

⑦

$$\frac{\partial E_z}{\partial t} = \frac{1}{\epsilon} \left[\frac{\partial H_y}{\partial x} - \frac{\partial H_x}{\partial y} \right]$$

$$\Rightarrow \frac{E_z^{n+1/2} - E_z^{n-1/2}}{\Delta t} = \frac{1}{\epsilon} \left[\frac{(H_y^n_{i,j+1/2} - H_y^n_{i,j-1/2})}{\Delta x} - \frac{(H_x^n_{i+1/2,j} - H_x^n_{i-1/2,j})}{\Delta y} \right]$$

$$\Rightarrow E_z^{n+1/2} = E_z^{n-1/2} - \frac{\Delta t}{\epsilon \cdot \Delta y} (H_x^n_{i+1/2,j} - H_x^n_{i-1/2,j}) + \frac{\Delta t}{\epsilon \cdot \Delta x} (H_y^n_{i,j+1/2} - H_y^n_{i,j-1/2})$$

$$\Rightarrow E_{zx}^{n-1/2} = E_{zx}^{n-1/2} + \frac{\Delta t}{\epsilon \cdot \Delta x} (H_y^n_{i,j+1/2} - H_y^n_{i,j-1/2})$$

$$A=1; \quad B = \frac{\Delta t}{\epsilon \cdot \Delta x}$$

$$\textcircled{a)} \quad E_z^{n+1/2} = E_z^{n-1/2} - \frac{\Delta t}{\epsilon \cdot \Delta y} (H_x^n_{i+1/2,j} - H_x^n_{i-1/2,j}) + \frac{\Delta t}{\epsilon \cdot \Delta x} (H_y^n_{i,j+1/2} - H_y^n_{i,j-1/2})$$

$$\Rightarrow E_{zy}^{n+1/2} = E_{zy}^{n-1/2} - \frac{\Delta t}{\epsilon \cdot \Delta y} (H_x^n_{i+1/2,j} - H_x^n_{i-1/2,j})$$

$$C=1; \quad D = \frac{\Delta t}{\epsilon \cdot \Delta y}$$

$$\textcircled{3} \quad \frac{\delta H_x}{\delta t} = \frac{1}{\mu} \left[- \frac{\delta \tau_z}{\delta y} \right]$$

$$\frac{H_x^{n+1/2}_{i-1/2, j+1} - H_x^{n-1/2}_{i-1/2, j+1}}{\Delta t} = - \frac{1}{\mu} \left[\frac{\tau_z^n_{i+1/2, j} - \tau_z^n_{i-1/2, j}}{\Delta y} \right]$$

$$\Rightarrow H_x^{n+1/2}_{i-1/2, j+1} = H_x^{n-1/2}_{i-1/2, j+1} - \frac{\Delta t}{\mu \cdot \Delta y} (\tau_z^n_{i+1/2, j} - \tau_z^n_{i-1/2, j})$$

$$E = 1; F = \frac{\Delta t}{\mu \cdot \Delta y}$$

$$\textcircled{4} \quad \frac{\delta H_y}{\delta t} = \frac{1}{\mu} \left[\frac{\delta \tau_z}{\delta y} \right]$$

$$\frac{H_y^{n+1/2}_{i, j} - H_y^{n-1/2}_{i, j}}{\Delta t} = \frac{1}{\mu} \left[\frac{\tau_z^n_{i, j+1/2} - \tau_z^n_{i, j-1/2}}{\Delta x} \right]$$

$$\Rightarrow H_y^{n+1/2}_{i, j} = H_y^{n-1/2}_{i, j} + \frac{\Delta t}{\mu \cdot \Delta x} (\tau_z^n_{i, j+1/2} - \tau_z^n_{i, j-1/2})$$

$$E = 1; F = \frac{\Delta t}{\mu \cdot \Delta x}$$