

**Problem 1.** Consider the merging problem in our PRAM discussion. Let  $A_1$  be the array (1, 17, 28, 29, 55, 61, 69, 80) and  $A_2$  be the array (10, 13, 25, 33, 38, 56, 72, 75). Give the content of array  $B_1$ .

**Problem 2.** Consider the sorting problem in EM. Let  $A$  be the input file of  $n$  integers (which is stored in  $O(n/B)$  blocks). Give an algorithm to produce  $O(n/M)$  files satisfying all the following requirements:

- Each file stores at most  $M$  integers of  $A$  in ascending order using  $O(M/B)$  blocks.
- All the files are mutually disjoint.
- The union of all the files is the set of integers in  $A$ .

Your algorithm must terminate in  $O(n/B)$  I/Os.

**Problem 3.** This question concerns the PRAM model. Suppose that we have already obtained a sorting algorithm  $\mathcal{A}$  finishing in  $f(n)$  steps when the number  $p$  of CPUs equals  $n$  (recall that  $n$  is the number of integers to sort). Consider now the scenario where  $p < n$ . Describe how to use  $\mathcal{A}$  to design an algorithm that finishes in  $O(\frac{n}{p} \cdot f(n))$  steps.

**Problem 4.** Give a PRAM algorithm that settles the sorting problem in  $O(\frac{n}{p} \log^2 n)$  steps.