PBKDF2: performance matters

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Purpose

Slowly convert a password $+\mbox{ salt}$ into a symmetric key of some length



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Slowly convert a password + salt into a symmetric key of some length

Origin

RSA labs, 1999. Described in PKCS#5 and then RFC2898



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- ▶ Key derivation (disk encryption, key management, etc.)

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Simplification

PBKDF2 can produce arbitrary length output.

We're going to ignore this capability from here on in: only considering the first block of output.

PBKDF2: how it was described

 $\mathsf{PBKDF2}_{\mathsf{PRF}}(\mathsf{pw},\mathsf{salt},\mathsf{i}) \coloneqq \mathit{U}_1 \oplus \mathit{U}_2 \oplus \cdots \oplus \mathit{U}_\mathsf{i}$

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Assumption: password and salt much shorter than SHA-256's 64-byte block size.

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Therefore, we need to compute 4i SHA-256 blocks.

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Actually, we only need compute 2 + 2i SHA-256 blocks.

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- ▶ Python core (≥3.4)
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Bad: compute 4*i* blocks

- Python (pypi pbkdf2)
- Ruby (pbkdf2 gem)
- ► Go (go.crypto)
- OpenBSD
- ► PolarSSL
- CyaSSL
- Java (OpenJDK)
- ► Common Lisp (ironclad)
 - ► Perl (Crypt::PBKDF2)
 - ► PHP
 - ► C#

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- ▶ Let's measure PBKDF2-HMAC-SHA1 for large iteration count (2²²)



Figure: PBKDF2-HMAC-SHA1, one block output, 2²² iterations

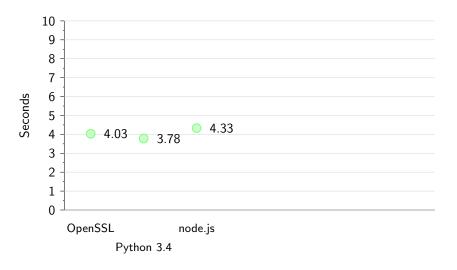


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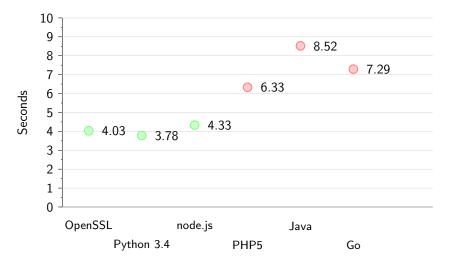


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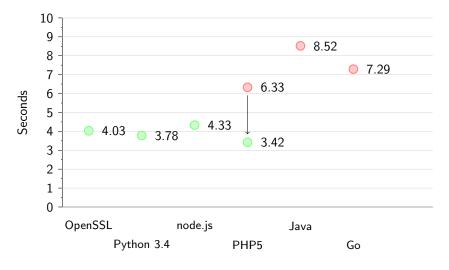


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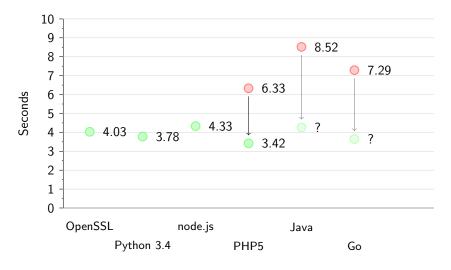


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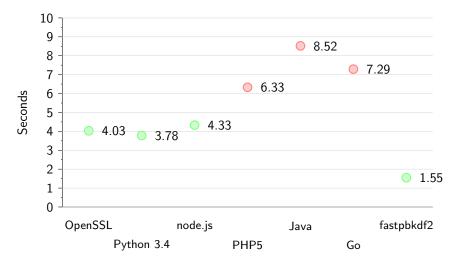


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- https://github.com/ctz/fastpbkdf2/

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- Most implementations waste time and power.
- If you use PBKDF2, you can probably drop in a faster implementation and either increase security margin, or improve time/power performance.

Thank you!

Questions?

Twitter: @jpixton
Mail: jbp@jbp.io

Web: https://jbp.io/

Slides: https://github.com/ctz/talks/

Code: https://github.com/ctz/fastpbkdf2/