$$S(A^*,f,i) = \left\{ e \middle| \left(e,f\right) \in A^* \right\}$$