

```
#!/bin/anaconda3/bin/python
```

```
import math
import sympy as sym
import math
import numpy as np
from numpy import linalg as la
import scipy
from scipy import integrate
import matplotlib.pyplot as plt
from mpl_toolkits.mplot3d import Axes3D
```

```
from ode_2 import ode_solve
```

```
print("Lets do the 2-body problem")
```

```
#Initial conditions
```

```
m_1 = 1.0
m_2 = 1000.0
#G = 6.67408e-11 #m^3 kg^-1 s^-2
G = 1
x_1 = np.array([0.0, 0.0])
x_2 = np.array([0.0, 10.0])
v_1 = np.array([9.0, 9.0])
v_2 = np.array([0.5, 0.0])
```

```
#Lets make a vector y that will give is a 1st order ode
```

```
#2D
```

```
#Y = np.array([x_1,y_1,x_2,x_2,dx_1,dy_1,dx_2,dy_2])
```

```
def func(Y, t):
```

```
    #Positions of the two bodies
```

```
    y_1 = np.array([ Y[0],Y[1] ])
    y_2 = np.array([ Y[2],Y[3] ])
```

```
    #Velocites
```

```
    dy_1 = np.array([ Y[4],Y[5] ])
    dy_2 = np.array([ Y[6],Y[7] ])
```

```
    #Accelerations
```

```
    dy_3 = -G*m_2*(y_1 - y_2)/(la.norm(y_1-y_2)**3)
    dy_4 = -G*m_1*(y_2 - y_1)/(la.norm(y_2-y_1)**3)
```

```
    #We will have our 8 ode's
```

```
    dy = np.array([dy_1[0],dy_1[1],dy_2[0],dy_2[1],dy_3[0],dy_3[1],dy_4[0],dy_4[1]])
```

```
    return dy
```

```
#End function
```

```
#Need a 1D vector for the input
```

```
Y=np.concatenate((x_1,x_2,v_1,v_2))
```

```
#Evenly spaced time
```

```
t = np.arange(0,100.0,0.001)
```

```
#Scipy's in built ode
```

```
sol = integrate.odeint(func,Y,t)
```

```
plt.plot(sol[:,0],sol[:,1])
```

```
plt.plot(sol[:,2],sol[:,3])
```

```
#plt.show()
```

```
#Our RK ode solver
```

```
sol_my = ode_solve(func,t,Y)
```

```
plt.plot(sol_my[:,0],sol_my[:,1])
```

```
plt.plot(sol_my[:,2],sol_my[:,3])
```

```
plt.ylabel('y')
```

```
plt.xlabel('x')
```

```
plt.show()
```

```
#error Between the two solvers
```

```
print(sol_my[:,0] - sol[:,0])
```