

VLSI CAD: LOGIC TO LAYOUT: Programming Assignment 2: Serious BDDs

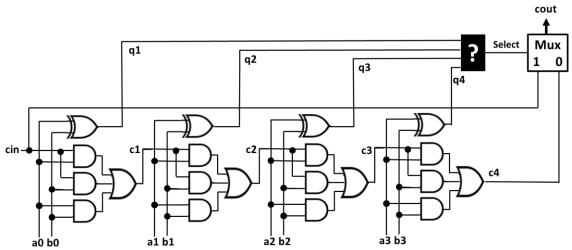
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You got a chance to try **kbdd** as part of Problem Set #2, where you ran a relatively small verification of two combinational logic networks. In this "programming" assignment, you get to use **kbdd** again, but now on some problems that too big to do by hand. You also get to think through a novel BDD application.

The assignment is in two parts, both focused on network repair applications, since these exercise a lot of the power of a good BDD package. You will write and exercise **kbdd** scripts to complete this programming assignment.

Part 1: Network Gate Repair

This part of the problem revisits the method we taught in lectures in Week2, and which we illustrated with a small example in the Tutorial for **kbdd**. Now, we want you to do this again – but on a network too complex to do any other way. Consider this new logic network:



We are showing just the carry chain (from carry-in "cin" to carry-out "cout") for a 4 bit adder, which adds a3,a2,a1,a0 to b3,b2,b1,b0. This is a more sophisticated architecture called a *carry-bypass* adder. The idea is to use internal information generated by each stage of the addition process to try to *predict* the output carry as

early as possible. In the best case, the predictor is correct and the MUX selects the input carry **cin** as the output carry (it is merely propagated). At worst, the multiplexor (**Mux**) has to wait for the "real" carry, **c4**, to ripple out to generate **cout**.

In this design, we believe the highlighted gate labeled "?" has been implemented incorrectly. Your job is *repair* this network and tell us the proper gate. The method from the lecture should work here – but this is a bigger network, you cannot just do this by hand.

Do this:

- Build a "correct" version of the circuit. This means you just need an ordinary
 4 bit adder with a carry-in and a carry-out from the high-order bit. You can
 do this however you like but do recall that **kbdd** has an adder primitive
 built in.
 - (**Hint**: it looks like this: **adder 4 cout_gold sum[3..0] a[3..0] b[3..0] cin**Note you still have to list the sum output bits even though you don't need to use them for this problem).
- Replace the "?" gate with a multiplexor, to emulate the gate you need to find.
 Note that you are working to repair a 4-input gate, with inputs q1,q2,q3,q4.
 So, you need a 16:1 mux, since any truth table for this gate is a function of 4 variables, so it has 2⁴ rows you need to solve for. You can write the equation for this in detail yourself, or you can recall that kbdd also has a MUX primitive built in.
 - (Hint: it looks like this: mux 4 Select q1 q2 q3 q4 d[15..0])
- Set up the BDD-based gate repair as we specified in the lecture: replace the gate with the mux; EXNOR the correct circuit with this incorrect circuit with the mux inserted; quantify away the right variables; satisfy this result; look *very carefully* at this result. Are all the variables still here? What value(s) if any satisfy this result?

Grading Details [50 points]:

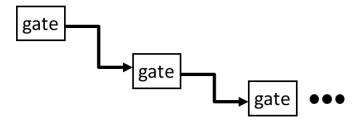
You can run **kbdd** however you want to solve this problem. We will create an "auxiliary quiz" (which looks just like a Problem Set) to let you answer questions about this result. You can submit as many times as you like – but for this one, you have to wait until the quiz is past the deadline to see the final result. (There's just not that many useful answers here...). Here is what we are going to ask:

- 1. **[20 pts]** *Is* this network repairable?
- 2. **[30 pts]** *How* is this network repairable? We will give you a list of possible repair options and you need to select the right one(s). The option "No repair possible" will be one of these options.

Part 2: Unknown Inversion Find-and-Repair

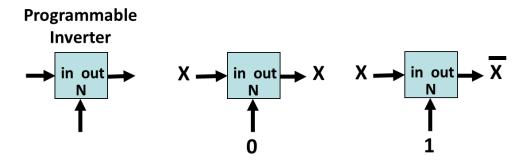
A common error in a large logic network is an incorrect inversion: on some internal wire, there is error that can be corrected by adding exactly one invertor to this wire in the network. But, we do *not know* where the error is. It turns out we can still use a BDD to solve this new, seemingly more difficult problem. We can find the wrong wire and then invert it to repair things.

It is easiest to see the idea – which you need to work out – on a small design. Suppose we have this small section of a larger logic network, and we want to ask the simpler question: which one of these two wires is incorrectly inverted?

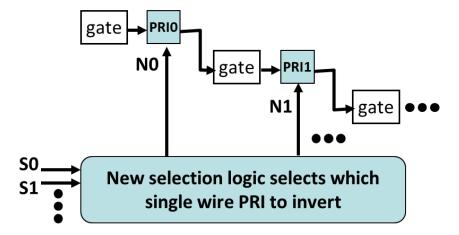


Then we modify the network as follows:

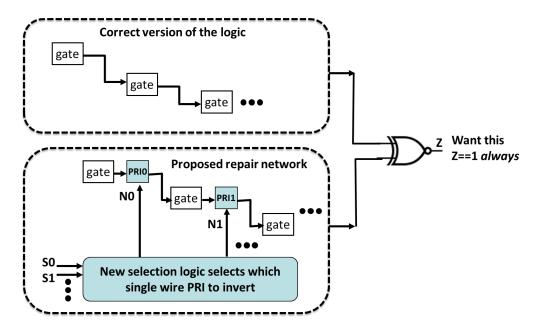
On each suspect wire, we insert a programmable inverter (PRI). A programmable inverter is a small piece of logic (2 inputs, 1 output) that has this function: if the control input N=0, then out=in; if the control input N=1, then out=in'. In other words, the N signal negates the input, when N=1.



• We then build another piece of new logic that *selects* one – and *only* one! – of the programmable inverters, and sets its control signal Ni = 1. All the other programmable inverters are set to Nj=0. This selection logic takes a new set of inputs the select which one of the PRI control inputs to set to 1. Suppose you had 16 potential wires to check for an inversion error. Then this selection logic has log₂(16) = 4 inputs, S3,S2,S1,S0, which we regard as a binary number, to select one PRI to enable. For example, if S3,S2,S1,S0=1001, then we will set N9=1, and set all other Nj=0, for j≠9. Let's call this version of the design, with the PRI's and the selection logic, the "proposed repair" network. This is shown below.

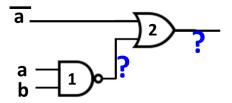


Just as with our previous network repair methods, we need to have available some correct version of the logic. We connect the correct logic output, and our "proposed repair" version of the network, to an EXNOR gate. We want to solve for values of the selection inputs Sn-1...S2S1S0 so that the output Z of the EXNOR is always 1. We use *quantification* again, and get rid of all inputs other than the selection inputs.

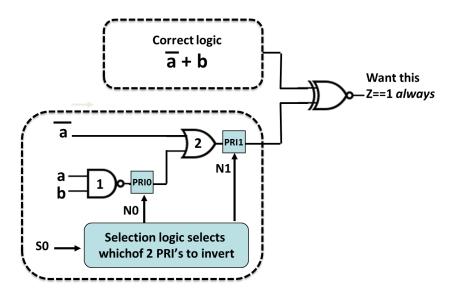


This is the general "recipe" for finding and correcting an inversion error on a wire. It is helpful to consider a very small, concrete example, to work through the details you need to determine to complete this problem. Here is a little example.

Suppose we have this small logic network. The wires with "?" labels are perhaps wrong. We want to determine which of these needs to have an inverter added.



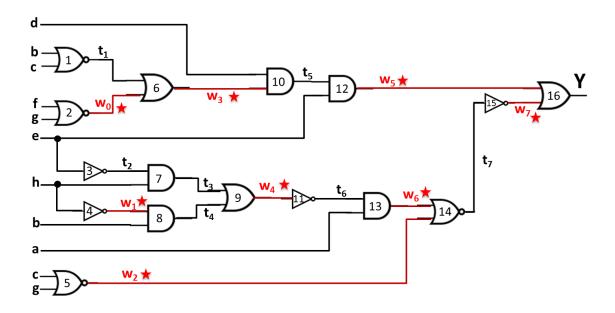
We perform the steps described above: we add a PRI to each suspect wire; we create selection logic to choose 1 of exactly 2 PRIs to invert (so, there is just one select input **SO**); we create a new network which is the EXNOR of our "proposed repair" network and a correct version of the logic (which in this case is easy to see); we quantify away the inputs. This construction looks like this:



Our advice to you is: Figure out exactly how to solve this little problem *first*. When you understand all the pieces, then you can use **kbdd** to execute this repair recipe on a bigger design. This is what you will do for credit for this assignment.

Do this:

• Here is a much bigger logic network to consider. We believe that one of these 8 lines highlighted (drawn in red with stars: w0, w1, w2, w3, w4, w5, w6, w7) in the network is incorrect, and that we can fix this by inverting one of these 8 wires. Use kbdd to execute this repair recipe on this logic network. You should be connecting a PRI to each of these wires, and you should connect the Ni selection logic output to the PRI you put on wire wi.



kbdd Script Submission Details

Pay close attention to these details here, since for this part, we will be grading your "live" kbdd script running out in the Coursera cloud.

- We will give you a *partial script* to start with. Do not change the commands in this script! This will define all the right input variables and the variable order. This will also define for you a correct version of the logic called **Y**.
- Use kbdd to describe the equation of one Programmable Invertor. The inputs of this PRI are pri_N (control) and pri_in (data input). Output of this PRI is called PRI. We want you to fill in the equation ("eval PRI something...") for one PRI.
- Use **kbdd** to describe the selection logic. The inputs to your selection logic are **S2,S1,S0** (3 inputs to select one of 8 outputs). The outputs of your selection logic are: **N7,N6,N5,N4,N3,N2,N1,N0**. You will write 8 lines of equations ("eval Ni something...") to define each of these **Ni**.
- Use **kbdd** to build a version of the Y function above called it **Y_repair** with the 8 PRIs inserted in the proper places.
- Use **kbdd** to build the **Z** function (we will name it capital "**Z**"!) as specified in this repair method. We will give a correct version of the function. This is just the EXNOR of the **Y** and **Y** repair logic, to make **Z**.
- Use kbdd to quantify away the "right stuff". Call this quantified function
 Z_quantify.
- Use kbdd to satisy Z_quantify, and use these results to tell us how to repair this network.

You will upload this script to the Coursera server, and we will append some additional **kbdd** commands to compare your answer to the right answer.

```
#HERE IS YOUR PARTIAL SCRIPT FOR PROGRAM 2 PART 2
# input variables - do NOT change this
boolean a b c d e f g h pri in pri N S2 S1 S0
# Here is the the correct logic function Y
eval Y a&c&!e&g&h + a&b&!h + d&e&!f&!g + !b&!c&d&e + a&!e&h + !c&!g
# YOU DO THIS: Define one programmable inverter block [8 points]
                (Signal input = pri in Output = PRI
                 Inversion control signal = pri N)
eval PRI you-fill-this-part-in
# YOU DO THIS: Define Selection Logic [8 points]
               (3 select inputs, 8 PRI control outputs Ni)
eval N0 you-fill-this-part-in
eval N1 you-fill-this-part-in
eval N2 you-fill-this-part-in
eval N3 you-fill-this-part-in
eval N4 you-fill-this-part-in
eval N5 you-fill-this-part-in
eval N6 you-fill-this-part-in
eval N7 you-fill-this-part-in
# YOU DO THIS: Build a correct implementation of the Y network
                with 8 programmable inverters (PRIs) embedded in it.
                Call it Y repair.
#Hint: Build this one one gate at a time from the diagram.
        16 gates \rightarrow 16 lines of Evals.
        Embed each PRI in equation for gate output it inverts.
eval t1 you-fill-this-part-in
eval w0 you-fill-this-part-in
eval t2 you-fill-this-part-in
eval w1 you-fill-this-part-in
eval w2 you-fill-this-part-in
eval w3 you-fill-this-part-in
eval t3 you-fill-this-part-in
eval t4 you-fill-this-part-in
eval w4 you-fill-this-part-in
eval t5 you-fill-this-part-in
eval t6 you-fill-this-part-in
eval w5 you-fill-this-part-in
eval w6 you-fill-this-part-in
eval t7 you-fill-this-part-in
eval w7 you-fill-this-part-in
eval Y repair you-fill-this-part-in
# Do EXNOR of the correct Y function and your Y_repair [16 points]
eval Z !(Y^Y_repair)
# YOU DO THIS: what is the right quantification to solve for repair?
quantify what-kind? Z quantify Z you-fill-this-part-in-what-variables?
# what values of Si's make this function == 1?
satisfy Z quantify
# You look at this result, and tell us how to repair network!
```

Grading Details [50 points]

- [6 points] Correct implementation of one Programmable Invertor PRI.
- **[8 points]** Correct implementation of the Selection Logic (3 select inputs, 8 PRI control outputs).
- **[16 points]** Correct implementation of the Z function.

We will also use the same auxiliary quiz to ask you a few questions about this exercise, since there are a few "So, what happened?" questions we want you to answer. You can submit as many times as you like; but as before, you won't be able to see the solution until after the deadline. (Again – we don't want people guessing the right answer(s) by just resubmitting lots of times. You will be asked to answer these questions in this quiz:

- 1. **[10 points]** What sort of quantification do you need to perform to be able to solve for the selection logic inputs, to repair this network?
- 2. **[10 points]** Which of the 8 highlighted wires has the error?