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# **Controlling Self-Driving Race Cars with Deep Neural Networks**

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UNIVERSITY OF OSNABRÜCK

DEPARTMENT OF NEUROINFORMATICS

BACHELOR'S THESIS

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## *Abstract*

This Thesis will be written in the next two months, and I'm pretty scared about that.  
TODO: sobald der komplette text steht bei den Formeln auf die nicht referenziert wird die nummern weg machen (equation\*)

## *Preface*

This document was written as the author's bachelor thesis at the department of neuroinformatics at the University of Osnabrück during summer 2017 and is an original and independent work by the author Christoph Stenkamp.

Christoph Stenkamp  
Osnabrück, 29th August, 2017

## *Acknowledgements*

Thanks to my parents, Marie, my supervisors, and my friends...

*“There are no surprising facts, only models that are surprised by facts; and if a model is surprised by the facts, it is no credit to that model.”*

Eliezer Yudkowsky

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# List of Abbreviations

The abbreviations used throughout the work are compiled in the following list below. Note that the abbreviations denote the singular form of the abbreviated words. Whenever the plural forms is needed, an s is added. Thus, for example, whereas ANN abbreviates *artificial neural network*, the abbreviation of *artificial neural networks* is written ANNs.

<b>ANN</b>	<b>Artificial Neural Network</b>
<b>CNN</b>	<b>Convolutional (artificial) Neural Network</b>
<b>CPU</b>	<b>Central Processing Unit</b>
<b>DDPG</b>	<b>Deep Deterministic Policy Gradient - Network</b>
<b>DQN</b>	<b>Deep-Q-Network</b>
<b>GUI</b>	<b>Graphical User Interface</b>
<b>MDP</b>	<b>Markov Decision Process</b>
<b>POMDP</b>	<b>Partially Observed Markov Decision Process</b>

# List of Symbols

*For my friends, family, and especially Marie.*

## Chapter 1

# Introduction

"sollte etwa 10% der Gesamtarbeit ausmachen"

### 1.1 Motivation

Google's self-driving car, Tesla autopilot, die vision von Ubers autonomous taxis, ...

#### 1.1.1 Problem Domain

#### 1.1.2 Goal of this thesis

### 1.2 Research Questions

### 1.3 Reading Guidelines

### 1.4 noclue

As put forward by *Lex Fridman* in his MIT lecture "*Deep Learning for Self-Driving Cars*"<sup>1</sup> the tasks for self-driving cars can be sub-divided into the following categories:

- **Localization and Mapping**
- **Scene Understanding**
- **Movement Planning**
- **Driver State**

[rrt\* macht halt sowas von 3., end-to-end macht die kiste insgesamt nen bisschen anders]

<https://arxiv.org/pdf/1704.03952.pdf>

Semi-autonomous vehicle components: Radar, Visible-light-camera, LIDAR, infrared-camera, stereo vision, GPS/IMU, CAN, Audio

Localization and Mapping: eg. *file : ///C : /Users/Marie/Downloads/VISAPP2015145.pdf*

Scene Understanding/Object Detection: Scene Segmentation Network (SegNet) Movement Planning: Previously by stuff like RRT\* (optimization-based control), however reinforcement learning!

End-to-End: NVIDIA Paper

dass Reinforcement Learning ja eigentlich nicht so der beste approach ist

Normally when dealing with self-driving cars, there are countless additional issues, each making up a whole new challenge on their own, like wheather conditions

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<sup>1</sup>MIT 6.S094, course website: <http://selfdrivingcars.mit.edu/>

(snow, rain, fog), pedestrians, other cars, reflections, merging into ongoing traffic, ... we make it easier here.

Or, according to the Torcs-paper: The racing problem could be split into a number of different components, including robust control of the vehicle, dynamic and static trajectory planning, car setup, inference and vision, tactical decisions (such as overtaking) and finally overall racing strategy. With only a single car on the track, the overall problem can be formalised as a partially observable Markov decision processes.

→ Because we only consider the case of a single car on the track it definitely is a POMDP! seeee next chapter yay

## Chapter 2

# Reinforcement Learning

As the task at hand was not only to provide a reinforcement learning agent, but also to convert a game itself into something the agent can successfully play, I will in this chapter go into detail about reinforcement learning in general, giving insights on the specific approach chosen. The descriptions will be kept as general as possible at first, with detailed explanations following in the sections about specific algorithms.

### 2.1 Reinforcement Learning Problems

Machine Learning can mainly be subdivided into three main categories: Supervised Learning, Unsupervised Learning, and Semi-supervised learning. The first deals with direct classification or regression using labelled data which consists of pairs of datapoints with their corresponding category or value. In unsupervised learning, no such label exists, and the data must be clustered into meaningful parts without any knowledge, for example by grouping objects by similarity in their properties. What will be mainly considered in this thesis will be a certain kind of semi-supervised learning: *Reinforcement learning* (RL). In RL, instead of labels for the data, there is a *weak teacher*, which provides feedback on actions performed by the learner.

#### Markov Decision Processes

RL can be understood by means of a decision maker (*agent*) performing in an *environment*. The agent makes observations in the environment (its input), takes actions (output) and receives rewards. In contrast to the classical ML approaches, in RL the agent is also responsible for exploration, as he has to acquire his knowledge actively. Thus, a reinforcement learning problem is given if the only way to collect information about the *underlying model* (the environment) is by interacting with it. As the environment does not explicitly provide actions the agent has to perform, its goal is to figure out the actions maximizing its cumulative reward until a training episode ends.

In the classical RL approach, the environment is divided into discrete time steps. If that is the case, the environment corresponds to a *Markov Decision Process* (MDP). Formally, a MDP is a 5-tuple  $\langle S, A, P, R, \gamma \rangle$ , consisting of the following:

$S$  – set of states  $s \in S$

$A$  – set of actions  $a \in A$

$P(s'|s, a)$  – transition probability function from state  $s$  to state  $s'$  under action  $a : S \times A \rightarrow S$

$R(r|s, a)$  – reward probability function for action  $a$  performed in state  $s : S \times A \times S \rightarrow \mathbb{R}$

$\gamma$  – discount factor for future rewards  $0 \leq \gamma \leq 1$

In general, both the state transition function and the reward function may be indeterministic, meaning that neither reward nor the following state are in complete control of the decision maker. Because of that, only expected values are examinable, depending on the random distribution of states. Given both  $s$  and  $s'$  however, the reward is assumed to be deterministic. I will refer to the actual result of a state transition at discrete point in time  $t$  as  $s_{t+1}$  and to the result of the reward function as  $r_t$ . If no point in time is explicitly specified, it is assumed that all variables use the same  $t$ .

While an *offline learner* gets as input the problem definition in the form of a complete MDP, where the only task left is to classify actions yielding high rewards from actions giving suboptimal results, the task for an *online reinforcement learning* agent is a lot harder, as it has to learn the MDP itself via trial and error. In the process of reinforcement learning, the agent will encounter states  $s$  of the environment, performing actions  $a$ . The future state  $s_{t+1}$  of the environment may be indeterministic, but depends on the history of previous states  $s_0, \dots, s_t$  as well as the action of the agent  $a_t$ . It is assumed that the *Markov property* holds, which means that a state  $s_{t+1}$  depends only on the current state  $s_t$  and current action  $a_t$ :  $p(s_{t+1}|s_t, a_t) = p(s_{t+1}|s_0, a_0, \dots, s_t, a_t)$

Throughout interacting with the environment, the agent receives rewards  $r$ , depending on his action  $a$  as well as the state of the environment  $s$ . In many RL problems, the full state of the environment is not known to the agent, and it only perceives an observation depending on the environment:  $o_t := o(s_t)$ <sup>1</sup>. This is referred to as *partial observability*, and the corresponding decision process is a *partially observable MDP*. Additionally, the agent knows when a final state of the environment is reached, terminating the current training episode. For the agent, an episode therefore consists of observations, actions and rewards ( $\mathcal{S} \times \mathcal{A} \times \mathbb{R}$ ) until at time  $t_t$  some terminal state  $s_{t_t}$  is reached:

$$\text{Episode} := ((s_0, a_0, r_0), (s_1, a_1, r_1), (s_2, a_2, r_2), \dots, (s_{t_t}, a_{t_t}, r_{t_t}))$$

### Value of a state

In the process of reinforcement learning, the agent tries to perform as well as possible in the previously unknown environment. For that, it uses an action-policy  $\pi$ , depending on some parameters  $\theta$ . The policy maps states to actions, which in the case of a *deterministic* policy leads to  $\pi_\theta(s) = a$ . Though a stochastic policy is possible, it will not be considered for now<sup>2</sup>. As the agent does not have supervised data on which actions are the ground truth, it must learn some kind of measure for the value of being in a certain state or performing a certain action. The commonly used measure for the value of a state when using policy  $\pi$  can be calculated by the immediate reward this state gives, summed with the expected value of the discounted future reward the agent will achieve by continuing to follow its policy  $\pi$  from this

<sup>1</sup>From now on, when the state of the environment is meant, it will be explicitly referred to as  $s_e$ , while  $s$  is reserved for the agent's observation of the environment  $o(s_e)$

<sup>2</sup>It is obvious, that the result of both the reward function and the state transition function depend on  $\pi$ . To be explicit about that, I will refer to a reward dependent on  $\pi$  as  $r^\pi$  and a state transition dependent on  $\pi$  as  $s^\pi$ . If state or reward depends on an explicit action instead, I refer to it as  $r^a$  and  $s^a$ . Whenever not necessary for clarity, I will also drop  $\pi$ 's dependence on  $\theta$ .



state on:

$$V^\pi(s_t) := \mathbb{E}_{s \sim \rho^\pi} \left[ \sum_{t'=t}^{t_t} (\gamma^{t'-t} * r_{t'}^\pi) \right] \quad (2.1)$$

As the future rewards depend on future states it can, as already mentioned, only be talked about the expected Value depending on the actual state distribution. This distribution depends on the agents policy, but may still be indeterministic<sup>3</sup>. The discounted state visitation distribution, which assigns each state a probability of visiting it according to policy  $\pi$ , is denoted  $\rho^\pi$ .

The actual, underlying Value of a state  $V^*(s)$  could accordingly be defined as the value of the state when using the best possible policy, which corresponds to the maximally achievable reward starting in state  $s_t$ :

$$V^*(s_t) := \max_{\pi} V^\pi(s_t)$$

While *passive learning* simply tries to learn the Value-function  $V^*$  without the need of action selection, an *active reinforcement learner* tries to estimate a good policy that can actually reach those high-value states. If the value of every state is known, then the optimal policy can be defined as the one achieving maximal value for every state of the MDP:  $\pi^* := \operatorname{argmax}_{\pi} V^\pi(s) \forall s \in \mathcal{S}$ . Knowing what an optimal policy does, the definition of the value  $V^\pi(s)$  2.1 can be written recursively as

$$\begin{aligned} V^\pi(s_t) &= \mathbb{E}_{s \sim \rho^\pi} \left[ \sum_{t'=t}^{t_t} (\gamma^{t'-t} * r_{t'}^\pi) \right] \\ &= r_t^\pi + \gamma * \mathbb{E}_{s \sim \rho^\pi} \left[ \sum_{t'=t+1}^{t_t} (\gamma^{t'-t} * r_{t'}^\pi) \right] \\ &= r_t^\pi + \gamma * V^\pi(s_{t+1}) \end{aligned} \quad (2.2)$$

This relation is known as the *Bellman Equation*, which allowed for the birth of dynamic programming<sup>4</sup>.

### Value of an action

While the definition of a state-value is useful, it alone does not help an agent to perform optimally, as neither the successor function  $P(s'|s, a)$ , nor the reward function  $R(r|s, a)$  are known to the agent. While so-called *model-based* reinforcement learning (also referred to as *Certainty Equivalence*) tries to learn both of those explicitly to reconstruct the entire MDP, *model-free* agents use a different measure of quality: the *Q-value*. It represents the expected value of performing action  $a_t$  in a state  $s_t$ , afterwards following the policy  $\pi$ :

$$Q^\pi(s_t, a_t) := \mathbb{E}_{s \sim \rho^\pi} [r_t^{a_t} + \gamma * V^\pi(s_{t+1}^{a_t})] \quad (2.3)$$

<sup>3</sup>That is one of the reasons to discount future rewards: The agent cannot be fully sure if it actually reaches the states it strives for. Also, using the discounted reward hopefully helps making the agent perform good actions as quickly as possible.

<sup>4</sup>Dynamic programming is another solution strategy for MDPs. In contrast to RL however, it requires the complete MDP as input to find an optimal policy, which cannot be given in many relevant situations.

With the Q-value  $Q^*$  of the optimal policy accordingly

$$\begin{aligned} Q^*(s_t, a_t) &= \mathbb{E}_{s \sim \rho^\pi} [r_t^{a_t} + \gamma * V^*(s_{t+1}^{a_t})] \\ &= \max_{\pi} Q^\pi(s_t, a_t) \end{aligned}$$

For the Q-value, the Bellman equation holds as well: If the correct Q-value under policy  $\pi$ ,  $Q^\pi(s_{t+1}, a_{t+1})$ , was known for all possible actions at time  $t$ , then the optimal action is the one maximizing the sum of immediate reward and corresponding Q-value. This is because of the definition of Bellman's *Principle of Optimality*, which states that “An optimal policy has the property that whatever the initial state and initial decision are, the remaining decisions must constitute an optimal policy with regard to the state resulting from the first decision” (quote [3]). Thanks to the principle of optimality, the value of our decision problem at time  $t$  can be re-written in terms of the immediate reward at  $t$  plus the value of the remaining decision problem at  $t + 1$ , resulting from the initial choices:

$$Q^\pi(s_t, a_t) = \mathbb{E}_{s \sim \rho^\pi} [r_t^{a_t} + \gamma * Q^\pi(s_{t+1}, \pi(s_{t+1}))] \quad (2.4)$$

As the Value of a state is defined as the maximally achievable reward from that state, the relation between  $Q$  and  $V$  can be expressed as

$$V(s_t) = \max_{a_t} Q(s_t, a_t) \quad (2.5)$$

### Quality of a policy

Any agent's goal is to find a policy that can follow the trajectory of the state distribution with the highest expected reward. If the actual Q-value for each action of each state is known, then the optimal policy can be defined as the one taking the optimal action in each state:

$$\pi^* = \operatorname{argmax}_a Q^*(s, a) \forall s, a \in \mathcal{S} \times \mathcal{A} \quad (2.6)$$

This policy guarantees maximum future reward at every state. Note however, that finding  $\operatorname{argmax}_a Q(s, a)$  is only easily possible if  $\mathcal{A}$  is discrete and finite (more on that later).

As for the actual performance of a policy, a useful measure is the *performance objective*  $J(\pi)$ , which stands for the cumulative discounted reward from the start state using the respective policy. To measure the performance objective, it is necessary to integrate over the whole state space  $\mathcal{S}$  with each state  $s$  weighted by its distribution due to  $\pi$ . As only non-stochastic policies are considered here, integration over the action space  $\mathcal{A}$  is not necessary. The integral can, as shown by [14], be expressed by the expectation of the Value of states following the distribution  $s \sim \rho^\pi$ :

$$\begin{aligned} J(\pi) &= \int_{\mathcal{S}} \rho^\pi(s) V^\pi(s) ds \\ &= \mathbb{E}_{s \sim \rho^\pi} [V^\pi(s)] \\ &= \mathbb{E}_{s \sim \rho^\pi} [Q^\pi(s, \pi(s))] \end{aligned} \quad (2.7)$$

We assume for now that once an agent knows  $Q^*$ , it can simply follow the policy that always takes the action yielding the highest value for every state (the *greedy policy*)<sup>5</sup>.

<sup>5</sup>in fact, the agent cannot act only according to the greedy policy, as it will need to *explore* the environment first. The problem of exploration will be considered later in this thesis.

Thus, the goal of a model-free RL agent is to get a maximally precise estimate of  $Q^*$ . To do that, it does not need to explicitly learn the reward- and transition function, but instead can model the Q-function directly. In RL settings with a highly limited amount of discrete states and actions, the respective Q-function estimate can be specified as a lookup table, whereas for areas of interest, the function is estimated using a nonlinear function approximator. The agent's approximation of  $Q^\pi$  will be denoted  $\hat{Q}^\pi$ .

Throughout exploration of the environment, the agent collects more information about it, continually updating its estimate  $\hat{Q}^\pi$ . For that, it uses samples from its episodes of interacting with the environment.

## 2.2 Temporal difference Learning

Throughout the process of reinforcement learning, the agent continually improves its estimates  $\hat{Q}^\pi$  of  $Q^\pi$ . The loss of its current estimate could be seen as the squared difference  $(\hat{Q}^\pi - Q^\pi)^2$ , however as the agent has no knowledge of  $Q^\pi$ , it needs some way of approximating it. For that, a Q-learning agent performs *iterative approximation*, using the information about the environment, to continually update its estimates of  $Q^\pi$ . Using the recursive definition of a Q-value given in the Bellman equation 2.4 allows for a technique called *temporal difference learning*[15]: At time  $t + 1$ , the agent can compare its estimate of the Q-function of the last step,  $\hat{Q}^\pi(s_t, a_t)$ , with a new estimate using the new information it gained from the environment:  $r_{t+1}$  and  $s_{t+1}$ . Because of the newly gained information from the underlying MDP, the new estimate will be closer to the actual function  $Q^\pi$  than the original value:

$$\hat{Q}^\pi(s_t, a_t) = r_t + \mathbb{E}_{s \sim \rho^\pi} [\gamma * \max_{a_{t+1}} \hat{Q}^\pi(s_{t+1}, a_{t+1})] \quad (2.8)$$

$$\approx r_t + \gamma * r_{t+1} + \mathbb{E}_{s \sim \rho^\pi} [\gamma^2 * \max_{a_{t+2}} \hat{Q}^\pi(s_{t+2}, a_{t+2})] \quad (2.9)$$

Keeping in mind that  $\hat{Q}^\pi$  is only an estimator of the  $Q^\pi$ -values of the underlying model, it becomes clear that equation 2.9 is closer to the actual  $Q^\pi$ , as it incorporates more information stemming from the model itself.

In temporal difference learning, the mean-squared error of the *temporal difference* from this Bellman equation,  $r_t + \gamma * Q(s_{t+1}, a_{t+1}) - Q(s_t, a_t)$ , gets minimized via iterative approximation. Even though  $r_t + \gamma * \hat{Q}^\pi(s_{t+1}, a_{t+1})$  also uses an estimate, it contains more information from the environment, and is thus a *more informed guess* than  $\hat{Q}^\pi(s_s, a_s)$ . That makes it reasonable to substitute the unknown  $Q^\pi(s_{t+1}, a_{t+1})$  by  $\hat{Q}^\pi(s_{t+1}, a_{t+1})$ .

It is noteworthy, that each update of the Q-function using the temporal difference will affect not only the last prediction, but all previous predictions.

### SARSA

The new knowledge about the environment can be incorporated in two different ways. For the first method, the agent samples a full tuple of  $\langle s_t, a_t, r_t, s_{t+1}, a_{t+1} \rangle$  from its interaction with the environment, to then calculate the temporal difference error in non-terminal states as  $TD := (r_t + \gamma * \hat{Q}^\pi(s_{t+1}, a_{t+1})) - \hat{Q}^\pi(s_t, a_t)$ . This algorithm of calculating the temporal difference error is known as SARSA, and it is an example of *on-policy* temporal difference learning. In on-policy learning, the

agent uses its own policy in every estimate of the Q-value. If the policy of the agent is not stochastic, this method can however lead to it getting stuck in local optima.

## Q-learning

In contrast to SARSA stands the *Q-learning* algorithm [18]. Q-learning does not need to sample the action  $a_{t+1}$ , as it calculates the Q-update at iteration  $i$  using the best possible action in state  $s_{t+1}$ <sup>6</sup>.

As the previous definition of Q-values was only correct in non-terminal states, a case differentiation must be introduced for terminal- and non-terminal states. In the following,  $y_t$  will stand for the updated estimate of the Q-value at  $t$ , sampling the necessary states, rewards and actions from interaction with the environment, almost resulting in the formula found in [10]. To express its dependence on the policy  $\pi$ , it will be superscripted by it:

$$y_t^\pi = \begin{cases} r_t & \text{if } t = t_t \\ r_t + \gamma * \max_{a'} \hat{Q}^\pi(s_{t+1}, a') & \text{otherwise} \end{cases} \quad (2.10)$$

The temporal difference error for time  $t$  is accordingly defined as

$$TD_t := y_t^\pi - \hat{Q}^\pi(s_t, a_t) \quad (2.11)$$

A Q-learning agent must thus observe a snapshot of the environment, consisting of the following input:  $\langle s_t, a_t, r_t, s_{t+1}, t + 1 == t_t \rangle$  (where the last element is the information if state  $s_{t+1}$  was a terminal state). That information is then used to calculate the temporal difference error.

In very limited settings, using the above error straight away allows for the update-rule in simple Q-learners: Consider an agent, specifying its approximation of the Q-function (his *model*) with a lookup-table, initialized to all zeros. It is proven by [19] that for finite-state Markovian problems with nonnegative rewards the update-rule for the Q-table (with  $0 \leq \alpha \leq 1$  as the learning rate)

$$\hat{Q}_{i+1}^\pi(s_t, a_t) \leftarrow \alpha * (r_t^{a_t} + \gamma * \hat{Q}_i^\pi(s_{t+1}, a_{t+1})) + (1 - \alpha) * \hat{Q}_i^\pi(s_t, a_t) \quad (2.12)$$

converges to the optimal  $Q^*$ -function, making the greedy policy  $\pi^*$  optimal<sup>7</sup>. Note, that the same update rule as for the Q-function could be performed for the V-function.

In contrast to SARSA, Q-learning is an *off-policy* algorithm, meaning that the policy it uses in its evaluation of the Q-value is not necessarily the one it actually uses: When calculating the temporal difference error, the agent considers Q-values  $\hat{Q}^{\pi_{greedy}}(s, a)$ , based on  $\pi_{greedy}(s) = \operatorname{argmax}_{a'} \hat{Q}(s, a')$ , as better approximation of the real action-value function  $Q^\pi(s, a)$ . Therefore, it learns about  $\pi_{greedy}$ , which is to always take the action promising maximum Value. Because following the deterministic  $\pi_{greedy}$  does not allow for *exploration*, this is not the policy the agent actually pursues.

When using off-policy algorithms with  $\pi$  as the policy we learn about and  $\beta$  as the policy we act upon, our performance objective  $J(\pi)$  (equation 2.7) must change,

<sup>6</sup>A slight deviation from this is *double-Q-learning*, an architecture I will go into detail about later on.

<sup>7</sup>Of course the agent will need some kind of exploration technique first, more on that later

as it must incorporate that while the value of a state is calculated using our deterministic  $\pi$ , the distribution of states follows from stochastic policy  $\beta$ :

$$\begin{aligned} J_\beta(\pi) &= \int_{\mathcal{S}} \rho^\beta(s) V^\pi(s) ds \\ &= \mathbb{E}_{s \sim \rho^\beta} [Q^\pi(s, \pi(s))] \end{aligned} \quad (2.13)$$

The process of reinforcement learning consists of two steps: *policy evaluation*, where the agent evaluates its current policy according to the knowledge gained from the environment, and based on that *policy improvement*. In the standard Q-learning considered here, those steps are interleaved, leading to a form of *generalized policy iteration*: the Q-learner learns its action value-function and its policy simultaneously. After updating its Q-function estimate via the temporal difference error, the agent updates its policy to be a *soft* version of the greedy policy  $\pi_{i+1}(s) := \arg\max_{a'} Q^{\pi_i}(s, a') \forall s \in \mathcal{S}$ , while keeping a mechanism allowing for exploration. Learning with this approach is however generally limited:  $\arg\max_{a'} Q(\cdot, a')$  can only easily be found in settings where the action space  $\mathcal{A}$  is finite and discrete, as it requires a global maximization over all possible actions. In a later section, I will go into detail about another architecture which does circumvents those problems by splitting up policy evaluation and policy improvement explicitly.

As there are also relevant situations in which discrete actions  $\mathcal{A} \subseteq \mathbb{N}^n$  are sufficient, I will stick to those situations for now. Also in these circumstances, a Q-learner using tables as Q-function-approximator reaches its limits really fast, as the state space  $\mathcal{S}$  may also be continuous or simply too big for a table to be useful. If that is the case, an update rule like in equation 2.12 becomes irrelevant quickly. Instead, a better idea is to use the definition of the temporal difference error to define a loss function, which is to be minimized throughout the process of RL. A commonly used loss-function is the *L2-Loss*, which allows for gradient descent, updating the parameters of the Q-function into the direction of the newly acquired knowledge. In this case, it may also be useful to calculate the loss of a batch of temporal differences simultaneously, which will be elaborated later on in more detail. The L2-Loss for batch *batch* with model-parameters  $\theta_i$ , making up the policy  $\pi_{\theta_i}$  is thus defined as the following:

$$L_{batch}(\theta_i) := \mathbb{E}_{s,a,r \sim batch} \left[ (y_{batch}^{\pi_{\theta_i}} - \hat{Q}_{batch}^{\pi_{\theta_i}}(s, a))^2 \right] \quad (2.14)$$

## 2.3 Q-Learning with Neural Networks

To understand this section, basic knowledge on how *Artificial Neural Networks* (ANNs) work and what they do is presupposed. Specifically, knowledge of *Convolutional Neural Networks* (CNNs)[21], mainly used in image processing, is required. As mentioned before, it is (in theory) not only possible to use a Q-table to estimate the  $Q^\pi$ -function, but any kind of function approximator. Thanks to the universality theorem, it is known that ANNs are an example of such<sup>8</sup>. The defining feature of ANNs

<sup>8</sup>For a proof of the universality theorem, I refer to chapter 4 of Michael A. Nielsen's book "Neural Networks and Deep Learning", Determination Press, 2015. The referred chapter is available at <http://neuralnetworksanddeeplearning.com/chap4.html>

in comparison to other Machine Learning techniques is their ability to store complex, abstract representations of their input when using a *deep* enough architecture.

### 2.3.1 Deep Q-learning

The reason to use neural function approximators instead of a simple Q-table approach for reinforcement learning problems is easy to see: While for a Q-table the states and actions of the Markov Decision Process must be discrete and very limited, this is not the case when using higher-level representations. If the agent's observation of a state of the game is high-dimensional (like for example an image), the chance for an agent to observe the exact same observation twice is extremely slight. Instead, an Artificial Neural Network can learn a higher-level representation of the state, grouping conceptually similar states, and thus generalize to new, previously unseen states. It is no surprise that the success of *Deep-Q-Networks* started its journey shortly after the introduction of CNNs, which are able to learn abstract representations of similar images and by now used in countless Computer Vision Applications.

*Deep-Q-Network (DQN)* refers to a family of off-policy, online, active, model-free Q-learning algorithms for discrete actions using Deep Neural Networks. Using ANNs as function approximators for the agent's model of the environment requires a Loss function depending on the Neural Network parameters, specified by  $\theta$ . These weights correspond to the parameters of the  $\hat{Q}$ -function of the agent. As previously mentioned, this kind of Q-learning defines its policy straight-forward, depending on the  $\arg\max_a$  of the Q-function. I will therefore replace the dependence of  $\hat{Q}^\pi(s, a)$  on  $\pi$  by a dependence on its parameters:  $\hat{Q}(s, a; \theta_i)$ . The update rule in Deep Networks depends on the gradient with respect to its loss,  $\nabla_{\theta_i} L(\theta_i)$ . As the DQN-architecture only considers discrete actions, there is one change that can be made in the definition of the Q-function: instead of giving both the state  $s$  and the action  $a$  as input to the network, in DQNs only the state is input to the network, with the network returning a separate Q-value for each actions  $a \in \mathcal{A}$ . This speeds up the inference, as one forward step is enough to calculate the Q-value of all actions in a certain state.

While there are attempts to use Artificial Neural Networks for Q-learning as early as 1994[12], some key components of modern Deep-Q-Networks were missing, leading to satisfactory performance only in very limited settings. In standard online RL tasks, the update step minimizing the loss specified in 2.14 is performed not for a batch, but for each time  $t$  right after the observation occurred to the agent. In those situations, the current parameters of the policy determine the next sample the parameters are trained on. It is easy to see, that those consecutive steps of MPDs tend to be correlated: It is very likely, that the maximizing action of time  $t$  is similar to the one at  $t + 1$ . Consecutive steps of an MDP are not representative of the distribution the whole underlying model. ANNs require independent and identically distributed samples, which is not given if the samples are generated sequentially. As shown by [7], the update using gradient descent is prone to feedback loops and thus oscillation in its result, thus never converging to an optimal  $Q^\pi$ -function.

It was not until *Deepmind's* famous papers in 2013[9] and 2015[10], that those issues were successfully addressed. One important step when using ANNs instead of Q-tables is to perform stochastic gradient descent using minibatches. In every gradient descent step of the Neural Network, neither only the last temporal difference error  $TD_t$  is considered (leading to oscillations), nor the entire sequence  $TD_0, \dots, TD_t$



(because batch updates are not time-efficient in ANNs). Instead, as usual when dealing with ANNs, minibatches are sampled from the set of all observations. When performing the gradient descent step, the weights for the target  $y_t$  are fixed, making the minimization of the temporal difference error a well-defined optimization problem (with clear-cut target values as in supervised learning) during the learning step.

The two important innovations introduced in the DQN-architecture were the use of a *target network* as well as the technique of *experience replay*, which in combination successfully solved the problem of oscillating and non-converging action-value functions, even though still no formal mathematical proof of convergence is given.

### Experience Replay

As mentioned above, learning only from the most recent experiences biases the policy towards those situations, limiting convergence of the Q-function. To address this issue, the DQN uses an experience replay memory: Every percept of the environment (the  $\langle s_t, a_t, r_t, s_{t+1}, t+1 == t_t \rangle$  - tuple) is added to a limited-size memory of the agent. When then performing the learning step, the agent samples random minibatches from this memory to perform learning on a maximally uncorrelated sample of experiences. In the original definition of DQN, those minibatches are drawn uniformly at random, while as of today, better techniques for sampling those minibatches are available[13], increasing the performance of the resulting algorithm significantly.

### Target Networks

During the training procedure, the DQN-algorithm uses a separate network to generate the target-Q-values which are used to compute the loss (eq. 2.14), necessary for the learning step of every iteration. The intuition behind why that is necessary is, that the Q-values of the *online network* shift in such a way, that a feedback loop can arise between the target- and estimated Q-values, shifting the Q-value more and more into one direction. To lessen the risk of such feedback loops, the DQN algorithm introduced the use of a second network for calculating the loss: the *target network*. This is only periodically updated with the weights of the online network used for the policy, which reduces the risk of correlations in the action-value  $Q_t$  and the corresponding target-value  $y_t$  (see equation 2.10).

The use of these two techniques leads to the Q-learning update rule, using the loss as put forward in [10]:

$$L_i(\theta_i) = \mathbb{E}_{\langle s_t, a_t, r_t, s_{t+1} \rangle \sim U(D)} \left[ \left( r + \gamma * \max_{a_{t+1}} \hat{Q}(s_{t+1}, a_{t+1}; \theta_i^-) - \hat{Q}(s_t, a_t; \theta_i) \right)^2 \right] \quad (2.15)$$

Where  $i$  stands for the current network update iteration,  $\theta_i$  for the current weights of the target network (updated every  $C$  iterations to be equal to the weights of the online network  $\theta_i$ ),  $Q(\cdot, \cdot; \theta)$  for the Q-value dependent on a ANN using the weights  $\theta$ ,  $\mathbb{E}[\cdot]$  for the expected value in an indeterministic environment,  $D$  for the contents of the replay memory of length  $|D|$  containing  $\langle s_t, a_t, r_t, s_{t+1} \rangle$ -tuples, and  $U(\cdot)$  for a uniform distribution.

As is the case with the experience replay mechanism, the usage of a target network was improved as well – modern algorithms do not perform a hard update of the target network every  $C$  steps, but instead perform *soft target network updates*, where every iteration, the weights of the target network are defined as  $\theta_i^- := \theta_i * \tau + \theta_i^- * (1 - \tau)$  with  $0 < \tau \ll 1$ , first introduced in [8]. This improves the stability of the algorithm

even more.

As a pseudocode for the DQN-architecture is already stated in the corresponding paper [10], listing it again here would be superfluous. Instead, I try to compare the pseudocode with the code of my actual implementation using Python and Tensorflow in appendix A.1. In the first two pages of the appendix, the necessary definitions of agent and network structure are introduced, before in page 38 there is the actual comparison between the pseudocode and its correspondences in the actual code, namely the `__init__`, `inference` and `q_learn`-functions of the model-class. Note that the blue lines of the pseudocode correspond to difference from the original DQN in favor of later improvements.

### 2.3.2 Double-Q-Learning

It is well known that Q-learning tends to ascribe unrealistically high Q-values to some action-state-combinations. The reason for this is, that to estimate the value of a state  $s_j$  it includes a maximization step over estimated action values  $Q(s_j, a)$ , where naturally, overestimated values are preferred over underestimated values. It is not possible that Q-value-estimates are completely precise: estimation errors can occur due to environmental noise, inaccuracies in function approximation (consider a flexible ANN trained on only a small sample so far - the ANN will overfit by covering all samples precisely. This overfitting leads to steep curves, over- or underestimating many values in between) and many other issues. Because Q-learning uses in every estimate of the value of a state  $s_j$  the maximum Q-value of state  $s_{j+1}$ , only those estimates are propagated where the noise of the estimation is in a positive direction. Because of that, state  $s_{j-1}$  will have the accumulated upward noise from both state  $s_j$  and  $s_{j+1}$ , and so forth. This leads to unrealistically high action-values. While this would not constitute a problem if all Q-values would be uniformly overestimated, [5] showed that its very likely that the Q-value  $Q(s_j, a)$  for only some actions  $a$  is overestimated – which changes the result of the  $\arg\max_a$  operation and thus leads to biased policies. They also show that the drop in DQN performance correlates with this overestimation of actions.

The solution suggested by [5] is called *Double-Q-learning*. In its original definition without using Neural Networks as function approximators, a double-Q-learner learns two value functions in parallel, by letting each experience update only one of the two value functions at random. For each update then, one function is used to determine the greedy policy, while the other is used to determine the value of this policy<sup>9</sup>. The authors proved that the lower bound for the overestimation of action-value,  $\max_{a'} Q^\pi(s, a') - V^*(s)$ , is  $> 0$  for the standard Q-learning update rule, whereas it is 0 in the case of DoubleQ. Additionally they showed that these overestimations are indeed harmful by showing the superiority of a DoubleQ-learner in comparison with a normal Q-learner.

*Deep-Double-Q-Learning (DDQN)* takes the Double-Q idea to the existing framework of Deep-Q-learning: Overestimations are reduced by decomposing the *max*-operation into *action selection* and *action evaluation*. Instead of introducing a second value function, DDQN re-uses the target-network of the DQN architecture in place

<sup>9</sup>“In DoubleQ, we still use the greedy policy to select actions, however we evaluate how good it is with another set of weights”. The intuition behind that is, that the probability of both value-functions always over-estimating the same actions is basically zero.



of the second value function. Although online network and target network are not fully decoupled, experiments showed that it provides a good candidate for independent action evaluation, without the need of additional functions. The technique of DDQN is thus to still use the online network to choose an action (evaluate the greedy policy according to the online network), but the target network to generate the target Q-value for that action (to estimate its value, instead of the max-operation in DQN). As shown by [5], DDQN improves over DQN both in terms of value accuracy and in terms of the actual quality of the policy.

When using Double-Q-Learning, the target-value of the calculation of the temporal difference error ( $y_t$  from equation 2.10 must thus be re-defined as

$$y_t^\pi = \begin{cases} r_t & \text{if } t = t_f \\ r_t + \gamma * Q(s_{t+1}, \operatorname{argmax}_{a'} Q(s_{t+1}, a'; \theta_i^-); \theta_i^-) & \text{otherwise} \end{cases} \quad (2.16)$$

It can be seen in appendix A.1 how small the actual change to normal DQN is: The only difference is the usage of the target network in line 21 (marked in blue).

### 2.3.3 Dueling Q-Learning

In many situations encountered during Q-learning, the value of all possible actions  $a_t$  in a state  $s_t$  is almost equal. Consider a simulated car, driving with full speed towards a wall, already so close that breaking or steering can't stop the car from driving into the wall. As all actions will end in the episode ending by the car hitting the wall, all actions will have roughly the same Q-value.

The idea of the *dueling architecture* [17] for DQN is to learn the action-state-value function more efficiently. For that, it splits up the Network into a *value stream* and separate *advantage streams*. As mentioned earlier, though the ANN resembles the  $\hat{Q}(s, a)$ -function, the actions are not input to the network, but instead it outputs  $|\mathcal{A}|$  Q-values, one for each action. A *Dueling Double Deep-Q-Network (DDDQN)* works by splitting an early layer of its corresponding network in half. One of the resulting streams is the value-stream, which results in one value, intuitively corresponding to the Value ( $\hat{V}_{s_t}$ ) of a state  $s_t$ , irrespective of the action that can be taken in this state. The other stream is the advantage stream, which has as output  $|\mathcal{A}|$  values, standing for the *Advantage* ( $A$ ) of taking a certain action in this state – it can be seen as a relative measure of the importance of each action. The relation between  $Q$ ,  $V$  and  $A$  is the following:

$$Q(s, a) = V(s) + A(s, a)$$

In the very last layer of the ANN those two streams are combined again, such that a DDDQN also outputs one Q-value for each action. Thanks to this, any DDQN can be transformed into a DDDQN by simply changing the structure of the used ANN. It is important to mention however, that the last layer can't simply calculate  $V(s) + A(s, a)$  – If that was done, then the network could simply set the V-stream to a constant, negating any advantage gain in splitting them up in the first place. However, as explained in equation 2.5, it holds that  $\operatorname{argmax}_{a'} Q(s, a') = V(s)$  – when using deterministic policies, then the value of the state corresponds to the Q-value of the best action that can be taken in this state. Therefore, it must be the case that the *argmax*-action has an advantage of zero. This can be used to calculate the  $Q(s, a)$  using the value-stream and the advantage-stream according to the following equation (where  $\theta$  corresponds to the shared weights,  $\theta^A$  to the weights specific to the

advantage-stream and  $\theta^V$  to those specific to the Value-stream):

$$Q(s, a; \theta, \theta^A, \theta^V) = V(s; \theta, \theta^V) + (A(s, a; \theta, \theta^A) - \max_{a'} A(s, a', \theta, \theta^A))$$

Actually, during testing it turned out that normalizing the advantage not with respect to the best action, but with respect to the average of all actions,  $\frac{1}{|\mathcal{A}|} \sum_{a'} A(s, a'; \theta, \theta^A)$  lead to better stability. By splitting up into separate advantage- and valuestream and combining the two streams in a fully-connected layer using the formula stated above, the authors achieved far better performance than their predecessor, DDQN, on the same dataset [17].

The reason to split into two streams is obvious: In the learning step of a DQN, the derivative is taken with respect to difference in the expected Q-value of an action and the better estimate of that Q-value. In normal DQNs, the network can thus only update the parameters responsible for one of its outputs. A DDDQN learns more effectively, as it learns a shared value of multiple actions: A temporal difference in one Q-value likely changes the value-stream of the network, which also changes the Q-value of other actions. Thanks to this, learning generalizes better across actions, without any changes to the underlying reinforcement learning algorithm. As shown by the authors [17], the difference is especially drastic in situations where many actions have similar outcomes.

In appendix A.1, I listed an exemplary source code of the implementation of an agent using python and tensorflow. The agent stands alone without an environment, and some crucial parts of it, like an implementation of its memory, are missing. However, all aspects mentioned in the previous sections are found in it, which is the algorithm of the actual Q-learning as described above and in [5], as well as the computation graph of the network using precisely the DDDQN-architecture as described above and in [17]. The last page of it (page 38) consists of a comparison of the Pseudocode of the DDDQN (as found in [10], with the changes from [5] and [8] incorporated in and marked blue), where each line of the pseudocode (to the left) corresponds precisely to the respective line of the actual python-code (to the right).

## 2.4 Policy Gradient Techniques

*Policy Gradient* (PG) techniques are in principle a far more straight-forward approach to reinforcement learning than temporal difference-methods like Q-learning. The idea behind PG techniques is really simple: The policy  $\pi_\theta(a|s) = \mathbb{P}[a|s; \theta]$  of an agent is explicitly modeled using a differentiable function approximator, like a neural network with weights  $\theta$ . There is no need to approximate the value-function of states or actions explicitly. The quality of the policy is again measured by its performance as in equation 2.13.

Before continuing to explain PG techniques, it makes sense to define another measure of the quality of an action: The *advantage*. The advantage will be what PG methods optimize for, and it can be defined analogously to the value of a state in equation 2.1, with the difference that this time, as we do not explicitly model the value of following states, we can only calculate it after having measured all of the

respective rewards from the environment:

$$A_t := \sum_{t'=t}^{t_t} (\gamma^{t'-t} * r_{t'}) \quad (2.17)$$

To use the policy gradient, the agent must calculate the advantage of every state it visited so far, to then set this advantage as the gradient of the output of its policy function of the corresponding state, to then train the network using backpropagation with respect to this gradient. If the reward was positive, gradient *ascent* will make the network more likely to produce this action in this state, and if the gradient was negative, it will lead to gradient *descent*, discouraging the network to repeat this action in the given state. Thus, the network will learn to repeat actions giving high rewards and to avoid those with negative rewards.

This may sound unintuitive at first, because there is no specific loss function the ANN can optimize for. However in fact, using the gradient with respect to the advantage corresponds to the loss  $\sum_t A_t \log p(a_i|s_i)$  – If  $A_t$  is positive, we want to increase the probability of action  $a_t$  for state  $s_i$ , and decrease it otherwise.

The main problem of purely using this approach is however the huge amount of exploration that is needed – the agent does not have any knowledge about what states are good or bad, but only increases the probability of individual actions that turned out to have a good score. Because of this, it can find good policies only by chance, after millions of iterations. If the agent knew the value of a state, it could optimize its policy in the direction of actions that it knows produce a high-valued state. For that, the policy network must get the gradient information of the action from something estimating this value-function, giving rise to *actor-critic architectures*.

### 2.4.1 Actor-Critic architectures

The technique introduced in the previous sections is a direct adaption of the Q-learning algorithm [15][18], adapted for higher-level function approximators. Standard Q-learning is a kind of *generalized policy iteration*, where the policy evaluation and policy improvement happen in the same step. The algorithm learns via temporal differences the state-action value  $Q^{\pi_{greedy}}(s, a)$  for the states it encountered with its current policy  $\pi$ . It then updates  $\pi$  to a soft version of that greedy policy:  $\pi_{i+1}(s) := \text{soft}(\text{argmax}_a Q^{\pi_{greedy}}(s, a) \forall s \in \mathcal{S})$ , where the *soft*-function ensures appropriate exploration. Learning the Q-function and the policy simultaneously is however generally limited:  $\text{argmax}_a Q(\cdot, a)$  can only easily be found in settings where the action space  $\mathcal{A}$  is finite and discrete, as it requires a global maximization over all possible actions. While discretizing the action space is possible, it gives rise to the *curse of dimensionality*, especially when the discretization is fine grained. An iterative optimization process like the *argmax*-operation would thus likely be intractable.

However in a lot of scenarios, the action space is not discrete, but continuous:  $A \subseteq \mathbb{R}^n$ . In such situations, the alternative is to move the policy into the *direction of the gradient of Q*. For that, it is necessary to model the policy explicitly with another function

approximator. This gives rise to *actor-critic* architectures, where both policy and Q-function are explicitly modeled: The *critic* corresponds again to a Bellman-function-approximator, using temporal differences to estimate the action-value  $Q^\pi(s, a)$ <sup>10</sup>. In contrast to the previous approach however, the policy is now explicitly modeled by the *actor*. In the case of a stochastic policy, it would be represented by a parametric probability distribution  $\pi_\theta(a|s) = \mathbb{P}[a|s; \theta]$ , however here we only consider the case of deterministic policies  $a = \pi_\theta(s)$ , which takes the necessity of averaging over all possible actions when calculating its performance objective according to equation 2.7 or equation 2.13. Note however, that using deterministic policies will (again) lead to the necessity of off-policy algorithms, as a purely deterministic policy does not allow for adequate exploration of state-space  $\mathcal{S}$  or action-space  $\mathcal{A}$ . Thus, to measure the performance of our policy, we must use function 2.13, which averages over the state distribution of our behaviour policy  $\beta \neq \pi$ .

To train both actor and critic, actor-critic algorithms rely on a version of the *policy gradient theorem*, which states a relation between the gradient of the policy and the gradient of its performance function. The idea behind actor-critic policy gradient algorithms is accordingly to adjust the parameters  $\theta$  of the policy in the direction of the performance gradient  $\nabla_\theta J(\pi_\theta)$ , as moving uphill into the direction of the performance gradient corresponds to maximizing the global performance of the policy<sup>11</sup>. The DPG technique is the policy gradient analogue to Q-learning: It learns a deterministic greedy policy in an off-policy setting, following a trajectory of states due to a noisy version of the learned policy.

### Deterministic Policy Gradient

The idea in the *Deterministic Policy Gradient (DPG)* technique is to use a relation between the gradient of the (deterministic) policy (represented by the actor), and the gradient of the action-value function Q. The existence of a relation is easy to see, because as introduced in equation 2.13, the performance of our policy  $\pi$  is measured using Q.

The *off-policy deterministic policy gradient theorem*, put forward in [14], states the following relation between the gradient of the performance objective of a policy  $J(\pi)$  (see equation 2.13) and the gradients of the policy-function  $\pi$  and the action-value function Q.

$$\begin{aligned} \nabla_\theta J_\beta(\pi_\theta) &\approx \int_{\mathcal{S}} \rho^\beta(s) \nabla_\theta \pi_\theta(a|s) Q^\pi(s, a) ds \\ &= \mathbb{E}_{s \sim \rho^\beta} \left[ \nabla_\theta \pi_\theta Q^\pi(s, \pi_\theta(s)) \right] \\ &= \mathbb{E}_{s \sim \rho^\beta} \left[ \nabla_\theta \pi_\theta(s) \nabla_a Q^\pi(s, a) \Big|_{a=\pi_\theta(s)} \right] \end{aligned} \quad (2.18)$$

There are two important things about this relation: first, it can be seen that the policy gradient does not depend on the gradient of the state distribution. Second, the approximation drops a term that depends on the action-value gradient,  $\nabla_\theta Q^\pi(s, a)$ . Since the position of the optima are however preserved, the term can be left out, making the approximation no less useful. Both claims are shown in [14].

<sup>10</sup>In that, it corresponds precisely to the previous approach. However, as we now allow for a continuous action-space  $\mathcal{A}$ , the network cannot return multiple Q-values at once, for each action  $a \in \mathcal{A}$ . Instead, the actions must also be inputs to the critic, which then outputs one  $Q(s, a)$ -value.

<sup>11</sup>The original policy gradient, introduced in [16], assumes on-policy learning with a stochastic policy. However, to derive the stochastic policy gradient, one must integrate over the whole action-space, making its usage less efficient and requiring more training than the DPG, introduced here.

The practical implication of this relation is the following:

When updating the policy, its parameters  $\theta_{i+1}$  are updated in proportion to the gradient  $\nabla_{\theta} J(\pi_{\theta})$ . In practice, each state suggests a different gradient, making it necessary to take the expectation w.r.t. the state distribution  $\rho^{\beta}$ :

$$\theta_{i+1} = \theta_i + \alpha * \mathbb{E}_{s \sim \rho^{\beta}} [\nabla_{\theta} J(\pi_{\theta})]$$

The deterministic policy gradient theorem (2.18) shows that to improve the performance of the policy, it makes sense to move it into the direction of the gradient of  $Q$  – where the gradient of  $Q$  can be decomposed into the gradient of the action-value with respect to the actions, and the gradient of the policy with respect to its parameters:

$$\theta_{i+1} = \theta_i + \alpha * \mathbb{E}_{s \sim \rho^{\beta}} \left[ \nabla_{\theta} \pi_{\theta}(s) \nabla_a Q^{\pi_i}(s, a) \Big|_{a=\pi_{\theta}(s)} \right]$$

In other words, to maximize the performance of the policy, one can re-use the gradient of those actions leading to maximal  $Q$ -values. In practice, the true function  $Q^{\pi}(s, a)$  is unknown and must be estimated.

The off-policy deterministic actor-critic algorithm learns a deterministic target policy  $\pi_{\theta}(s)$  from trajectories generated by an arbitrary stochastic policy,  $\beta(a|s) = \mathbb{P}[a|s]$ . For that, it uses an actor-critic architecture: The critic estimates the  $Q$ -function using a differentiable function approximator, using  $Q$ -learning as explained in the sections above, with the weights specified as  $w$ . The actor updates the *policy* parameters  $\theta$  in the direction of the gradient of  $Q$  (instead of maximizing it globally as in the sections above<sup>12</sup>). Note that for the update of the policy parameters, only the gradient w.r.t. the weight of the actions as input of the  $Q$ -functions are relevant, not the trained weights of the approximator  $Q^w$  itself. Figure 2.1 visualizes the idea behind the algorithm graphically.

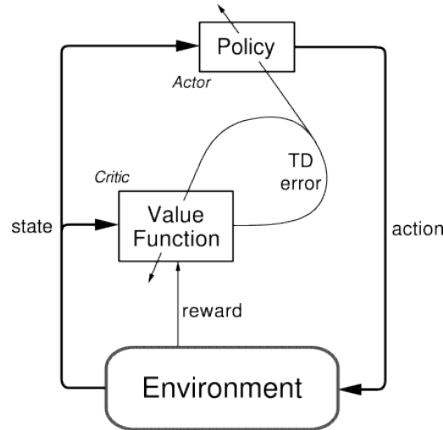


FIGURE 2.1: The actor-critic architecture. Reprinted from [11].

Using the above knowledge, one can derive the *off-policy deterministic actor critic* algorithm. In the first step of this algorithm, the critic calculates the temporal difference error to update its own parameters like in previous sections, and then the actor

<sup>12</sup>“The critic estimates the action-value function while the actor ascends the gradient of the action-value-function” (quote [14])

updates its parameters in the direction of the critic's action-value gradient:

$$TD_i = \mathbb{E}_{s,a,r} [(r_t + \gamma * Q^{w_i}(s_{t+1}, \pi_\theta(s_{t+1}))) - Q^{w_i}(s_t, a_t)] \quad (2.19)$$

$$w_{i+1} = \mathbb{E}_{s,a} [w_i + \alpha_w * TD_i \nabla_w Q^w(s_t, a_t)] \quad (2.20)$$

$$\theta_{i+1} = \mathbb{E}_{s,a} [\theta_i + \alpha_\theta * \nabla_\theta \pi_\theta(s_t) \nabla_a Q^w(s_t, a_t)|_{a=\pi_\theta(s)}] \quad (2.21)$$

With  $\alpha_w$  and  $\alpha_\theta$  as the learning-rates of the critic and the actor, respectively.

As stated by [14], these algorithm may have convergence issues in practice, due to a bias introduced by approximating  $Q^\pi(s, a)$  with  $Q^w(s, a)$ . It is thus important, that the approximation  $Q^w(s, a)$  is *compatible*, preserving the true gradient  $\nabla_a Q^\pi(s, a) \approx \nabla_a Q^w(s, a)$ . This is the case when the gradients are orthogonal, and  $w$  minimizes  $MSE(\theta, w)$ . However, the necessary conditions are approximately fulfilled when using a differentiable critic that finds  $Q^w(s, a) \approx Q^\pi(s, a)$ .

### Deep DPG

The *Deep DPG Algorithm* is an off-policy actor-critic, online, active, model-free, deterministic policy gradient algorithm for continuous action-spaces. The basic idea behind *Deep DPG (DDPG)*[8] is to combine the ideas of the DQN (section 2.3.1) with the architecture and learning rule using the deterministic policy gradient. For that, they also use parameterized deterministic actor function  $\pi_\theta(s) = a$ , as well as a critic function  $Q^w(s, a)$ . As the algorithm is also off-policy, it will learn the policy  $\pi_{\theta_{\text{target}}}$ , while following a trajectory arising through another, stochastic policy  $\beta$ . This policy will again be a *soft* version of the learned policy  $\pi$  that allows for adequate exploration:  $\beta := \text{soft}(\pi)$ .

The update of the critic is performed analogously to the Q-value approximator in the Deep-Q-Network architecture. A minibatch of  $\langle s_t, a_t, r_t, s_{t+1}, t = t_t \rangle$ -tuples are sampled from a replay memory of limited size, to then perform Q-learning via temporal differences (see 2.14 and 2.15). An obvious difference to the Q-learning in the above sections is however, that not the greedy  $\argmax_{a'} Q(s, a')$ -policy is used in the determination of the targetvalue, but the agent's own parameterized policy  $\pi_\theta(s)$ . Just like in Deep-Q-Learning, it is necessary to use target networks to ensure convergence of Q – in fact, Lillicrap et. al. [8] were the first to use the previously mentioned soft target updates.

The update of the actor then follows the deterministic policy gradient theorem from equation 2.18: Its estimation of the policy gradient bases on the minibatch-samples used in the critic. For that, it calculates the expectation of the action-gradients it adopted from the critic network. This expectation is an approximation of its policy gradient, allowing the actor to perform a stochastic gradient ascent step to optimize its performance objective.

In practice, it turned out that the usage of target networks for both actor and critic is necessary to ensure stability of the algorithm, such that in practice, there are four different networks: the actors  $Q(s, a; \theta^Q)$  and  $Q(s, a; \theta^{Q^-})$  as well as the critics  $\pi(s; \theta^\pi)$  and  $\pi(s; \theta^{\pi^-})$ . Incorporating all those changes leads to the following pseudocode snippet of the agent's learning step, adopted from [8]:

Target-value of the critic:

$$y_t := \begin{cases} r_t & \text{if } t = t_t \\ r_t + \gamma * Q(s_{t+1}, \pi(s_{t+1}; \theta^{\pi^-}); \theta^{Q^-}) & \text{otherwise} \end{cases} \quad (2.22)$$



Loss the critic minimizes:

$$L_i(\theta_i^\pi) := \mathbb{E}_{\langle s_t, a_t, r_t, s_{t+1} \rangle \sim U(D)} \left[ \left( y_t - Q(s_t, a_t; \theta^Q) \right)^2 \right] \quad (2.23)$$

Sampled policy gradient the actor maximizes for:

$$\nabla_{\theta^\pi} J_\beta(\pi_\theta) \approx \mathbb{E}_{\langle s_t, a_t, r_t, s_{t+1} \rangle \sim U(D)} \left[ \nabla_a Q(s_t, \pi(s_t); \theta^Q) \nabla_{\theta^\pi} \pi(s_t; \theta^\pi) \right] \quad (2.24)$$

The correspondences of this ANN implementation and the correspondences of the general definitions can easily be seen: Equations 2.22 and 2.23 correspond to definitions 2.19 and 2.20, whereas equation 2.24 corresponds to equation 2.21.

For a complete code of the DDPG-implementation, I refer to appendix A.2. Analogously to the DQN-agent, an exemplary source code of the implementation of an agent with a DDPG-model can be found there, using python and tensorflow. The agent stands alone without an environment, and some crucial parts of it, like an implementation of its memory, are missing. On page 41, there is again a comparison of the pseudocode (as provided in [8]) and the correspondences in actual-python code, where each line of the of the pseudocode (to the left) corresponds precisely to the respective line of the actual python-code (to the right).

## 2.5 Exploration techniques

There is one main difference between supervised learning and reinforcement learning, which I mentioned right at the beginning of this chapter: in RL, the only way to collect information about the environment is by interacting with it. In supervised learning it is no problem to shuffle the dataset beforehand, giving the learner i.i.d. samples, which are sure to be representative about the dataset. In RL however, this is not possible: Consider the situation where the agent drives a car around a track – as long as the agent doesn't drive the car well enough, it will probably not reach high speeds, and will thus learn nothing about situations in which it drives at high speeds. Another problem which was also mentioned before is that so far, only deterministic policies  $\pi(s) = a$  were considered. It is obvious that in practice, purely using deterministic policies leads to a complete lack of *exploration* of the state space  $\mathcal{S}$  of the MDP: Once the agent found one path to a terminal state, it will continue *exploiting* this path, which almost guarantees a suboptimal solution. In order to explore the full state space instead of sticking with the first local optimum found, a stochastic, non-greedy policy is necessary.

The two algorithms considered here were both variants of Q-learning, which is an off-policy algorithm. In practice that means that the agent learned about some greedy, deterministic policy while following another policy, which I said was a *noisy* version of that greedy policy. A noisy version helps ensuring adequate exploration. The big advantage of off-policy algorithms is thus, that the problem of exploration can be treated independently of the learning algorithm – whatever the mechanism for exploration will be, it is easy to incorporate it in both of the explained algorithms by letting it implement the previously mentioned *soft*( $\pi$ ) method, which takes as input a greedy, deterministic policy and yields a version of it that accounts for adequate state space exploration.

In the following subsection, I will start with exploration techniques for discrete actions, before then explaining methods that can be used in the case of continuous action spaces  $\mathcal{A}$ .

### 2.5.1 Exploration for discrete action-spaces



## Chapter 3

# Related work

[as mentioned before, there are two levels in the thesis - on the abstract level, the aim is to build a good agent for self-driving cars. On the practical level, it is still one specific simulation of a game, and one at first has to make the given game a RL problem, before you can even talk about trying to solve that. To show how that is normally done, there is the first section. In the second section I will then talk about successful approaches of self-driving cars in reality. That is at first subdivided into real-life and games. Our game is (like so many others) supposed to work as a bridge between real-life and games. As for that, I will also talk about what data is normally available, ...

### 3.1 Reinforcement Learning Frameworks

[hier zuerst noch ne kurze zusammenfassung, und das bild mit der environment-agent metaphor!] Gym/Universe Torcs schreiben dass die Arcade Learning Environment (Bellemare et al., 2013 aus dem Dueling) zu Gym wurde (I guess) torcs: im DDPG-paper steht "Torcs has previously been used as a testbed in other policy learning approaches (Koutnik et al., 2014b). "!!!!!!!!!!!!!! fußnote dass ich auch im code nen evaluator für ddpd hab der gym und pendulum swingup nutzt

In the previous chapter, I outlined the general structure of a reinforcement learning problem. In summary, it consists of agent and environment, where the environment is discretized into timesteps and only partially observed by the agent (POMDP). Each timestep, the agent gets an observation of the environment's state (making up its *internal state* and a scalar reward, and chooses an action to return to the environment. A graphical description of this interaction is depicted in figure 3.1.

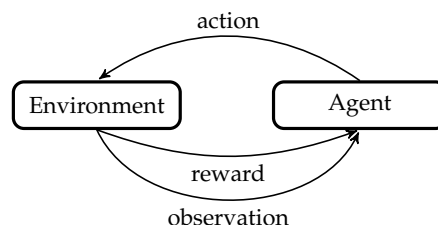


FIGURE 3.1: Interaction between agent and environment in RL

When developing RL agents, it is not enough to create algorithm, but also to have a specification of agent environment that allows for a dataflow as described above. The original Deep-Q-Network [9] as well as its follow-ups [5][17] trained their agents on several ATARI games using the *Arcade Learning Environment (ALE)* [2]. The ALE

was developed with the intention to evaluate the generality of several AI techniques, especially general game playing, reinforcement learning and planning. The important contribution of [2] was to provide a testbed for any kind of agent, by providing a simple common interface to more than a hundred different tasks. The ALE consists of an Atari-Simulator as well as a game-handling layer, which transformed all of the included Atari-games to a standard reinforcement learning problem. Doing that, it provided the accumulated score so far (corresponding to the reward), the information whether game ended (indicating the end of a training episode), as well as a  $160 \times 210$  2D array of 7-bit pixels (corresponding to the agent's observation). As the game screen does not correspond to the internal state of the simulator, the ALE corresponds to a POMDP. The possible input to the simulation consists of 18 discrete actions.

Environments with discrete actions only are however severely limited, and most of the interesting real-world applications, as for example autonomous driving, require however real-valued action spaces. The test scenarios for the Deep-DPG algorithm consisted thus of a number of simulated physics-tasks, using the MuJoCo physics environment.

Both of the above mentioned environments are by now, among many others, merged into the *OpenAI gym* environment [4]. The OpenAI gym<sup>1</sup> is created as a toolkit, helping reinforcement learning research by including a collection of benchmark problems with a common interface. The idea is to provide consistent, standardized environments, such that algorithms are easy to benchmark. In that respect, their goal was to provide the reinforcement-learning-pendant of a labeled dataset, such as ImageNet. Aside the previously mentioned ALE as well as a number of physics tasks using the MuJoCo physics-engine, the openAI gym contains the boardgame Go, two-dimensional continuous control tasks (*Box2D games*), a 3D-shooter by the name of *Doom*, and several other tasks. These tasks are varied in their complexity, input and output: some of them use low-dimensional state representations consisting of only a four-dimensional vector of scalars, while others use a 2D-pixel image of RGB colors.

The goal of openAI gym is to be as convenient and accessible as possible. For that, one of their design decisions was to make a clear cut between agent and environment, only the latter of which is provided by OpenAI. The exemplary sourcecode found in algorithm 1, taken from <https://gym.openai.com/docs>, outlines the ease of creating an agent working in the gym framework. The code outlines how the general dataflow between agent and environment usually takes place: After a reset, the environment provides the first *observation* to the agent. Afterwards, it is the agent's turn to provide an action. Even though not featured in this easy example, the action is performed by usage of the observation. Once an agent has calculated the action and provided it to the environment, it can perform another simulation step, returning  $\langle observation, reward, done, info \rangle$ , which is a tuple consisting of another observation of the environment's state, a scalar reward, the information if the episode is finished and it is time to reset the environment, as well as some information for debugging, typically not used in the final description of an agent. In the remainder of this work, I will refer to this dataflow as a baseline on how the interaction of environment and agent should look like.

It is worth noting, that the openAI gym is not even

---

<sup>1</sup><https://gym.openai.com>

**Algorithm 1** Interaction with the openAI gym environment

---

```

import gym
env = gym.make('CartPole-v0')
for i_episode in range(20):
    observation = env.reset()
    for t in range(100):
        env.render()
        print(observation)
        action = env.action_space.sample()
        observation, reward, done, info = env.step(action)
        if done:
            print("Episode finished after {} timesteps".format(t+1))
            break

```

---

Name	Paper/Link	Trained on Game	Used as inputs	Used as reward	Furhter distinctivenesses
Tensorkart	Link	Mariokart	Y	Z	only pretraining
original DDPG	[8]	Torcs	vision	bla	ne
original DDPG	[8]	Torcs	lowdim	bla	ne
Thatguy	irgendowonmedium	Torcs	vision	besser	ne
NVIDIA	paperlink	real data	vision	bla	ne

## 3.2 Self-driving cars

### 3.2.1 real-life

Nvidias deep-drive RRT\* Tesla

#### available data in real-life

Lidar <https://arxiv.org/pdf/1704.03952.pdf>

### 3.2.2 games

Leon wollte hier ne Tabelle von verschiedenen games und den respective inputs die sie nutzen...!

Tensorkart hier in den fußnoten die ganzen non-scientific quellen wie tensorkart undso

Das Aufteilen von autonomous driving into the subcomponents, wie bei der vorlesung von Julian... oder, as quoted by TORCS-Paper: "The racing problem could be split into a number of different components, including robust control of the vehicle, dynamic and static trajectory planning, car setup, inference and vision, tactical decisions (such as overtaking) and finally overall racing strategy"

DDPG auf torc hat übrigens im pixel-case nen sehrsehr ähnlichen punktestand wie im low-dimensional case (1840 vs 1876 im best case, -393 vs -401 im average case).

TORCS!!!!UNBEDINGT ERWÄHNEN DASS die geschrieben haben dass TORCS ein POMDP ist!!

## Chapter 4

# Program Architecture

[irgendwas von wegen "general to specific"]

### 4.1 Characteristics and design decisions

As stated in chapter 3.1, the usual framework for solving reinforcement learning tasks is fairly rigid. However, the task of this work differed in some respects from the usual implementation of a reinforcement learning agent, which led to the necessity of differing from the usual framework in numerous situations. In the following sections, I will provide an overview of the difference between this project and other work in the reinforcement learning domain. Furthermore, I will discuss some of the design decisions that found their way into the final version of the program as well as challenges that occurred during its implementation and their respective solution. For that, I will explain general principles in the first section of this subchapter, and go into detail about some of the specific details about the implementation in the subsequent section.

#### 4.1.1 Characteristics of this project

There are several differences in this project than in known literature in the reinforcement learning community. The most important difference to the agents presented in chapter 2 is, that those are developed as general-purpose problem solvers, with the intention to solve any arbitrary task given to them. In this approach, that is not the case – the goal is to solve the specific, given game. This allows in principle to incorporate expert knowledge of the task domain, to for example forbid certain combinations of the output or to use specific types of exploration, which are specifically useful in this scenario. Specifically, the game which is supposed to be played is a racing game, which has implications in several domains, for example making the standard  $\epsilon$ -greedy approach for exploration much worse as in many other domains. Next to that, the game which is supposed to be played is, in contrast to games solved in openAI's gym-environment (3.1), live. While the game could in theory be manually paused for every RL step, it is worth trying to let the agent run "live", such it runs fluently and its progress can manually be inspected. Another challenge was the fact, that the game is coded in a programming language for which no efficient deep learning architectures exist, which led to the necessity of a proprietary communication between the environment and its agent.

The fact that there is only one game, which is supposed to be learned, also extended the entire problem domain: While usually the focus of developing RL agents can lie purely on the agent, assuming that the environment and consequently its definition of state/observation and reward is fixed, the focus of this work was to learn this one game as well as possible – in other words it is also necessary to test

what a useful definition of observation or reward looks like. Many of the subsequent design decisions are made with the idea in mind, that it must be as easy as possible to compare different agents using a unique combination of state-definition, reward-definition, model and exploration technique.

Furthermore, the question of how important supervised pretraining is addressed in this thesis. For that, the game must provide a way of recording manual actions and their corresponding state and to record that in a way, that a learner can read it and train on this data. The natural questions arising are how good an agent relying purely on supervised training is in comparison to others, as well as if there is a way to combine pre-training with reinforcement training.

### 4.1.2 Characteristics of the game

The given game is a simple but realistic racing simulation. As of now, it consists of one car driving one track. While it is certainly necessary to implement additional AI drivers or different tracks, no such thing is considered in the current implementation. The main focus of the given simulation lies on realistic physics. There are important differences to simpler racing games, like many of those implemented for the Atari-console, on which the original DQN was tested.

The input expected from an agent consists of three continuous actions: The *throttle* increases the simulated motor-torque, which leads faster rotation of the tires and thus applying forward force to the car, which then accelerates general case. The *brake* simulates a continuous brake force slowing down the rotation of the tires. It is not possible to finish a while constantly accelerating as much as possible without breaking. It is important to note that slip and spin is also handled in the game: While the rotation of the tires can be accelerated or decelerated fairly abrupt due to their small mass, the car itself has a higher mass and thus more inertia, which forbids abrupt changes in movement. As the cars are rigidly attached to the car, they lose grip on the street, which lessens the impact of consequent forces applied to the tires. The last command an agent must output is the *steering*, which turns the front tires of the car, leading the car applying force to the respective side the tires steered towards.

It is the task of an agent to provide commands for the values of throttle, brake and steering, which are continuous in their respective domains:  $throttle \in [0, 1]$ ,  $brake \in [0, 1]$  and  $steer \in [-1, 1]$ . Of course, as is the general case in reinforcement learning problems, the agent does not know the implications of its actions in advance but must learn them via trial and error. It should however also be kept in mind that the agent provides those actions *to the car*, and that the car must be seen as part of the environment as well, as the actions do not have a reliable impact on its behaviour. For instance, if the car is moving at fast paces, hitting the brake will not lead to an abrupt stop, as the car's inertia still applies a forward force. Also, the impact of the steering changes with the movement of the car. For example, the turning circle of the car has a much slower radius in smaller speeds. Another consequence of the realism of the physics implemented in this simulation is the fact that simultaneous braking and steering at high velocities has almost no effect: Because of the high speed, the car has a strong forward force. That leads in combination with the braking to the front tires slipping a lot, which reduces the impact on forces applied to them on the actual car – it will not follow the direction of the steering but continue its forward pace determined by the stronger force, namely the inertia.

The track itself is a circular course with a combination of unique curves, requiring the car to steer left as well as right. Along every point of the course, there are three different surfaces with different frictions – the street itself provides the most grip,

while the off-track surface is far more slippery. Between the track-surface and the off-track-surface there the curb of the track which manifests as a small bump with separate friction properties. At a distinct distance from the middle of the track there is a wall which cannot be traversed.

### The game as a reinforcement learning problem

As detailed in chapter 2, reinforcement learning agents are solvers for (possibly only Partially Observable) Markov Decision Processes with unknown transition relations. In other words, for the agent to successfully learn how to operate in an unknown environment, this environment must correspond precisely to a tuple of  $\langle S, A, P, R, \gamma \rangle$  (details explained in section 2.1). Because in this simulation only the case of a single agent without any other cars on the track is considered, the racing problem can be formalized as a Markov Decision Processes with a similar reasoning than Wymann et al. [20, chapter 4] put forward for TORCS. As is the general case in simulations, while every update-step of the physics aims to simulate a continuous process, those updates must be discretized in the temporal domain. As however both agent and environment run live, the temporal discretization of the agent can not always correspond to that of the environment if an update-step in the agent takes longer than in the environment. To put that into numbers, the fixed timestep for the environment's physics is at 500 updates per second, while the agent discretizes to maximally 20 actions per second.

As mentioned in the previous section, the action space required by the agent is continuous with  $\mathcal{A} \subset \mathbb{R}^3$ .

The environment's state is a linear combination of different factors, as for example the car's speed, absolute position, current slip-values and much more. While certainly finite, it consists of many high-dimensional values  $\mathcal{S}_e \subset \mathbb{R}^N$ . Because of certain factors in the implementation of the environment itself, the environment is indeterministic<sup>1</sup>. As can in principle be argued that the environment's state corresponds to all information stored in the game's section of the computer's RAM, the game trivially fulfills the markov property. As the environment is only a single-agent system, the transition function of the environments follows directly from state and action:  $\mathcal{S}_e \times \mathcal{A} \rightarrow \mathcal{S}_e$ .

In the basic definition of the game, there is no formal definition of a reward returned by the environment. While it could in theory be argued, that the inverse of the time needed to complete a lap could be taken as the reward, it is obvious that it is infeasible due to many reasons: Finishing one lap takes several seconds, which means there are easily hundreds of iterations between the start state and this final state. Next to the obviously arising *credit assignment problem*, the chance of an agent even getting to such a final state, without all intermediate rewards equal to zero, is practically zero. Instead, it makes sense to give more dense rewards. As mentioned in section 4.1.1, the reward also is subject of experiments in the scope of this thesis. For the game to correspond to a proper environment, this reward must be a scalar value, depending on state and action.

<sup>1</sup>The game is programmed in Unity, which has non-predictable physics. As discussed for example in <https://forum.unity3d.com/threads/is-unity-physics-is-deterministic.429778/>, this is because of the fact that any random-number-generator depends on the current system time, which is never fully equal in subsequent trials. Because the calculation of some states can be more complicated than others, this effect can snowball even more – longer calculation in one step leads to later timing of a subsequent update step, which can lead to a whole other trajectory along the state space, even though the start state was equal.

Though it is in theory possible to implement an agent that takes the entire underlying state of the environment as its input, an approach like that is far from feasible, as this state also contains much information only necessary for rendering the game. Instead, in the chosen approach the agent only receives an *observation* of the environment's state.

Summarizing all those factors, it becomes obvious that the given game can clearly be defined in terms of a *Partially Observable Indeterministic Markov Decision Process*.

It is worth noting, that while the dimensionality of the observation is likely much smaller than the dimensionality of the state, any feasible observation will be high-dimensional or real-valued. The chance for any particular combination of parameters to appear multiple times vanishingly low, which makes the use of function approximation necessary.

While the notion of *POMDPs* itself contains no definition of final states, it is necessary to have final as a hard limit of the horizon in the calculation of state-values. Another design decision in the course of the implementation of this project was, that the agent itself can define what it wants to see as the end of an episode. It is a matter of testing after how many seconds the agent shall give up on a trial, or if steering into a wall should be seen as the end of a training episode. Because of that, the environment provides only candidates of what could terminate an episode to the agent, such that the agent can decide to reset the environment or not.

### 4.1.3 Characteristics of the agent

As stated above, it was a design decision to leave as many options open to the agent as possible, such that several agent can each have their own respective definitions of certain features. To summarize from the above chapters, the features unique to every agent are:

- The definition of the agent's *observation-function*, providing its internal state  $s = o(s_e)$
- Definition of the *reward-function*, returning a scalar from state, action and subsequent state:  $S_e \times \mathcal{A} \times S_e \rightarrow \mathbb{R}$
- Definition of its internal *model*, basing on which it calculates its policy
- Under which conditions an episode is considered to be terminated
- Definition of the agent's *exploration technique*
- If and how the agent relies on pretraining with supervised data

It is due to this design decision that the program flow of this project cannot follow the exact same structure than the one put forward in algorithm 1. One big structural difference is for example that the outer loop (line 3) becomes obsolete, as the agent decides under what conditions the environment must be reset. In the following section, I will provide some detail of what those things look like blablabla



## 4.2 Implemented features/functions/vectors to pick from

### 4.2.1 The vectors

### 4.2.2 Exploration

### 4.2.3 Reward

### 4.2.4 Performance measure

## 4.3 Implementation

The associated programs are, as long as not explicitly stated otherwise, written by the author of this work and are licensed under the GNU General Public License (GNU GPLv3). Their source codes are attached in the appendix of this work and can additionally be found digitally on the enclosed CD-ROM as well as online. Version control of this project relied on GitHub<sup>2</sup>, and was split into three repositories: The source code of the actual game written with the game engine Unity 3D (*Ba-rAIce*<sup>3</sup>), the source code of the implementation, written in Python (*Ba-rAIce-ANN*<sup>4</sup>), as well as the present text, written in L<sup>A</sup>T<sub>E</sub>X (*BAText*<sup>5</sup>). To ease connections between the following descriptions and their correspondences in the actual source code, the footnotes will refer as a hyperlink to the files on GitHub, using their relative path (every Python-file belongs to the agent, all other files to the game). In order to ensure that no work after the deadline is considered, it is referred to the signed commits **THE, SIGNED, COMMITS**.

The game is programmed using Unity Personal with a free license for students<sup>6</sup>. It is tested under version 2017.1.0f3<sup>7</sup>. Scripts belonging to the game are coded using the programming language C#. The agent was programmed with Python 3.5, relying on the open-source machine learning library TensorFlow[1]<sup>8</sup> in version 1.3. For a listing of all further used python-packages and their versions, it is referred to the *requirements.txt*-file in the respective repository.

While the author of this work contributed most of the work to change the given game such that it can be learned and played by a machine, the original version of the game was given in advance, coded by the first supervisor of this work. While it will be explicitly stated what was already given later in this chapter, it is also referred to the respective branch on Github (*Ba-rAIce – LeonsVersion*<sup>9</sup>). The implementation of the agent was however not influenced by any other people than the author of this work.

<sup>2</sup><https://github.com/>

<sup>3</sup><https://github.com/cstenkamp/BA-rAIce>

<sup>4</sup><https://github.com/cstenkamp/BA-rAIce-ANN>

<sup>5</sup><https://github.com/cstenkamp/BAText>

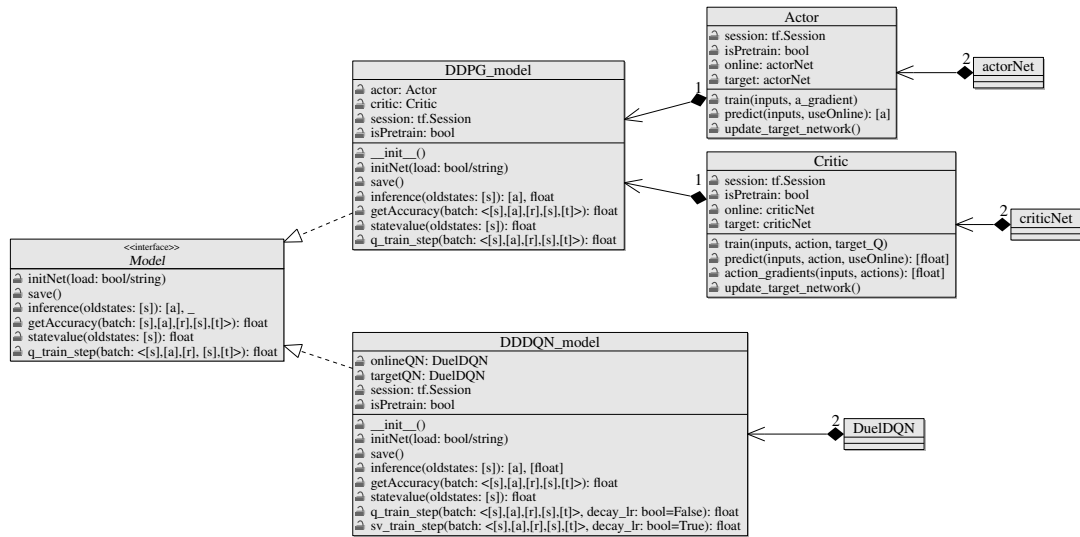
<sup>6</sup><https://store.unity.com/products/unity-personal>

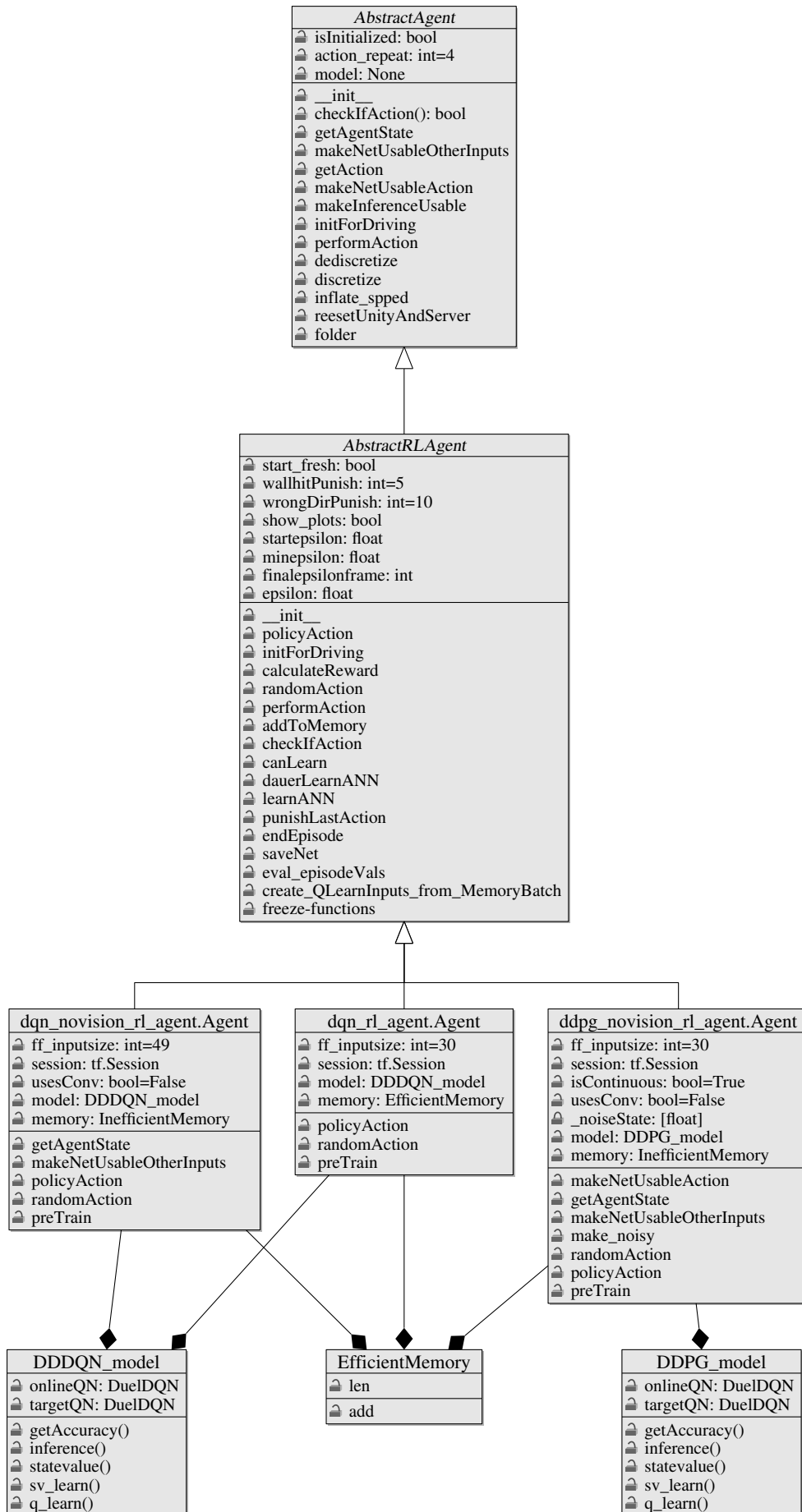
<sup>7</sup>As of now, 29th August, 2017, there is a bug in Unity that causes it to crash due to a memory leak if UI components are updated too often (which happens after a few hours of running). Because of that, in the current release of this project, all updates of the Unity UI are disabled in AI-Mode. A bug report to Unity was filed (case 935432) on 27th July, 2017, and it was promised that this issue will soon be fixed. Once that is the case, the variable `DEBUG_DISABLEGUI_AI_MODE` in *AiInterface.cs* can be set to `false`.

<sup>8</sup><https://www.tensorflow.org/>

<sup>9</sup><https://github.com/cstenkamp/BA-rAIce/tree/LeonsVersion>







### 4.3.1 The game

-screenshot von der GUI

**What Leon did already**

**Communication**

-nochmal drauf eingehen dass das spiel live ist -den sockets post -das von leon gemalte ablaufdiagramm

### 4.3.2 The agent

-Unbedingt auf jeden Fall UML-diagramm -Hier im Fließtext nur kleine Versionen der UML-Diagramme, und im Anhang dann die vollständigen versionen!

**Challenges and Solutions**

**Pretraining**

**The different agents**

DQN vs DDPG, sehend vs nicht-sehend, ...

**Network architecture**

1. dqn-algorithm - anzahl layer, Batchnorm, doubles dueling - clipping wieder rein, reference auf das dueling - grundsätzlich gegen batchnorm entschieden, siehe reddit post - MIT GRAFIK - Adam und tensorflow quoten, siehe zotero 2. ddp - anzahl layer, Batchnorm - MIT GRAFIK

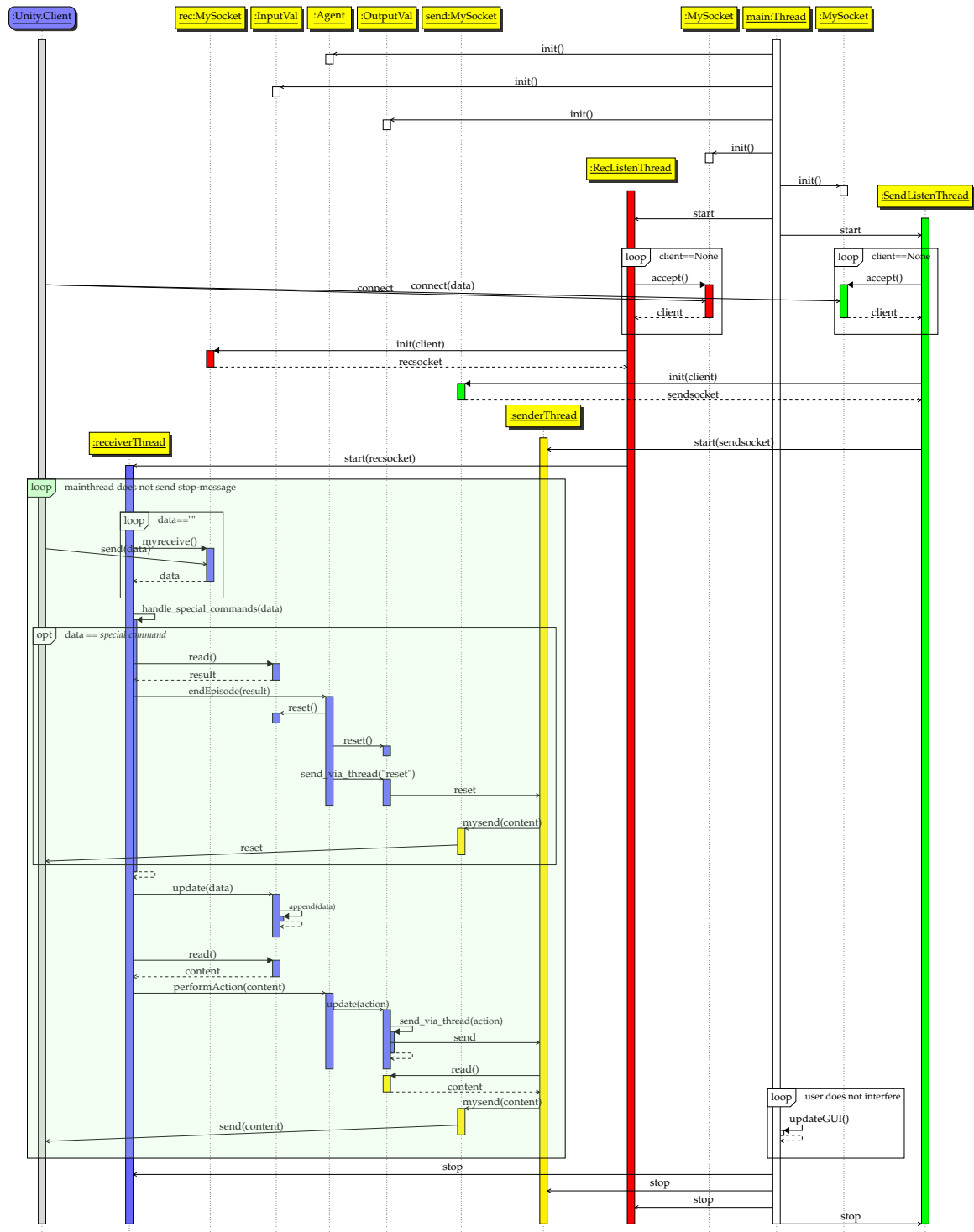
-schöne grafik. -auf meinen DQN-config eingehen und(!!!) ne DDPG-config machen, using the "experiment details" vom ddp paper

In the original DDPG-algorithm [8], the authors used *batch normalization* [6] to have the possibility of using the same network hyperparameters for differently scaled input-values. In the learning step when using minibatches, batch normalization normalizes each dimension across the samples in a batch to have unit mean and variance, whilst keeping a running mean and variance to normalize in non-learning steps. In Tensorflow, batchnorm can be added with an additional layer and an additional input, specifying the phase (learning step/non-learning step)<sup>10</sup>. Though Lillicrap et al. seemed to have success on using batch normalization, in practice it lead to unstability, even on simple physics tasks in openAI's gym. As I am not the only one having this issue<sup>11</sup>, I left out batch normalization for good.

---

<sup>10</sup>cf. [https://www.tensorflow.org/api-docs/python/tf/contrib/layers/batch\\_norm](https://www.tensorflow.org/api-docs/python/tf/contrib/layers/batch_norm)

<sup>11</sup>redditlink



## Chapter 5

# Analysis, Results and open Questions

testing took place on a win10 machine, ... Answer all of the research questions explicitly!!!

## Chapter 6

# Discussion

"Fragestellung aus der Einleitung wird erneut aufgegriffen und die Arbeitsschritte werden resümiert" Zusammen mit der Conclusion 10% der Gesamtlänge

## Chapter 7

# Conclusion and future directions

Die paper die bei openAI erwähnt waren die das ganze in viel kreasser sind, die Dota spielen können etc!

## Appendix A

# Comparison Pseudocode & Python-code

### A.1 DQN

The following section describes the structure of an actual reinforcement learning agent, using a **Dueling Deep-Q-Network** as its model (as described in [17]), performing **Double Q-learning** (as described in [5]). The last page consists of a comparison between the pseudocode of the general program flow of a DDQN-network (taken from [10], with changes from [5] and [8] in blue) to the left and its corresponding python-code to the right, where each line of the pseudocode corresponds exactly to the respective line of the python-code. For information on which python- and tensorflow version are used, please see chapter+4. This code is extracted from the actual implementation within the scope of this thesis, with some changes abstracting away irrelevant details.

```

1  class Agent():
2  def __init__(self, inputsize):
3      self.inputsize = inputsize
4      self.model = DDDQN_model
5      self.memory = Memory(10000, self) #for definition see code
6      self.action_repeat = 4
7      self.update_frequency = 4
8      self.batch_size = 32
9      self.replaystartsize = 1000
10     self.epsilon = 0.05
11     self.last_action = None
12     self.repeated_action_for = self.action_repeat

14     def runInference(self, gameState, pastState):
15         self.addToMemory(gameState, pastState)
16         inputs = self.getAgentState(*gameState)
17         self.repeated_action_for += 1
18         if self.repeated_action_for < self.action_repeat:
19             toUse, toSave = self.last_action
20         else:
21             self.repeated_action_for = 0
22             if self.canLearn() and np.random.random() > self.epsilon:
23                 action, _ = self.model.inference(inputs)
24                 toSave = self.dediscretize(action[0])
25                 toUse = "["+str(throttle)+", "+str(brake)+", "+str(steer)+"]"
26             else:
27                 toUse, toSave = self.randomAction() #for definition see code
28             self.last_action = toUse, toSave
29             self.containers.outputval.update(toUse, toSave)
30             self.numsteps += 1
31             if self.numsteps % self.update_frequency == 0 and len(self.memory) > self.replaystartsize:
32                 self.learnStep()

34     def learnStep(self):
35         QLearnInputs = self.memory.sample(self.batch_size)

```



```

36     self.model.q_learn(QLearnInputs)

38     def addToMemory(self, gameState, pastState):
39         s = self.getAgentState(*pastState) #for definition see code
40         a = self.getAction(*pastState) #for definition see code
41         r = self.calculateReward(*gameState)#for definition see code
42         s2= self.getAgentState(*gameState) #for definition see code
43         t = False #will be updated if episode did end
44         self.memory.append([s,a,r,s2,t])

47     class DuelDQN():
48     def __init__(self, name, inputsize, num_actions):
49         with tf.variable_scope(name, initializer = tf.random_normal_initializer(0, 1e-3)):
50             #for the inference
51             self.inputs = tf.placeholder(tf.float32, shape=[None, inputsize], name="inputs")
52             self.fc1 = tf.layers.dense(self.inputs, 400, activation=tf.nn.relu)
53             #modifications from the Dueling DQN architecture
54             self.streamA, self.streamV = tf.split(self.fc1,2,1)
55             xavier_init = tf.contrib.layers.xavier_initializer()
56             neutral_init = tf.random_normal_initializer(0, 1e-50)
57             self.AW = tf.Variable(xavier_init([200,self.num_actions]))
58             self.VW = tf.Variable(neutral_init([200,1]))
59             self.Advantage = tf.matmul(self.streamA,self.AW)
60             self.Value = tf.matmul(self.streamV,self.VW)
61             self.Qout = self.Value + tf.subtract(self.Advantage,tf.reduce_mean(self.Advantage,axis=1,keep_dims=
                ↳ True))
62             self.Qmax = tf.reduce_max(self.Qout, axis=1)
63             self.predict = tf.argmax(self.Qout,1)
64             #for the learning
65             self.targetQ = tf.placeholder(shape=[None],dtype=tf.float32)
66             self.targetA = tf.placeholder(shape=[None],dtype=tf.int32)
67             self.targetA_OH = tf.one_hot(self.targetA, self.num_actions, dtype=tf.float32)
68             self.compareQ = tf.reduce_sum(tf.multiply(self.Qout, self.targetA_OH), axis=1)
69             self.td_error = tf.square(self.targetQ - self.compareQ)
70             self.q_loss = tf.reduce_mean(self.td_error)
71             q_trainer = tf.train.AdamOptimizer(learning_rate=0.00025)
72             q_OP = q_trainer.minimize(self.q_loss)
73             self.trainables = tf.get_collection(tf.GraphKeys.TRAINABLE_VARIABLES, scope=name)

76     def _netCopyOps(fromNet, toNet, tau = 1):
77         op_holder = []
78         for idx,var in enumerate(fromNet.trainables[:]):
79             op_holder.append(toNet.trainables[idx].assign((var.value()*tau) + ((1-tau)*toNet.trainables[idx].
                ↳ value())))
80     return op_holder

```

```

1 Initialize replay memory  $D$  to capacity  $N$ 

5 Initialize action-value function  $Q(s, a; \theta)$  with random weights  $\theta$ 

8 Initialize target action-value function  $Q(s, a; \theta^-)$  with weights  $\theta^- = \theta$ 
For episode = 1,  $M$  do
10 Initialize sequence  $s_1 = \{x_1\}$  and preprocessed sequence  $\phi_1 = \phi(s_1)$ 
For  $1 = 1, T$  do
12 With probability  $\epsilon$  select random action  $a_t$ 
13 otherwise select  $a_t = \operatorname{argmax}_a Q(\phi(s_t), a; \theta)$ 

15 Execute action  $a_t$  in emulator and observe reward  $r_t$  and image  $x_{t+1}$ 
16 Set  $s_{t+1} = s_t, a_t, x_{t+1}$  and preprocess  $\phi_{t+1} = \phi(s_{t+1})$ 
17 Store transition  $(\phi_t, a_t, r_t, \phi_{t+1})$  in  $D$ 

19 Sample random minibatch of transitions  $(\phi_j, a_j, r_j, \phi_{j+1})$  from  $D$ 
20 Define  $a^{max}(\phi_{j+1}; \theta) = \operatorname{argmax}_a Q(\phi_{j+1}, a'; \theta)$ 
21 Define  $Q^{j+1} = Q(\phi_{j+1}, a^{max}(\phi_{t+1}; \theta); \theta^-)$ 

23 If episode terminates at step  $j + 1$  then set  $y_j = r_j$ ,
     $\hookrightarrow$  Otherwise set  $y_j = r_j + \gamma * Q^{j+1}$ 

24 Perform a gradient descent step on  $(y_j - Q(\phi_j, a_j; \theta))^2$  with respect
     $\hookrightarrow$  to the network parameters  $\theta$ 
25 Update target network:  $\theta^- \leftarrow \tau * \theta + (1 - \tau) \theta^-$ 
End For
26 End For

```

```

1 #see agent
2 class DDDQN_model():
3     def __init__(self, sess, inputsize, num_action):
4         self.sess = sess
5         self.onlineQN = DuelDQN("onlineNet", inputsize, num_action)
6         self.targetQN = DuelDQN("targetNet", inputsize, num_action)
7         self.sess.run(tf.global_variables_initializer())
8         self.sess.run(_netCopy0ps(self.targetQN, self.onlineQN))
9
10    #see agent
11    def inference(self, statesBatch): #called for every step t
12
13        return self.sess.run([self.onlineQN.predict, self.onlineQN.Qout], feed_dict={
14             $\hookrightarrow$  self.onlineQN.inputs: statesBatch})
15
16        #see agent
17        #see agent
18        def q_learn(self, batch): #also called for every step t
19            oldstates, actions, rewards, newstates, terminals = batch
20            action = self.sess.run(self.onlineQN.predict, {self.onlineQN.inputs:newstates
21                 $\hookrightarrow$  })
22            folgeQ = self.sess.run(self.targetQN.Qout, {self.targetQN.inputs:newstates})
23            doubleQ = folgeQ[range(len(terminals)),action]
24            consider_stateval = -(terminals - 1)
25
26            targetQ = rewards + (0.99 * doubleQ * consider_stateval)
27            self.sess.run(self.onlineQN.q_OP, feed_dict={self.onlineQN.inputs:oldstates,
28                 $\hookrightarrow$  self.onlineQN.targetQ:targetQ, self.onlineQN.targetA:actions})
29            self.sess.run(_netCopy0ps(self.onlineQN, self.targetQN, 0.001))
30        return

```

## A.2 DDPG

The following section describes the structure of an actual reinforcement learning agent, using an **actor-critic architecture** as its model, basing on the Deep Deterministic Policy gradient, as described in [14] and [8]. The last page consists of a comparison between the pseudocode of the general program flow of a DDPG-agent (taken from [8]) to the left and its corresponding python-code to the right, where each line of the pseudocode corresponds exactly to the respective line of the python-code. For information on which python- and tensorflow version are used, please see chapter 4. This code is extracted from the actual implementation within the scope of this thesis, with some changes abstracting away irrelevant details.

```

1  class Actor(object):
2  def __init__(self, inputs_size, num_actions, actionbounds, session):
3      with tf.variable_scope("actor"):
4          self.online = lowdim_actorNet(inputs_size, num_actions, actionbounds)
5          self.target = lowdim_actorNet(inputs_size, num_actions, actionbounds, name="target")
6          self.smoothTargetUpdate = _netCopyOps(self.online, self.target, 0.001)
7          # provided by the critic network
8          self.action_gradient = tf.placeholder(tf.float32, [None, num_actions], name="actiongradient")
9          self.actor_gradients = tf.gradients(self.online.scaled_out, self.online.trainables, -self.
           ➡ action_gradient)
10         self.optimize = tf.train.AdamOptimizer(1e-4).apply_gradients(zip(self.actor_gradients, self.online.
           ➡ trainables))
11 def train(self, inputs, a_gradient):
12     self.session.run(self.optimize, feed_dict={self.online.ff_inputs:inputs, self.action_gradient:
           ➡ a_gradient})
13 def predict(self, inputs, which="online"):
14     net = self.online if which == "online" else self.target
15     return self.session.run(net.scaled_out, feed_dict={net.ff_inputs:inputs})
16 def update_target_network(self):
17     self.session.run(self.smoothTargetUpdate)
18
19 class Critic(object):
20 def __init__(self, inputs_size, num_actions, session):
21     with tf.variable_scope("critic"):
22         self.online = lowdim_criticNet(inputs_size, num_actions)
23         self.target = lowdim_criticNet(inputs_size, num_actions, name="target")
24         self.smoothTargetUpdate = _netCopyOps(self.online, self.target, 0.001)
25         self.target_Q = tf.placeholder(tf.float32, [None, 1], name="target_Q")
26         self.loss = tf.losses.mean_squared_error(self.target_Q, self.online.Q)
27         self.optimize = tf.train.AdamOptimizer(1e-3).minimize(self.loss)
28         self.action_grads = tf.gradients(self.online.Q, self.online.actions)
29 def train(self, inputs, action, target_Q):
30     return self.session.run([self.optimize, self.loss], feed_dict={self.online.ff_inputs:inputs, self.
           ➡ online.actions: action, self.target_Q: target_Q})
31 def predict(self, inputs, action, which="online"):
32     net = self.online if which == "online" else self.target
33     return self.session.run(net.Q, feed_dict={net.ff_inputs:inputs, net.actions: action})
34 def action_gradients(self, inputs, actions):
35     return self.session.run(self.action_grads, feed_dict={self.online.ff_inputs:inputs, self.online.
           ➡ actions: actions})
36 def update_target_network(self):
37     self.session.run(self.smoothTargetUpdate)
38
39 def _netCopyOps(fromNet, toNet, tau = 1):

```

```

40 op_holder = []
41 for idx,var in enumerate(fromNet.trainables[:]):
42     op_holder.append(toNet.trainables[idx].assign((var.value()*tau) + ((1-tau)*toNet.trainables[idx].
         ↳ value())))
43 return op_holder

45 def dense(x, units, activation=tf.identity, decay=None, minmax = float(x.shape[1].value) ** -.5):
46     return tf.layers.dense(x, units,activation=activation, kernel_initializer=tf.
         ↳ random_uniform_initializer(-minmax, minmax), kernel_regularizer=decay and tf.contrib.layers.
         ↳ l2_regularizer(1e-2))

48 class lowdim_actorNet():
49     def __init__(self, inputs_size, num_actions, actionbounds, outerscope="actor", name="online"):
50         tanh_min_bounds,tanh_max_bounds = np.array([-1]), np.array([1])
51         min_bounds, max_bounds = np.array(list(zip(*actionbounds)))
52         self.name = name
53         with tf.variable_scope(name):
54             self.ff_inputs = tf.placeholder(tf.float32, shape=[None, inputs_size], name="ff_inputs")
55             self.fc1 = dense(self.ff_inputs, 400, tf.nn.relu, decay=decay)
56             self.fc2 = dense(self.fc1, 300, tf.nn.relu, decay=decay)
57             self.outs = dense(self.fc2, num_actions, tf.nn.tanh, decay=decay, minmax = 3e-4)
58             self.scaled_out = ((self.outs - tanh_min_bounds)/ (tanh_max_bounds - tanh_min_bounds)) * (
         ↳ max_bounds - min_bounds) + min_bounds)
59             self.trainables = tf.get_collection(tf.GraphKeys.TRAINABLE_VARIABLES, scope=outerscope+"/"+self.
         ↳ name)

61 class lowdim_criticNet():
62     def __init__(self, inputs_size, num_actions, outerscope="critic", name="online"):
63         self.name = name
64         with tf.variable_scope(name):
65             self.ff_inputs = tf.placeholder(tf.float32, shape=[None, inputs_size], name="ff_inputs")
66             self.actions = tf.placeholder(tf.float32, shape=[None, num_actions], name="action_inputs")
67             self.fc1 = dense(self.ff_inputs, 400, tf.nn.relu, decay=True)
68             self.fc1 = tf.concat([self.fc1, self.actions], 1)
69             self.fc2 = dense(self.fc1, 300, tf.nn.relu, decay=True)
70             self.Q = dense(self.fc2, 1, decay=True, minmax=3e-4)
71             self.trainables = tf.get_collection(tf.GraphKeys.TRAINABLE_VARIABLES, scope=outerscope+"/"+self.
         ↳ name)

```

4	Randomly initialize critic network $Q(s, a   \theta^Q)$ with weights $\theta^Q$	1	<b>class</b> DDPG_model():
5	and actor $\pi(s   \theta^\pi)$ with weights $\theta^\pi$ .	2	<b>def</b> __init__(self, session):
7	Initialize target network $Q'$ weights $\theta^{Q'} \leftarrow \theta^Q$	3	self.session = session
8	and $\pi'$ with weights $\theta^{\pi'} \leftarrow \theta^\pi$	4	self.critic = Critic(self.session)
9	Initialize replay buffer R	5	self.actor = Actor(self.session)
10	<b>for</b> episode = 1, M <b>do</b>	6	self.session.run(tf.global_variables_initializer())
11	Initialize a random process $\mathcal{N}$ for action exploration	7	self.session.run(_netCopyOps(self.actor.target, self.actor.online))
12	Receive initial observation state $s_1$	8	self.session.run(_netCopyOps(self.critic.target, self.critic.online))
13	<b>for</b> t = 1, T <b>do</b>	9	#replay buffer defined by the agent
14	Select action $a_t = \pi(s_t   \theta^\pi) + \mathcal{N}_t$ according to the current policy and ➔ exploration noise	11	#exploration noise added by the agent
15	Execute action $a_t$ and observe reward $r_t$ and observe new state $s_{t+1}$	12	#agent samples all observations
16	Store transition $(s_t, a_t, r_t, s_{t+1})$ in R	13	<b>def</b> inference(self, oldstates): #called for every step t
18	Sample a random minibatch of N transitions $(s_t, a_t, r_t, s_{t+1})$ from R	14	<b>return</b> self.actor.predict(oldstates, "target", is_training=False)
19	targetActorAction = $\pi'(s_{t+1}   \theta^{\pi'})$	15	#agent adds exploration noise afterwards
20	targetCriticQ = $Q'(s_{t+1}, \text{targetActorAction}   \theta^{Q'})$	16	#done by the agent
21	Set $y_i = r_i + \gamma * \text{targetCriticQ}$ #only in nonterminal states	17	#done by the agent
23	Update critic by minimizing the loss: $L = \frac{1}{N} \sum_i (y_i - Q(s_i, a_i   \theta^Q))^2$	18	<b>def</b> train_step(self, batch): #also called for every step t
24	Find the sampled policy gradient:	19	oldstates, actions, rewards, newstates, terminals = batch
25	a.i = $\pi(s_i   \theta^\pi)$	20	targetActorAction = self.actor.predict(newstates, "target")
26	$\nabla_{\theta^\pi} J \approx \frac{1}{N} \sum_i \nabla_a Q(s_i, a_i   \theta^Q) \nabla_{\theta^\pi} \pi(s_i   \theta^\pi)$	21	targetCriticQ = self.critic.predict(newstates, targetActorAction, "target")
27	Update the actor policy using the sampled policy gradient	22	cumrewards = np.reshape([rewards[i] if terminals[i] <b>else</b> rewards[i]+0.99* ➔ targetCriticQ[i] for i in range(len(rewards))], (len(rewards), 1))
28	Update the target networks:	23	_, loss = self.critic.train(oldstates, actions, cumrewards)
29	$\theta^{Q'} \leftarrow \tau * \theta^Q + (1 - \tau) \theta^{Q'}$	25	onlineActorActions = self.actor.predict(oldstates)
30	$\theta^{\pi'} \leftarrow \tau * \theta^Q + (1 - \tau) \theta^{\pi'}$	26	grads = self.critic.action_gradients(oldstates, onlineActorActions)
31	<b>end for</b>	27	self.actor.train(oldstates, grads[0])
32	<b>end for</b>	28	#updating the targetnets
		29	self.critic.update_target_network()
		30	self.actor.update_target_network()
		31	<b>return</b>

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## Declaration of Authorship

I, Christoph Stenkamp, hereby certify that the work presented here is, to the best of my knowledge and belief, original and the result of my own investigations, except as acknowledged, and has not been submitted, either in part or whole, for a degree at this or any other university.

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city, date