

Data Structures and Algorithms

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Session: String Matching Algorithms

String Matching Problem¹

- Finding all valid shifts with which a given pattern P occurs in a given text T

¹Chapter 32, CLRS, Third Edition

Illustration

$s = 0$

S	T	E	P	S	T	Y	L	E
---	---	---	---	---	---	---	---	---

S	T	Y
---	---	---

Illustration

$s = 0$

S	T	E	P	S	T	Y	L	E
---	---	---	---	---	---	---	---	---

S	T	Y
---	---	---

$s = 1$

S	T	E	P	S	T	Y	L	E
---	---	---	---	---	---	---	---	---

S	T	Y
---	---	---

Illustration

$s = 0$

S	T	E	P	S	T	Y	L	E
---	---	---	---	---	---	---	---	---

S	T	Y
---	---	---

$s = 1$

S	T	E	P	S	T	Y	L	E
---	---	---	---	---	---	---	---	---

S	T	Y
---	---	---

$s = 2$

S	T	E	P	S	T	Y	L	E
---	---	---	---	---	---	---	---	---

S	T	Y
---	---	---

Illustration

$s = 0$

S	T	E	P	S	T	Y	L	E
---	---	---	---	---	---	---	---	---

S	T	Y
---	---	---

$s = 1$

S	T	E	P	S	T	Y	L	E
---	---	---	---	---	---	---	---	---

S	T	Y
---	---	---

$s = 2$

S	T	E	P	S	T	Y	L	E
---	---	---	---	---	---	---	---	---

S	T	Y
---	---	---

$s = 3$

S	T	E	P	S	T	Y	L	E
---	---	---	---	---	---	---	---	---

S	T	Y
---	---	---

Illustration

$s = 0$

S	T	E	P	S	T	Y	L	E
S	T	Y						

$s = 1$

S	T	E	P	S	T	Y	L	E
	S	T	Y					

$s = 2$

S	T	E	P	S	T	Y	L	E
	S	T	Y					

$s = 3$

S	T	E	P	S	T	Y	L	E
	S	T	Y					

$s = 4$

S	T	E	P	S	T	Y	L	E
				S	T	Y		

Illustration

$s = 0$

S	T	E	P	S	T	Y	L	E
S	T	Y						

$s = 1$

S	T	E	P	S	T	Y	L	E
	S	T	Y					

$s = 2$

S	T	E	P	S	T	Y	L	E
	S	T	Y					

$s = 3$

S	T	E	P	S	T	Y	L	E
	S	T	Y					

$s = 4$

S	T	E	P	S	T	Y	L	E
				S	T	Y		

$s = 5$

S	T	E	P	S	T	Y	L	E
				S	T	Y		

Illustration

$s = 0$

S	T	E	P	S	T	Y	L	E
---	---	---	---	---	---	---	---	---

S	T	Y
---	---	---

$s = 1$

S	T	E	P	S	T	Y	L	E
---	---	---	---	---	---	---	---	---

S	T	Y
---	---	---

$s = 2$

S	T	E	P	S	T	Y	L	E
---	---	---	---	---	---	---	---	---

S	T	Y
---	---	---

$s = 3$

S	T	E	P	S	T	Y	L	E
---	---	---	---	---	---	---	---	---

S	T	Y
---	---	---

$s = 4$

S	T	E	P	S	T	Y	L	E
---	---	---	---	---	---	---	---	---

S	T	Y
---	---	---

$s = 5$

S	T	E	P	S	T	Y	L	E
---	---	---	---	---	---	---	---	---

S	T	Y
---	---	---

$s = 6$

S	T	E	P	S	T	Y	L	E
---	---	---	---	---	---	---	---	---

S	T	Y
---	---	---

Naive String Matching Algorithm

```
Algorithm NaiveStringMatchingAlgorithm( $T, P$ )  
Input Text  $T$  of size  $n$  and Pattern  $P$  of size  $m$   
Define  $s$  as the shift index to  $T$   
for  $s \in (0 \dots n - m)$  do  
     $j = 0$   
    while  $j < m$  &  $T[s + j] = P[j]$  do  
         $j = j + 1$   
    end while  
    if  $j = m$  then  
        print 'Valid at shift  $s$ '  
    end if  
end for
```

Figure: Naive String Algorithm

Analysis of Naive String Matching Algorithm

Algorithm NaiveStringMatchingAlgorithm(T, P)

Input Text T of size n and Pattern P of size m

Define s as the shift index to T

for $s \in (0 \dots n - m)$ **do**

$j = 0$

while $j < m$ & $T[s + j] = P[j]$ **do**

$j = j + 1$

end while $\implies c_1 \times m$ times

if $j = m$ **then**

 print 'Valid at shift s '

end if

end for $\implies c_2 \times (n - m + 1)$ times

Figure: Naive String Matching Algorithm

$$T(n) = c_1 c_2 (n - m + 1) m = O((n - m + 1) m)$$

****Note:** Preprocessing time is 0

Thank you