spinal cord	96.911
Brain stem	0
Mandible	7399.72

- · Parotid gland and brain stem have shadow prices of zero
  - Modifying these constraints is not beneficial
- Mandible has highest shadow price
  - If slight increase in mandible dose is acceptable, total healthy tissue dose can be significantly reduced

## IMRT Optimization in Practice

- Radiation machines are connected to treatment planning software that implements and solves optimization models (linear and other types)
  - Pinnacle by Phillips
  - RayStation by RaySearch Labs
  - Eclipse by Varian

#### Extensions

- Selection of beam angles
  - Beam angles can be selected jointly with intensity profiles using **integer optimization** (topic of next week)
- Uncertainty
  - Often quality of IMRT treatments is degraded due to uncertain organ motion (e.g., in lung cancer, patient breathing)
  - Can manage uncertainty using a method known as robust optimization

## Efficiency

- Manually designing an IMRT treatment is inefficient and impractical
- Linear optimization provides an *efficient* and *systematic* way of designing an IMRT treatment
  - Clinical criteria can often be modeled using constraints
  - By changing the model, treatment planner can explore tradeoffs

#### Clinical Benefits

- Ultimately, IMRT benefits the patient
  - In head and neck cancers, saliva glands were rarely spared prior to IMRT; optimized IMRT treatments spare saliva glands
  - In prostate cancer, optimized IMRT treatments reduce toxicities and allow for higher tumor doses to be delivered safely
  - In lung cancer, optimized IMRT reduces risk of radiation-induced pneumonitis