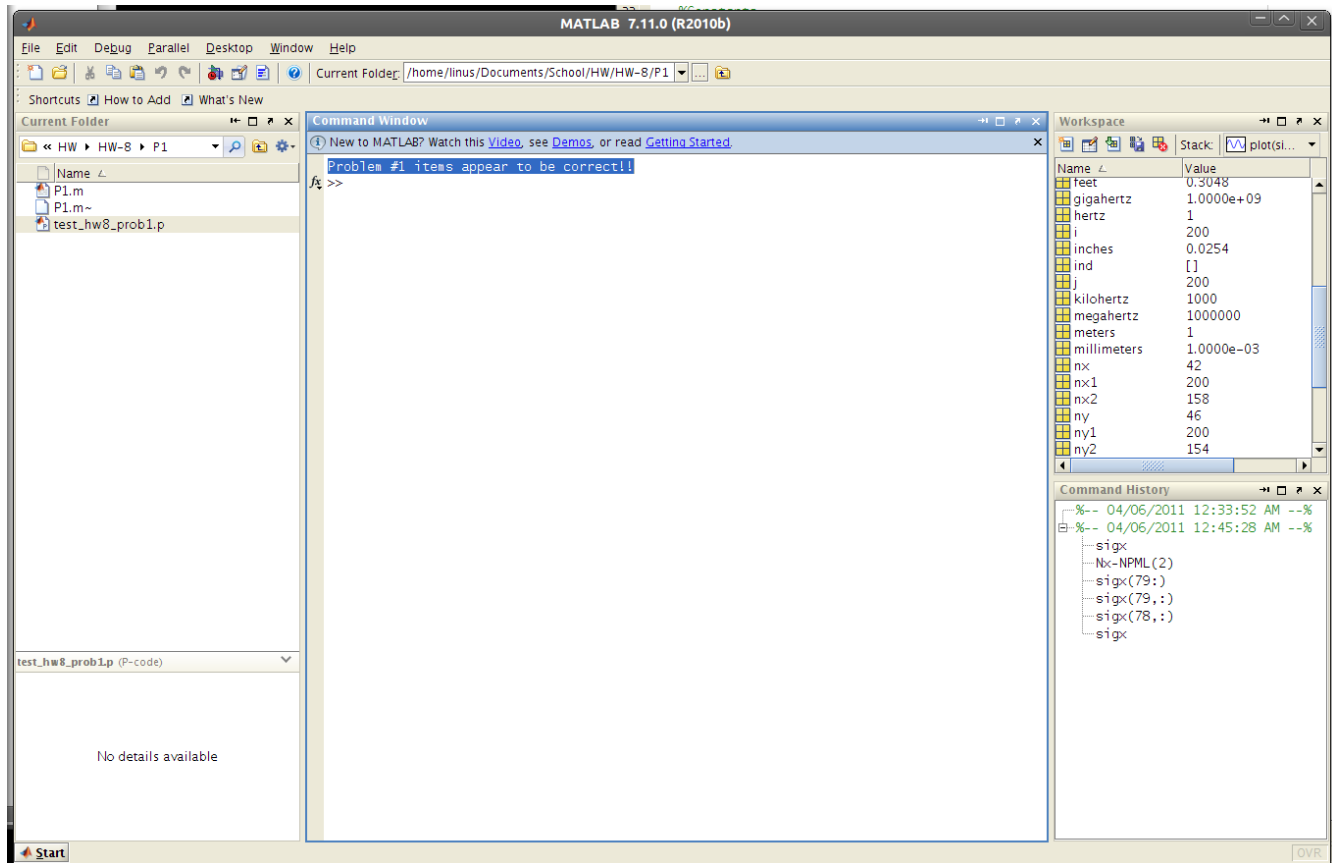


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04/06/2011
EEL 5390 – Special Topics (FDTD)
HW #8

Notes:

P1 – Calculate PML Parameters



```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%  
% Pre-Program Work  
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
```

```
% Initialize MATLAB  
close all; clc;  
clear all;
```

```
% UNITS  
meters = 1;  
decimeters = 1e-1 * meters;  
centimeters = 1e-2 * meters;  
millimeters = 1e-3 * meters;  
inches = 2.54 * centimeters;  
feet = 12 * inches;  
seconds = 1;  
hertz = 1/seconds;  
kilohertz = 1e3 * hertz;  
megahertz = 1e6 * hertz;  
gigahertz = 1e9 * hertz;
```

```
%Constants  
c0 = 299792458; %m/s  
e0 = 8.854187817*10^-12; %F/m  
u0 = 1.256637061*10^-6; %H/m
```

```

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% Initialization of Parameters
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

Nx = 100;
Ny = 100;
NPML = [20 21 22 23];
dx = 0.1;
dy = 0.1;
dt = 1.6e-10;
tau = 3.3e-9;
STEPS = 500;

% Compute 2x Grid
Nx2 = 2*Nx;
Ny2 = 2*Ny;

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% Calculate PML Parameters
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

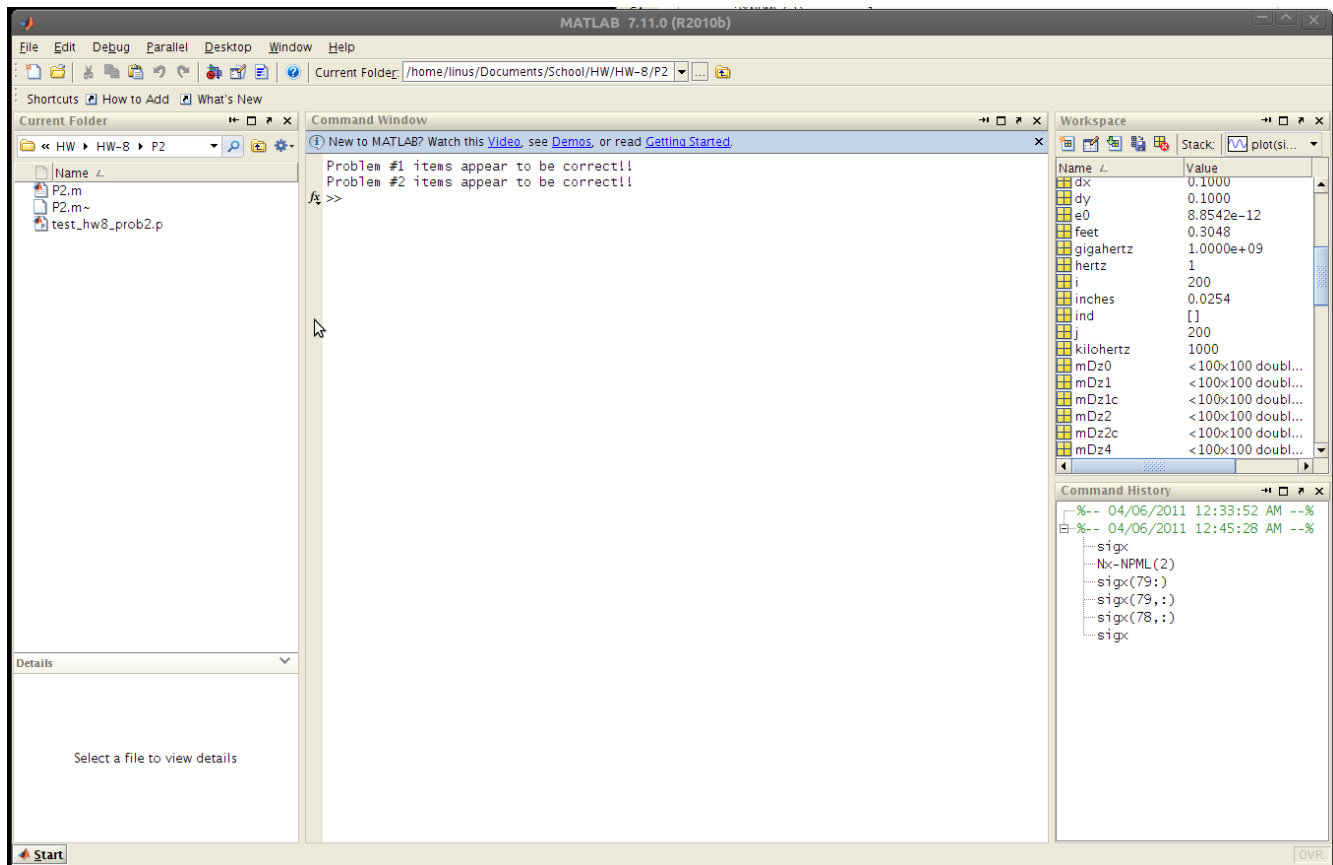
% Compute sigx
sigx = zeros(Nx2, Ny2);
for nx=1:2*NPML(1)
    i = 2*NPML(1) - nx + 1;
    sigx(i, :) = (0.5*e0/dt)*(nx/2/NPML(1))^3;
end
for nx=1:2*NPML(2)
    i = Nx2 - 2*NPML(2) + nx;
    sigx(i, :) = (0.5*e0/dt)*(nx/2/NPML(2))^3;
end

% Compute sigy
sigy = zeros(Nx2, Ny2);
for ny=1:2*NPML(3)
    j = 2*NPML(3) - ny + 1;
    sigy(:,j) = (0.5*e0/dt)*(ny/2/NPML(3))^3;
end
for ny=1:2*NPML(4)
    j = Ny2 - 2*NPML(4) + ny;
    sigy(:,j) = (0.5*e0/dt)*(ny/2/NPML(4))^3;
end

test_hw8_prob1

```

P2 – Compute Update Coefficients



```

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%FDTD Initialization
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
  
```

% Material Properties

```

URxx = ones(Nx,Ny);
URyy = ones(Nx,Ny);
ERzz = ones(Nx,Ny);
  
```

% Update Coefficients

```

sigHx = sigx(1:2:Nx2, 2:2:Ny2);
sigHy = sigy(1:2:Nx2, 2:2:Ny2);

mHx0 = 1/dt + (sigHy/(2*e0));
mHx1 = (1/dt - (sigHy/(2*e0)))./mHx0;
mHx2 = -(c0./URxx)./mHx0;
mHx3 = -((c0*dt/e0)*(sigHx./URxx))./mHx0;

sigHx = sigx(2:2:Nx2, 1:2:Ny2);
sigHy = sigy(2:2:Nx2, 1:2:Ny2);
mHy0 = (1/dt)+(sigHx/(2*e0));
mHy1 = (1/dt - (sigHx/(2*e0)))./mHy0;
mHy2 = -(c0./URyy)./mHy0;
mHy3 = -((c0*dt/e0)*sigHy./URyy)./mHy0;
  
```

```

sigDx = sigx(1:2:Nx2, 1:2:Ny2);
sigDy = sigy(1:2:Nx2, 1:2:Ny2);
mDz0 = (1/dt) + ((sigDx + sigDy)/(2*e0)) + (sigDx.*sigDy)*dt/(4*e0^2);
mDz1 = ((1/dt) - ((sigDx + sigDy)/(2*e0)) - (sigDx.*sigDy)*dt/(4*e0^2)) ./mDz0;
mDz2 = c0./mDz0;
mDz4 = - (dt/e0^2)*sigDx.*sigDy./mDz0;

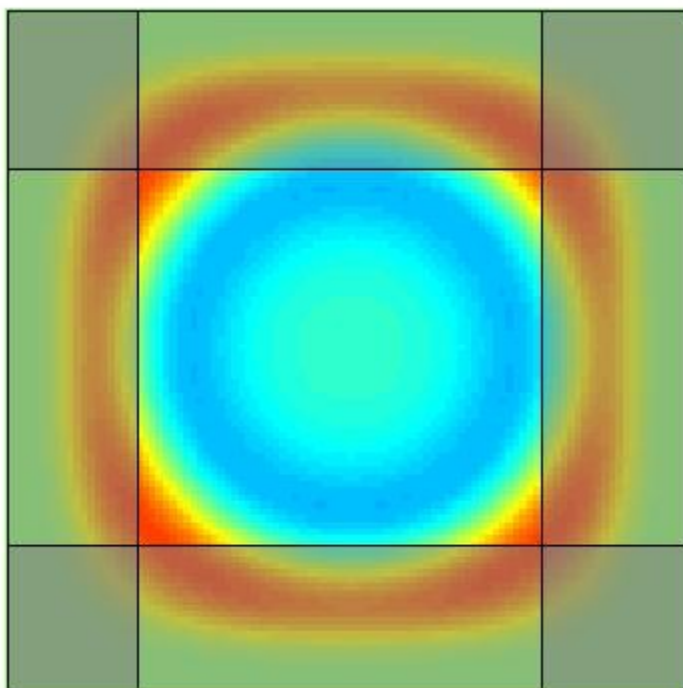
mEz1 = 1./ERzz;

```

test_hw8_prob2

P2 – 2D FDTD with PML

STEP200 of 500



Appendix

P3.m

[illegible]

```

sigx = zeros(Nx2, Ny2);
for nx=1:2*NPML(1)
    i = 2*NPML(1) - nx + 1;
    sigx(i, :) = (0.5*e0/dt)*(nx/2/NPML(1))^3;
end
for nx=1:2*NPML(2)
    i = Nx2 - 2*NPML(2) + nx;
    sigx(i, :) = (0.5*e0/dt)*(nx/2/NPML(2))^3;
end

```

```

% Compute sigy
sigy = zeros(Nx2, Ny2);
for ny=1:2*NPML(3)
    j = 2*NPML(3) - ny + 1;
    sigy(:,j) = (0.5*e0/dt)*(ny/2/NPML(3))^3;
end
for ny=1:2*NPML(4)
    j = Ny2 - 2*NPML(4) + ny;
    sigy(:,j) = (0.5*e0/dt)*(ny/2/NPML(4))^3;
end

```

```

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%FDTD Initialization
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

```

```

% Material Properties
URxx = ones(Nx,Ny);
URyy = ones(Nx,Ny);
ERzz = ones(Nx,Ny);

```

```

% Update Coefficients
sigHx = sigx(1:2:Nx2, 2:2:Ny2);
sigHy = sigy(1:2:Nx2, 2:2:Ny2);

mHx0 = (1/dt) + (sigHy/(2*e0));
mHx1 = ((1/dt) - (sigHy/(2*e0)))./mHx0;
mHx2 = -(c0./URxx)./mHx0;
mHx3 = -((c0*dt/e0)*(sigHx./URxx))./mHx0;

sigHx = sigx(2:2:Nx2, 1:2:Ny2);
sigHy = sigy(2:2:Nx2, 1:2:Ny2);
mHy0 = (1/dt)+(sigHx/(2*e0));
mHy1 = ((1/dt) - (sigHx/(2*e0)))./mHy0;
mHy2 = -(c0./URyy)./mHy0;
mHy3 = -((c0*dt/e0)*sigHy./URyy)./mHy0;

sigDx = sigx(1:2:Nx2, 1:2:Ny2);
sigDy = sigy(1:2:Nx2, 1:2:Ny2);
mDz0 = (1/dt) + ((sigDx + sigDy)/(2*e0)) + (sigDx.*sigDy)*dt/(4*e0^2);
mDz1 = ((1/dt) - ((sigDx + sigDy)/(2*e0)) - (sigDx.*sigDy)*dt/(4*e0^2)) ./mDz0;
mDz2 = c0./mDz0;
mDz4 = - (dt/e0^2)*sigDx.*sigDy./mDz0;

mEz1 = 1./ERzz;

```



```

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% Source
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
t0 = 6*tau;
t = [0:STEPS-1]*dt;
g = exp(-((t-t0)/tau).^2);
nx_src = 1+floor(Nx/2);
ny_src = 1+floor(Ny/2);

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%FDTD Initialization
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

%Fields
Hx = zeros(Nx,Ny);
Hy = zeros(Nx,Ny);
Dz = zeros(Nx,Ny);
Ez = zeros(Nx,Ny);

%Curl Terms
CEx = zeros(Nx,Ny);
CEy = zeros(Nx,Ny);
CHz = zeros(Nx,Ny);

%Integration Terms
ICEx = zeros(Nx,Ny);
ICEy = zeros(Nx,Ny);
IDz = zeros(Nx,Ny);

figure('Color', 'w');

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% Execute Simulation
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

for T = 1:STEPS

    % Compute Curl of E

    %% CEx
    for ny=1:Ny-1
        for nx=1:Nx
            CEx(nx,ny) = (Ez(nx,ny+1) - Ez(nx,ny))/dy;
        end
    end

    for nx=1:Nx
        CEx(nx,Ny) = (Ez(nx,1) - Ez(nx,Ny))/dy;
    end

    %% CEy
    for nx=1:Nx-1
        for ny=1:Ny
            CEy(nx,ny) = - (Ez(nx+1,ny) - Ez(nx,ny))/dx;
        end
    end
end

```

```

for ny=1:Ny
    CEy(Nx,ny) = - (Ez(1,ny) - Ez(Nx,ny))/dx;
end

% Update H Integrations
ICEx = ICEx + CEx;
ICEy = ICEy + CEy;

% Update H Field
Hx = mHx1.*Hx + mHx2.*CEx + mHx3.*ICEx;
Hy = mHy1.*Hy + mHy2.*CEy + mHy3.*ICEy;

%Update Curl of H
CHz(1,1) = (Hy(1,1) - Hy(Nx,1))/dx - (Hx(1,1) - Hx(1,Ny))/dy;

for nx=2:Nx
    CHz(nx,1) = (Hy(nx,1)-Hy(nx-1,1))/dx - (Hx(nx,1)-Hx(nx,Ny))/dy;
end

for nx=2:Nx
    CHz(1,ny) = (Hy(1,ny)-Hy(Nx,ny))/dx - (Hx(1,ny)-Hx(1,ny-1))/dy;
    for ny=2:Ny
        CHz(nx,ny) = (Hy(nx,ny)-Hy(nx-1,ny))/dx - (Hx(nx,ny)-Hx(nx,ny-1))/dy;
    end
end

%Update D Integrations
IDz = IDz + Dz;

% Update Dz
Dz = mDz1.*Dz + mDz2.*CHz + mDz4.*IDz;

%Inject Source
Dz(nx_src,ny_src) = Dz(nx_src,ny_src) + g(T);

% Update Ez
Ez = mEz1.*Dz;

if mod(T,1) == 0
    draw2d(xa,ya, ERzz, Ez, NPML, 0.03);
    axis equal tight off;
    title(['STEP' num2str(T) ' of ' num2str(STEPS)]);
    drawnow;
end

if T==200
    break;
end
end

```

draw2d.m

```
function [ output_args ] = Draw2D( xa, ya, ERzz, Ez, NPML, ColorAxis)
%DRAW2D Summary of this function goes here
% Detailed explanation goes here

[Nx Ny] = size(Ez);

cla; hold on;

imagesc(xa,ya,Ez);
caxis([-1*ColorAxis, ColorAxis]);

%Fill in PML

if NPML(1)
    x = [xa(1) xa(NPML(1)) xa(NPML(1)) xa(1) xa(1)];
    y = [ya(1) ya(1) ya(Ny) ya(Ny) ya(1)];
    c = 0.5 * [1 1 1];
    fill(x,y,c, 'FaceAlpha',0.5);
end
if NPML(2)
    x = [xa(Nx-NPML(2)) xa(Nx) xa(Nx) xa(Nx-NPML(2)) xa(Nx-NPML(2))];
    y = [ya(1) ya(1) ya(Ny) ya(Ny) ya(1)];
    c = 0.5 * [1 1 1];
    fill(x,y,c, 'FaceAlpha',0.5);
end
if NPML(3)
    x = [xa(1) xa(Nx) xa(Nx) xa(1) xa(1)];
    y = [ya(1) ya(1) ya(NPML(3)) ya(NPML(3)) ya(1)];
    c = 0.5 * [1 1 1];
    fill(x,y,c, 'FaceAlpha',0.5);
end
if NPML(4)
    x = [xa(1) xa(Nx) xa(Nx) xa(1) xa(1)];
    y = [ya(Ny-NPML(4)) ya(Ny-NPML(4)) ya(Ny) ya(Ny) ya(Ny-NPML(4))];
    c = 0.5 * [1 1 1];
    fill(x,y,c, 'FaceAlpha',0.5);
end

hold off;

end
```