

Solutions:

① a) $x^2 + (y/4)^2 + z^2 = 1$: ellipsoid

$y=0$: $x^2 + z^2 = 1$: circle centered at $(0,0)$ w/
radius 1 on $x-z$ plane

b) $(x/3)^2 + (y/5)^2 - 5z^2 = 1$: hyperboloid (one sheet)

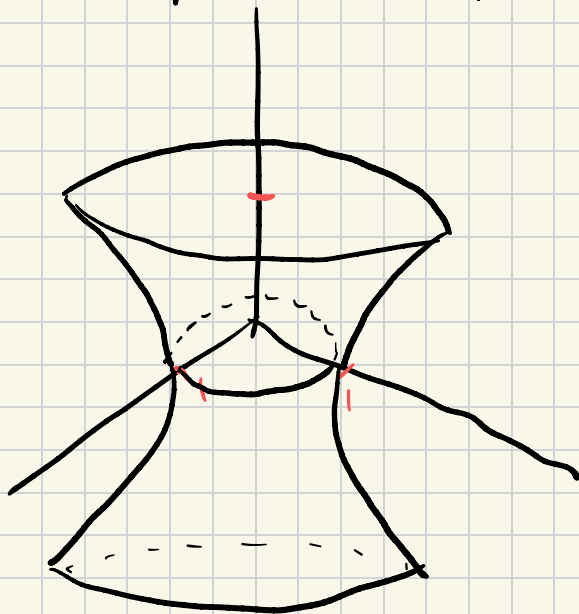
$y=1$: $(x/3)^2 + 1/25 - 5z^2 = 1$

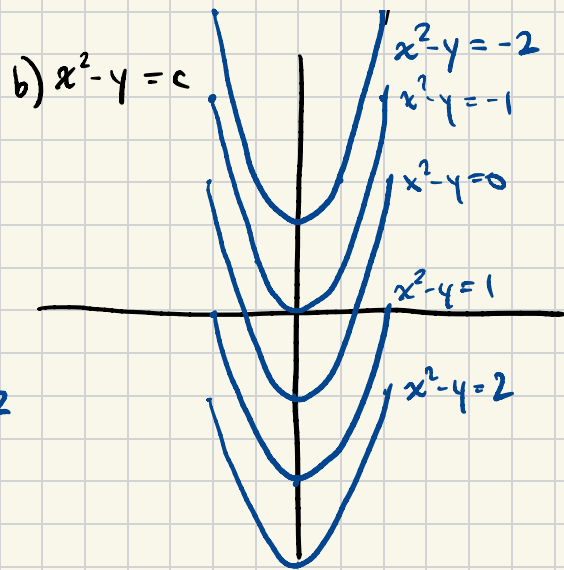
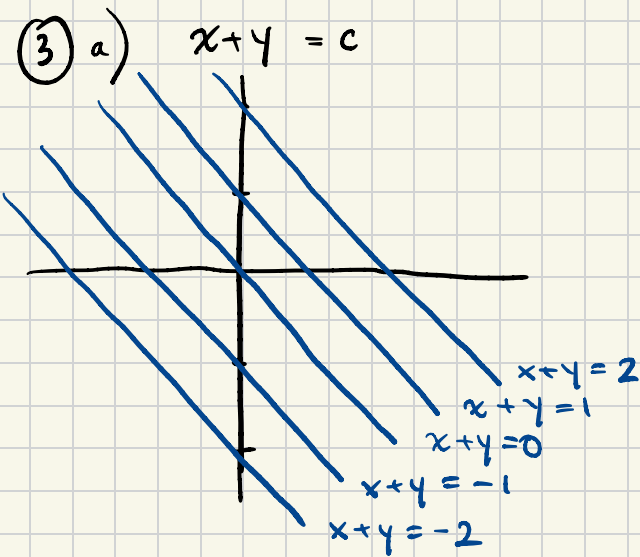
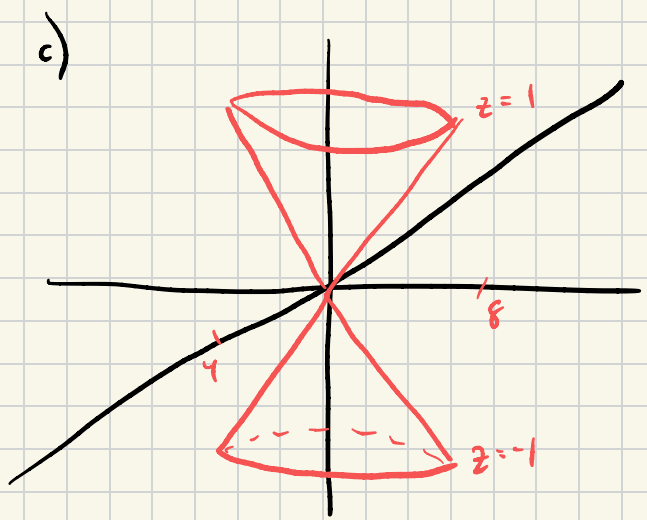
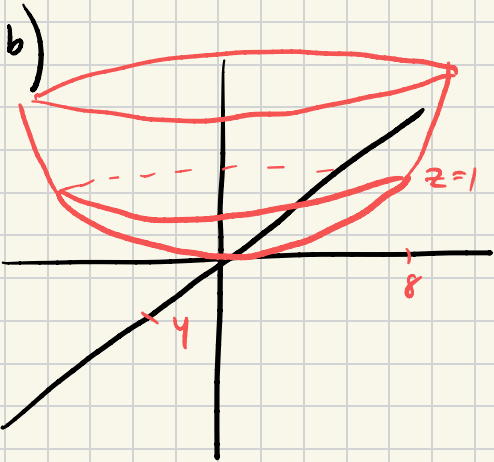
$\Rightarrow (x/3)^2 - 5z^2 = 24/25$ hyperbola

c) $y = 3x^2$: parabolic cylinder

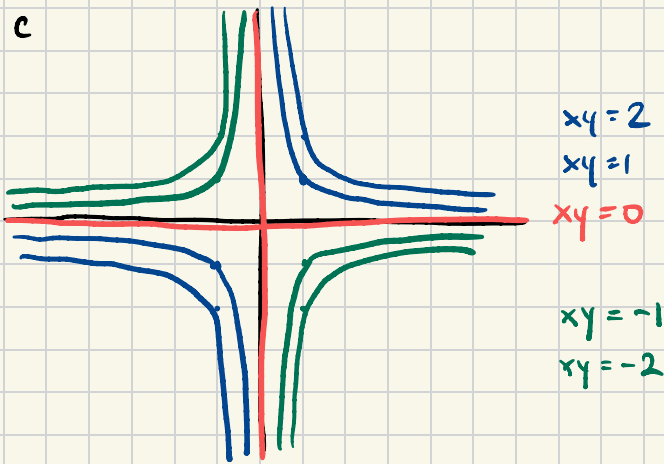
$z=27$: parabola on plane $z=27$

② a) $x^2 + y^2 - z^2 = 1$: hyperboloid (one sheet)





c) $xy = c$



④

$f(x, y, z) = x^2 + y^2 - z^2$, $f(x, y, z) = -2, -1, 0, 1, 2$

$x^2 + y^2 - z^2 = 0$:

Elliptic cone

$x^2 + y^2 - z^2 = -1$:

Two-sheeted Hyperbola

$x^2 + y^2 - z^2 = -2$:

Two-sheeted Hyperbola

$x^2 + y^2 - z^2 = 1$:

One-sheeted Hyperbola

$x^2 + y^2 - z^2 = 2$:

One-sheeted Hyperbola

