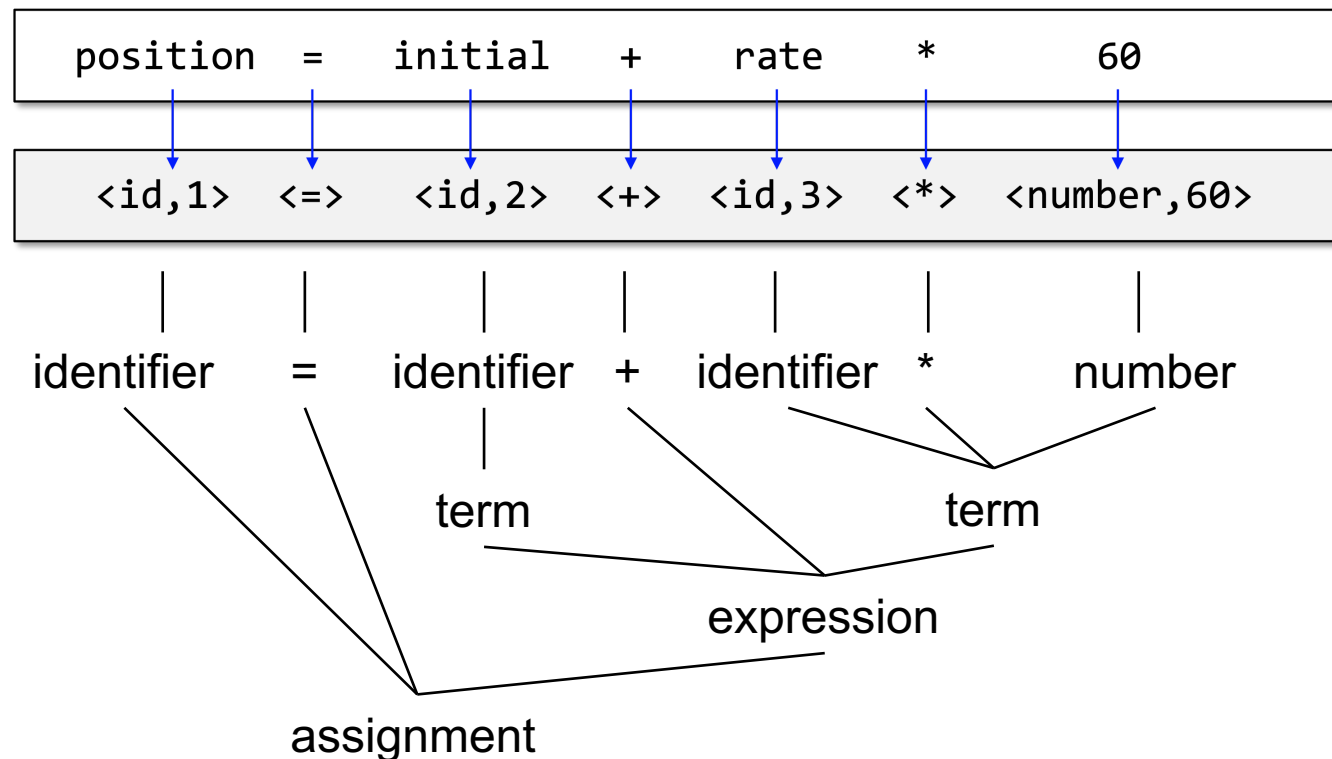
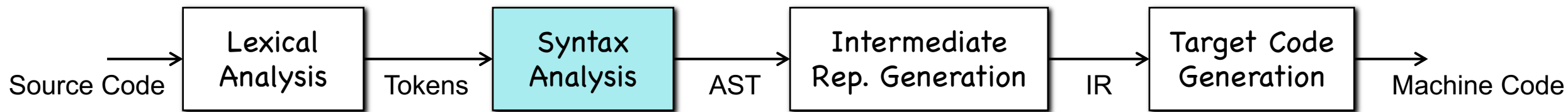


Chapter 4-2

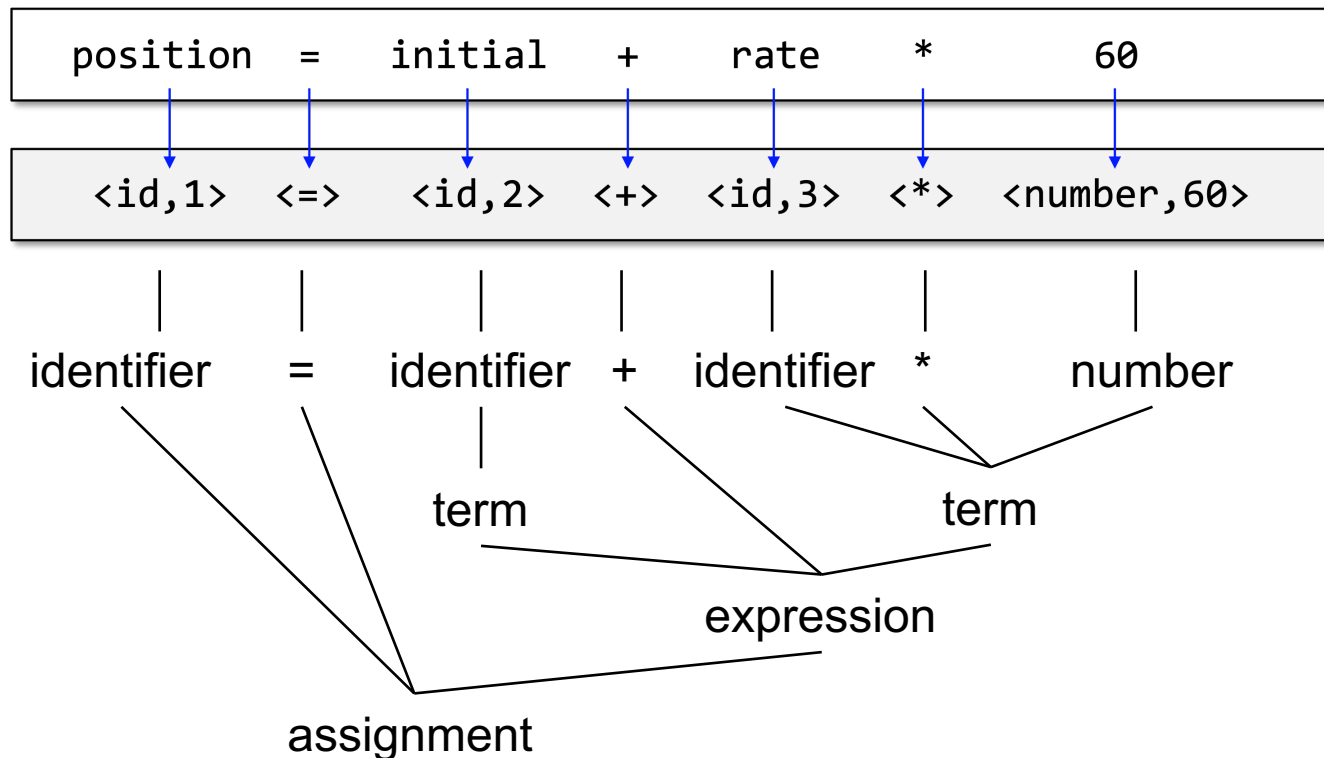
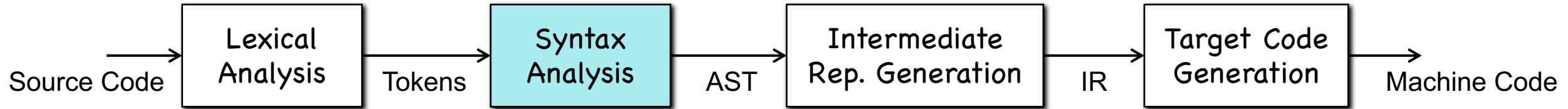
Syntax Analysis

Syntax Analysis



assignment \rightarrow identifier = expression
 expression \rightarrow term + term
 term \rightarrow identifier
 | identifier * number

Syntax Analysis



- A procedure of building the parse or syntax tree
 - Top-down parsing
 - Bottom-up parsing

assignment \rightarrow identifier = expression
 expression \rightarrow term + term
 term \rightarrow identifier
 | identifier * number

PART I: Top-Down Parsing

Top-Down Parsing

- Top-down parsing can be viewed as the problem of constructing a parse tree **in preorder**

| | | |
|---------------------|---------------|------------------------|
| E | \rightarrow | $T E'$ |
| E' | \rightarrow | $+ T E' \mid \epsilon$ |
| T | \rightarrow | $F T'$ |
| T' | \rightarrow | $* F T' \mid \epsilon$ |
| F | \rightarrow | $(E) \mid \text{id}$ |
| id + id * id | | |

Top-Down Parsing

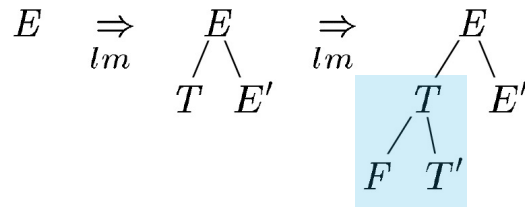
- Top-down parsing can be viewed as the problem of constructing a parse tree **in preorder**

$$E \xRightarrow{lm} \begin{array}{c} E \\ / \quad \backslash \\ T \quad E' \end{array}$$

| | | |
|---------------------|---------------|--------------------------|
| E | \rightarrow | $T E'$ |
| E' | \rightarrow | $+ T E' \mid \epsilon$ |
| T | \rightarrow | $F T'$ |
| T' | \rightarrow | $* F T' \mid \epsilon$ |
| F | \rightarrow | $(E) \mid \mathbf{id}$ |
| id + id * id | | |

Top-Down Parsing

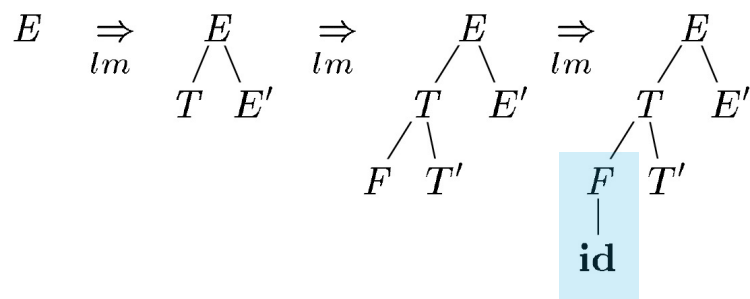
- Top-down parsing can be viewed as the problem of constructing a parse tree **in preorder**



| | | |
|---------------------|---------------|------------------------|
| E | \rightarrow | $T E'$ |
| E' | \rightarrow | $+ T E' \mid \epsilon$ |
| T | \rightarrow | $F T'$ |
| T' | \rightarrow | $* F T' \mid \epsilon$ |
| F | \rightarrow | $(E) \mid \text{id}$ |
| id + id * id | | |

Top-Down Parsing

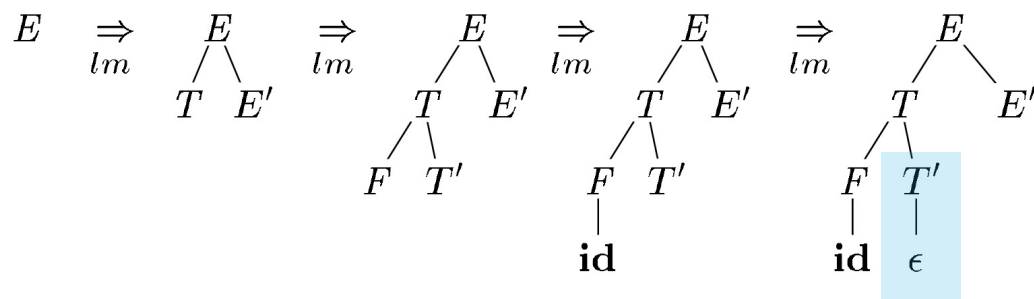
- Top-down parsing can be viewed as the problem of constructing a parse tree **in preorder**



| | | |
|---------------------|---------------|------------------------|
| E | \rightarrow | $T E'$ |
| E' | \rightarrow | $+ T E' \mid \epsilon$ |
| T | \rightarrow | $F T'$ |
| T' | \rightarrow | $* F T' \mid \epsilon$ |
| F | \rightarrow | $(E) \mid \text{id}$ |
| id + id * id | | |

Top-Down Parsing

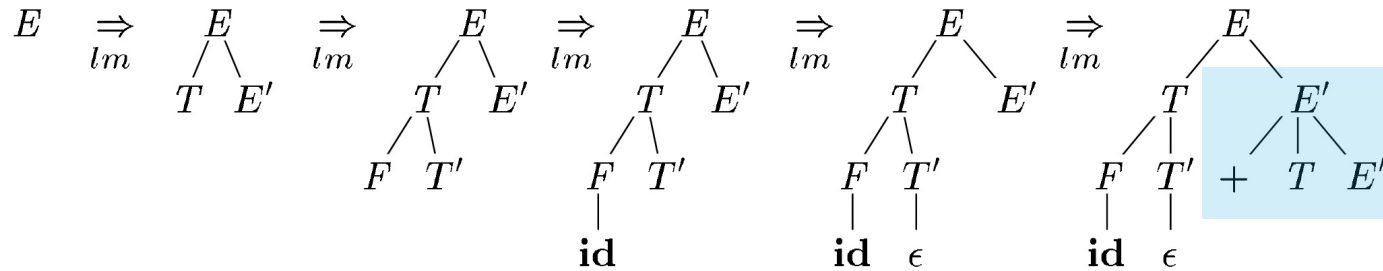
- Top-down parsing can be viewed as the problem of constructing a parse tree **in preorder**



| | | |
|---------------------|---------------|------------------------|
| E | \rightarrow | $T E'$ |
| E' | \rightarrow | $+ T E' \mid \epsilon$ |
| T | \rightarrow | $F T'$ |
| T' | \rightarrow | $* F T' \mid \epsilon$ |
| F | \rightarrow | $(E) \mid id$ |
| id + id * id | | |

Top-Down Parsing

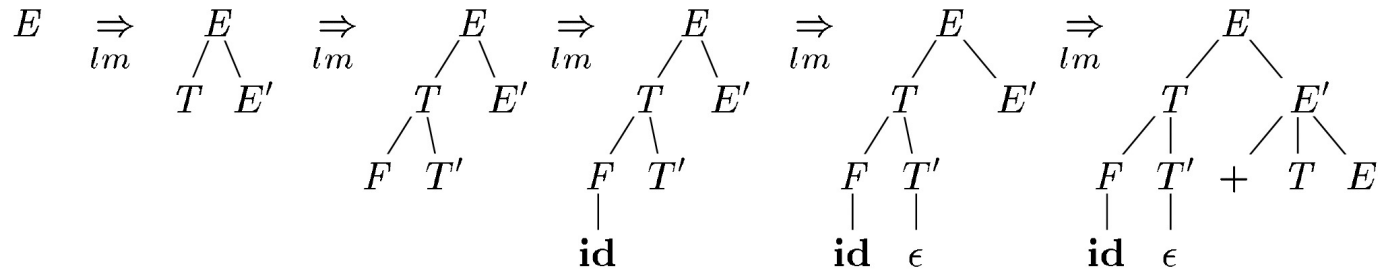
- Top-down parsing can be viewed as the problem of constructing a parse tree **in preorder**



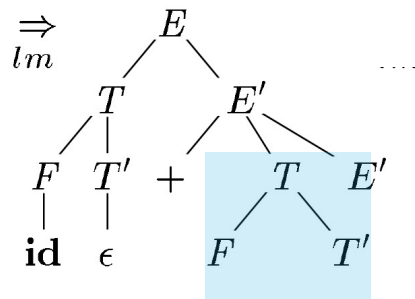
| | | |
|---------------------|---------------|------------------------|
| E | \rightarrow | $T E'$ |
| E' | \rightarrow | $+ T E' \mid \epsilon$ |
| T | \rightarrow | $F T'$ |
| T' | \rightarrow | $* F T' \mid \epsilon$ |
| F | \rightarrow | $(E) \mid \text{id}$ |
| id + id * id | | |

Top-Down Parsing

- Top-down parsing can be viewed as the problem of constructing a parse tree **in preorder**

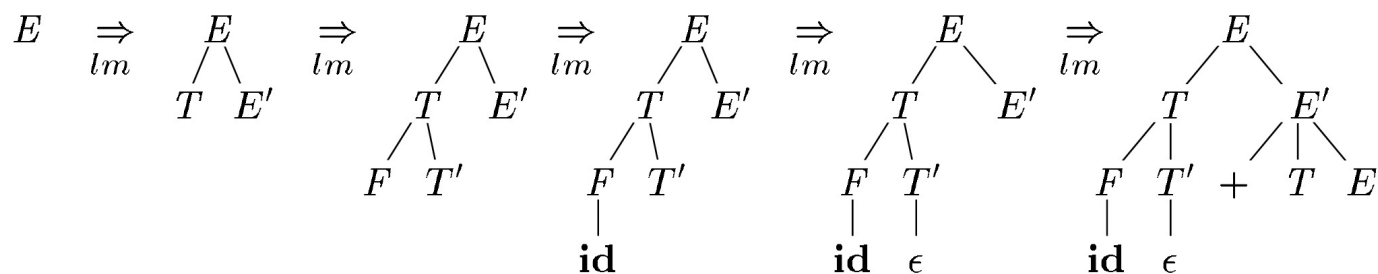


| | | |
|---|---------------|------------------------|
| E | \rightarrow | $T E'$ |
| E' | \rightarrow | $+ T E' \mid \epsilon$ |
| T | \rightarrow | $F T'$ |
| T' | \rightarrow | $* F T' \mid \epsilon$ |
| F | \rightarrow | $(E) \mid \text{id}$ |
| $\text{id} + \text{id} * \text{id}$ | | |



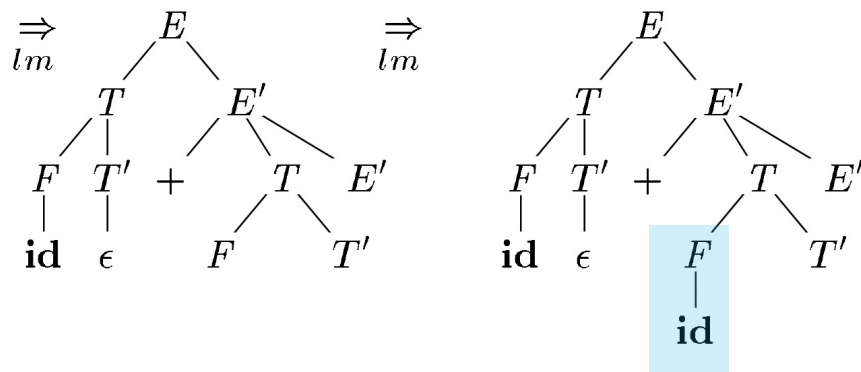
Top-Down Parsing

- Top-down parsing can be viewed as the problem of constructing a parse tree **in preorder**



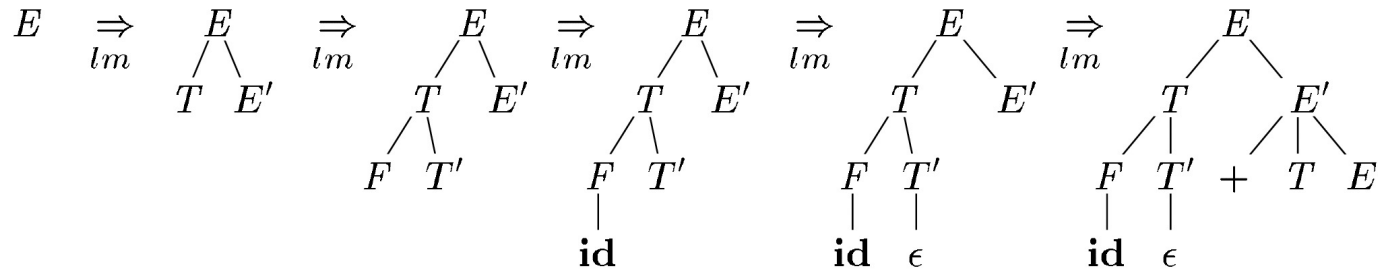
| | | |
|------|---------------|------------------------|
| E | \rightarrow | $T E'$ |
| E' | \rightarrow | $+ T E' \mid \epsilon$ |
| T | \rightarrow | $F T'$ |
| T' | \rightarrow | $* F T' \mid \epsilon$ |
| F | \rightarrow | $(E) \mid \text{id}$ |

id + id * id

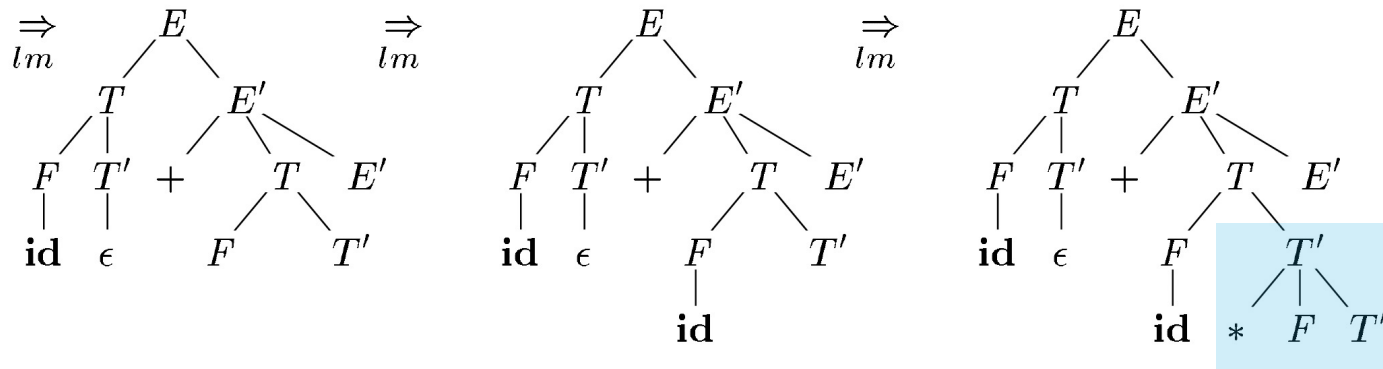


Top-Down Parsing

- Top-down parsing can be viewed as the problem of constructing a parse tree **in preorder**

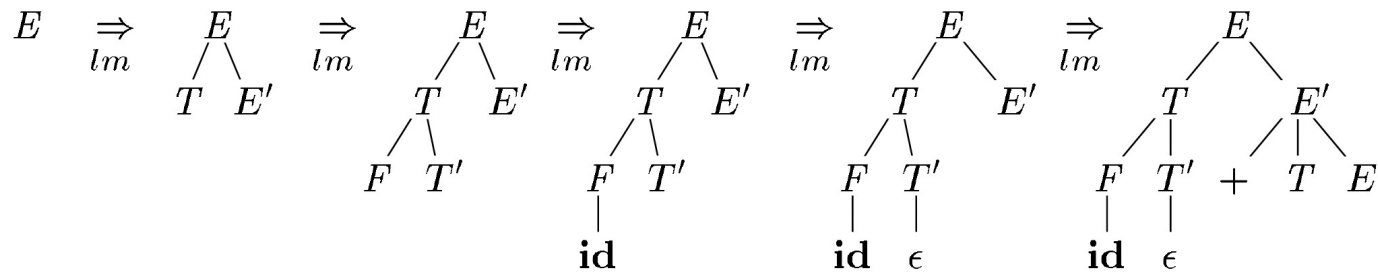


| | | |
|---------------------|---------------|------------------------|
| E | \rightarrow | $T E'$ |
| E' | \rightarrow | $+ T E' \mid \epsilon$ |
| T | \rightarrow | $F T'$ |
| T' | \rightarrow | $* F T' \mid \epsilon$ |
| F | \rightarrow | $(E) \mid id$ |
| id + id * id | | |

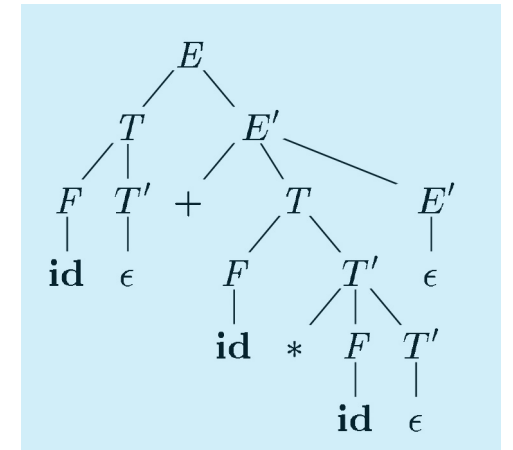
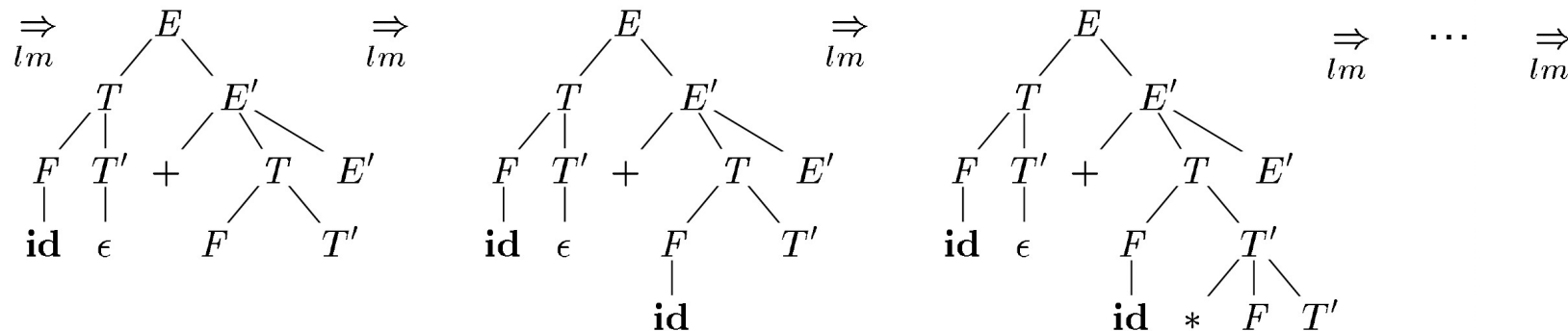


Top-Down Parsing

- Top-down parsing can be viewed as the problem of constructing a parse tree **in preorder**



| |
|--|
| $ \begin{array}{ll} E & \rightarrow T E' \\ E' & \rightarrow + T E' \mid \epsilon \\ T & \rightarrow F T' \\ T' & \rightarrow * F T' \mid \epsilon \\ F & \rightarrow (E) \mid \mathbf{id} \end{array} $ |
| $\mathbf{id} + \mathbf{id} * \mathbf{id}$ |



Building a Parser in Practice

- Each non-terminal has a procedure or function for parsing
- => Recursive-Descent Parser

Building a Parser in Practice

- Each non-terminal has a procedure or function for parsing
- \Rightarrow Recursive-Descent Parser
- **Example:** $S \rightarrow c A b; A \rightarrow a b \mid a$

```
bool S() {  
  
  
  
  
  
  
  
  
  
}
```

```
bool A() {  
  
  
  
  
  
  
  
  
  
}
```


Building a Parser in Practice

- Each non-terminal has a procedure or function for parsing
- => Recursive-Descent Parser
- **Example:** $S \rightarrow c A b$; $A \rightarrow a b \mid a$

```
bool S() {
    if (*cursor == 'c') cursor++;
    else return false;
    if (!A()) return false;
    if (*cursor == 'b') cursor++;
    else return false;
    return true;
}
```

```
bool A() {
    temp = cursor;
    cursor = temp;
    if (*cursor == 'a') {
        cursor++;
        if (*cursor == 'b') return true;
    }

    cursor = temp;
    if (*cursor == 'a') return true;
    return false;
}
```

Building a Parser in Practice


```
TreeNode* S() {
    TreeNode *S = new TreeNode;
    if (*cursor == 'c') { cursor++; S.addChildNode('c'); }
    else return null;

    if (TreeNode *A = A()) { S.addChildNode(A); }
    else return null;

    if (*cursor == 'b') { cursor++; S.addChildNode('b'); }
    else return null;

    return S;
}
```

or function for parsing



```
bool S() {
    if (*cursor == 'c') cursor++;
    else return false;
    if (!A()) return false;
    if (*cursor == 'b') cursor++;
    else return false;
    return true;
}
```

```
bool A() {
    temp = cursor;
    cursor = temp;
    if (*cursor == 'a') {
        cursor++;
        if (*cursor == 'b') return true;
    }

    cursor = temp;
    if (*cursor == 'a') return true;
    return false;
}
```

Building a Parser in Practice

- Each non-terminal has a procedure or function for parsing
- => Recursive-Descent Parser
- **Example:** $S \rightarrow c A b$; $A \rightarrow a b \mid a$

```
bool S() {  
    if (*cursor == 'c') cursor++;  
    else return false;  
    if (!A()) return false;  
    if (*cursor == 'b') cursor++;  
    else return false;  
    return true;  
}
```

```
bool A() {  
    temp = cursor;  
    cursor = temp;  
    if (*cursor == 'a') {  
        cursor++;  
        if (*cursor == 'b') return true;  
    }  
  
    cursor = temp;  
    if (*cursor == 'a') return true;  
    return false;  
}
```


Building a Parser in Practice

- Each non-terminal has a procedure or function for parsing
- => Recursive-Descent Parser
- **Example:** $S \rightarrow c A b$; $A \rightarrow a b \mid a$

```
bool S() {
    if (*cursor == 'c') cursor++;
    else return false;
    if (!A()) return false;
    if (*cursor == 'b') cursor++;
    else return false;
    return true;
}
```

```
bool A() {
    temp = cursor;
    cursor = temp;
    if (*cursor == 'a') {
        cursor++;
        if (*cursor == 'b') return true;
    }

    cursor = temp;
    if (*cursor == 'a') return true;
    return false;
}
```



Building a Parser in Practice

- Each non-terminal has a procedure or function for parsing
- => Recursive-Descent Parser
- **Example:** $S \rightarrow c A b$; $A \rightarrow a b \mid a$



```
bool S() {
    if (*cursor == 'c') cursor++;
    else return false;
    if (!A()) return false;
    if (*cursor == 'b') cursor++;
    else return false;
    return true;
}
```

```
bool A() {
    temp = cursor;
    cursor = temp;
    if (*cursor == 'a') {
        cursor++;
        if (*cursor == 'b') return true;
    }

    cursor = temp;
    if (*cursor == 'a') return true;
    return false;
}
```

Building a Parser in Practice

- Each non-terminal has a procedure or function for parsing
- => Recursive-Descent Parser
- **Example:** $S \rightarrow c A b$; $A \rightarrow a b \mid a$



Let's parse

| | | |
|---|---|---|
| c | a | b |
|---|---|---|

```
bool S() {
    if (*cursor == 'c') cursor++;
    else return false;
    if (!A()) return false;
    if (*cursor == 'b') cursor++;
    else return false;
    return true;
}
```

```
bool A() {
    temp = cursor;
    cursor = temp;
    if (*cursor == 'a') {
        cursor++;
        if (*cursor == 'b') return true;
    }

    cursor = temp;
    if (*cursor == 'a') return true;
    return false;
}
```

Building a Parser in Practice

- Each non-terminal has a procedure or function for parsing
- => Recursive-Descent Parser
- **Example:** $S \rightarrow c A b$; $A \rightarrow a b \mid a$



Let's parse

| | | |
|---|---|---|
| c | a | b |
|---|---|---|

```
bool S() {
    if (*cursor == 'c') cursor++;
    else return false;
    if (!A()) return false;
    if (*cursor == 'b') cursor++;
    else return false;
    return true;
}
```

```
bool A() {
    temp = cursor;
    cursor = temp;
    if (*cursor == 'a') {
        cursor++;
        if (*cursor == 'b') return true;
    }

    cursor = temp;
    if (*cursor == 'a') return true;
    return false;
}
```

Building a Parser in Practice

- Each non-terminal has a procedure or function for parsing
- => Recursive-Descent Parser
- **Example:** $S \rightarrow c A b; A \rightarrow a b \mid a$



Let's parse

| | | |
|---|---|---|
| c | a | b |
|---|---|---|

```
bool S() {
    if (*cursor == 'c') cursor++;
    else return false;
    if (!A()) return false;
    if (*cursor == 'b') cursor++;
    else return false;
    return true;
}
```

```
bool A() {
    temp = cursor;
    cursor = temp;
    if (*cursor == 'a') {
        cursor++;
        if (*cursor == 'b') return true;
    }

    cursor = temp;
    if (*cursor == 'a') return true;
    return false;
}
```


Building a Parser in Practice

- Each non-terminal has a procedure or function for parsing
- => Recursive-Descent Parser
- **Example:** $S \rightarrow c A b$; $A \rightarrow a b \mid a$



Let's parse

| | | |
|---|---|---|
| c | a | b |
|---|---|---|

```
bool S() {
    if (*cursor == 'c') cursor++;
    else return false;
    if (!A()) return false;
    if (*cursor == 'b') cursor++;
    else return false;    ???
    return true;
}
```

```
bool A() {
    temp = cursor;
    cursor = temp;
    if (*cursor == 'a') {
        cursor++;
        if (*cursor == 'b') return true;
    }

    cursor = temp;
    if (*cursor == 'a') return true;
    return false;
}
```

Building a Parser in Practice

- Each non-terminal has a procedure or function for parsing
- => Recursive-Descent Parser
- **Problem 1: Backtracking may be necessary**
 - when one derivation does not work, we may try others

Building a Parser in Practice

- Each non-terminal has a procedure or function for parsing
- => Recursive-Descent Parser
- **Problem 1:** Backtracking may be necessary
 - when one derivation does not work, we may try others
- **Problem 2: A left-recursive grammar can cause infinite loops**
 - when expanding a non-terminal, we may find itself and expand it again

Building a Parser in Practice

- Each non-terminal has a procedure or function for parsing
- => Recursive-Descent Parser
- **Problem 1:** Backtracking may be necessary
 - when one derivation does not work, we may try others
- **Problem 2:** A **left-recursive** grammar can cause **infinite loops**
 - when expanding a non-terminal, we may find itself and expand it again
- **Example:** $A \rightarrow A b \mid a$

Building a Parser in Practice

- Each non-terminal has a procedure or function for parsing
- => Recursive-Descent Parser

- **Problem 1:** Backtracking may be necessary

- when one derivation does not work, we m

- **Problem 2:** A left-recursive grammar

- when expanding a non-terminal, we may

- **Example:** $A \rightarrow A b \mid a$

```
bool A() {
    temp = cursor;
    cursor = temp;
    if (A()) {
        cursor++;
        if (*cursor == 'b') return true;
    }

    cursor = temp;
    if (*cursor == 'a') return true;
    return false;
}
```

Eliminating Left-Recursion

- A grammar is left-recursive if it has a non-terminal A such that there is a derivation $A \Rightarrow^+ A\alpha$

Eliminating Left-Recursion

- A grammar is left-recursive if it has a non-terminal A such that there is a derivation $A \Rightarrow^+ A\alpha$
- **Example:** $A \rightarrow A\alpha \mid \beta$ is left-recursive

Eliminating Left-Recursion

- A grammar is left-recursive if it has a non-terminal A such that there is a derivation $A \Rightarrow^+ A\alpha$
- **Example:** $A \rightarrow A\alpha \mid \beta$ is left-recursive, can be transformed into

$$\begin{array}{l} A \rightarrow \beta A' \\ A' \rightarrow \alpha A' \mid \epsilon \end{array}$$

Eliminating Left-Recursion

- A grammar is left-recursive if it has a non-terminal A such that there is a derivation $A \Rightarrow^+ A\alpha$
- **Example:** $A \rightarrow A\alpha \mid \beta$ is left-recursive, can be transformed into

$$\begin{array}{l} A \rightarrow \beta A' \\ A' \rightarrow \alpha A' \mid \epsilon \end{array}$$

$$A \rightarrow A\alpha_1 \mid A\alpha_2 \mid \cdots \mid A\alpha_m \mid \beta_1 \mid \beta_2 \mid \cdots \mid \beta_n$$

?????

Eliminating Left-Recursion

- A grammar is left-recursive if it has a non-terminal A such that there is a derivation $A \Rightarrow^+ A\alpha$
- **Example:** $A \rightarrow A\alpha \mid \beta$ is left-recursive, can be transformed into

$$\begin{array}{l} A \rightarrow \beta A' \\ A' \rightarrow \alpha A' \mid \epsilon \end{array}$$

$$A \rightarrow A\alpha_1 \mid A\alpha_2 \mid \cdots \mid A\alpha_m \mid \beta_1 \mid \beta_2 \mid \cdots \mid \beta_n$$

$$\begin{array}{l} A \rightarrow \beta_1 A' \mid \beta_2 A' \mid \cdots \mid \beta_n A' \\ A' \rightarrow \alpha_1 A' \mid \alpha_2 A' \mid \cdots \mid \alpha_m A' \mid \epsilon \end{array}$$

Eliminating Left-Recursion

- 1) arrange the nonterminals in some order A_1, A_2, \dots, A_n .
- 2) **for** (each i from 1 to n) {
- 3) **for** (each j from 1 to $i - 1$) {
- 4) replace each production of the form $A_i \rightarrow A_j \gamma$ by the
 productions $A_i \rightarrow \delta_1 \gamma \mid \delta_2 \gamma \mid \dots \mid \delta_k \gamma$, where
 $A_j \rightarrow \delta_1 \mid \delta_2 \mid \dots \mid \delta_k$ are all current A_j -productions
- 5) }
- 6) eliminate the immediate left recursion among the A_i -productions
- 7) }

$A \rightarrow A\alpha_1 \mid A\alpha_2 \mid \dots \mid A\alpha_m \mid \beta_1 \mid \beta_2 \mid \dots \mid \beta_n$

$A \rightarrow \beta_1 A' \mid \beta_2 A' \mid \dots \mid \beta_n A'$
 $A' \rightarrow \alpha_1 A' \mid \alpha_2 A' \mid \dots \mid \alpha_m A' \mid \epsilon$

Eliminating Left-Recursion

- 1) arrange the nonterminals in some order A_1, A_2, \dots, A_n .
- 2) **for** (each i from 1 to n) {
- 3) **for** (each j from 1 to $i - 1$) {
- 4) replace each production of the form $A_i \rightarrow A_j \gamma$ by the
 productions $A_i \rightarrow \delta_1 \gamma \mid \delta_2 \gamma \mid \dots \mid \delta_k \gamma$, where
 $A_j \rightarrow \delta_1 \mid \delta_2 \mid \dots \mid \delta_k$ are all current A_j -productions
- 5) }
- 6) eliminate the immediate left recursion among the A_i -productions
- 7) }

$A \rightarrow A\alpha_1 \mid A\alpha_2 \mid \dots \mid A\alpha_m \mid \beta_1 \mid \beta_2 \mid \dots \mid \beta_n$

$A \rightarrow \beta_1 A' \mid \beta_2 A' \mid \dots \mid \beta_n A'$
 $A' \rightarrow \alpha_1 A' \mid \alpha_2 A' \mid \dots \mid \alpha_m A' \mid \epsilon$

Eliminating Left-Recursion

- 1) arrange the nonterminals in some order A_1, A_2, \dots, A_n .
- 2) **for** (each i from 1 to n) {
- 3) **for** (each j from 1 to $i - 1$) {
- 4) replace each production of the form $A_i \rightarrow A_j \gamma$ by the
 productions $A_i \rightarrow \delta_1 \gamma \mid \delta_2 \gamma \mid \dots \mid \delta_k \gamma$, where
 $A_j \rightarrow \delta_1 \mid \delta_2 \mid \dots \mid \delta_k$ are all current A_j -productions
- 5) }
- 6) eliminate the immediate left recursion among the A_i -productions
- 7) }

$A \rightarrow A\alpha_1 \mid A\alpha_2 \mid \dots \mid A\alpha_m \mid \beta_1 \mid \beta_2 \mid \dots \mid \beta_n$

$A \rightarrow \beta_1 A' \mid \beta_2 A' \mid \dots \mid \beta_n A'$
 $A' \rightarrow \alpha_1 A' \mid \alpha_2 A' \mid \dots \mid \alpha_m A' \mid \epsilon$

Eliminating Left-Recursion

- 1) arrange the nonterminals in some order A_1, A_2, \dots, A_n .
- 2) **for** (each i from 1 to n) {
- 3) **for** (each j from 1 to $i - 1$) {
- 4) replace each production of the form $A_i \rightarrow A_j \gamma$ by the
 productions $A_i \rightarrow \delta_1 \gamma \mid \delta_2 \gamma \mid \dots \mid \delta_k \gamma$, where
 $A_j \rightarrow \delta_1 \mid \delta_2 \mid \dots \mid \delta_k$ are all current A_j -productions
- 5) }
- 6) eliminate the immediate left recursion among the A_i -productions
- 7) }

This algorithm is guaranteed to work if the input grammar does NOT include
 (1) cycles ($A \Rightarrow^+ A$) or (2) ϵ productions

Eliminating Left-Recursion

- 1) arrange the nonterminals in some order A_1, A_2, \dots, A_n .
- 2) **for** (each i from 1 to n) {
- 3) **for** (each j from 1 to $i - 1$) {
- 4) replace each production of the form $A_i \rightarrow A_j \gamma$ by the
 productions $A_i \rightarrow \delta_1 \gamma \mid \delta_2 \gamma \mid \dots \mid \delta_k \gamma$, where
 $A_j \rightarrow \delta_1 \mid \delta_2 \mid \dots \mid \delta_k$ are all current A_j -productions
- 5) }
- 6) eliminate the immediate left recursion among the A_i -productions
- 7) }

Any grammar can be converted to a grammar that does NOT include

(1) cycles ($A \Rightarrow^+ A$) or (2) ϵ productions*

** with possible exception of the empty string*

Eliminating Left-Recursion

- Example

$$\begin{array}{l} S \rightarrow Aa \mid b \\ A \rightarrow Ac \mid Sd \end{array}$$

$$\begin{array}{l} A \rightarrow A\alpha \mid \beta \end{array} \Rightarrow \begin{array}{l} A \rightarrow \beta A' \\ A' \rightarrow \alpha A' \mid \epsilon \end{array}$$

Eliminating Left-Recursion

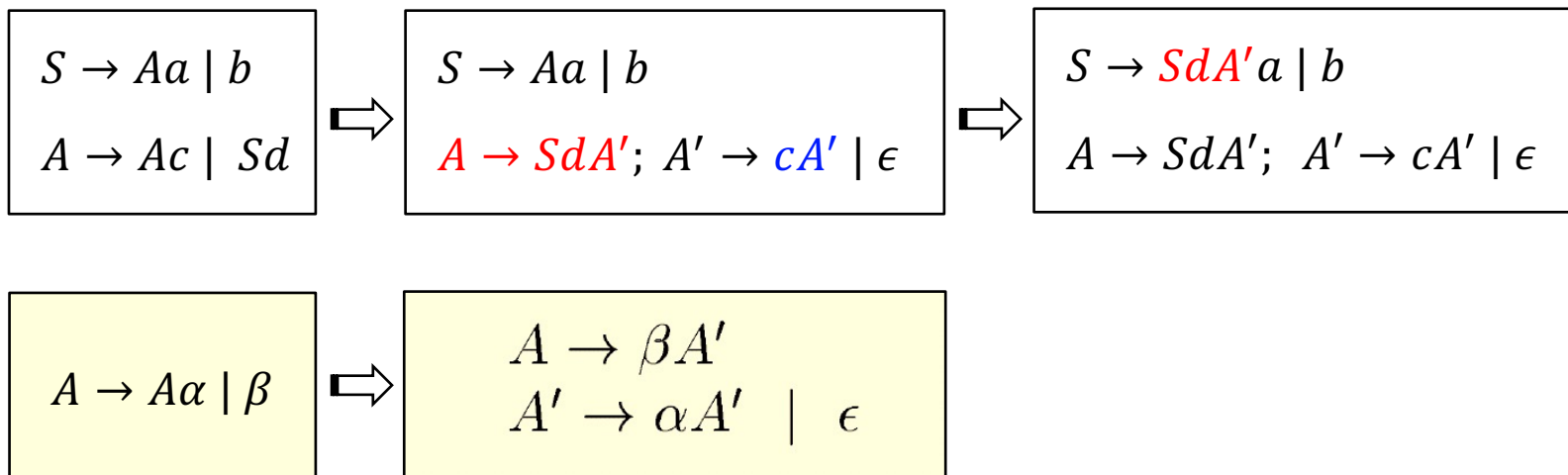
• Example

$$\begin{array}{l}
 S \rightarrow Aa \mid b \\
 A \rightarrow \textcolor{blue}{A}c \mid \textcolor{red}{S}d
 \end{array}
 \Rightarrow
 \begin{array}{l}
 S \rightarrow Aa \mid b \\
 A \rightarrow \textcolor{red}{S}dA'; A' \rightarrow \textcolor{blue}{c}A' \mid \epsilon
 \end{array}$$

$$\begin{array}{l}
 A \rightarrow A\alpha \mid \beta
 \end{array}
 \Rightarrow
 \begin{array}{l}
 A \rightarrow \beta A' \\
 A' \rightarrow \alpha A' \mid \epsilon
 \end{array}$$

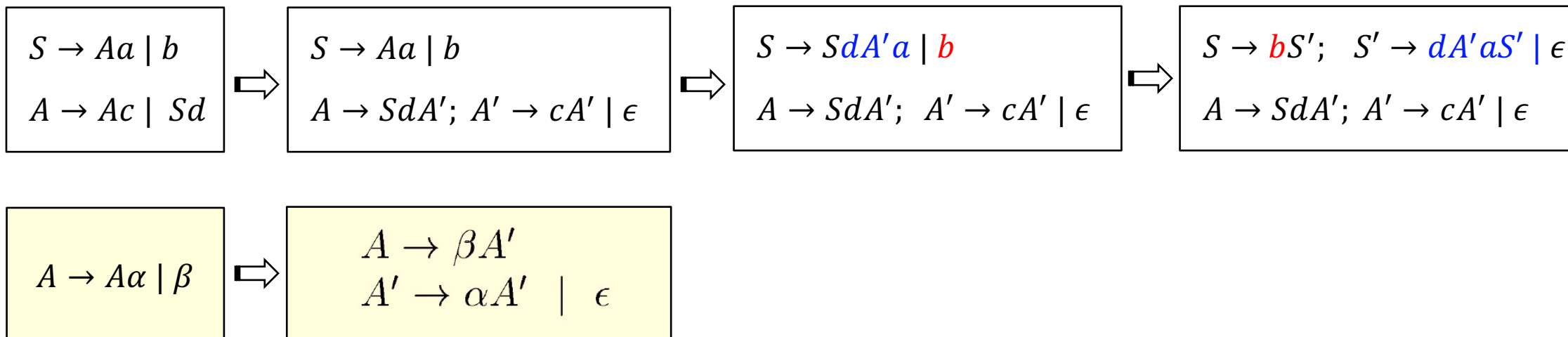
Eliminating Left-Recursion

• Example




Eliminating Left-Recursion

• Example



Building a Parser in Practice

- Each non-terminal has a procedure or function for parsing
- => Recursive-Descent Parser
- **Problem 1:** Backtracking may be necessary
 - when one derivation does not work, we may try others
-  **Problem 2:** A **left-recursive** grammar can cause **infinite loops**
 - when expanding a non-terminal, we may find itself and expand it again

Predictive Parsing

- Predictive parsers are recursive descent parser **w/o backtracking**

Predictive Parsing

- Predictive parsers are recursive descent parser **w/o backtracking**
- LL(1)
 - L: scanning input from left to right
 - L: leftmost derivation
 - 1: Using one input symbol of lookahead at each step

Predictive Parsing

- Predictive parsers are recursive descent parser w/o backtracking
- LL(1)
 - L: scanning input from left to right
 - L: leftmost derivation
 - 1: Using one input symbol of lookahead at each step
- LL(1) grammar (Not ambiguous! Not left-recursive!)
 - **Rich enough** to cover most programming constructs

Predictive Parsing

- Predictive Parsing

- LL(1)

- L: $S \rightarrow E$

- L: $E \rightarrow TE'$

- 1: $E' \rightarrow +TE' \mid (E) \mid \epsilon$

| NON - TERMINAL | INPUT SYMBOL | | | | | |
|-------------------|---------------------------|---------------------------|-----------------------|---------------------|---------------------------|---------------------------|
| | id | + | * | (|) | \$ |
| E | $E \rightarrow TE'$ | | | $E \rightarrow TE'$ | | |
| E' | | $E' \rightarrow +TE'$ | | | $E' \rightarrow \epsilon$ | $E' \rightarrow \epsilon$ |
| T | $T \rightarrow FT'$ | | | $T \rightarrow FT'$ | | |
| T' | | $T' \rightarrow \epsilon$ | $T' \rightarrow *FT'$ | | $T' \rightarrow \epsilon$ | $T' \rightarrow \epsilon$ |
| F | $F \rightarrow \text{id}$ | | | $F \rightarrow (E)$ | | |

- LL(1) grammar (Not ambiguous! Not left-recursive!)

- Rich enough to cover most programming constructs

Predictive Parsing

• Predictive

• LL(1)

• L: S

• L: E

• 1: T

| NON - TERMINAL | INPUT SYMBOL | | | | | |
|-------------------|---------------------------|---------------------------|-----------------------|---------------------|---------------------------|---------------------------|
| | id | + | * | (|) | \$ |
| E | $E \rightarrow TE'$ | | | $E \rightarrow TE'$ | | |
| E' | | $E' \rightarrow +TE'$ | | | $E' \rightarrow \epsilon$ | $E' \rightarrow \epsilon$ |
| T | $T \rightarrow FT'$ | | | $T \rightarrow FT'$ | | |
| T' | | $T' \rightarrow \epsilon$ | $T' \rightarrow *FT'$ | | $T' \rightarrow \epsilon$ | $T' \rightarrow \epsilon$ |
| F | $F \rightarrow \text{id}$ | | | $F \rightarrow (E)$ | | |

backtracking

• LL(1) grammar (Not ambiguous! Not left-recursive!)

- **Rich enough** to cover most programming constructs
- To build the predictive table, let's define **FIRST(α)**; **FOLLOW(α)**

First() and Follow()

- $\text{FIRST}(\alpha)$:
 - A set of terminals that α may start with

First() and Follow()

- $\text{FIRST}(\alpha)$:
 - A set of terminals that α may start with
- $\text{FOLLOW}(\alpha)$:
 - A set of terminals that can appear immediately to the right of α

First()

- $\text{FIRST}(\alpha)$:
 - A set of terminals that α may start with
 - If X is a terminal, $\text{FIRST}(X) = \{X\}$

First()

- $\text{FIRST}(\alpha)$:
 - A set of terminals that α may start with
 - If X is a terminal, $\text{FIRST}(X) = \{X\}$
 - If $X \rightarrow \epsilon$ is a production, $\epsilon \in \text{FIRST}(X)$

First()

- $\text{FIRST}(\alpha)$:
 - A set of terminals that α may start with

- If X is a terminal, $\text{FIRST}(X) = \{X\}$
- If $X \rightarrow \epsilon$ is a production, $\epsilon \in \text{FIRST}(X)$

$$X \rightarrow Y_1 Y_2 \dots Y_{i-1} Y_i \dots Y_k \rightarrow Y_i \dots Y_k$$

- If $X \rightarrow Y_1 Y_2 \dots Y_k$, $\epsilon \in \bigcap_{j=1}^{i-1} \text{FIRST}(Y_j) \wedge a \in \text{FIRST}(Y_i) \Rightarrow a \in \text{FIRST}(X)$

First()

- $\text{FIRST}(\alpha)$:
 - A set of terminals that α may start with

- If X is a terminal, $\text{FIRST}(X) = \{X\}$
- If $X \rightarrow \epsilon$ is a production, $\epsilon \in \text{FIRST}(X)$

$$X \rightarrow Y_1 Y_2 \dots Y_{i-1} Y_i \dots Y_k \rightarrow Y_i \dots Y_k$$

- If $X \rightarrow Y_1 Y_2 \dots Y_k$, $\epsilon \in \bigcap_{j=1}^{i-1} \text{FIRST}(Y_j) \wedge a \in \text{FIRST}(Y_i) \Rightarrow a \in \text{FIRST}(X)$

First()

- $\text{FIRST}(\alpha)$:
 - A set of terminals that α may start with
 - If X is a terminal, $\text{FIRST}(X) = \{X\}$
 - If $X \rightarrow \epsilon$ is a production, $\epsilon \in \text{FIRST}(X)$
 - If $X \rightarrow Y_1 Y_2 \dots Y_k$, $\epsilon \in \bigcap_{j=1}^{i-1} \text{FIRST}(Y_j) \wedge a \in \text{FIRST}(Y_i) \Rightarrow a \in \text{FIRST}(X)$
 $\epsilon \in \bigcap_{j=1}^k \text{FIRST}(Y_j) \Rightarrow \epsilon \in \text{FIRST}(X)$

$$X \rightarrow Y_1 Y_2 \dots Y_k \rightarrow \epsilon$$

First()

- **Example:** $S \rightarrow c A b; A \rightarrow a b \mid a$
- $\text{FIRST}(S) = \{c\}$
- $\text{FIRST}(A) = \{a\}$
- $\text{FIRST}(a) = \{a\}$
- $\text{FIRST}(b) = \{b\}$
- $\text{FIRST}(c) = \{c\}$

First()

- **Exercise:** write First() for all symbols in the following grammar

$E \rightarrow T X$

$X \rightarrow + E$

$X \rightarrow \varepsilon$

$T \rightarrow \text{int } Y$

$T \rightarrow (E)$

$Y \rightarrow * T$

$Y \rightarrow \varepsilon$

First()

- **Exercise:** write First() for all symbols in the following grammar

$E \rightarrow T X$
 $X \rightarrow + E$
 $X \rightarrow \varepsilon$
 $T \rightarrow \text{int } Y$
 $T \rightarrow (E)$
 $Y \rightarrow * T$
 $Y \rightarrow \varepsilon$

| Symbol | First |
|--------|------------------|
| (| (|
|) |) |
| + | + |
| * | * |
| int | int |
| Y | $\varepsilon, *$ |
| X | $\varepsilon, +$ |
| T | int, (|
| E | int, (|

Follow()

- FOLLOW(α):
 - A set of terminals that can appear immediately to the right of α

Follow()

- FOLLOW(α):
 - A set of terminals that can appear immediately to the right of α
 - $\$ \in \text{FOLLOW}(S)$, where $\$$ is string's end marker, S the start non-terminal

Follow()

- FOLLOW(α):
 - A set of terminals that can appear immediately to the right of α
 - $\$ \in \text{FOLLOW}(S)$, where $\$$ is string's end marker, S the start non-terminal
 - $A \rightarrow \alpha B \beta \Rightarrow \text{FIRST}(\beta) \setminus \{\epsilon\} \subseteq \text{FOLLOW}(B)$

| | |
|------------|---------|
| αB | β |
|------------|---------|

Follow()

- FOLLOW(α):
 - A set of terminals that can appear immediately to the right of α
 - $\$ \in \text{FOLLOW}(S)$, where $\$$ is string's end marker, S the start non-terminal
 - $A \rightarrow \alpha B \beta \Rightarrow \text{FIRST}(\beta) \setminus \{\epsilon\} \subseteq \text{FOLLOW}(B)$
 - $A \rightarrow \alpha B$ or $A \rightarrow \alpha B \beta$ where $\epsilon \in \text{FIRST}(\beta) \Rightarrow \text{FOLLOW}(A) \subseteq \text{FOLLOW}(B)$

| | |
|--------------------------|-----|
| $A \text{ or } \alpha B$ | ... |
|--------------------------|-----|

Follow()

- FOLLOW(α):
 - A set of terminals that can appear immediately to the right of α
 - $\$ \in \text{FOLLOW}(S)$, where $\$$ is string's end marker, S the start non-terminal
 - $A \rightarrow \alpha B \beta \Rightarrow \text{FIRST}(\beta) \setminus \{\epsilon\} \subseteq \text{FOLLOW}(B)$
 - $A \rightarrow \alpha B$ or $A \rightarrow \alpha B \beta$ where $\epsilon \in \text{FIRST}(\beta) \Rightarrow \text{FOLLOW}(A) \subseteq \text{FOLLOW}(B)$

| | |
|--------------------------|-----|
| $A \text{ or } \alpha B$ | ... |
|--------------------------|-----|

- **Note: repeat the procedure until fixed point!**

Follow()

- **Example:** $S \rightarrow c A b; A \rightarrow a b \mid a$
- $\text{FOLLOW}(S) = \{\$ \}$
- $\text{FOLLOW}(A) = \{b\}$

Follow()

- **Example:** $S \rightarrow c A b; A \rightarrow a b \mid a$
- $\text{FOLLOW}(S) = \{\$ \}$
- $\text{FOLLOW}(A) = \{b\}$
- **Example:** $S \rightarrow c A A; A \rightarrow a b \mid a$
- $\text{FOLLOW}(S) = \{\$ \}$

Follow()

- **Example:** $S \rightarrow c A b; A \rightarrow a b \mid a$
- $\text{FOLLOW}(S) = \{\$ \}$
- $\text{FOLLOW}(A) = \{b\}$
- **Example:** $S \rightarrow c A A; A \rightarrow a b \mid a$
- $\text{FOLLOW}(S) = \{\$ \}$
- $\text{FOLLOW}(A) \supseteq \text{FIRST}(A) \setminus \{\epsilon\} = \{a\}$

Follow()

- **Example:** $S \rightarrow c A b; A \rightarrow a b \mid a$
- $\text{FOLLOW}(S) = \{\$ \}$
- $\text{FOLLOW}(A) = \{b\}$
- **Example:** $S \rightarrow c A A; A \rightarrow a b \mid a$
- $\text{FOLLOW}(S) = \{\$ \}$
- $\text{FOLLOW}(A) \supseteq \text{FIRST}(A) \setminus \{\epsilon\} = \{a\}$
- $\text{FOLLOW}(A) \supseteq \text{FOLLOW}(S) = \{\$ \}$

Follow()

- **Exercise:** write Follow() for all symbols in the grammar

$E \rightarrow T X$
 $X \rightarrow + E$
 $X \rightarrow \varepsilon$
 $T \rightarrow \text{int } Y$
 $T \rightarrow (E)$
 $Y \rightarrow * T$
 $Y \rightarrow \varepsilon$

| Symbol | First |
|--------|-------------------|
| (| (|
|) |) |
| + | + |
| * | * |
| int | int |
| Y | ε , * |
| X | ε , + |
| T | int, (|
| E | int, (|

Follow()

- **Exercise:** write Follow() for all symbols in the grammar

$E \rightarrow T X$
 $X \rightarrow + E$
 $X \rightarrow \varepsilon$
 $T \rightarrow \text{int } Y$
 $T \rightarrow (E)$
 $Y \rightarrow * T$
 $Y \rightarrow \varepsilon$

| Symbol | First | Follow |
|--------|------------------|----------|
| (| (| N/A |
|) |) | |
| + | + | |
| * | * | |
| int | int | |
| Y | $\varepsilon, *$ |), \$, + |
| X | $\varepsilon, +$ |), \$ |
| T | int, (|), \$, + |
| E | int, (|), \$ |

Predictive Parsing Table

- To build a parsing table $M[A, a]$, for each $A \rightarrow \alpha$
 - $\forall a \in \text{FIRST}(\alpha): M[A, a] = A \rightarrow \alpha$
 - $\epsilon \in \text{FIRST}(\alpha) \Rightarrow \forall b \in \text{FOLLOW}(A): M[A, b] = A \rightarrow \alpha$

| | | |
|------|---------------|------------------------|
| E | \rightarrow | $T E'$ |
| E' | \rightarrow | $+ T E' \mid \epsilon$ |
| T | \rightarrow | $F T'$ |
| T' | \rightarrow | $* F T' \mid \epsilon$ |
| F | \rightarrow | $(E) \mid \text{id}$ |

| NON - TERMINAL | INPUT SYMBOL | | | | | |
|-------------------|---------------------------|---------------------------|-------------------------|-----------------------|---------------------------|---------------------------|
| | id | + | * | (|) | \$ |
| E | $E \rightarrow T E'$ | | | $E \rightarrow T E'$ | | |
| E' | | $E' \rightarrow + T E'$ | | | $E' \rightarrow \epsilon$ | $E' \rightarrow \epsilon$ |
| T | $T \rightarrow F T'$ | | | $T \rightarrow F T'$ | | |
| T' | | $T' \rightarrow \epsilon$ | $T' \rightarrow * F T'$ | | $T' \rightarrow \epsilon$ | $T' \rightarrow \epsilon$ |
| F | $F \rightarrow \text{id}$ | | | $F \rightarrow (E)$ | | |

Predictive Parsing Table

- To build a parsing table $M[A, a]$, for each $A \rightarrow \alpha$
 - $\forall a \in \text{FIRST}(\alpha): M[A, a] = A \rightarrow \alpha$
 - $\epsilon \in \text{FIRST}(\alpha) \Rightarrow \forall b \in \text{FOLLOW}(A): M[A, b] = A \rightarrow \alpha$

| | | |
|------|---------------|------------------------|
| E | \rightarrow | $T E'$ |
| E' | \rightarrow | $+ T E' \mid \epsilon$ |
| T | \rightarrow | $F T'$ |
| T' | \rightarrow | $* F T' \mid \epsilon$ |
| F | \rightarrow | $(E) \mid \text{id}$ |

| NON - TERMINAL | INPUT SYMBOL | | | | | |
|-------------------|---------------------------|---------------------------|-------------------------|-----------------------|---------------------------|---------------------------|
| | id | + | * | (|) | \$ |
| E | $E \rightarrow T E'$ | | | $E \rightarrow T E'$ | | |
| E' | | $E' \rightarrow + T E'$ | | | $E' \rightarrow \epsilon$ | $E' \rightarrow \epsilon$ |
| T | $T \rightarrow F T'$ | | | $T \rightarrow F T'$ | | |
| T' | | $T' \rightarrow \epsilon$ | $T' \rightarrow * F T'$ | | $T' \rightarrow \epsilon$ | $T' \rightarrow \epsilon$ |
| F | $F \rightarrow \text{id}$ | | | $F \rightarrow (E)$ | | |

Predictive Parsing Table

- To build a parsing table $M[A, a]$, for each $A \rightarrow \alpha$
 - $\forall a \in \text{FIRST}(\alpha): M[A, a] = A \rightarrow \alpha$
 - $\epsilon \in \text{FIRST}(\alpha) \Rightarrow \forall b \in \text{FOLLOW}(A): M[A, b] = A \rightarrow \alpha$

| | | |
|------|---------------|------------------------|
| E | \rightarrow | $T E'$ |
| E' | \rightarrow | $+ T E' \mid \epsilon$ |
| T | \rightarrow | $F T'$ |
| T' | \rightarrow | $* F T' \mid \epsilon$ |
| F | \rightarrow | $(E) \mid \text{id}$ |

| NON - TERMINAL | INPUT SYMBOL | | | | | |
|-------------------|---------------------------|---------------------------|-------------------------|-----------------------|---------------------------|---------------------------|
| | id | + | * | (|) | \$ |
| E | $E \rightarrow T E'$ | | | $E \rightarrow T E'$ | | |
| E' | | $E' \rightarrow + T E'$ | | | $E' \rightarrow \epsilon$ | $E' \rightarrow \epsilon$ |
| T | $T \rightarrow F T'$ | | | $T \rightarrow F T'$ | | |
| T' | | $T' \rightarrow \epsilon$ | $T' \rightarrow * F T'$ | | $T' \rightarrow \epsilon$ | $T' \rightarrow \epsilon$ |
| F | $F \rightarrow \text{id}$ | | | $F \rightarrow (E)$ | | |

Predictive Parsing Table



- To build a parsing table $M[A, a]$, for each $A \rightarrow \alpha$
 - $\forall a \in \text{FIRST}(\alpha): M[A, a] = A \rightarrow \alpha$
 - $\epsilon \in \text{FIRST}(\alpha) \Rightarrow \forall b \in \text{FOLLOW}(A): M[A, b] = A \rightarrow \alpha$

| | | |
|------|---------------|------------------------|
| E | \rightarrow | $T E'$ |
| E' | \rightarrow | $+ T E' \mid \epsilon$ |
| T | \rightarrow | $F T'$ |
| T' | \rightarrow | $* F T' \mid \epsilon$ |
| F | \rightarrow | $(E) \mid \text{id}$ |

| NON - TERMINAL | INPUT SYMBOL | | | | | |
|-------------------|---------------------------|---------------------------|-------------------------|-----------------------|---------------------------|---------------------------|
| | id | + | * | (|) | \$ |
| E | $E \rightarrow T E'$ | | | $E \rightarrow T E'$ | | |
| E' | | $E' \rightarrow + T E'$ | | | $E' \rightarrow \epsilon$ | $E' \rightarrow \epsilon$ |
| T | $T \rightarrow F T'$ | | | $T \rightarrow F T'$ | | |
| T' | | $T' \rightarrow \epsilon$ | $T' \rightarrow * F T'$ | | $T' \rightarrow \epsilon$ | $T' \rightarrow \epsilon$ |
| F | $F \rightarrow \text{id}$ | | | $F \rightarrow (E)$ | | |

- Choose the production according to the table, empty means error

Building a Parser in Practice

- Each non-terminal has a procedure or function for parsing
- => Recursive-Descent Parser
-  **Problem 1:** Backtracking may be necessary
 - when one derivation does not work, we may try others
-  **Problem 2:** A **left-recursive** grammar can cause **infinite loops**
 - when expanding a non-terminal, we may find itself and expand it again

LL(1) Grammar: Formal Definition

- LL(1) grammar (Not ambiguous! Not left-recursive!)
- A grammar is LL(1) if and only if any $A \rightarrow \alpha \mid \beta$ satisfies:
 - (1) For no terminal a do both α and β derive strings starting with a (by left factoring)
 - (2) At most one of α and β derive the empty string
 - (3) If $\beta \Rightarrow^* \epsilon$, α doesn't derive strings starting with terminals in FOLLOW(α)

| | | |
|------|---------------|--------------------------|
| E | \rightarrow | $T E'$ |
| E' | \rightarrow | $+ T E' \mid \epsilon$ |
| T | \rightarrow | $F T'$ |
| T' | \rightarrow | $* F T' \mid \epsilon$ |
| F | \rightarrow | $(E) \mid \mathbf{id}$ |

Recursive Predictive Parsing

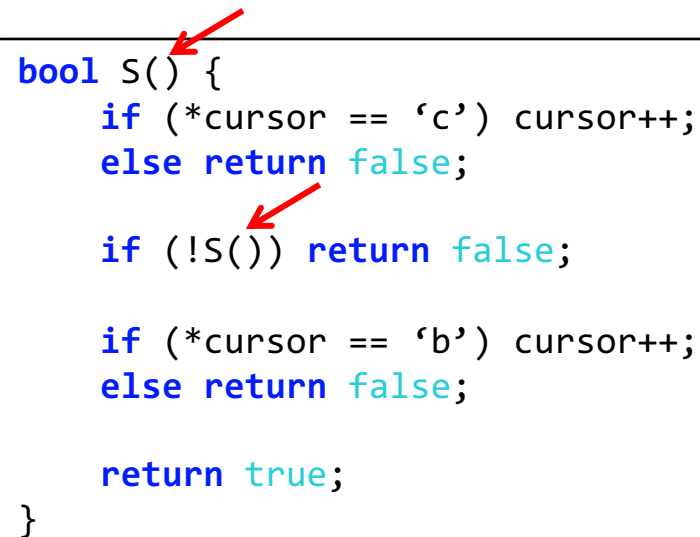
- Each non-terminal has a procedure or function for parsing
- => Recursive-Descent Parser
- **Example:** $S \rightarrow a S b \mid \epsilon$

```
bool S() {
    if (*cursor == 'c') cursor++;
    else return false;

    if (!S()) return false;

    if (*cursor == 'b') cursor++;
    else return false;

    return true;
}
```



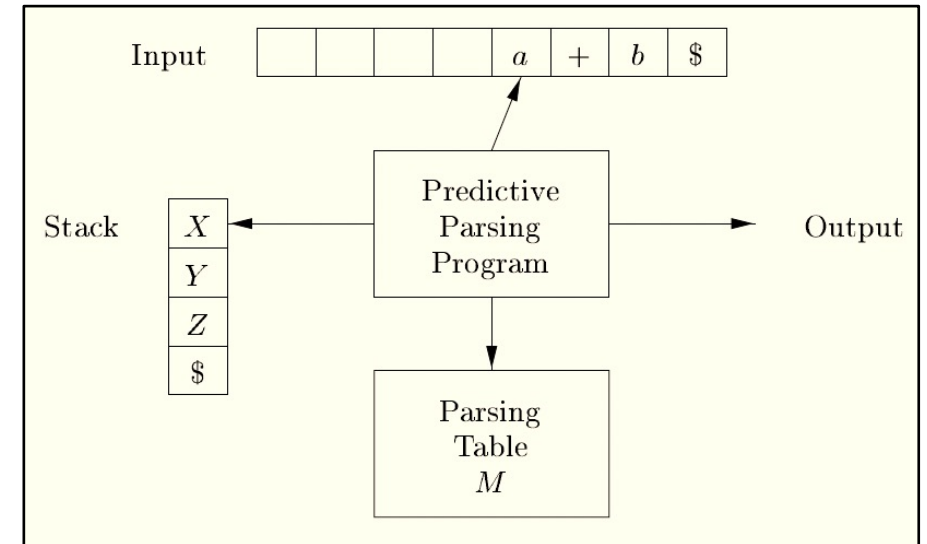
Non-recursive Predictive Parsing

Non-recursive Predictive Parsing

- How can we build a predictive parser without recursion?
- Maintain a stack explicitly!

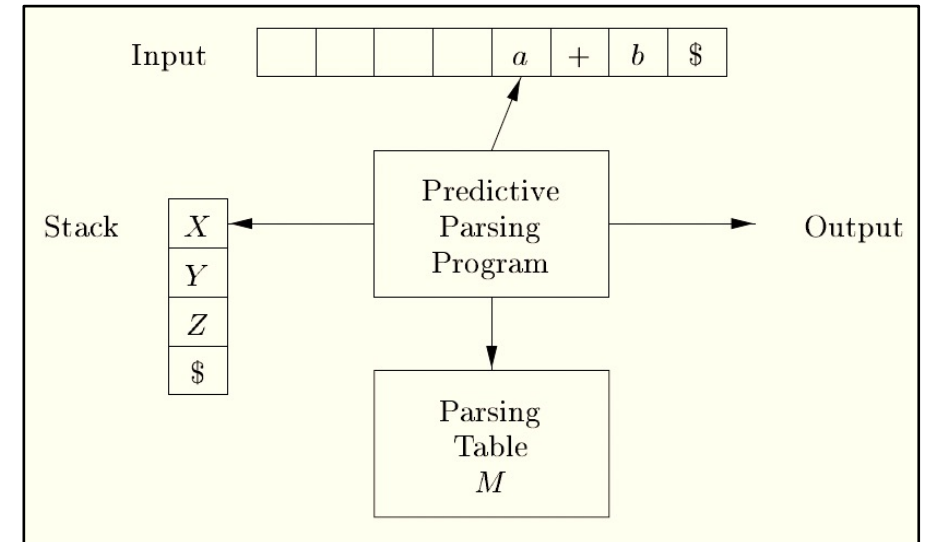
Non-recursive Predictive Parsing

- How can we build a predictive parser without recursion?
- Maintain a stack explicitly!



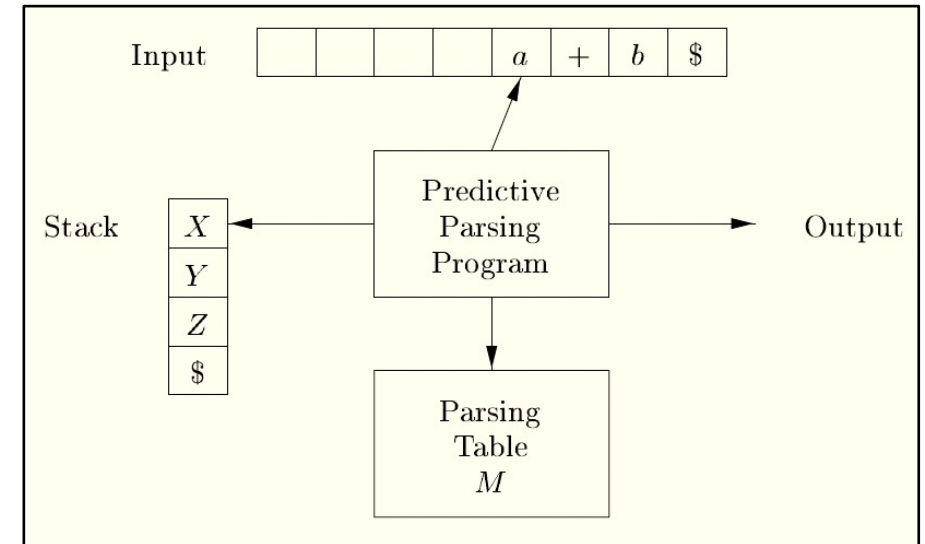
Non-recursive Predictive Parsing

- How can we build a predictive parser without recursion?
- Maintain a stack explicitly!
- Initially, we put S in the stack
- When $A \rightarrow \alpha$ is applied, pop A , push α



Non-recursive Predictive Parsing

- How can we build a predictive parser without recursion?
- Maintain a stack explicitly!
- Initially, we put S in the stack
- When $A \rightarrow \alpha$ is applied, pop A , push α
- Building the PDA from CFG!
- Parsing table is the set of transition functions of PDA!



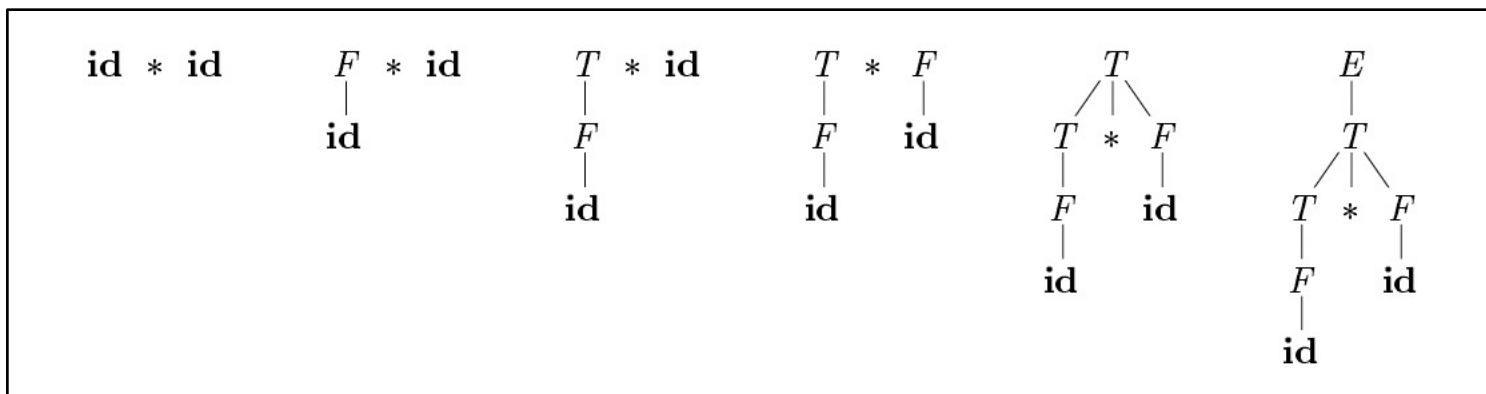
PART II: Bottom-Up Parsing

Bottom-up Parsing

- Top-down parsing can be viewed as the problem of constructing a parse tree **in preorder**
- Bottom-up parsing can be viewed as the problem of constructing a parse tree **in post-order**

Bottom-up Parsing

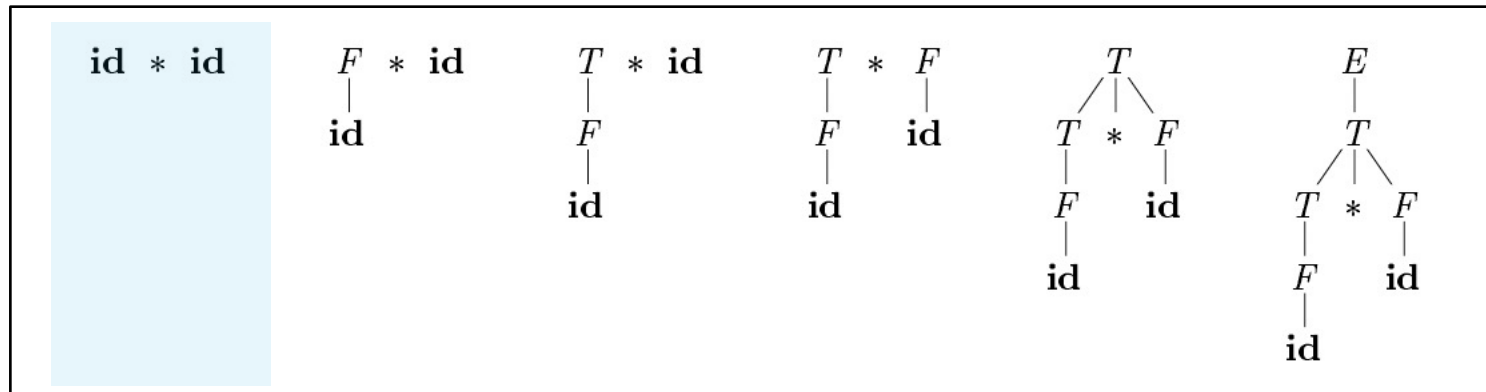
- Top-down parsing can be viewed as the problem of constructing a parse tree **in preorder**
- Bottom-up parsing can be viewed as the problem of constructing a parse tree **in post-order**



$$\begin{array}{lcl}
 E & \rightarrow & E + T \mid T \\
 T & \rightarrow & T * F \mid F \\
 F & \rightarrow & (E) \mid \text{id}
 \end{array}$$

Bottom-up Parsing

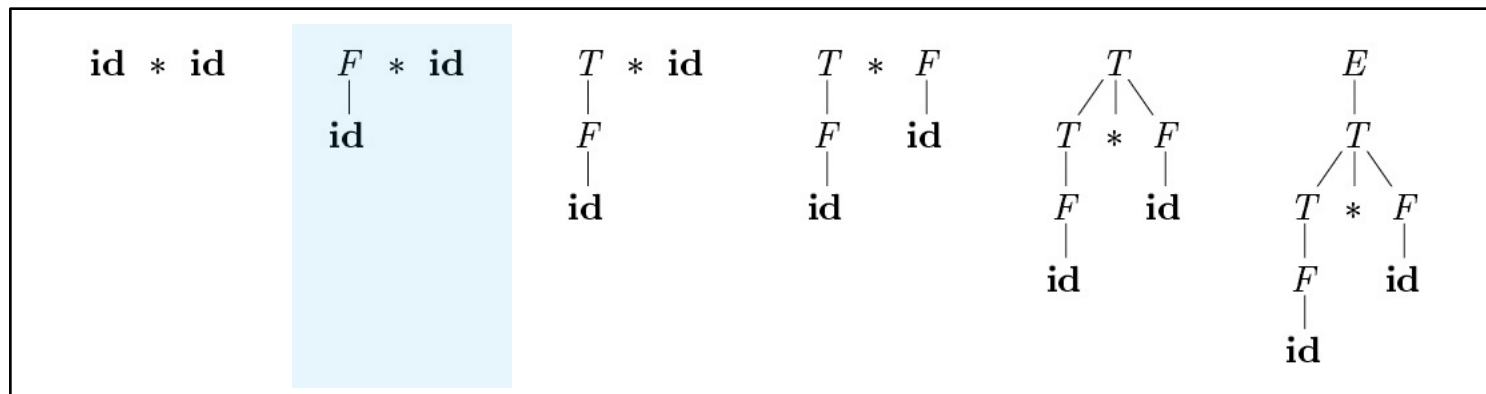
- Top-down parsing can be viewed as the problem of constructing a parse tree **in preorder**
- Bottom-up parsing can be viewed as the problem of constructing a parse tree **in post-order**



$$\begin{array}{lcl}
 E & \rightarrow & E + T \mid T \\
 T & \rightarrow & T * F \mid F \\
 F & \rightarrow & (E) \mid \text{id}
 \end{array}$$

Bottom-up Parsing

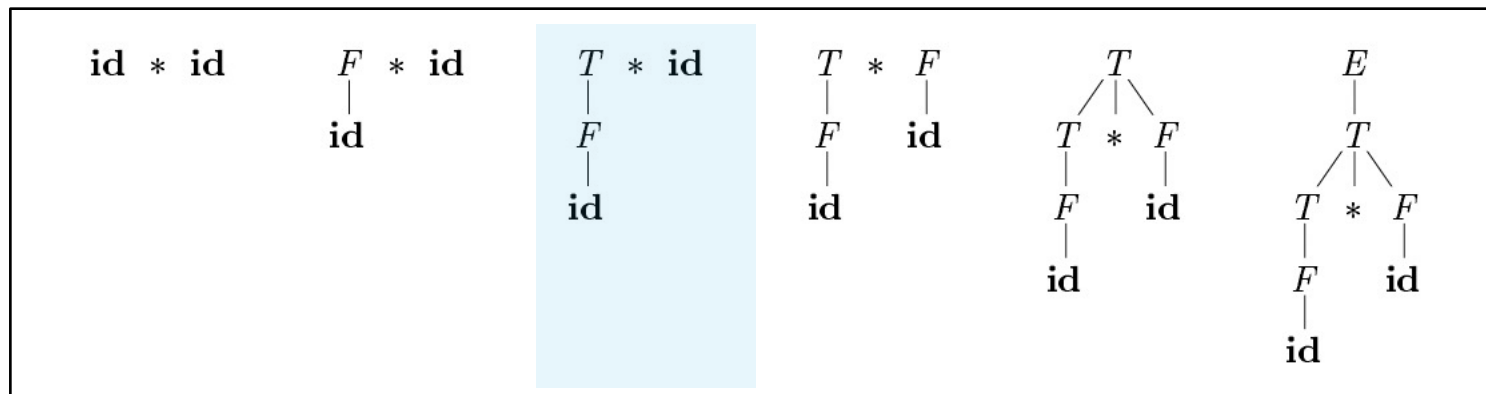
- Top-down parsing can be viewed as the problem of constructing a parse tree **in preorder**
- Bottom-up parsing can be viewed as the problem of constructing a parse tree **in post-order**



$$\begin{array}{lcl}
 E & \rightarrow & E + T \mid T \\
 T & \rightarrow & T * F \mid F \\
 F & \rightarrow & (E) \mid \text{id}
 \end{array}$$

Bottom-up Parsing

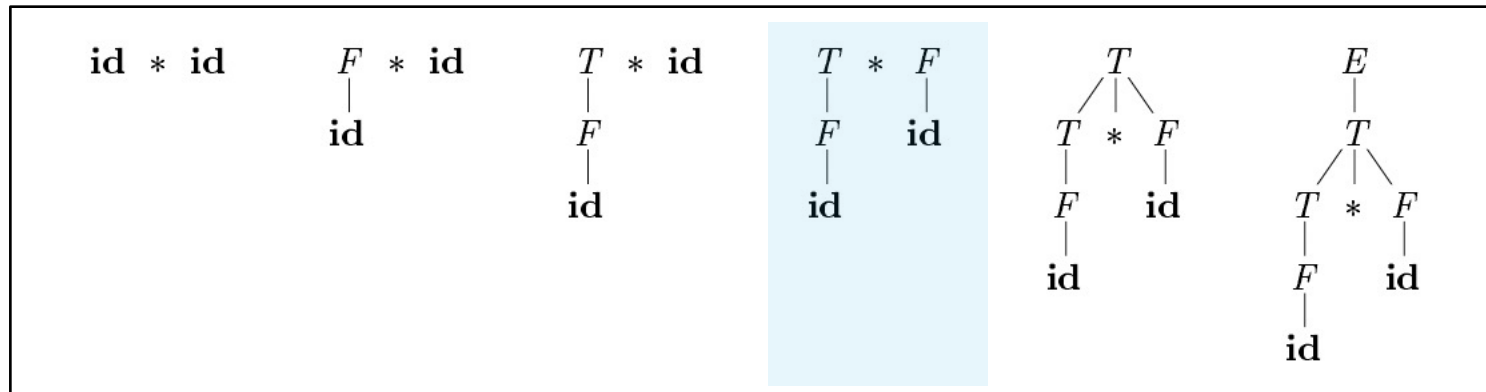
- Top-down parsing can be viewed as the problem of constructing a parse tree **in preorder**
- Bottom-up parsing can be viewed as the problem of constructing a parse tree **in post-order**



$$\begin{array}{lcl}
 E & \rightarrow & E + T \mid T \\
 T & \rightarrow & T * F \mid F \\
 F & \rightarrow & (E) \mid \text{id}
 \end{array}$$

Bottom-up Parsing

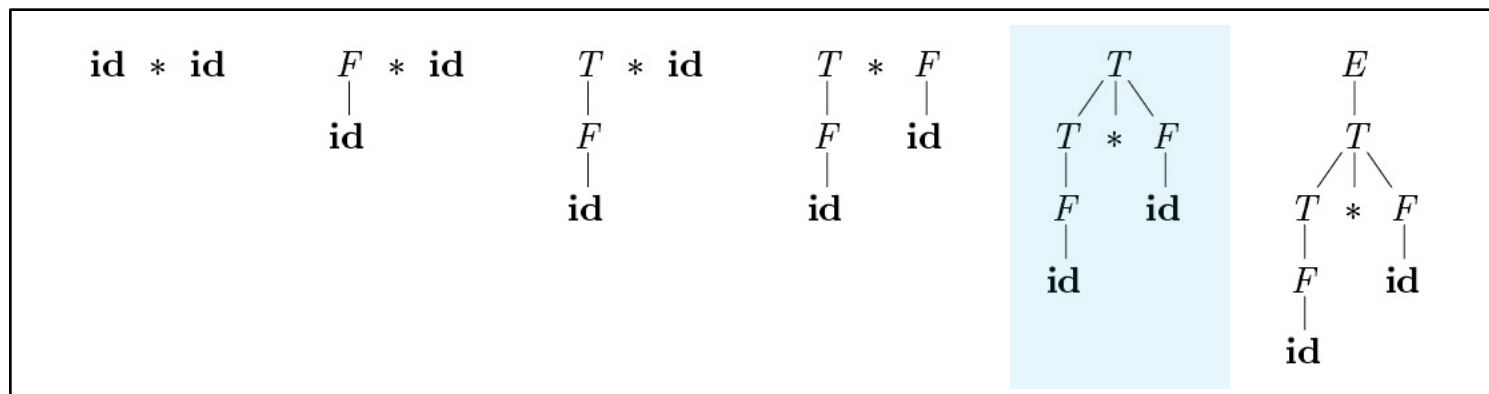
- Top-down parsing can be viewed as the problem of constructing a parse tree **in preorder**
- Bottom-up parsing can be viewed as the problem of constructing a parse tree **in post-order**



$$\begin{array}{lcl}
 E & \rightarrow & E + T \mid T \\
 T & \rightarrow & T * F \mid F \\
 F & \rightarrow & (E) \mid \text{id}
 \end{array}$$

Bottom-up Parsing

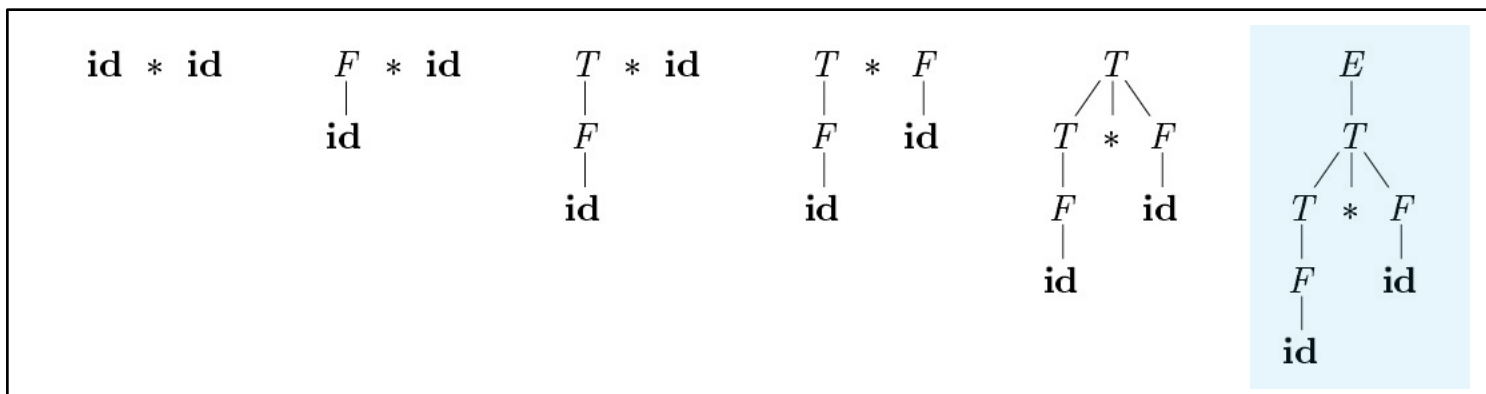
- Top-down parsing can be viewed as the problem of constructing a parse tree **in preorder**
- Bottom-up parsing can be viewed as the problem of constructing a parse tree **in post-order**



$$\begin{array}{lcl}
 E & \rightarrow & E + T \mid T \\
 T & \rightarrow & T * F \mid F \\
 F & \rightarrow & (E) \mid id
 \end{array}$$

Bottom-up Parsing

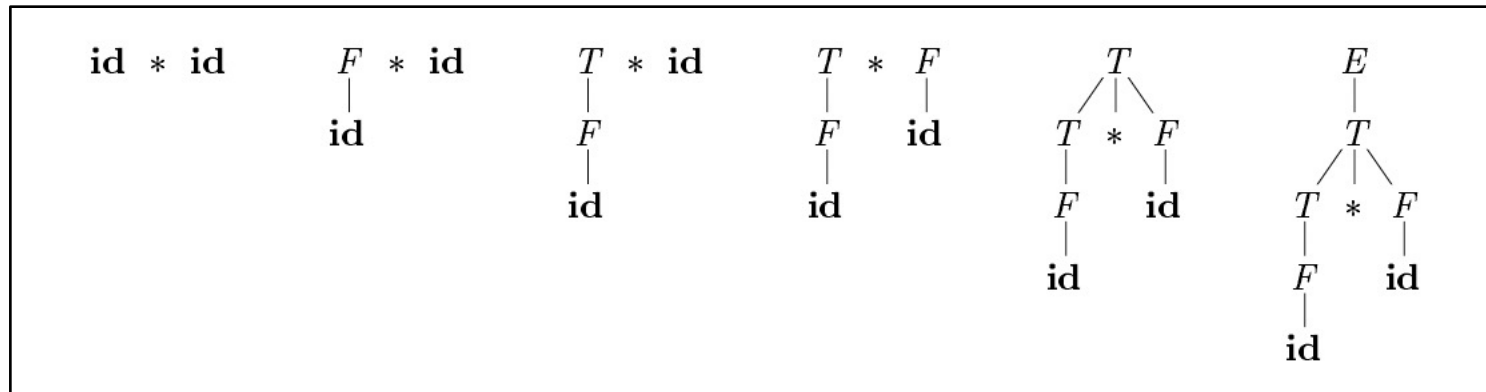
- Top-down parsing can be viewed as the problem of constructing a parse tree **in preorder**
- Bottom-up parsing can be viewed as the problem of constructing a parse tree **in post-order**



$$\begin{array}{lcl}
 E & \rightarrow & E + T \mid T \\
 T & \rightarrow & T * F \mid F \\
 F & \rightarrow & (E) \mid \text{id}
 \end{array}$$

Bottom-up Parsing

- Keep shifting until we see the right-hand side of a rule
- Keep reducing as long as the tail of our shifted sequence matches the right-hand side of a rule. Then go back to shifting



| | | |
|-----|---------------|-----------------|
| E | \rightarrow | $E + T \mid T$ |
| T | \rightarrow | $T * F \mid F$ |
| F | \rightarrow | $(E) \mid id$ |

Bottom-up Parsing

- Keep shifting until we see the right-hand side of a rule
- Keep reducing as long as the tail of our shifted sequence matches the right-hand side of a rule. Then go back to shifting
- Once we have the right-hand side of a rule:
 - Do we reduce right away, or do we keep shifting more symbols?
 - What if there are multiple rules with the same RHS to reduce by?

LR(0)

- LL(1) top-down parsing, we dealt with the tough decisions by just saying
 - "if we have to make decisions, it's not an LL(1) grammar".

LR(0)

- LL(1) top-down parsing, we dealt with the tough decisions by just saying
 - "if we have to make decisions, it's not an LL(1) grammar".
- We'll start out by looking at LR(0) parsing
 - We only worry about how to handle grammars that **don't require us to make decisions during parsing**

LR(0)

- LL(1) top-down parsing, we dealt with the tough decisions by just saying
 - "if we have to make decisions, it's not an LL(1) grammar".
- We'll start out by looking at LR(0) parsing
 - We only worry about how to handle grammars that **don't require us to make decisions during parsing**
 - Left-to-right scanning
 - Right-most derivation
 - Zero symbols of lookahead

LR(0)

- Keep shifting until we see the right-hand side of a rule
- Keep reducing as long as the tail of our shifted sequence matches the right-hand side of a rule. Then go back to shifting

LR(0)

- Keep shifting until we see the right-hand side of a rule
- Keep reducing as long as the tail of our shifted sequence matches the right-hand side of a rule. Then go back to shifting
- If this algorithm ever has to make decisions about which rule to
- reduce by, we give up and say "the grammar is not LR(0)".

LR(0)

- Keep shifting until we see the right-hand side of a rule
- Keep reducing as long as the tail of our shifted sequence matches the right-hand side of a rule. Then go back to shifting
- If this algorithm ever has to make decisions about which rule to
- reduce by, we give up and say "the grammar is not LR(0)".
 - LR(1), SLR(1), ...
 - Refer to Chapter 4, the Dragon book!

LR(0)

???

- Keep shifting until **we see the right-hand side of a rule**
- Keep reducing as long as the tail of our shifted sequence matches the right-hand side of a rule. Then go back to shifting
- If this algorithm ever has to make decisions about which rule to
- reduce by, we give up and say "the grammar is not LR(0)".
 - LR(1), SLR(1), ...
 - Refer to Chapter 4, the Dragon book!

LR(0)

??? DFA/NFA!!!

- Keep shifting until **we see the right-hand side of a rule**
- Keep reducing as long as the tail of our shifted sequence matches the right-hand side of a rule. Then go back to shifting
- If this algorithm ever has to make decisions about which rule to
- reduce by, we give up and say "the grammar is not LR(0)".
 - LR(1), SLR(1), ...
 - Refer to Chapter 4, the Dragon book!

Recognizing the RHS

$$E \rightarrow E + T$$

$$E \rightarrow T$$

$$T \rightarrow T * F$$

$$T \rightarrow F$$

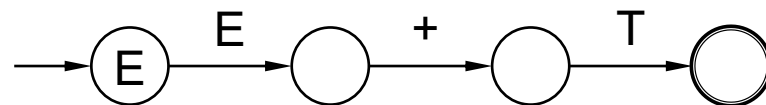
$$F \rightarrow (E)$$

$$F \rightarrow \mathbf{id}$$

Create DFAs for the RHS of each rule and mark the initial states with the LHS.

Recognizing the RHS

$$E \rightarrow E + T$$



Create DFAs for the RHS of each rule and mark the initial states with the LHS.

$$E \rightarrow T$$

$$T \rightarrow T * F$$

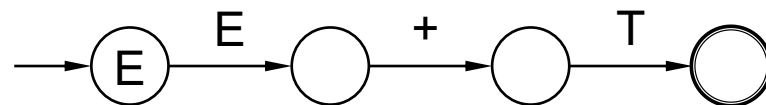
$$T \rightarrow F$$

$$F \rightarrow (E)$$

$$F \rightarrow \text{id}$$

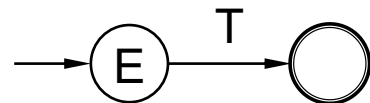
Recognizing the RHS

$$E \rightarrow E + T$$



Create DFAs for the RHS of each rule and mark the initial states with the LHS.

$$E \rightarrow T$$



$$T \rightarrow T * F$$

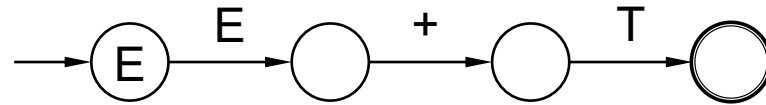
$$T \rightarrow F$$

$$F \rightarrow (E)$$

$$F \rightarrow \text{id}$$

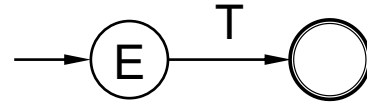
Recognizing the RHS

$$E \rightarrow E + T$$

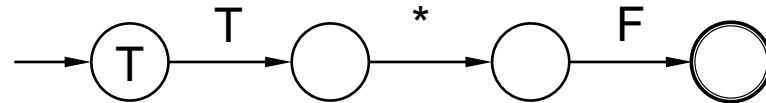


Create DFAs for the RHS of each rule and mark the initial states with the LHS.

$$E \rightarrow T$$



$$T \rightarrow T * F$$



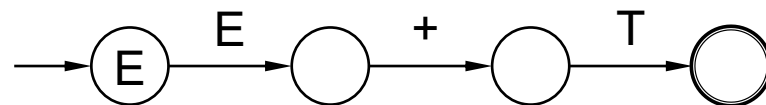
$$T \rightarrow F$$

$$F \rightarrow (E)$$

$$F \rightarrow \text{id}$$

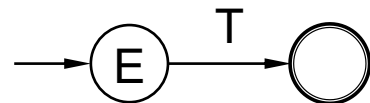
Recognizing the RHS

$E \rightarrow E + T$

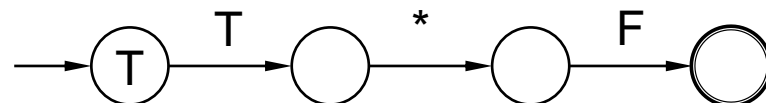


Create DFAs for the RHS of each rule and mark the initial states with the LHS.

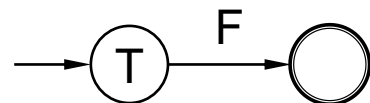
$E \rightarrow T$



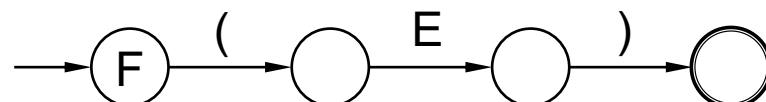
$T \rightarrow T * F$



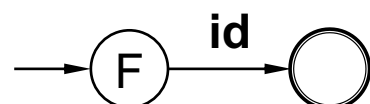
$T \rightarrow F$



$F \rightarrow (E)$

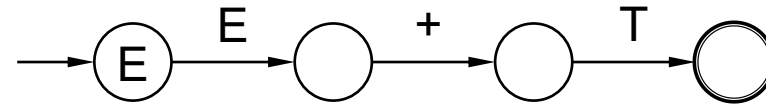


$F \rightarrow \text{id}$

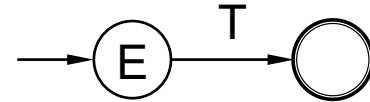


Recognizing the RHS

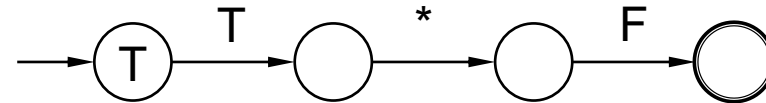
$E \rightarrow E + T$



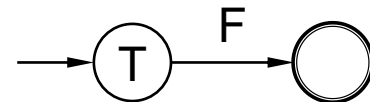
$E \rightarrow T$



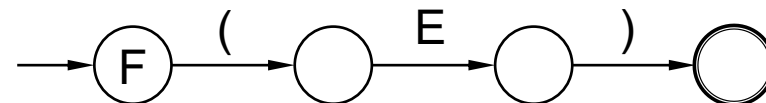
$T \rightarrow T * F$



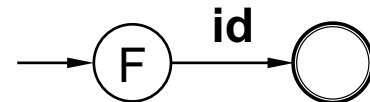
$T \rightarrow F$



$F \rightarrow (E)$



$F \rightarrow \text{id}$

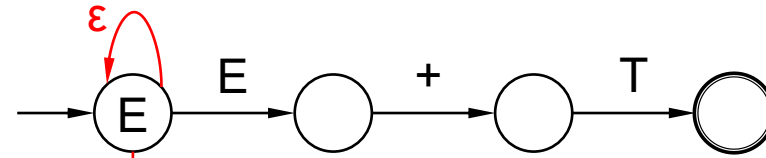


Create DFAs for the RHS of each rule and mark the initial states with the LHS.

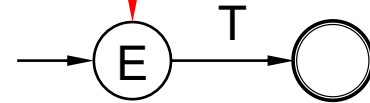
For each state with a transition leading **outwards on a nonterminal**, connect the state (using ϵ -transitions) to all the states marked with that nonterminal.

Recognizing the RHS

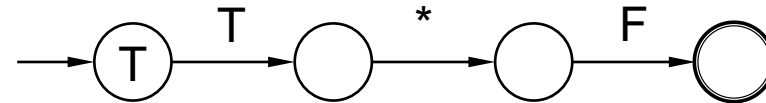
$E \rightarrow E + T$



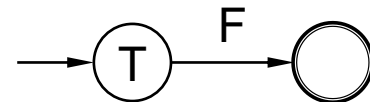
$E \rightarrow T$



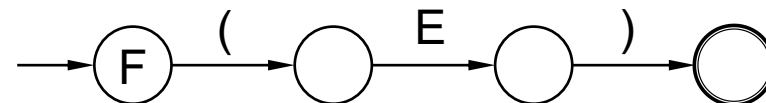
$T \rightarrow T * F$



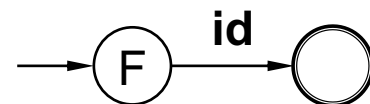
$T \rightarrow F$



$F \rightarrow (E)$



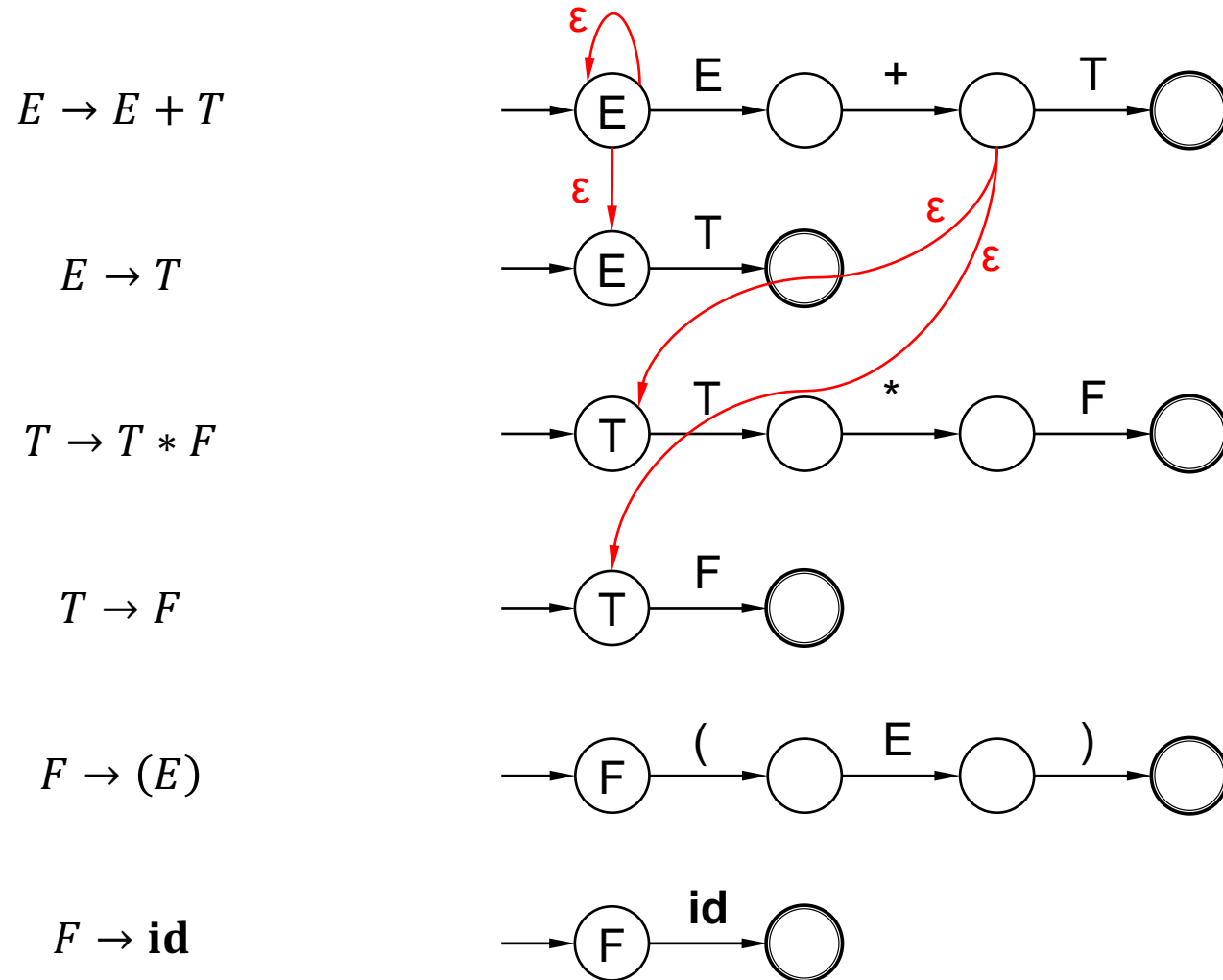
$F \rightarrow \text{id}$



Create DFAs for the RHS of each rule and mark the initial states with the LHS.

For each state with a transition leading **outwards on a nonterminal**, connect the state (using ϵ -transitions) to all the states marked with that nonterminal.

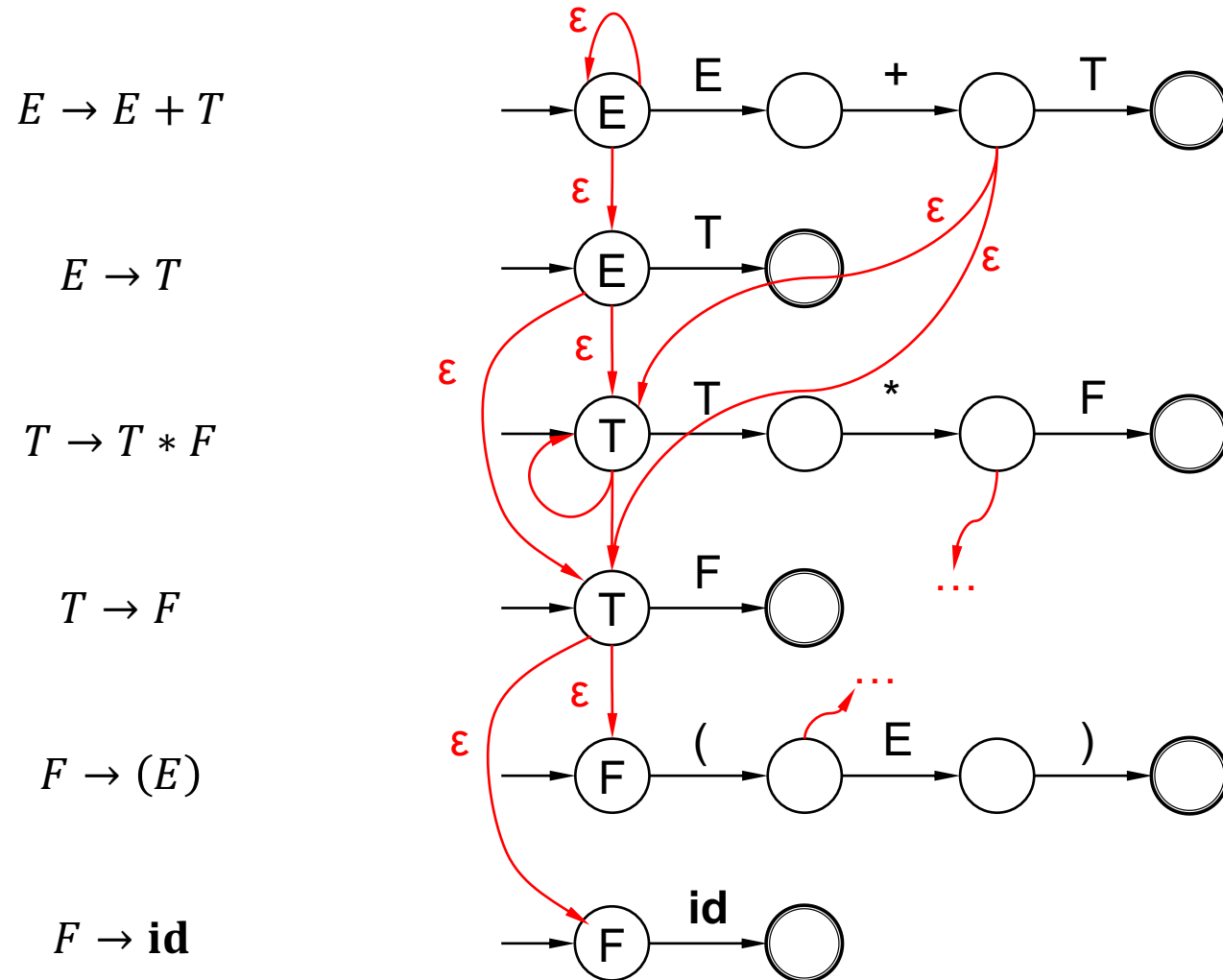
Recognizing the RHS



Create DFAs for the RHS of each rule and mark the initial states with the LHS.

For each state with a transition leading **outwards on a nonterminal**, connect the state (using ϵ -transitions) to all the states marked with that nonterminal.

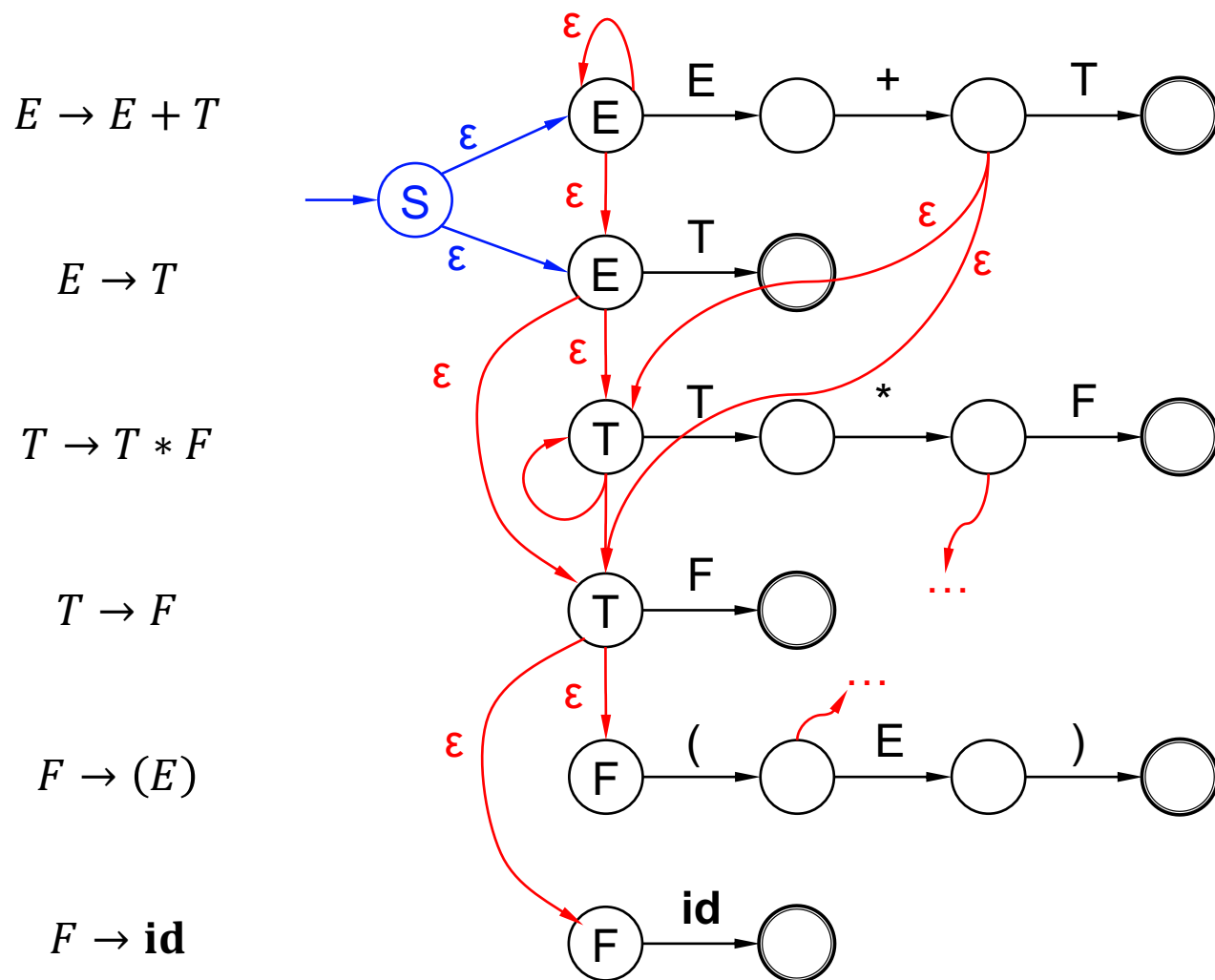
Recognizing the RHS



Create DFAs for the RHS of each rule and mark the initial states with the LHS.

For each state with a transition leading **outwards on a nonterminal**, connect the state (using ϵ -transitions) to all the states marked with that nonterminal.

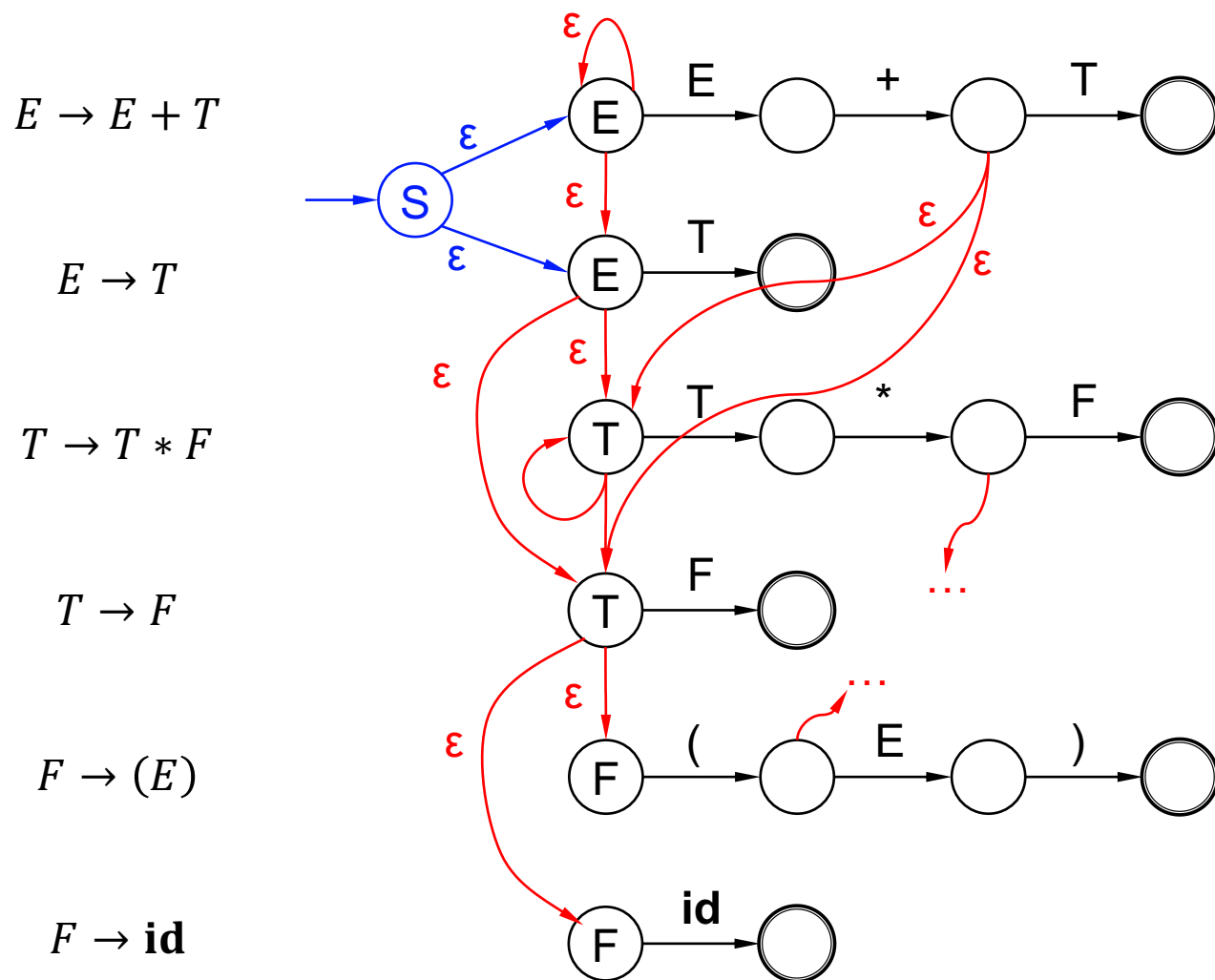
Recognizing the RHS



Create DFAs for the RHS of each rule and mark the initial states with the LHS.

For each state with a transition leading **outwards on a nonterminal**, connect the state (using ϵ -transitions) to all the states marked with that nonterminal.

Recognizing the RHS

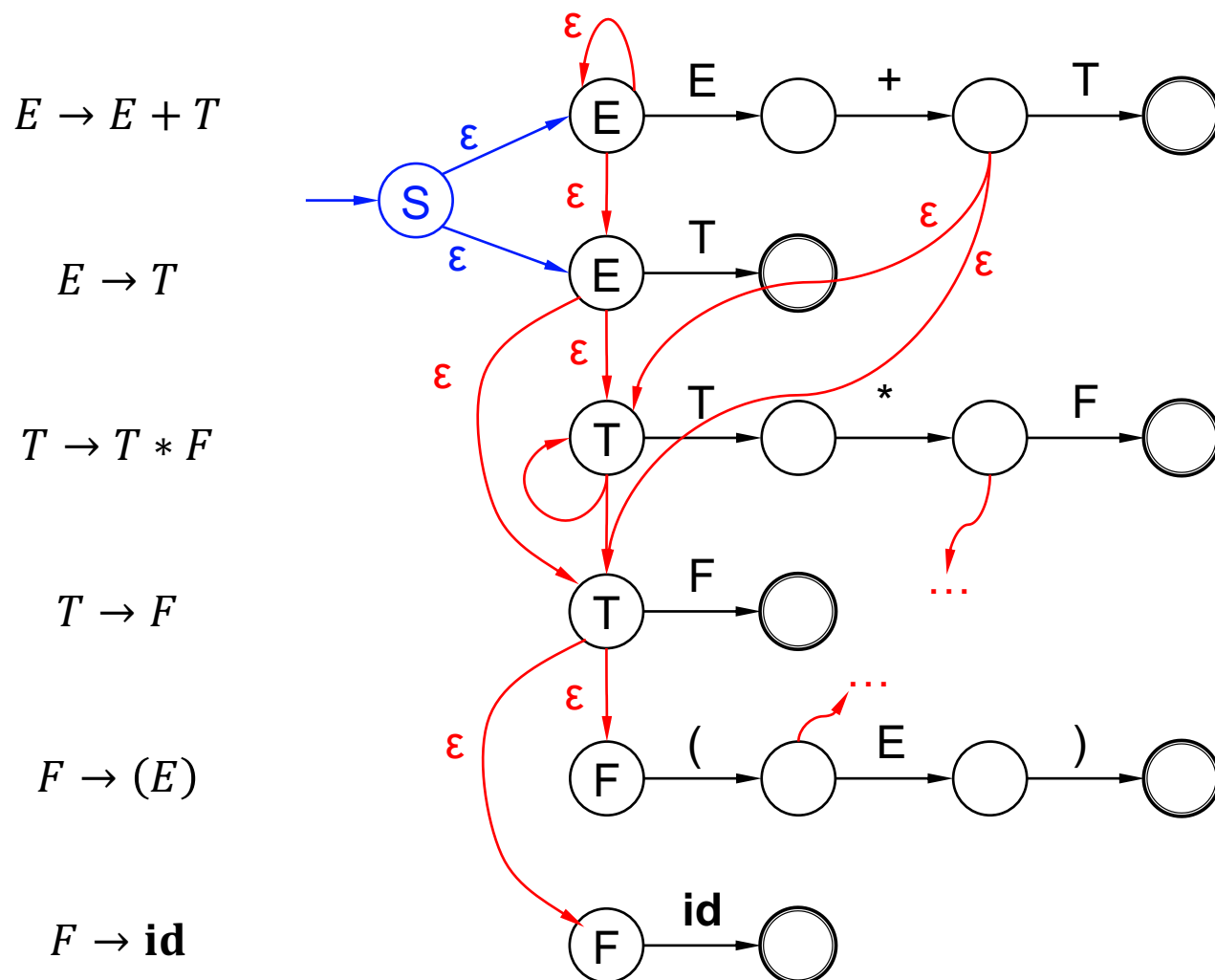


Create DFAs for the RHS of each rule and mark the initial states with the LHS.

For each state with a transition leading **outwards on a nonterminal**, connect the state (using ϵ -transitions) to all the states marked with that nonterminal.

We can transform it into a DFA

Recognizing the RHS



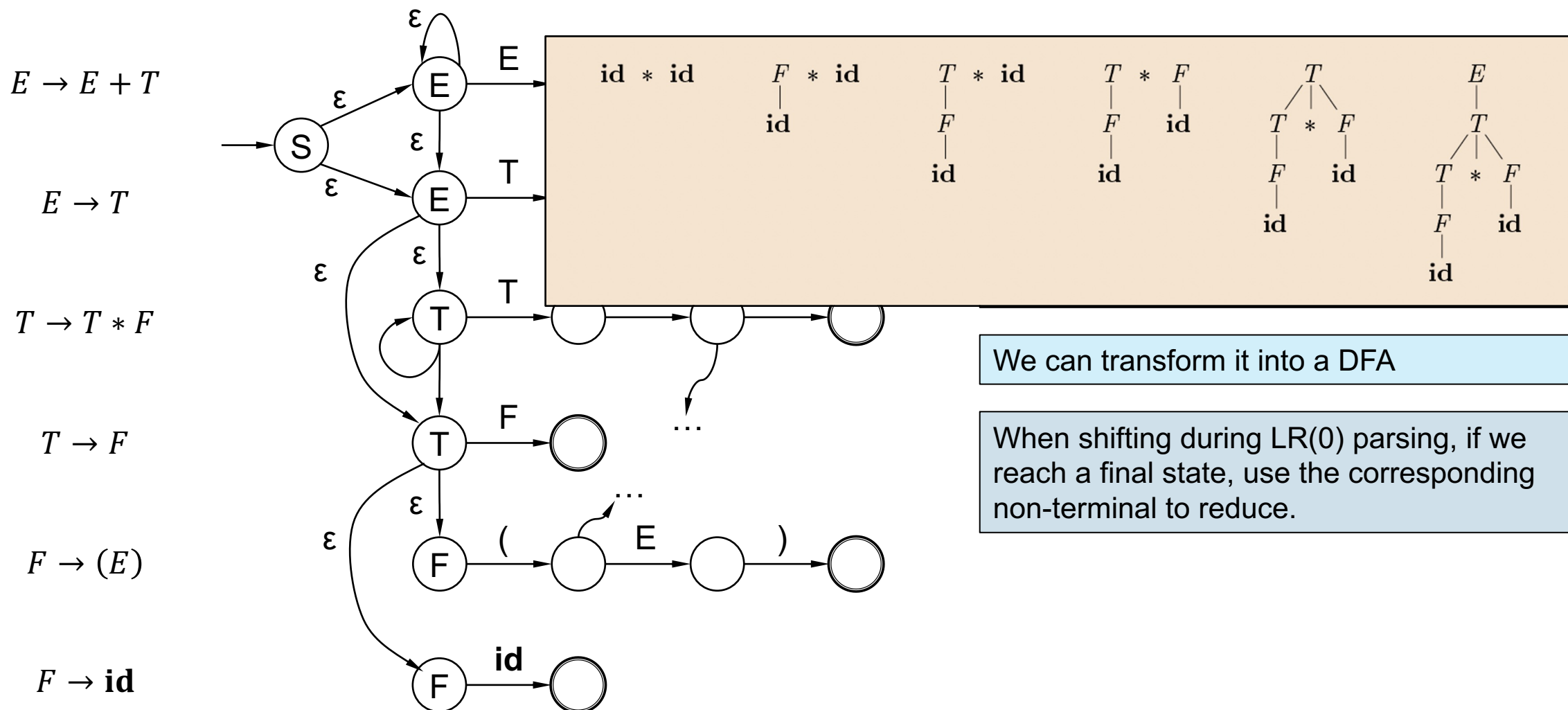
Create DFAs for the RHS of each rule and mark the initial states with the LHS.

For each state with a transition leading **outwards on a nonterminal**, connect the state (using ϵ -transitions) to all the states marked with that nonterminal.

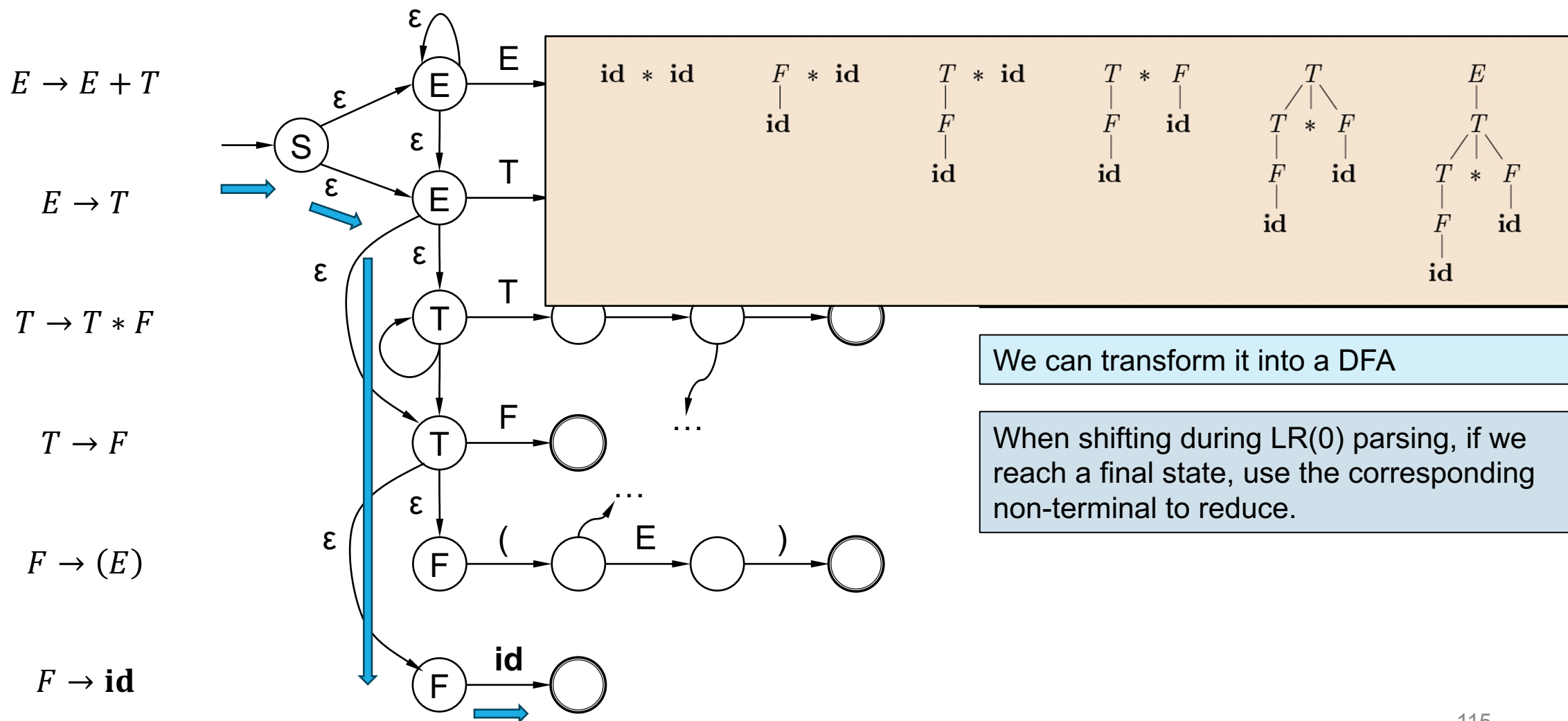
We can transform it into a DFA

When shifting during LR(0) parsing, if we reach a final state, use the corresponding non-terminal to reduce.

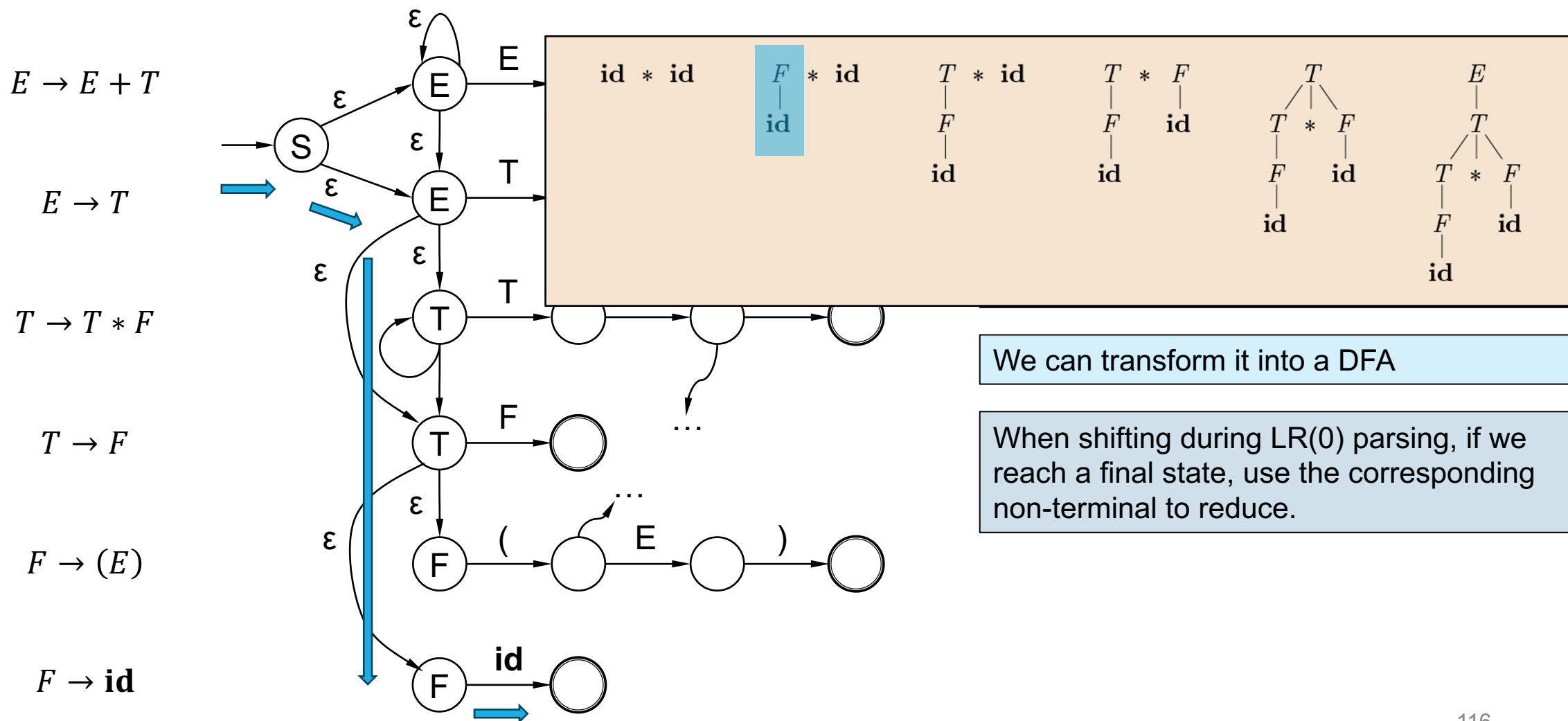
Recognizing the RHS



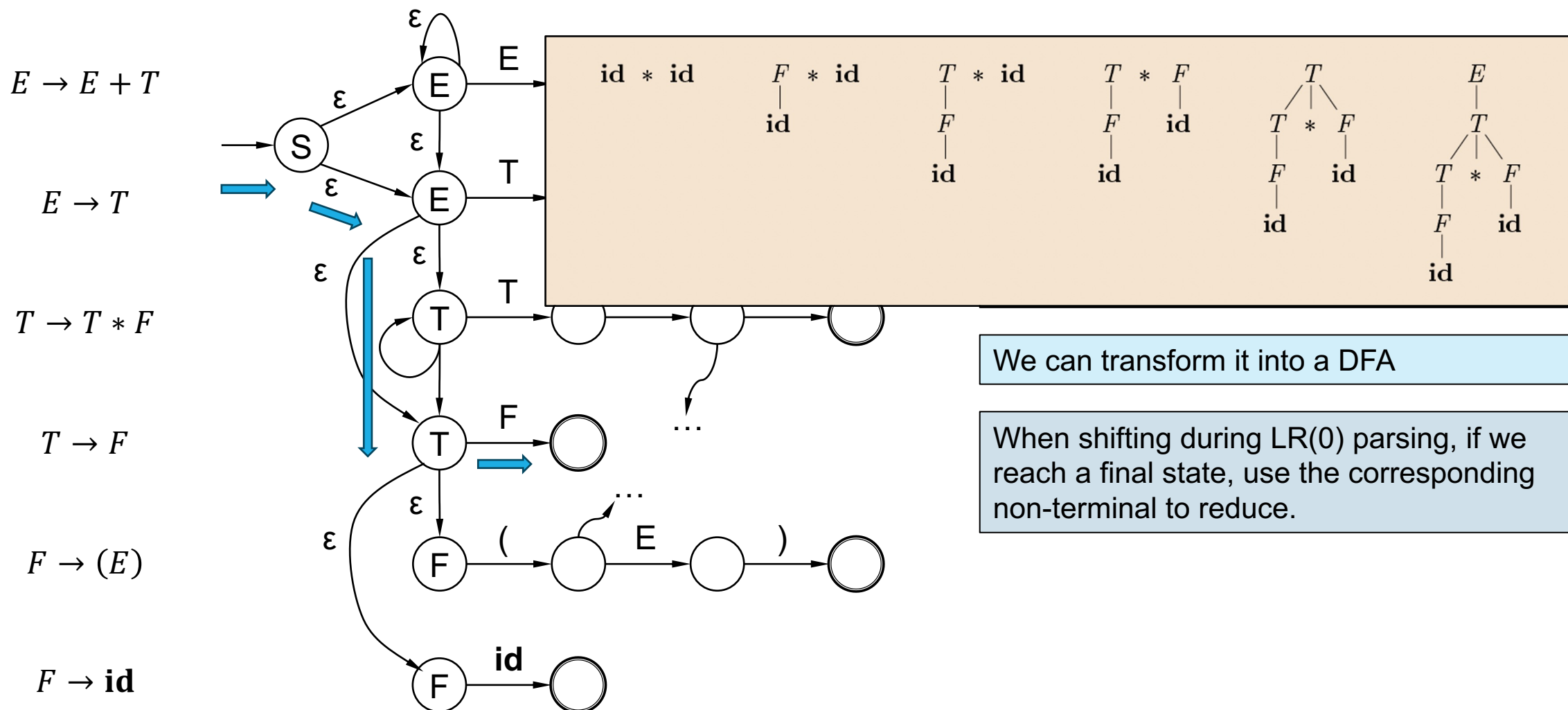
Recognizing the RHS



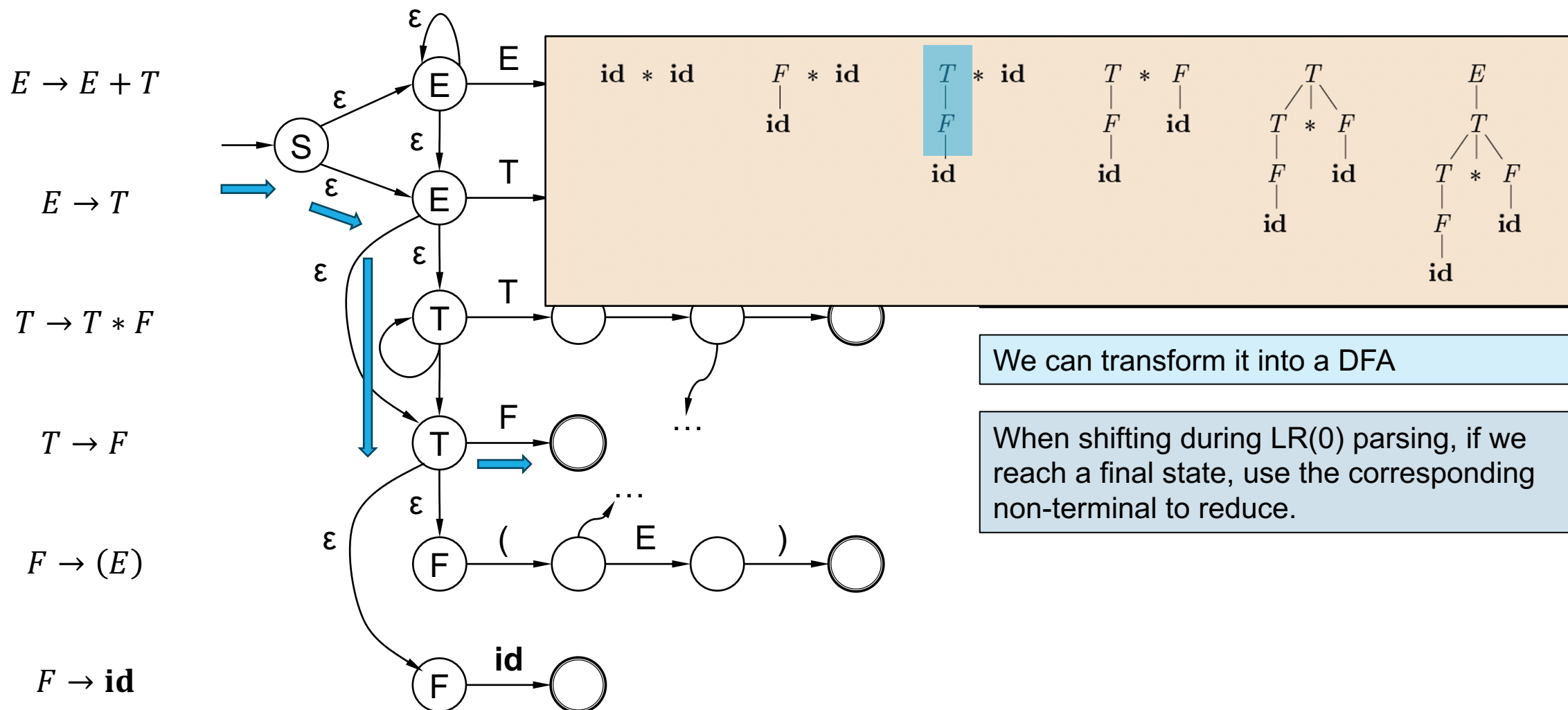
Recognizing the RHS



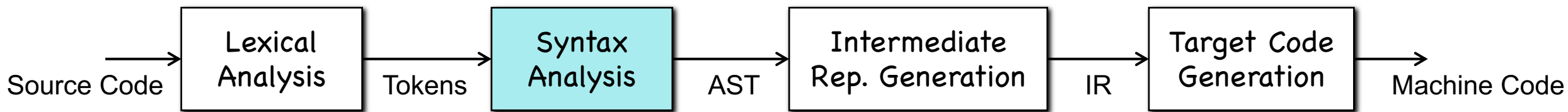
Recognizing the RHS



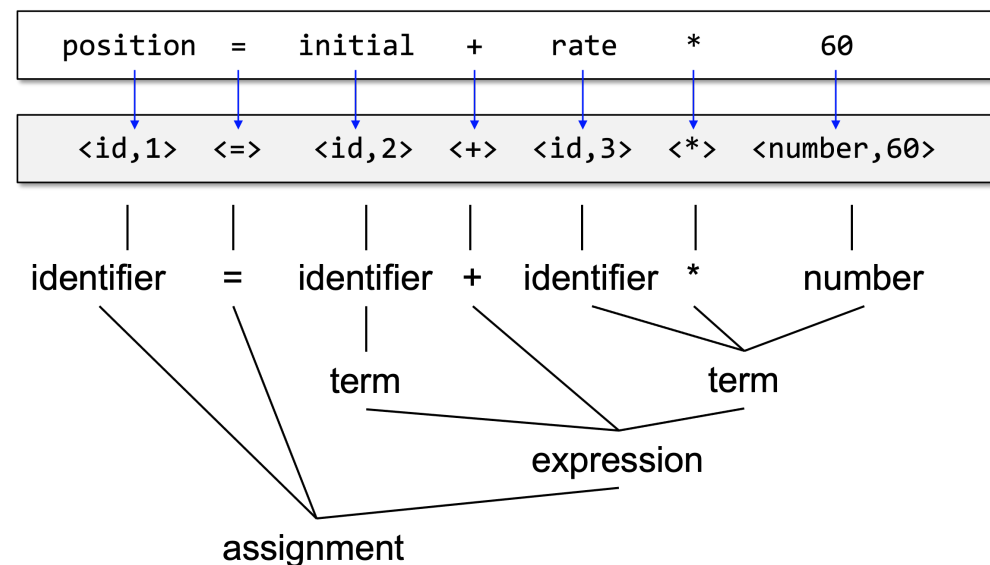
Recognizing the RHS



Summary



- Syntax analysis is a procedure of building the parse/syntax tree
 - Top-down parsing and LL parsing
 - Recursive-descent parsers
 - Eliminating left-recursive
 - Predictive parsers, LL(1) parsers
 - Non-recursive predictive parser vs. PDA
 - Bottom-up parsing and LR parsing
 - LR(0) parser
 - Refer to § 4.5, Chapter 4, the Dragon book!



THANKS!