

Problem Set 3

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Shortish Answer

- Suppose that we have a test scaled with the Rasch model whose first 3 items have known difficulties -1, 0, and 1.5. An examinee with ability θ got the first item right, the second item right, and the third item wrong. Can you write the likelihood of observing this sequence of item responses as a function of θ ?

$$\frac{e^{\theta-d}}{1 + e^{\theta-d}}$$

Item dif -1: $\frac{e^{\theta+1}}{1+e^{\theta+1}}$

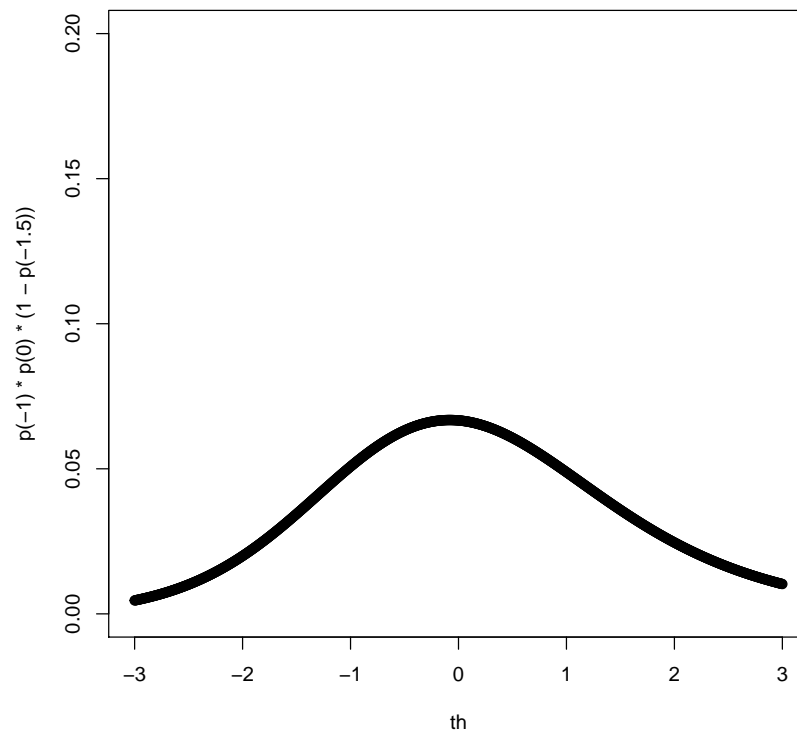
Item dif 0: $\frac{e^{\theta-0}}{1+e^{\theta-0}}$

Item dif 1.5: $\frac{e^{\theta+1.5}}{1+e^{\theta+1.5}}$

- Can you plot this as a function of θ ?

```
th<-seq(-3,3,length.out=1000)
p<-function(b) exp(th-b)/(1+exp(th-b))

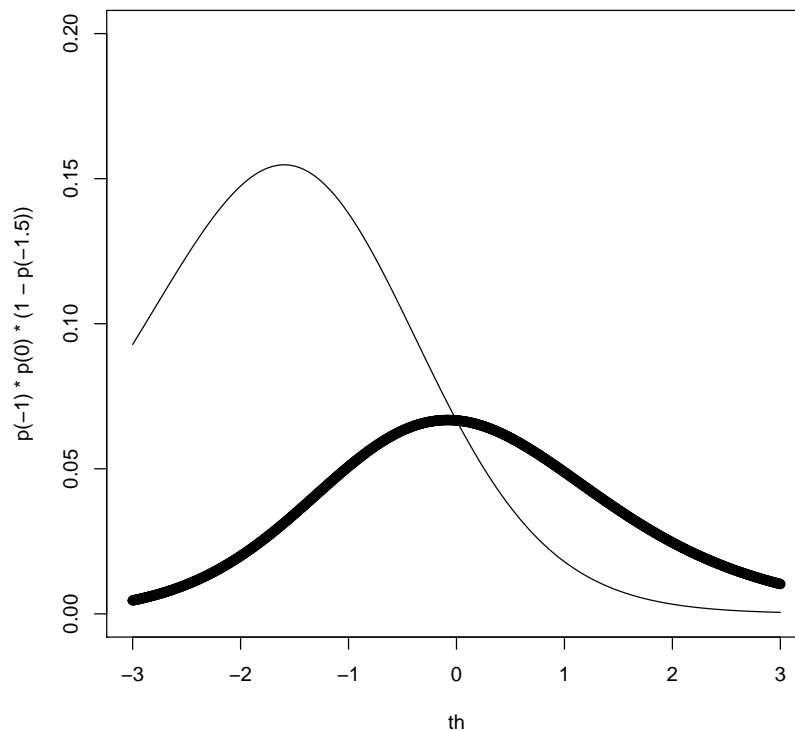
plot(th,p(-1)*p(0)*(1-p(-1.5)), ylim = c(0,.2)) # question 4
```



14

- 15 3. If $\theta=0.5$, what is the likelihood of that response sequence?
- 16 4. If $\theta=0.5$, what is the most likely response sequence given the known
- 17 item difficulties?
- 18 5. At what value of θ does a response sequence of 1-1-0 (that is: they got
- 19 the first and second items right and the third item wrong) become more
- 20 likely than a response sequence of 1-0-0?

```
plot(th,p(-1)*p(0)*(1-p(-1.5)), ylim = c(0,.2))
lines(th,p(-1)*(1-p(0))*(1-p(-1.5))) # question 5
```



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22 6. Returning to questions 1 and 2, can you plot the "test information" as a
 23 function of theta (see Eqn 2-6 in Lord).

24 Sum of information function $\sum IIF = TIF$

25 7. Where is the function in #6 maximized? What do you think this implies?

26 8. For an item response dataset of your choosing, consider the relationship
 27 between theta and the SE across the three IRT models for dichotomous
 28 items. How much of a difference does the choice of model have on the size
 29 of the error estimate?