Assignment 0

Robot Kinematics and Dynamics

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1 Overview

Welcome to Robot Kinematics and Dynamics! This assignment serves to ensure you can get started with the tools we will be using this semester, as well as a brief overview of some of the prerequisite information we'll be assuming you already know. The topics and processes covered in this assignment will be heavily used throughout this class. Please meet with course staff if you have trouble with any part of the assignment, so we can make sure you are ready for assignment 1.

2 Background

In this section, we will give a brief review of the main concepts covered in lecture as they pertain to the labs.

2.1 Matrices

In this course, we will make extensive use of matrices and matrix multiplication. While we will not need the anything but the basics of linear algebra, you must absolutely be comfortable with the following:

- matrix multiplication
- transposition
- inversion
- rank
- vector norms
- determinants
- cross products
- dot products

2.2 Calculus

We expect you to know the following calculus concepts:

- Derivatives (including trigonometric functions)
- Partial Derivatives

2.3 Course Logistics (Specific to CMU)

In this class you would be using the following websites regularly:

- Course Website: This site will act as the central hub for the course. The course calendar, due dates, syllabus, etc. can be found on this site.
- Piazza: This is the best way to ask course staff questions, and see course announcements.
- Canvas: We'll be releasing all the assignments on Canvas, as well as keeping track of your grades.
- Gradescope: Create an account using your CMU email. You should have already been added to the course. If you haven't, please contact the course staff via a Piazza post.

3 Written Questions

For the following problems, fully evaluate all answers unless otherwise specified.

Answers for written questions must be typed. We recommend LaTeX, Microsoft Word, OpenOffice, or similar. However, diagrams can be hand-drawn and scanned in.

Unless otherwise specified, all units are in radians, meters, and seconds, where appropriate.

1) Piazza	5 points
You should have received an email inviting you to the course Piazza instance. We course announcements via Piazza. To ensure that you have been properly added, p to the Assignment 0 release post. On this post there will be a code, submit that cocanswer to this question.	lease go

2) Matrices and Matrix Operations

(1) [6 points] Which of the following are valid expressions? Give your answer as a list of numbers (for example: 1,2,4).

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1. \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}
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$$2. \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix} \times \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

4.
$$\begin{bmatrix} 1 \\ 1 \end{bmatrix} \times \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}$$

5.
$$\begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix} \times \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

6.
$$\begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix} \times (\begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix})^{\top}$$

(2) [15 points] Evaluate the following:

1.
$$\begin{bmatrix} a & b & c \\ d & e & f \end{bmatrix} \times \begin{bmatrix} 3 \\ 1 \\ 7 \end{bmatrix}$$

2. $\begin{bmatrix} 9 & 3 \\ 0 & 1 \end{bmatrix} \times \begin{bmatrix} 2 & 1 \\ 4 & 3 \end{bmatrix}$

3. $\begin{bmatrix} 2 & 1 \\ 4 & 3 \end{bmatrix} \times \begin{bmatrix} 9 & 3 \\ 0 & 1 \end{bmatrix}$

4. Given the rotation matrix $R = \begin{bmatrix} \cos(x) & -\sin(x) \\ \sin(x) & \cos(x) \end{bmatrix}$

(a) Determine ${\cal R}^{-1}$

(b) Determine R^T

(c) Do you see a relationship between ${\cal R}^{-1}$ and ${\cal R}^T$

5. Given the matrices $A=\left[\begin{smallmatrix}1&3\\4&15\end{smallmatrix}\right]$ and $B=\left[\begin{smallmatrix}1&2\\4&8\end{smallmatrix}\right]$

(a) Determine det(A)

(b) Determine rank(A). Is A full rank?

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(c)	Determine $\det(B)$		
(d)	Determine $rank(B)$. Is B full rank?		
(e)	Do you notice a relationship between the rank and the determatrices?	erminant of these	

- 6. Given the vectors $\mathbf{x} = [1,2,3]$ and $\mathbf{y} = [4,5,6]$
 - (a) Determine $\mathbf{x} \cdot \mathbf{y}$



(b) Determine $\mathbf{x} \times \mathbf{y}$

	(c) Determine $\ \mathbf{x}\ $ and $\ \mathbf{y}\ $
	7. Invert $\begin{bmatrix} 1 & 1 \\ 2/3 & 1 \end{bmatrix}$.
3) Calcu	lus
(1)	[4 points] Find the derivative of $x\cos(x)$.
(2)	[10 points] Find the partial derivatives with respect to x and y of $f(x,y)=x\sin(y)+y^2\cos(x)$.

4 Feedback

1) Feedback Form 5 points
We are always looking to improve the class! To that end, we're looking for your feedback on the assignments. When you've completed the assignment, please fill out the feedback form.

5 Code Questions

In this section, we will re-enforce the written questions with practical examples. These questions, written in Matlab, will be the beginning of your code for the hands-on lab. To begin, you must install Matlab. A free copy is available to all CMU students at:

http://www.cmu.edu/computing/software/all/matlab/

Once you've installed Matlab on a personal computer, open Matlab and navigate to Code Handout folder. In this folder there will be a few exercises. These exercises will review the basics of Matlab syntax.

1) Exercise 01 20 points

For this exercise, edit the ex_01.m file. In the file is four variables.

- Set A to be the 2x2 matrix $\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$.
- Set B to be the 2x3 matrix $\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix}$.
- Set C to be A times B.
- Set D to be $(B)^{\top}$ times A.

2) Exercise 02 10 points

For this exercise, edit the ex_02.m file. In it are two variables.

- Set a to be an array containing values from 0 to 100 (inclusive), incrementing by 0.2. Hint: look into the : 1 operator.
- Set b to be the 100x100 identity matrix. Hint: look at the eye² function.
- 3) Exercise 03 20 points

In this exercise, we'll review Matlab's function syntax. The file $ex_03.m$ contains a function that outputs a matrix R. Fill it out so that the function multiplies its parameters A, B as A times B times A times B.

4) Submission

To submit, run create_submission.m. It will first check that your submitted files run without error, and perform a small sanity check. Note, this is not going to grade your submission! The function will create a file called handin.tar.gz. Upload it to Canvas to complete the submission.

http://www.mathworks.com/help/matlab/ref/colon.html

²http://www.mathworks.com/help/matlab/ref/eye.html

6 Submission Checklist

Create a PDF of your answers to the written questions with the name writeup.pdf and submit it to Gradescope.
Make sure you have writeup.pdf in the same folder as the create_submission.m script.
Run create_submission.m in Matlab.
Upload handin.tar.gz to Canvas.
After completing the entire assignment, fill out the feedback form ³ .

³https://canvas.cmu.edu/courses/18336/quizzes/39692