



Secondary analysis

in gene expression studies

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Secondary analysis



Getting an expression matrix

- Assume bulk gene expression
- Microarray: itensities -> probe/gene symbol mapping -> gene expression matrix
- RNA-seq: raw reads -> alignments -> quantification -> gene expression matrix



Gene expression matrix

Rows are genes

. . .

- Columns are samples
- We assume columns to be somewhat normalized, so gene expression levels are representative across all samples

```
GSM3703675 GSM3703676 GSM3703677 GSM3703678 GSM3703679 GSM3703680 GSM3703681 GSM3703682
Dhx36
          6.868925
                                 7.265303
                                            7.711423
                                                                              7.782933
                     7.802883
                                                        7.925366
                                                                   8.064470
                                                                                          7.878214
Arl6ip4
          8.610726
                     8.349129
                                 8.961090
                                            8.863572
                                                       8.210400
                                                                   8.298973
                                                                              8.612580
                                                                                          8.380108
                                 9.782122
                                            9.205673
Tram1
          8.117650
                     7.725020
                                                        8.632618
                                                                   8.403167
                                                                              10.311316
                                                                                          9.872407
Mir425
                                 5.128062
                                            4.936080
                                                                   4.785895
                                                                              4.397090
          4.124838
                     4.674299
                                                       4.404071
                                                                                          4.670425
Pex6
          8.295669
                     8.071793
                                 7.823910
                                            8.110941
                                                        7.758333
                                                                   7.989627
                                                                              7.529114
                                                                                          7.686020
          8.768137
                                 9.358366
                                            9.096089
                                                        8.752107
                                                                   8,696490
                                                                              9.641165
                                                                                          9.123614
Nans
                     8,620869
```

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Once we have an expression matrix

Conceptual analysis steps are the same:

- Quality controls: PCA + outlier/batch removal if needed
- Differential expression design
- Performing differential expression
- DE genes: looking for possible biological pathways, transcriptional factors, regulators...



Sources of variance

It is important to identify sources of gene expression variance

- Variation included by design: cell type, treatment, cases vs controls
- Biological sources of variation: cell cycle, sex of mice/donor, cell types present in the sample
- Unwanted variaton: batch effect, donor effect
- Technical variation: microarray variation, sequencing variation



libraries

```
if (!requireNamespace("BiocManager", quietly = TRUE)) install.packages("BiocManager")
if (!requireNamespace("ggplot2", quietly = TRUE)) install.packages("ggplot2")
if (!requireNamespace("pheatmap", quietly = TRUE)) install.packages("pheatmap")
if (!requireNamespace("RColorBrewer", quietly = TRUE)) install.packages("RColorBrewer")
if (!requireNamespace("ggrepel", quietly = TRUE)) install.packages("ggrepel")
if (!requireNamespace("dplyr", quietly = TRUE)) install.packages("dplyr")

if (!requireNamespace("limma", quietly = TRUE)) BiocManager::install("limma")
if (!requireNamespace("Biobase", quietly = TRUE)) BiocManager::install("Biobase")
if (!requireNamespace("sva", quietly = TRUE)) BiocManager::install("sva")
if (!requireNamespace("fgsea", quietly = TRUE)) BiocManager::install("fgsea")
```



```
library(Biobase)
library(limma)
library(sva)
library(ggplot2)
library(pheatmap)
library(RColorBrewer)
library(ggrepel)
library(ggrepel)
library(fgsea)
blueWhiteRed <- colorRampPalette(c("#3859A8", "#EEEEEEE", "#EE2930"))(10)
load("gse129260.Rdata")</pre>
```



head(exprs(gse129260))

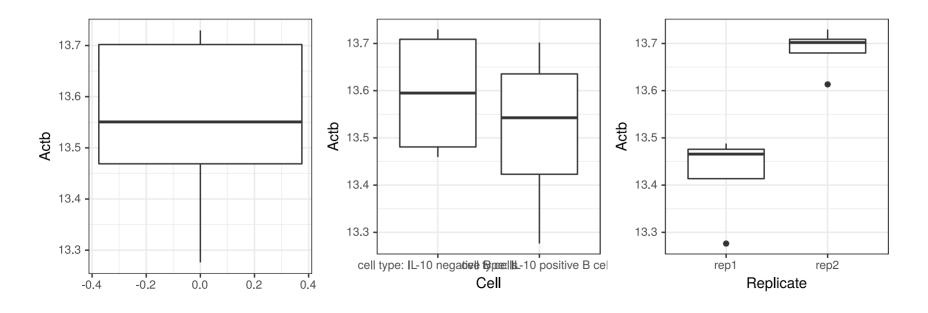
```
##
         GSM3703675 GSM3703676 GSM3703677 GSM3703678 GSM3703679 GSM3703680
                                                             13.76204
## Rps29
         13.76204
                    13.83782
                               13.72959
                                         13.76204
                                                   13.97115
                                                 13.72959
## Rpl37a 13.54983
                   13.70194
                               13.64128
                                         13.64128
                                                             13.79243
## Rplp2 13.62928
                   13.68329
                               13.65993
                                         13.68329
                                                  13.65993
                                                             13.68329
## Tpt1 13.64128
                                                             13.65993
                   13.65993
                               13.59760
                                         13.62928 13.76204
## Rpl41 13.53492
                   13.50823
                               13.61335 13.56125
                                                  13.52919
                                                             13.54983
## Eef1a1 13.68329
                                                             13.58597
                     13.66878
                               13.46390
                                         13.54537
                                                   13.53492
##
         GSM3703681 GSM3703682
## Rps29
         13.68329
                     13.76204
## Rpl37a 13.72959
                   13.79243
## Rplp2
         13.65993
                     13.65993
## Tpt1 13.64128
                    13.62928
## Rpl41 13.59760
                    13.64128
## Eef1a1 13.49293
                     13.47191
```



```
someGenes <- exprs(gse129260)[c("Actb", "Ddx3y", "Il10"), ]</pre>
 plotData <- t(someGenes)</pre>
 plotData <- as.data.frame(plotData)</pre>
 plotData <- cbind(plotData, pData(gse129260))</pre>
head(plotData, 4)
##
                          Ddx3v
                                     Il10
                                                                         Cell
                  Actb
## GSM3703675 13.47191 7.674220 12.655218 cell type: IL-10 positive B cells
## GSM3703676 13.45945 6.702041 9.000712 cell type: IL-10 negative B cells
## GSM3703677 13.27625 7.122010 11.919731 cell type: IL-10 positive B cells
## GSM3703678 13.48798 6.043041 9.508046 cell type: IL-10 negative B cells
##
                           Treatment Replicate
## GSM3703675 stimulation: anti-CD40
                                           rep1
## GSM3703676 stimulation: anti-CD40
                                           rep1
## GSM3703677 stimulation: LPS
                                           rep1
## GSM3703678 stimulation: LPS
                                           rep1
```

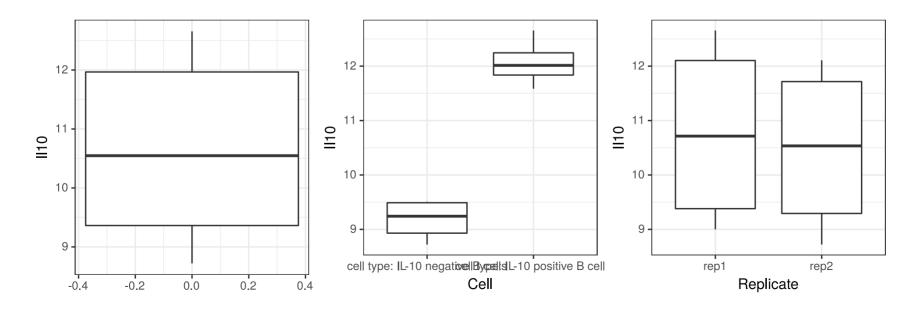


```
ggplot(plotData, aes(y=Actb)) +
  geom_boxplot() + theme_bw()
ggplot(plotData, aes(x=Cell, y=Actb)) +
  geom_boxplot() + theme_bw()
ggplot(plotData, aes(x=Replicate, y=Actb)) +
  geom_boxplot() + theme_bw()
```



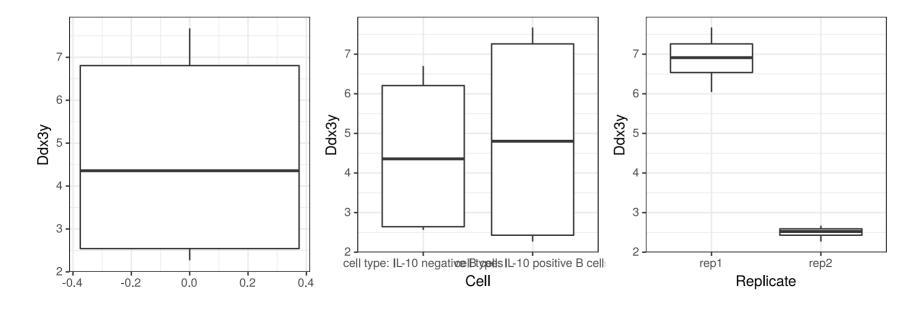


```
ggplot(plotData, aes(y=Il10)) +
  geom_boxplot() + theme_bw()
ggplot(plotData, aes(x=Cell, y=Il10)) +
  geom_boxplot() + theme_bw()
ggplot(plotData, aes(x=Replicate, y=Il10)) +
  geom_boxplot() + theme_bw()
```





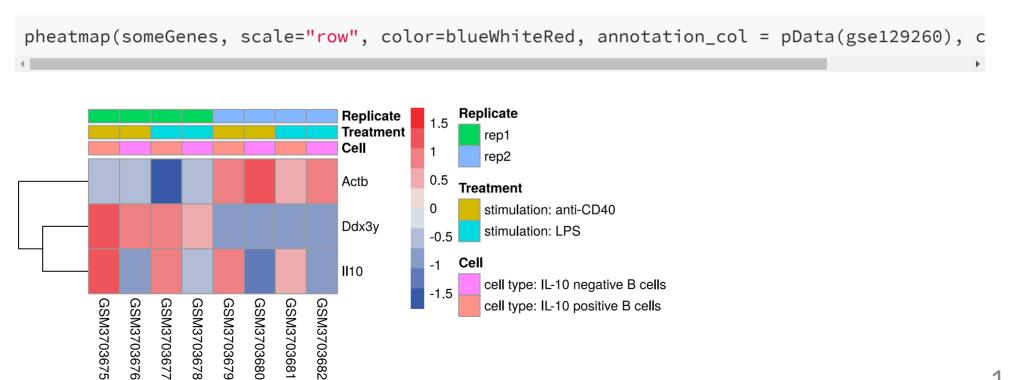
```
ggplot(plotData, aes(y=Ddx3y)) +
  geom_boxplot() + theme_bw()
ggplot(plotData, aes(x=Cell, y=Ddx3y)) +
  geom_boxplot() + theme_bw()
ggplot(plotData, aes(x=Replicate, y=Ddx3y)) +
  geom_boxplot() + theme_bw()
```





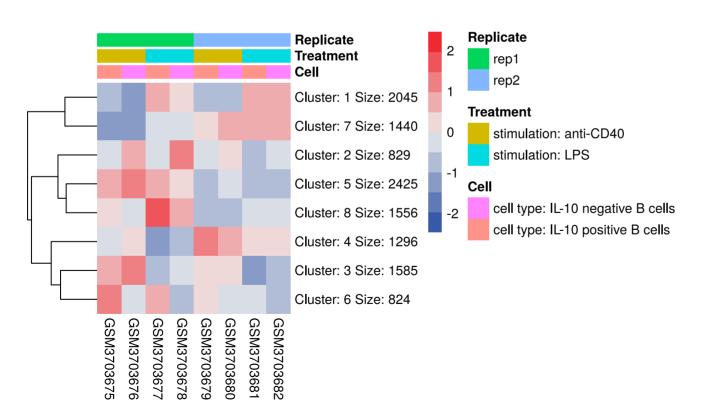
Heatmaps:

In gene set expression studies we usually use heatmaps to visualize expression levels:





Heatmaps: clustered



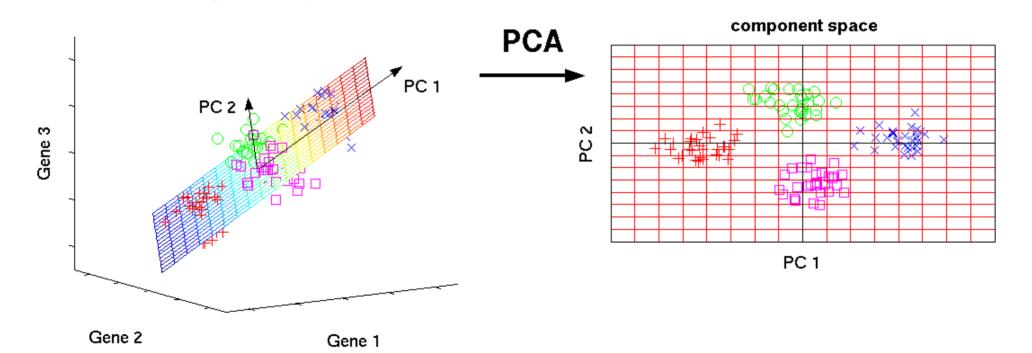


PCA (principal component analysis):

- PCA puts samples in new space
- Principal components (new coordinates) explain as much variance as possible in original space
- Samples in original space are far from each other if a lot of genes are differentially expressed between them



original data space

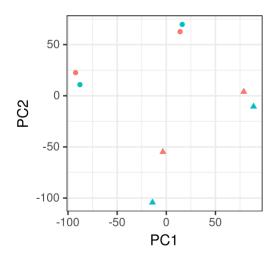




```
pcas <- prcomp(t(exprs(gse129260)), scale. = T)
plotData <- cbind(pcas$x[, 1:2], pData(gse129260))</pre>
```



```
ggplot(plotData, aes(x=PC1, y=PC2, color=Cell, shape=Treatment)) +
  geom_point() + theme_bw() + theme(aspect.ratio = 1)
ggplot(plotData, aes(x=PC1, y=PC2, color=Replicate, shape=Treatment)) +
  geom_point() + theme_bw() + theme(aspect.ratio = 1)
```

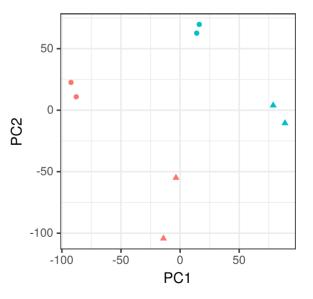


Treatment

- stimulation: anti-CD40
- ▲ stimulation: LPS

Cell

- cell type: IL-10 negative B cells
- cell type: IL-10 positive B cells



Replicate

- rep1
- rep2

Treatment

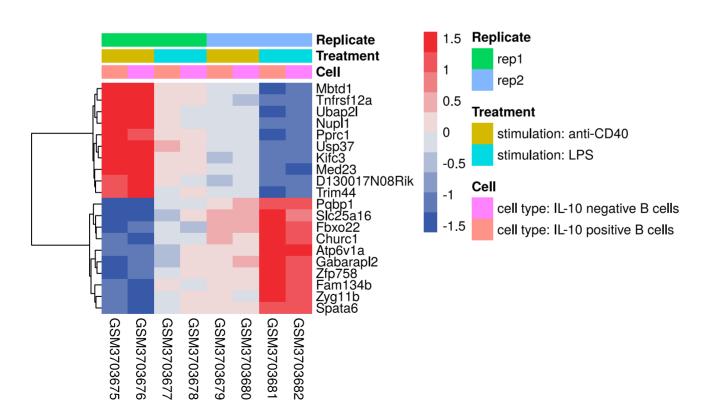
- stimulation: anti-CD40
- ▲ stimulation: LPS



```
rotation <- pcas$rotation
 PC1GenesDown <- head(rownames(rotation[order(rotation[, 1]), ]), 10)</pre>
 PC1GenesUp <- tail(rownames(rotation[order(rotation[, 1]), ]), 10)</pre>
print(PC1GenesDown)
##
    [1] "Usp37"
                         "Kifc3"
                                          "Pprc1"
                                                           "Mbtd1"
    [5] "Tnfrsf12a"
                         "D130017N08Rik" "Ubap2l"
                                                          "Nupl1"
    [9] "Med23"
                         "Trim44"
##
print(PC1GenesUp)
                     "Atp6v1a"
                                 "Fbxo22"
                                              "Pabp1"
                                                           "Slc25a16"
##
    [1] "Zyg11b"
##
    [6] "Gabarapl2" "Fam134b"
                                 "Churc1"
                                              "Zfp758"
                                                           "Spata6"
```



Heatmaps: PC1 genes

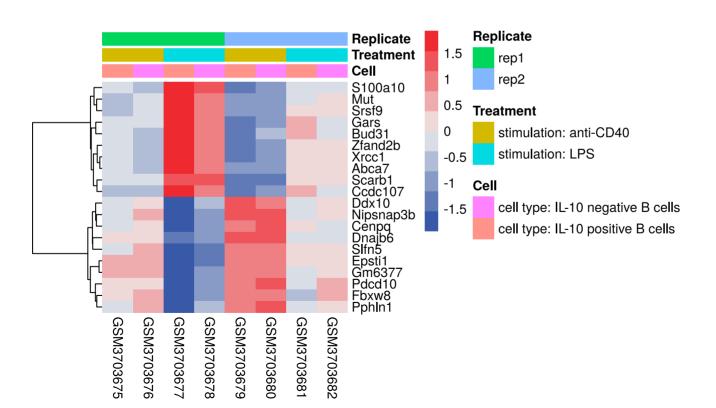




```
rotation <- pcas$rotation
PC2GenesDown <- head(rownames(rotation[order(rotation[, 2]), ]), 10)</pre>
 PC2GenesUp <- tail(rownames(rotation[order(rotation[, 2]), ]), 10)</pre>
 print(PC2GenesDown)
##
    [1] "Xrcc1"
                  "Abca7"
                            "Mut"
                                       "S100a10" "Gars" "Scarb1" "Zfand2b"
##
    [8] "Bud31"
                  "Ccdc107" "Srsf9"
print(PC2GenesUp)
                    "Pdcd10"
                                 "Fbxw8"
                                             "Dnajb6"
    [1] "Epsti1"
                                                          "Gm6377"
##
##
    [6] "Slfn5"
                    "Ddx10"
                                 "Nipsnap3b" "Pphln1"
                                                          "Cenpq"
```



Heatmaps: PC2 genes





Can we remove unwanted sources of variance?

In our experiment we wanted to get variance from Treatment + Cell type

- Can we identify sources of unwanted variance?
- If we know source of variance, can we remove it?



Batch correction: ComBat from SVA

SVA package:

- Allows to identify latent variables
- Allows to remove unwanted variance (ComBat)
- "Adjusting batch effects in microarray expression data using empirical Bayes methods"



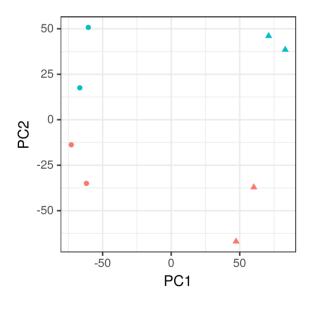
Batch correction: ComBat

```
batch <- pData(gse129260)$Replicate</pre>
 modcombat <- model.matrix(~1, data=pData(gse129260))</pre>
 combat_gse129260 = ComBat(dat=exprs(gse129260), batch=batch, mod=modcombat)
## Found2batches
## Adjusting for0covariate(s) or covariate level(s)
## Standardizing Data across genes
## Fitting L/S model and finding priors
## Finding parametric adjustments
## Adjusting the Data
```



Batch correction: ComBat

```
pcas <- prcomp(t(combat_gse129260), scale. = T)
plotData <- cbind(pcas$x[, 1:2], pData(gse129260))
ggplot(plotData, aes(x=PC1, y=PC2, color=Cell, shape=Treatment)) +
  geom_point() + theme_bw() + theme(aspect.ratio = 1)</pre>
```



Treatment

- stimulation: anti-CD40
- ▲ stimulation: LPS

Cell

- cell type: IL-10 negative B cells
- cell type: IL-10 positive B cells



##

GSM3703675 stimulation: anti-CD40

GSM3703676 stimulation: anti-CD40

GSM3703677 stimulation: LPS

GSM3703679 stimulation: anti-CD40

GSM3703680 stimulation: anti-CD40

GSM3703678

rep1

rep1

rep1

rep1

rep2

rep2

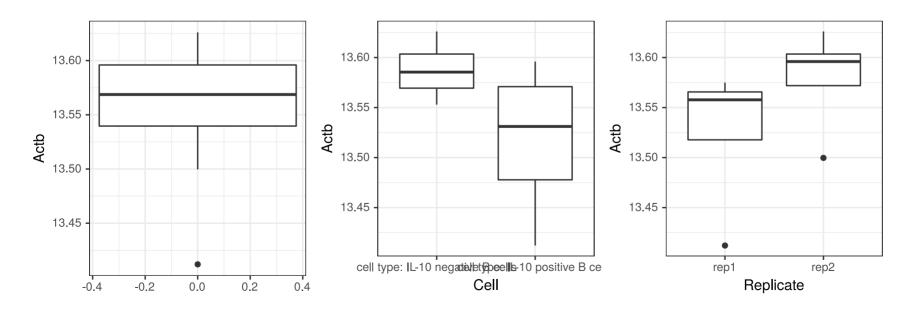
GSM3703679 13.59598 4.334017 12.307073 cell type: IL-10 positive B cells ## GSM3703680 13.62604 4.532145 8.903688 cell type: IL-10 negative B cells

Treatment Replicate

stimulation: LPS

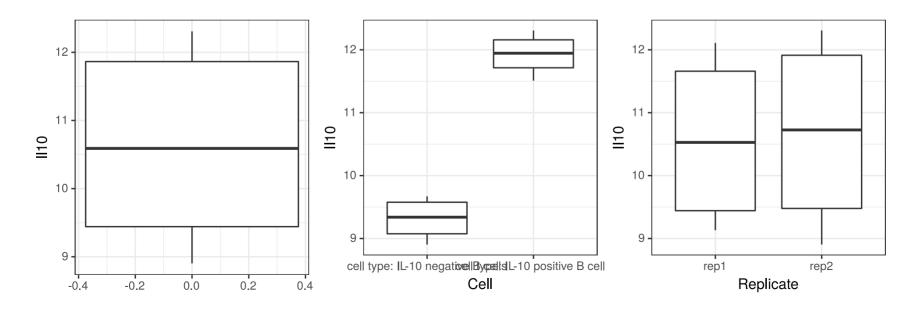


```
ggplot(plotData, aes(y=Actb)) +
  geom_boxplot() + theme_bw()
ggplot(plotData, aes(x=Cell, y=Actb)) +
  geom_boxplot() + theme_bw()
ggplot(plotData, aes(x=Replicate, y=Actb)) +
  geom_boxplot() + theme_bw()
```



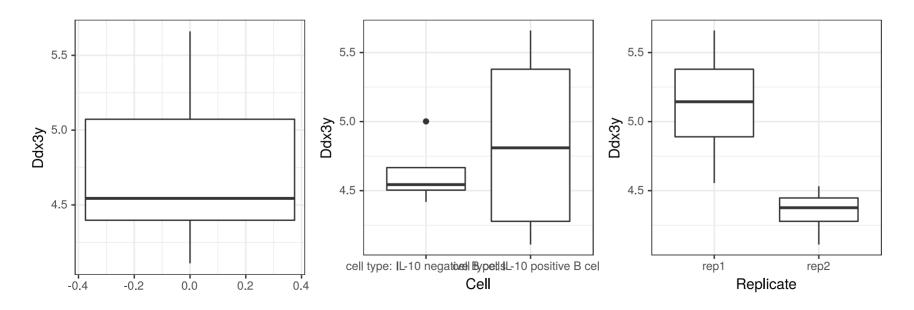


```
ggplot(plotData, aes(y=Il10)) +
  geom_boxplot() + theme_bw()
ggplot(plotData, aes(x=Cell, y=Il10)) +
  geom_boxplot() + theme_bw()
ggplot(plotData, aes(x=Replicate, y=Il10)) +
  geom_boxplot() + theme_bw()
```





```
ggplot(plotData, aes(y=Ddx3y)) +
  geom_boxplot() + theme_bw()
ggplot(plotData, aes(x=Cell, y=Ddx3y)) +
  geom_boxplot() + theme_bw()
ggplot(plotData, aes(x=Replicate, y=Ddx3y)) +
  geom_boxplot() + theme_bw()
```





Variance

- Varince in transcriptional data comes from both signal and noise
- In ideal scenario the only source of variance is included by your experimental design
- In reality: batch effect, donor effect (super common for human data)
- We can remove unwanted sources of variance if they introduce too much variance



Once we have an expression matrix

Conceptual analysis steps are the same:

- Quality controls: PCA + outlier/batch removal if needed
- Differential expression design
- Performing differential expression
- DE genes: looking for possible biological pathways, transcriptional factors, regulators...



Linear models

The most simple linear models are:

$$y = kx + b$$

- We know both y and x and we try to predict k and b
- ullet Usually both x and y are numeric



Linear models: x can be factor

Let's look at expression of gene Il10

$$y = k_{pos} x_{pos} + k_{neg} x_{neg}$$

where

- $x_{pos}=1$ and $x_{neg}=0$ if sample is //10-positive
- $x_{pos}=0$ and $x_{neg}=1$ if sample is //10-negative.



Linear models:

```
model_simple <- model.matrix(~0 + Cell, data = pData(gse129260))
colnames(model_simple) <- c("Negative", "Positive")
model_simple</pre>
```



Linear models:

```
exprs(gse129260)["Il10", ]
## GSM3703675 GSM3703676 GSM3703677 GSM3703678 GSM3703679 GSM3703680
## 12.655218
               9.000712 11.919731 9.508046 12.107867 8.721228
## GSM3703681 GSM3703682
## 11.585481 9.483412
linear_fit <- lm.fit(model_simple, exprs(gse129260)["Il10", ])</pre>
linear_fit$coef
## Negative Positive
## 9.178349 12.067074
```



Linear models:

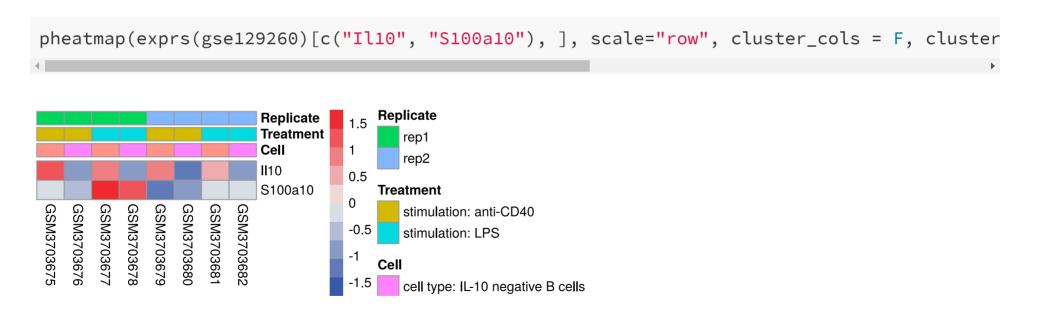
We can model expression of Il10 gene as:

- Il10 = 9.178349 if sample is II10 negative
- Il10=12.067074 if sample is II10 positive



More complicated linear models

- Il10 can be well-modeled with single factor variable
- Let's look at S100a10 gene





Linear models: Treatment

```
treatment_model <- model.matrix(~0 + Treatment, data = pData(gse129260))
colnames(treatment_model) <- c("aCD-40", "LPS")
treatment_model</pre>
```



Linear models: Treatment + Replicate

```
treatment_rep_model <- model.matrix(~0 + Treatment + Replicate, data = pData(gse129260))
colnames(treatment_rep_model) <- c("aCD-40", "LPS", "Rep2")
treatment_rep_model</pre>
```

```
##
              aCD-40 LPS Rep2
## GSM3703675
                            0
## GSM3703676
## GSM3703677
                            0
## GSM3703678
                            0
                            1
## GSM3703679
## GSM3703680
## GSM3703681
## GSM3703682
## attr(,"assign")
## [1] 1 1 2
## attr(,"contrasts")
## attr(,"contrasts")$Treatment
## [1] "contr.treatment"
##
## attr(,"contrasts")$Replicate
## [1] "contr.treatment"
```



Linear models:

```
exprs(gse129260)["S100a10", ]

## GSM3703675 GSM3703676 GSM3703677 GSM3703678 GSM3703679 GSM3703680

## 9.514830 9.427012 10.549706 10.256628 8.977444 9.178550

## GSM3703681 GSM3703682

## 9.569274 9.572045

linear_fit <- lm.fit(treatment_rep_model, exprs(gse129260)["S100a10", ])

linear_fit$coef</pre>

## aCD-40 LPS Rep2

## 9.580817 10.293271 -0.612716
```



Linear models: Treatment + Replicate

- Including several variables in the design allows us to calculate effects for each variable
- First variable is usually a target for differential expression
- Only the first variable will have both 0/1 effect calculated



Linear models: full model

```
full_model <- model.matrix(~0 + Treatment + Cell + Replicate, data = pData(gse129260))
colnames(full_model) <- c("aCD-40", "LPS", "Il10pos", "Rep2")
full_model</pre>
```

```
##
              aCD-40 LPS Il10pos Rep2
## GSM3703675
## GSM3703676
## GSM3703677
## GSM3703678
## GSM3703679
## GSM3703680
## GSM3703681
## GSM3703682
## attr(,"assign")
## [1] 1 1 2 3
## attr(,"contrasts")
## attr(,"contrasts")$Treatment
## [1] "contr.treatment"
##
## attr(,"contrasts")$Cell
## [1] "contr.treatment"
```



Linear models: full model

```
linear_fit <- lm.fit(full_model, exprs(gse129260)["Il10", ])</pre>
linear_fit$coef
                            Il10pos
##
      aCD-40
                    LPS
                                          Rep2
## 9.3251086 9.3280201 2.8887248 -0.2964297
linear_fit <- lm.fit(full_model, exprs(gse129260)["S100a10", ])</pre>
linear_fit$coef
##
      aCD-40
                    LPS
                            Il10pos
                                          Rep2
## 9.5586898 10.2711438 0.0442547 -0.6127160
```



Linear models: full model with 1

```
full_model <- model.matrix(~1 + Treatment + Cell + Replicate, data = pData(gse129260))
colnames(full_model) <- c("Intercept", "LPS", "Il10pos", "Rep2")
full_model</pre>
```

```
##
              Intercept LPS Il10pos Rep2
## GSM3703675
## GSM3703676
## GSM3703677
## GSM3703678
## GSM3703679
## GSM3703680
## GSM3703681
## GSM3703682
## attr(,"assign")
## [1] 0 1 2 3
## attr(,"contrasts")
## attr(,"contrasts")$Treatment
## [1] "contr.treatment"
##
## attr(,"contrasts")$Cell
## [1] "contr.treatment"
```



Linear models: full model with 1



Linear models

- Linear models are usefull for calculating effects of variables
- ~ 0 + Annotation1 + Annotation2 ... will calculate means for both factors in Annotation1, and calculate effects for other annotations (excluding Annotation1)
- ~ 1 + Annotation1 + Annotation2 ... will calculate means for one the Annotation1 factors, and calculate effects for all annotations (including remaining factor in Annotation1)



Once we have an expression matrix

Conceptual analysis steps are the same:

- Quality controls: PCA + outlier/batch removal if needed
- Differential expression design
- Performing differential expression
- DE genes: looking for possible biological pathways, transcriptional factors, regulators...



Performing DE (differential expression)

- Performing DE is usually much easier than designing proper DE:)
- We will use limma in this example
- Let's check which design get more results



Performing limma

```
cell_full_model <- model.matrix(~0 + Cell + Treatment + Replicate, data=pData(gse129260))
colnames(cell_full_model) <- c("ill0neg", "il10pos", "LPS", "rep2")

fit <- lmFit(gse129260, cell_full_model)

fit2 <- contrasts.fit(fit, makeContrasts(il10pos - il10neg, levels=cell_full_model))
fit2 <- eBayes(fit2, trend = T)

de <- topTable(fit2, adjust.method="BH", number=Inf, sort.by = "P")</pre>
```



Differential expression

```
head(de)
```

```
##
                     ID Gene.symbol Gene.ID mean_expression
                                                                logFC
## Cd9
             1416066 at
                               Cd9
                                      12527
                                                  9.408102
                                                            1.2672152
## Il10
             1450330 at
                               Il10 16153
                                                 10.622712
                                                            2.8887248
## Mzb1
             1428947 at
                               Mzb1
                                     69816
                                                 10.836028 0.9663412
## Pon3
             1419298 at
                               Pon3 269823
                                                  5.266634 1.5167428
             1455530 at Ighv14-2 668421
## Ighv14-2
                                                  7.709365 -2.0150553
                                Mt1 17748
## Mt1
           1422557 s at
                                                  9.510878 1.7284823
##
             AveExpr
                                     P.Value
                                              adj.P.Val
                              t
## Cd9
            9.408102 13.164815 3.503802e-07 0.002167242 6.623000
## Il10
           10.622712 12.644593 4.950996e-07 0.002167242 6.368938
## Mzb1
           10.836028 12.512033 5.418104e-07 0.002167242 6.301640
## Pon3
         5.266634 11.570981 1.054446e-06 0.002874045 5.791615
## Ighv14-2 7.709365 -11.398509 1.197519e-06 0.002874045 5.691623
## Mt1
            9.510878
                       9.946067 3.758758e-06 0.006867570 4.758682
```



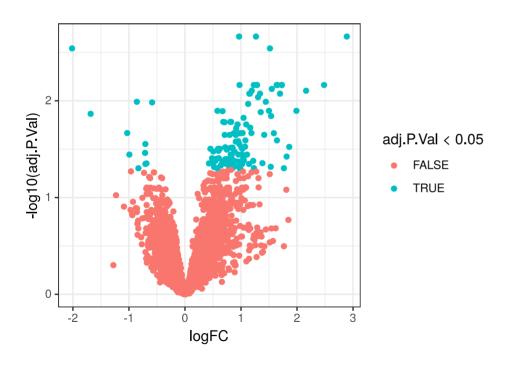
Volcano plot

- Volcano plot is the usual way to display DE results
- X axis is log fold change showing the direction of the change
- Y axis is -log10(p adjusted) showing the significane of DE



DE: Volcano plot

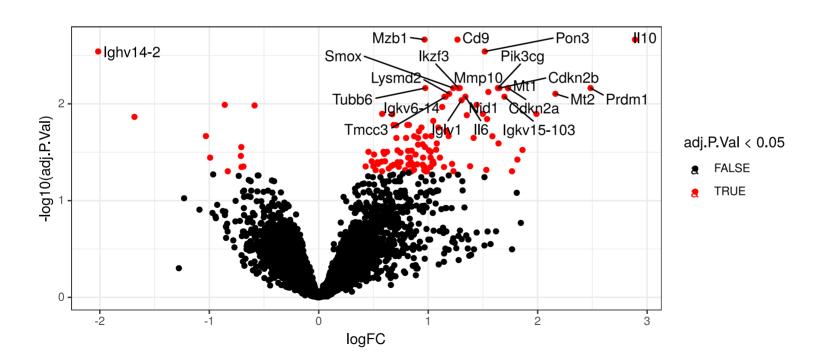
```
ggplot(de, aes(x=logFC, y=-log10(adj.P.Val), color=adj.P.Val < 0.05)) +
  geom_point() + theme_bw()</pre>
```





DE: Volcano plot (fancy)

```
ggplot(de, aes(x=logFC, y=-log10(adj.P.Val), color=adj.P.Val < 0.05)) +
  geom_point() + theme_bw() + scale_color_manual(values=c("black", "red")) +
  geom_text_repel(data=de %>% dplyr::filter(adj.P.Val < 0.01), aes(label=Gene.symbol, col</pre>
```





Performing limma: bad model

```
cell_bad_model <- model.matrix(~0 + Cell, data=pData(gse129260))
colnames(cell_bad_model) <- c("ill0neg", "ill0pos")

fit_bad <- lmFit(gse129260, cell_bad_model)

fit_bad2 <- contrasts.fit(fit_bad, makeContrasts(ill0pos - ill0neg, levels=cell_bad_model
fit_bad2 <- eBayes(fit_bad2, trend = T)

de_bad <- topTable(fit_bad2, adjust.method="BH", number=Inf, sort.by = "P")</pre>
```



Comparing results

```
de %>% filter(adj.P.Val < 0.05) %>% count()
## # A tibble: 1 x 1
##
        n
##
   <int>
## 1 124
de_bad %>% filter(adj.P.Val < 0.05) %>% count()
## # A tibble: 1 x 1
##
##
   <int>
## 1
```



Differential expression

- Good design empowers you to find differences that you want to find in your data
- Design with a smaller number of variables ignores additional information and assumes samples in a group to be the same
- Design with a smaller number of variables is still something you might want to do



Once we have an expression matrix

Conceptual analysis steps are the same:

- Quality controls: PCA + outlier/batch removal if needed
- Differential expression design
- Performing differential expression
- DE genes: looking for possible biological pathways, transcriptional factors, regulators...



- In most cases gene expression changes are not coming one gene by one
- Genes that are changed are regulated by biological processes (pathways)
- We have bunch of databases that describe gene sets: sets of genes that regulate or regulated by biological process
- Technically speaking, for us pathway is just a set of genes



- Pathways
- GO terms
- Targets of transcriptional factors
- Gene sets produced by other datasets



Let's didcuss terms firts:

• Universe: genes that are expressed in the dataset (in our case size of the universe 12000):

$$U = \{g_1, g_2, \dots, g_n\}, \ \ |U| = n \approx 12000$$

• We have N pathways:

$$P_i = \{g_{i,1}, g_{i,2}, \dots, g_{i,m_i}\} \ |P_i| = m_i, \;\; g_{i,j} \in U$$



- We have results of our DE
- "Pathway behaves non-random" = "Genes from pathways are not changing randomly"
- We want to identify pathways that behave non-random in our DE results



Simple implementation: exact Fisher test

Exact Fisher test (or hypergeometric test)

- We only choose significantly expressed genes
- We test overlaps of these genes with pathway
- Identify if overlap is random



Loading kegg Pathways

```
load("keggSymbolMouse.rdata")
 upRegulatedGenes <- de %>% filter(adj.P.Val < 0.05 & logFC > 0) %>% pull("Gene.symbol")
 length(upRegulatedGenes)
## [1] 113
 randomGeneSet <- keggSymbolMouse[["Cardiac muscle contraction - Mus musculus (mouse)"]]</pre>
 randomGeneSet <- randomGeneSet[randomGeneSet %in% rownames(de)]
 length(randomGeneSet)
## [1] 41
 length(intersect(randomGeneSet, upRegulatedGenes))
## [1] 1
```



Hypergeometric test

https://en.wikipedia.org/wiki/Hypergeometric_distribution

- N = 12000: total number of genes (TOTAL)
- K = 41: number of genes in pathway (SUCCESSES)
- n = 113: number of DE genes (DRAWS)
- k = 1: overlap (SUCCESSFUL DRAWS)

Null hypothesis -- genes are drawn from 12000 genes at random with respect to the pathway



Running hypergeometric test

```
N <- nrow(de)
K <- length(randomGeneSet)
n <- length(upRegulatedGenes)
k <- length(intersect(upRegulatedGenes, randomGeneSet))
phyper(k - 1, K, N - K, n, lower.tail = F)</pre>
```

```
## [1] 0.32197
```



Non-random set

```
nonRandomGeneSet <- keggSymbolMouse[["Cytokine-cytokine receptor interaction - Mus muscul")</pre>
 nonRandomGeneSet <- nonRandomGeneSet[nonRandomGeneSet %in% rownames(de)]</pre>
 N <- nrow(de)
 K <- length(nonRandomGeneSet)</pre>
 n <- length(upRegulatedGenes)</pre>
 k <- length(intersect(upRegulatedGenes, nonRandomGeneSet))</pre>
 print(c(N, K, n, k))
## [1] 12000 135
                      113
 phyper(k - 1, K, N - K, n, lower.tail = F)
## [1] 0.000279903
```



Hypergeometric tests

- Require you to define gene set to test:
 - Setting arbitrary threshold (< 0.01 or < 0.05)
 - Only work with decent amount of genes (hard to calculate overlaps for 20 genes)
- Very robust with large number of genes
- Many databases offer you hypergeometric test with FDR correction (multiple pathways tests)
- http://software.broadinstitute.org/gsea/msigdb/annotate.jsp (you can enter my email for now: zayats1812@mail.ru)



Hypergeometric tests

 http://software.broadinstitute.org/gsea/msigdb/annotate.jsp (you can enter my email for now: zayats1812@mail.ru)

```
cat(upRegulatedGenes)
```

Cd9 Il10 Mzb1 Pon3 Mt1 Tubb6 Smox Mmp10 Ikzf3 Pik3cg Prdm1 Cdkn2a Cdkn2b Nid1 Lysmd2 Mt2 Il6 Igkv6



GSEA (gene-set enrichment analysis)

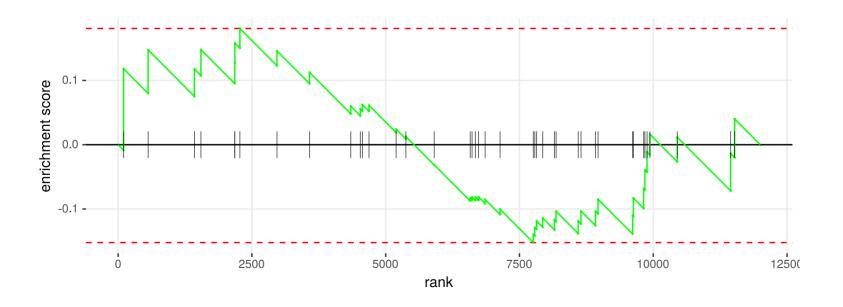
- GSEA uses information about all genes in DE to score pathways
- Genes are ranked by their difference in DE (usually by t statistic)
- We try to identify pathways for which genes are distributed at random



GSEA (gene-set enrichment analysis)

We will use fgsea package (the guys in our lab are amazing):

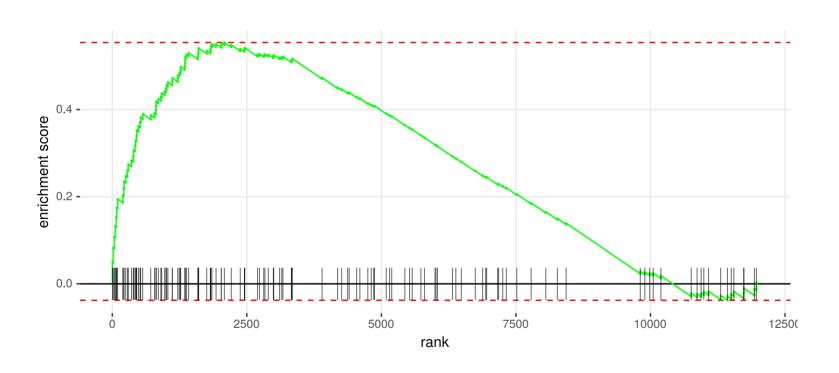
```
stats <- de$t
names(stats) <- de$Gene.symbol
plotEnrichment(randomGeneSet, stats)</pre>
```





GSEA (gene-set enrichment analysis)

plotEnrichment(nonRandomGeneSet, stats)





- Based on enrichment score we can calculate p value for each pathway
- fgsea allows us to do it quickly (f for FAST) for all the pathways in the same time



```
fgseaResults <- fgseaMultilevel(keggSymbolMouse, stats, minSize = 15, maxSize = 500)
head(fgseaResults, 3)</pre>
```

```
##
                                                                             pathway
## 1:
                                           ABC transporters - Mus musculus (mouse)
## 2: AGE-RAGE signaling pathway in diabetic complications - Mus musculus (mouse)
## 3:
                                     AMPK signaling pathway - Mus musculus (mouse)
##
                         padj log2err
                                                         NES size
             pval
                                                ES
## 1: 0.142384106 0.22833549 0.1501629 0.4237276 1.2876147
## 2: 0.001864951 0.00925438 0.4550599 0.4582477 1.6770374
## 3: 0.941176471 0.94571807 0.0343128 0.1846762 0.7202221
##
                                       leadingEdge
        Abcg1, Abcc1, Abca1, Abcb1b, Abca7, Abcd1, ...
## 1:
## 2:
               Il6, Prkcz, Foxo1, Pim1, Jak2, Ccl2,...
## 3: Foxo1, Igf1r, Rab2a, Creb3l2, Cpt1a, Ppp2r5a,...
```



```
topPathwaysUp <- fgseaResults[ES > 0, ][head(order(pval), n=5), pathway]
topPathwaysDown <- fgseaResults[ES < 0, ][head(order(pval), n=5), pathway]
topPathways <- c(topPathwaysUp, rev(topPathwaysDown))</pre>
```



plotGseaTable(keggSymbolMouse[topPathways], stats, fgseaResults, gseaParam = 0.5)

Pathway

essing in endoplasmic reticulum - Mus musculus (mouse)
associated herpesvirus infection - Mus musculus (mouse)
Pathways in cancer - Mus musculus (mouse)
TNF signaling pathway - Mus musculus (mouse)
Proteasome - Mus musculus (mouse)
Nucleotide excision repair - Mus musculus (mouse)
RNA transport - Mus musculus (mouse)
osome biogenesis in eukaryotes - Mus musculus (mouse)
Spliceosome - Mus musculus (mouse)

Gene ranks	NES	pval	padj
Manufacture consesses a section of the contract of the contrac	2.31	3.4e-11	4.4e-09
	2.18	3.6e-09	3.1e-07
	2.06	9.1e-08	6.0e-06
	1.75	1.5e-06	4.8e-05
Management of the second of th	2.09	1.8e-06	5.2e-05
	-2.20	7.8e-06	1.5e-04
t no e e e e e e e e e e e e e e e e e e	-2.31	7.5e-07	2.8e-05
	-1.98	3.1e-07	1.4e-05
II a company	-2.28	2.7e-07	1.4e-05
1 THEORY CO. S. C. S.	-2.75	5.8e-16	1.5e-13
0 3000 6000 9000 1200	00		



- Does not require a priori threshold to define DE genes
- Can detect a lot of small changes
- Detects up/down pathways in the same time



Conclusion

Secondary analysis is about making sense of the data:

- Making sense of the variance
- Making sense of differential expression design
- Making sense of differential expression results

Once we have differential expression we can try to guess what's going on:

- Biological pathways
- TF targets



Questions?