PBKDF2: performance matters

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ANGER TO





1. Quick intro to PBKDF2









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- 2. The standard is bad









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- 3. Your implementation is bad
- 4. A faster PBKDF2



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Usage

- Password verification (web sites, network services, etc.)
- Key derivation (disk encryption, key management, etc.)



Performance

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Simplification

PBKDF2 can produce arbitrary length output.

We're going to ignore this capability from here on in: only considering the first block of output.

PBKDF2: how it was described



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$$\begin{split} \mathsf{PBKDF2}_{\mathsf{PRF}}(\mathsf{pw},\mathsf{salt},\mathsf{i}) &\coloneqq U_1 \oplus U_2 \oplus \cdots \oplus U_{\mathsf{i}} \\ & \mathsf{where} \\ & U_1 \coloneqq \mathsf{PRF}(\mathsf{pw},\mathsf{salt} \parallel \mathsf{0}_{32}) \\ & U_n \coloneqq \mathsf{PRF}(\mathsf{pw},U_{n-1}) \end{split}$$

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```

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\mathsf{block}\ 1 : \mathit{key} \oplus \mathsf{ipad}
\mathsf{block}\ 2 : \mathit{msg}
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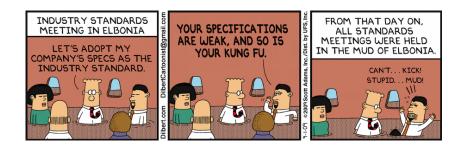
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Therefore, we need to compute 4i SHA-256 blocks.



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 with $U_1 \coloneqq \mathsf{HMAC ext{-}H(pw, salt} \parallel \mathsf{0}_{32})$ $U_n \coloneqq \mathsf{HMAC ext{-}H(pw}, U_{n-1})$

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Actually, we only need compute 2 + 2i SHA-256 blocks.

Survey of defender implementations

I looked at the following PBKDF2s:

- ► FreeBSD 10
- ► GRUB 2.0
- ► Truecrypt 7.1a
- Android (disk encryption)
- Android (BouncyCastle)
- Django
- OpenSSL
- ▶ Python core (\geq 3.4)
- Python (pypi pbkdf2)
- Ruby (pbkdf2 gem)
- ► Go (go.crypto)

- OpenBSD
- PolarSSL/mbedTLS
- CyaSSL/wolfSSL
- SJCL
- Java
- ► Common Lisp (ironclad)
- Perl (Crypt::PBKDF2)
- ► PHP5
- .NET framework
- scrypt/yescrypt¹
- BouncyCastle

¹never called for scrypt/yescrypt with iterations != 1

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Measured on Intel Atom N2800 (1.86GHz), best of five runs, CPU time in user mode.

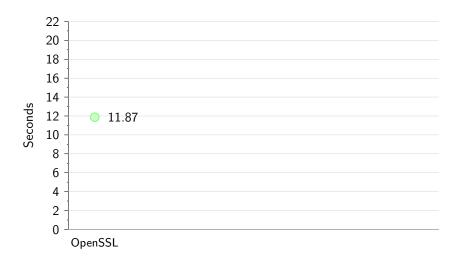


Figure: PBKDF2-HMAC-SHA1, one block output, 2²² iterations

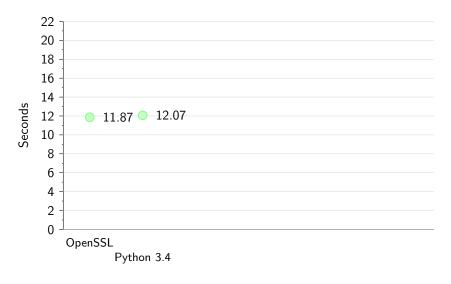


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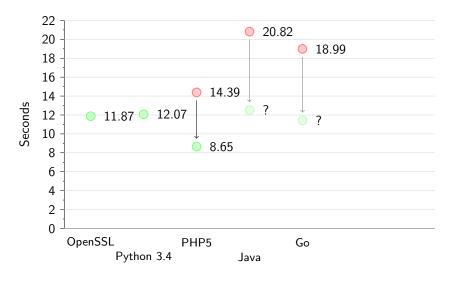


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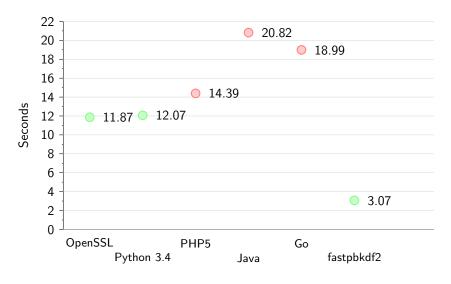


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- https://github.com/ctz/fastpbkdf2/

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- Most implementations waste time and power.
- If you use PBKDF2, you can probably drop in a faster implementation and either increase security margin, or improve time/power performance.
- ▶ Please try not to use PBKDF2 any more.

Thank you!

Questions?

Twitter: @jpixton
Mail: jbp@jbp.io

Web: https://jbp.io/

Slides and benchmarking code: https://github.com/ctz/talks/