

### Question:

```
122 Eigen::MatrixXd waypoints = TransformGlobleToLocal(px, py, psi, ptsx, ptsy);
123 Eigen::VectorXd local_ptsx = waypoints.row(0);
124 Eigen::VectorXd local_ptsy = waypoints.row(1);
125
126 // fit polynimial
127 Eigen::VectorXd coeffs = polyfit(local_ptsx, local_ptsy, 3);
128 double cte = polyeval(coeffs, 0);
129 double epsi = -atan(coeffs[1]); // x=0 position
130
131 //consoder delay 0.1
132 double delay_t = 0.1;
133 double x_delay = 0 + v * cos(psi) * delay_t;
```

#### REQUIRED

As you mention in line 129,  $x=0$  in car coordinate, so is  $\psi$  but you're still using  $\psi$  from global coordinate which can be large number despite the car is driving in straight line.

I don't get your point here, I think I have already transfer to vehicle coordinate.

### CarModel:

The car model is a bicycle model which consists of 6 variables:  $[x, y, \psi, v, cte, \epsilon]$ . They are  $x$  and  $y$  vehicle position, vehicle orientation, vehicle speed, cross track error and orientation error. To measure the constrains, the model has been transformed to the following equations.

```
fg[1 + x_start + t] = x1 - (x0 + v0 * CppAD::cos(psi0) * dt);
fg[1 + y_start + t] = y1 - (y0 + v0 * CppAD::sin(psi0)*dt);
fg[1 + psi_start + t] = psi1 - (psi0 - v0 * delta0 / Lf * dt); //modify turn direction as mentioned
fg[1 + v_start + t] = v1 - (v0 + a0 * dt);
fg[1 + cte_start + t] = cte1 - ((f0 - y0) + v0 * CppAD::sin(epsi0)*dt);
fg[1 + epsi_start + t] = epsi1 - ((psi0 - psides0) - v0 * delta0 / Lf * dt); //modify turn direction as mentioned
```

$L_f$  measures the distance between the front of the vehicle and its mass center.  $f_0$  is the evaluation of the polynomial  $f$  at point  $x_0$  and  $\psi_{sides0}$  is the tangential angle of the polynomial  $f$  evaluated at  $x_0$ .

### Timestep Length and Elapsed Duration (N & dt)

The number  $N$  determines the number of variables optimized by the controller. So, higher  $N$  will result in extra computational cost. Here is the code for time consuming.

```
start = clock();
count++;
vector<double> result = mpc.Solve(state, coeffs);
stop = clock();
durationTime += ((double)(stop - start)) / CLOCKS_PER_SEC;
if (count == 10){
    std::cout << "Time consume" << durationTime << std::endl;
}
```

N	dt	Time consume(10 times)	Path follow stable
5	0.1	0.146	Unable to follow
10	0.1	0.284	yes

15	0.1	0.416	Unable to follow
20	0.1	1.57	Unable to follow
10	0.05	0.264	Yes but less stable
10	0.15	0.4137	Yes but less stable
10	0.2	0.628	Yes but less stable
5	0.2	0.13	Unable to follow

It was found that if  $N * dt$  is too low, the vehicle will oscillate around the lane center. If  $N * dt$  is too high, the prediction period is too long and the vehicle may leave the sharp turn.

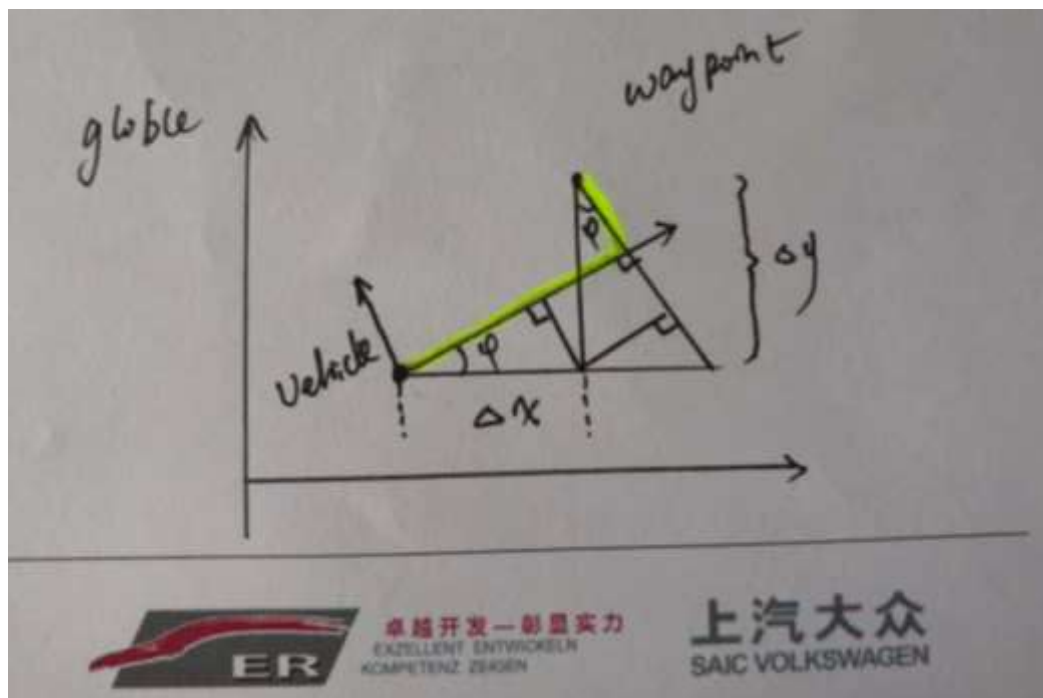
If  $N$  is too high, the computational time increase, and so long time may lead to unable to follow. if  $N$  is too low, the MPC curve becomes too volatile for the car to be able to drive.

The influence of  $dt$  is not observed that clear.

The conclusion above may also be affected by other parameters I choose, like the parameters of cost functions and the speed to follow. And I guess the main reason for my first question is because the speed chosen, when I turn the value from 45 to 20, it becomes much better. Since the predicted position is more accurate in short distance.

### Polynomial Fitting and MPC Preprocessing

Before fitting the path returned from the simulator, we have to transfer the waypoints from global position to vehicle coordinate.



```

Eigen::MatrixXd TransformGlobalToLocal(double x, double y, double psi, const vector<double> &ptsx, const vect
    assert(ptsx.size() == ptsy.size());
    int len = ptsx.size();
    Eigen::MatrixXd waypoints(2, len);
    for (int i = 0; i < len; i++) {
        waypoints(0, i) = cos(psi) * (ptsx[i] - x) + sin(psi) * (ptsy[i] - y);
        waypoints(1, i) = -sin(psi) * (ptsx[i] - x) + cos(psi) * (ptsy[i] - y);
    }
    return waypoints;
}

```

## Model Predictive Control with Latency

Latency was considered in the main function. The next state was predicted before calling the MPC solve by using vehicle model.

```

//consider delay 0.1
double delay_t = 0.1;
double x_delay = 0 + v * cos(psi) * delay_t;
double y_delay = 0 + v * sin(psi) * delay_t;
double psi_delay = 0 - v * delta / 2.67 * delay_t; //modify turn directic
double v_delay = v + a * delay_t;
double cte_delay = (cte - 0) + v * sin(epsi)*delay_t;
double epsi_delay = epsi - v * delta / 2.67 * delay_t;

Eigen::VectorXd state(6);
state << x_delay, y_delay, psi_delay, v_delay, cte_delay, epsi_delay;

```