# FDTD Sources

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# Abstract

This document describes and formulates the various sources that can be used in FDTD models.

### 1D Sources

# Gaussian Pulse

The Gaussian Pulse is an impulse function that allows us to excite the problem with a broad range of frequencies all at the same time.

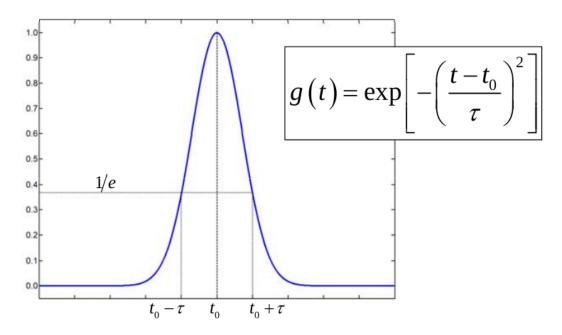


Figure 1: A Gaussian Pulse centered at  $t_0$ 

To find the frequency content of the Pulse we must perform the Fourier Transform on the pulse.

$$g(t) = \exp\left(-\frac{t^2}{\tau^2}\right) \Longrightarrow G(f) = \frac{1}{\sqrt{\pi}B} \exp\left[-\frac{f^2}{B^2}\right]$$

This shows that the frequency content of the Gaussian Pulse extends from DC up to B where

$$B = \frac{1}{\pi \tau} \tag{1}$$

#### Pulse Design

To design the pulse for our simulations we must first decide on the maximum frequency we are interested in  $f_{max}$  then compute the pulse width with this upper frequency

$$B = f_{max} = \frac{1}{\pi \tau} \Longrightarrow \tau \le \frac{1}{\pi f_{max}}$$

For simplification we can approximate  $\tau$  as

$$\tau \cong \frac{0.5}{f_{max}} \tag{2}$$

In order to properly resolve our Guassian pulse, which should be completed by at least 10 to 20 time steps, we need to recalculate  $\Delta t$ . We now need to re-evaluate this value in conjuction with the Courant Stability Condition. We will determine  $\Delta t$  based on the maximum frequency and pick the smallest  $\Delta t$ .

$$\Delta t \le \frac{\tau}{10} \tag{3}$$

Finally to properly inject our source without any adverse reactions within our model we must include delay 1.1. This will allow the pulse to ease into the problem space without producing large field gradients.

$$t_0 \ge 6\tau \tag{4}$$

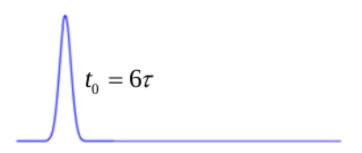


Figure 2: A Gaussian Pulse delayed by  $t_0 = 6\tau$ 

#### Matlab Example

% Parameters

#### Program 1 The Gaussian Source

```
fmax = 1e9;
                                           Max Frequency
dt = 0.5*dz/c0
                                           \%Time\ Step
tau = 0.5/fmax;
                                           %Pulse Duration
% Compute Gaussian Source
                                           %position of source
nzc = round(Nz/2)
dt = 0.6*dz/c0
ta = [0:STEPS-1]*dt;
                                           \%time \ axis
                                           \%Pulse\ Position
t0 = 6*tau
s = dz/(2*c0) + dt/2
                                           %Total delay between E and H
Esrc = \exp(-((ta-t0/tau).^2);
                                           %E field source
A = - \mathbf{sqrt}(ER(nzc)/UR(nzc));
                                           % 2\pi mplitude of H field
Hsrc = A * exp(-((ta-t0+s)/tau).^2);
                                           % H field source
```