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#!/bin/anaconda3/bin/python
```

```
import math
import numpy as np
```

```
#System of ode solver
```

```
# DESC: Uses the Runge-Kutta Method for Systems of Differential Equations, Chapter 5.9 Algorithm 5.7
```

```
#
```

```
# USAGE: ode_solve(func, time, initial_conditions)
```

```
#
```

```
#      func                :: A function of y and t. Returns a 1D numpy array of 1st order diffireential equations to solve.
```

```
#      time                :: A 1D array of equally spaced time points. Must have more then one entry.
```

```
#      initial_conditions  :: A 1D numpy array of initial conditions for the y entry of func.
```

```
def ode_solve(f, t, ic):
```

```
    #Assume you are given equally spaced time with more then 1 entry
```

```
    h = t[1] - t[0]
```

```
    #Store the output in a 2D array. 1st component is time, 2nd component is the input parameters
```

```
    sol = np.zeros([len(t),len(ic)])
```

```
    #Save initial contiation to t = a
```

```
    sol[0,:] = ic
```

```
    w = ic
```

```
    i = 1
```

```
    while(i < len(t)):
```

```
        #want to have same amount of data points as is time provided, so dont use last time point
```

```
        k1 = h*f(w,t[i-1])
```

```
        #print("Lenth, f, w, k1, t", len(f(w,t[i-1])), len(w),len(k1),len(t))
```

```
        k2 = h*f(w + 0.5*k1, t[i-1] + h/2.0)
```

```
        k3 = h*f(w + 0.5*k2, t[i-1] + h/2.0)
```

```
        k4 = h*f(w + k3, t[i-1] + h)
```

```
        w = w + (k1 + 2.0*k2 + 2.0*k3 + k4)/6.0
```

```
        #Store solution
```

```
        sol[i,:] = w
```

```
        i = i + 1
```

```
    #End While
```

```
    return sol
```

```
#End ode_solve
```

```
#Book problem 5.9 #1c Test
```

```
#Y = [u1,u2,u3]
```

```
#def ft(Y,t):
```

```
#    dy = np.array([ Y[1], -Y[0] - 2.0*math.exp(t) + 1.0, -Y[0] - math.exp(t) + 1.0])
```

```
#    return dy
#end
#y = np.array([1.0,0.0,1.0])

#t = np.arange(0,2.0,0.5)

#sol = ode_solve(ft, t,y)

#print("sol is ",sol)
#[[ 1.         0.         1.         ]
# [ 0.70787076 -1.24988663  0.39884862]
# [-0.33691753 -3.01764179 -0.29932294]
# [-2.41332734 -5.40523279 -0.92346873]

#And we get the books results.
```