Markov Chain Monte Carlo algorithm

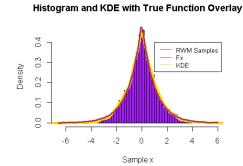
Clement KK Tan 2024-01-06

R Markdown for Part A Sample Mean and Deviation and Part B Chain Values Description of Markov Chain Monte Carlo Algorithm

The purpose of this algorithm is to generate and simulate random numbers generated in the distribution theory for the probability density function given. The answers for Parts A and B are given in this 1-page report. The histograms and KDEs and the plot of bR over a grid of s-values are shown in R markdown and Python which indicate the graphs in both coding files are generally consistent in shapes.

Part A

| Sample Mean: (R markdown) | 0.02920703 |
|---|------------|
| Sample Standard Deviation: (R markdown) | 1.262088 |



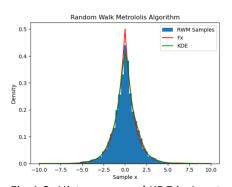


Fig.1.1: Histogram and KDE in R markdown

Fig.1.2: Histogram and KDE in Jupyter Python

Part B (Chain, Initial Value, Mj and Vj derived from R markdown codes)

| Chain Number | Initial Value | Sample Mean Mj | Within Sample Variance Vj |
|---------------------|---------------|----------------|---------------------------|
| Chain 1 | -1.36 | -29.86 | 485.46 |
| Chain 2 | -0.25 | -35.97 | 670.03 |
| Chain 3 | 0.49 | -17.69 | 231.78 |
| Chain 4 | 0.43 | 10.64 | 780.27 |

| Overall Within Sample Variance (W): (R markdown) | 541.88 |
|---|--------|
| Overall Sample Mean (M): (R markdown) | -18.22 |
| Overall Between Sample Variance (B): (R markdown) | 320.97 |
| Convergence diagnostics R Value: (R markdown) | 1.26 |

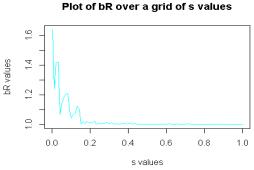


Fig.1.3: Plot of bR graph in R markdown

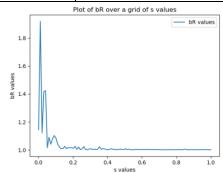


Fig.1.4: Plot of bR graph in Jupyter Python