

XX50215 Statistics for Data Science

Problems 5 - Solutions

1. A random point (X,Y) is distributed uniformly on the square with vertices $(1,1)$, $(1,-1)$, $(-1, 1)$, $(-1,-1)$. That is the joint pdf $f(x,y) = 0.25$ on the square. Determine the probabilities of the following events.
 - a. $X^2 + Y^2 \leq 1$
 - b. $2X - Y > 0$
 - c. $|X + Y| < 2$
2. I leave for work between 8AM and 8:30AM and takes between 40 and 50 minutes to get there. Assuming that departure time and journey length are independent and each is uniformly distributed what is the probability that I will arrive before 9AM?
3. If a stick is broken at random into three pieces, what is the probability that the pieces can be put together in a triangle?
4. Suppose that the random variable Y has a binomial distribution with n trials and success probability X , where n is a constant and X is a $\text{uniform}(0,1)$ random variable. Find EY and $\text{Var } Y$.
5. Show that any random variable is uncorrelated with a constant.
6. How many terms are in the expansion of $(x_1 + x_2 + x_3)^4$?