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ORIGINAL ARTICLE

Fast map matching, an algorithm integrating hidden Markov model with precomputation

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Wide deployment of Global Positioning System (GPS) sensors has generated a large amount of data with numerous applications in transportation research. Due to the observation error, a map matching process is commonly performed to infer a path on a road network from a noisy GPS trajectory. The increasing data volume calls for the design of efficient and scalable map matching algorithms. This article presents Fast Map Matching (FMM), an algorithm integrating hidden Markov model with precomputation, and provides an open source implementation. An upper bounded origin-destination table is precomputed to store all pairs of shortest paths within a certain length in the road network. As a benefit, repeated routing queries known as the bottleneck of map matching are replaced with hash table search. Additionally, several degenerate cases and a problem of reverse movement are identified and addressed in FMM. Experiments on a large collection of real-world taxi trip trajectories demonstrate that FMM has achieved a considerable single-processor map matching speed of 25,000 to 45,000 points/second varying with the output mode. Investigation on the running time of different steps in FMM reveals that after precomputation is employed, the new bottleneck is located in candidate search and more specifically, the projection of a GPS point to the polyline of a road edge. Reverse movement in the result is also effectively reduced by applying a penalty.

Keywords: Map matching; precomputation; performance improvement;

1. Introduction

Benefiting from the rapid development of wireless communication and positioning technologies, Global Positioning System (GPS) sensors have been widely deployed on vehicles,

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smart phones and bicycles to collect movement information. Compared with traditional stationary sensors used in transportation research such as loop detector mounted at fixed locations in a road network to monitor velocity and traffic volume, GPS sensor is recognized as a promising data collection approach which is cost effective with a broad spatial coverage (Li et al. 2014). It typically reports ID, latitude, longitude of the tracked object and time-stamp of record while some advanced sensors also report velocity, heading and acceleration (White et al. 2000). Due to the uncertainties caused by inevitable measurement error and low sampling rate (Li et al. 2013), continuous movement on a road network is observed as a sequence of periodically reported GPS observations with an offset from the true locations. In order to infer the path traversed by the object, a map matching (MM) process is frequently performed, which is an important preprocessing step in many GPS data relevant studies such as route navigation (Yuan et al. 2010a), travel time estimation (Rahmani et al. 2015), traffic modelling (Castro et al. 2012) and activity recognition (Liao et al. 2007).

In the literature, many algorithms have been proposed to solve the MM problem. In Quddus et al. (2007), early MM algorithms are classified into four categories including geometric, topological, probabilistic and other advanced. Most of them are sensitive to GPS error, sampling rate and initial map matching results (Newson and Krumm 2009, Zeng et al. 2015). Since Hidden Markov Model (HMM) was first employed to solve MM problem in Newson and Krumm (2009) and Lou et al. (2009), it has been widely adopted in later studies because of the elegant and extensible integration of GPS error, geometry, topology and other factors in the path inference. Along that direction, most of the efforts are devoted to improving the accuracy of MM by introducing new information such as speed limit (Yuan et al. 2010b), turning angle (Li et al. 2013) and curvedness (Zeng et al. 2015) or designing more robust and realistic objective functions for path inference (Yuan et al. 2010b, Wei et al. 2012, Chen et al. 2014). However, performance improvement in MM is not fully exploited in those studies (Marchal et al. 2005, Huang et al. 2013).

Considering the increasing size of GPS data, it is necessary to develop MM algorithms capable of handling a large amount of data in a short time. Concentrated primarily on performance improvement, this article proposes Fast Map Matching, an algorithm integrating HMM with precomputation. The algorithm contains two stages where in the first precomputing stage, an upper bounded origin-destination table is created from the road network to store information about all pairs of shortest paths whose lengths are under a certain threshold. In the second stage, MM is performed where computationally expensive routing queries are replaced with hash table search. Contributions of this article are highlighted below:

- (1) An efficient and robust MM algorithm is developed with open source implementation provided. Several degenerate cases in MM are discovered and settled in this article. A problem of reverse movement is identified in previous algorithms and addressed by applying a penalty.
- (2) Various aspects of the algorithm are evaluated with a large GPS trajectory dataset. The results demonstrate that FMM has achieved a considerable single processor MM speed of 25,000 to 45,000 points/second varying with the output mode. Investigation on the running time of the steps in FMM reveals that after precomputation is employed, the bottleneck has shifted from previously known repeated routing queries to candidate search and more specifically, the projection of a GPS point to the polyline of a road edge. Reverse movement in the result is effectively reduced by applying a penalty.

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The remainder of this article is organized as follows. Section 2 provides a systematic literature review and Section 3 gives the preliminaries. The algorithm is presented in Section 4. In Section 5, a case study on a real-world GPS dataset is reported. Finally, conclusions are drawn and future work is planned in Section 6.

2. Related work

In the literature, several approaches have been proposed to improve the performance of MM, which can be classified into four categories: spatial indexing, trajectory simplification, parallel computing and advanced routing algorithms.

Spatial indexing technologies such as R-tree (Guttman 1984) and Quad-tree (Finkel and Bentley 1974) have been widely employed in MM algorithms to accelerate the search of neighboring edges around GPS point (Marchal *et al.* 2005, Li *et al.* 2011, Wei *et al.* 2012, Chen *et al.* 2014). However, the contribution of spatial indexing is limited to candidate search and it is commonly used in collaboration with other methods.

Trajectory simplification approaches improve the performance by reducing the number of points to be matched, which are effective especially for dense and duplicated observations. In Li et al. (2014), three simplification algorithms incremental, slicing and global window are proposed by assigning weights to GPS points based on the geometric information of the trajectory and filtering those with small weights. In the authors' recent work (Li et al. 2015), an oriented bounding rectangle (OBR) algorithm is proposed to cluster points in a trajectory based on moving direction, which is also capable of handling outliers. However, these algorithms are restricted to dense GPS data.

Parallel computing is also a promising technology for high performance MM because not only matching individual trajectory but also searching candidate edges for each GPS point within a trajectory can be parallelized. With the rapid development of distributed and parallel computing technologies, considerable improvement has been reported in previous studies. In Li et al. (2011), an online map matching framework is designed and tested on a 16 nodes cluster with an overall performance of around 20,000 points/second. Similarly, in Huang et al. (2013), the highest speed is reported as 120,000 points/second on a 20 nodes cluster. However, the potential improvement of single processor's performance is not fully exploited in those studies.

Compared with above three categories, advanced routing algorithms attract more attention because the bottleneck of HMM based map matching algorithm has been widely recognized as repeated routing queries (Lou et al. 2009, Wei et al. 2012, Rahmani and Koutsopoulos 2013, Zhe and Zhang 2015). Apart from classical Dijkstra algorithm (Dijkstra 1959), various advanced routing algorithms have been proposed for accelerating shortest path queries such as A* (Hart et al. 1968) and ALT (Goldberg and Harrelson 2005). However, their contribution to MM is limited because they primarily focus on the query of a large graph where origin and destination are distant while in MM context, the distance between consecutive GPS observations is likely to be small. In Rahmani and Koutsopoulos (2013), traversing the whole network graph is avoided by constructing a local search tree according to the distance estimated from the time interval between GPS observations. A more significant improvement is achieved in Chen et al. (2014) where the number of repeated queries is reduced by adding dummy nodes and links connecting GPS point with neighboring edges in the network graph. Consequently, multiple sources to multiple targets routing queries are converted to a single query passing a sequence of dummy nodes. However, it frequently updates the network graph for each of reverse movement are identified and addressed.

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trajectory, which degrades the performance. Another approach to address the problem is to precompute some routing results. In Zhe and Zhang (2015), an upper bounded origin and destination table is created from the road network and queried to obtain the shortest path distance between candidates. FMM developed in this article improves the performance based on the same principle but differs from their work in several aspects. Firstly, the bottleneck of repeated routing queries is fully addressed with a much higher performance achieved. Secondly, various aspects of integrating precomputation into MM are reported including sensitivities to configurations, running time constitution and han-

dling of long distance routing queries. Thirdly, several degenerate cases and a problem

3. Preliminaries

A road network is represented as a directed graph denoted by G = (V, E) where V is the set of nodes and E is the set of edges. Each node in V is stored as a point representing intersections and dead ends of road segments. Each edge $e \in E$ represents a directed road segment with ID of eid starting from a source node with ID of s to a target node with ID of s. The geometry of s is a polyline denoted by s with a length of s. Therefore, edge s is stored as a tuple denoted by

$$e = (eid, s, t, geom, L) \tag{1}$$

Movement on e is constrained to the direction from node s to t. For brevity, edge e is also written as (s,t) in subsequent content.

Based on the format of GPS data collected in this article, a GPS observation p records the latitude lat and longitude long of a tracked object at a specific time-stamp ts, denoted as a tuple p = (lat, long, ts), which is also referred as a GPS point. A GPS trajectory tr is a sequence of temporally ordered GPS points denoted by $tr = \langle p_1, p_2, ..., p_N \rangle$, which is stored as a polyline. For simple explanation, the tracked object is assumed to be a vehicle in later content.

4. Fast Map Matching algorithm

Similar with most previous work, FMM takes a GPS trajectory set TR and a road network G as input. For each trajectory, it exports a path stored as a sequence of edges traversed by the vehicle together with its geometry. Figure 1 displays the whole process of FMM, which consists of two stages precomputing and map matching.

4.1. Precomputing stage

In the precomputing stage, all pairs of shortest paths (SP) in G whose lengths are under a threshold Δ are calculated and stored in an Upper Bounded Origin Destination Table (UBODT) in a compressive manner. Each row in UBODT corresponds to the SP from an origin node n_o to a destination node n_d and is denoted by

$$R(n_o, n_d) = (n_o, n_d, next_n, next_e, prev_n, dist)$$
 (2)

UBODT

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Map matching stage Precomputing stage Input Trajectory Candidate GPS candidate search trajectory Intermediate results Optimal path Path Road geometry Process Geometry Optimal UBODT construction

Figure 1. Process of fast map matching algorithm

Complete path

construction

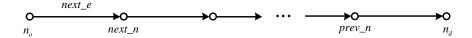


Figure 2. Information stored in a row of UBODT for the shortest path from origin node n_o to destination node n_d .

where $next_n$ and $next_e$ represent the next node and next edge visited after n_o , respectively. The previous node visited before n_d is stored in $prev_n$ and dist is the SP distance. Figure 2 gives an illustration for these information stored in UBODT.

UBODT is constructed by iterating through every node s in G and calling a classical single-source Dijkstra algorithm starting from s with upper bound of Δ , as shown in Algorithm 1. In each iteration, a shortest path tree is generated, from which the fields in $R(n_0, n_d)$ are derived, as indicated by line 4-10 in Algorithm 1.

After construction, UBODT is stored as a hash-table with a composite key of (n_0, n_d) , which is implemented as a linear chaining structure (Cormen et al. 2001) configured by two parameters: the number of buckets H, which is commonly selected as a prime value, and a multiplier M to compute a unique key as $n_o \times M + n_d$, which can be selected as the number of nodes in G. Given a row $R(n_o, n_d)$, it is inserted into the bucket with index h of

$$h = (n_o \times M + n_d) \bmod H \tag{3}$$

Output

Complete

path

where $0 \le h \le H$. The performance of query in UBODT is closely related with a load factor defined as lf = |UBODT|/H, which indicates the average number of elements stored in a bucket of the hash table.

From UBODT, SP information can be queried efficiently. The SP distance from node n_o to n_d , denoted by $l^N(n_o, n_d)$, is retrieved directly as

$$l^{N}(n_o, n_d) = R(n_o, n_d).dist$$
(4)

Based on the column $next_n$ stored in UBODT, the edges in the SP from n_o to n_d ,

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Algorithm 1: UBODT construction algorithm

Input:

```
G = (V, E): graph of a road network RN
      \Delta: Upper bound of distance for all pairs of shortest paths
      UBODT: a table with columns of (n_o, n_d, next\_n, next\_e, prev\_n, dist)
 1 for s in G.V do
       /* A shortest path tree is returned as a set of nodes visited
       within \Delta (NodesVisited), corresponding predecessors (Pred) and
       distances (Dist)
      NodesVisited, Pred, Dist = Single\_Source\_UpperBounded\_Dijkstra(s, \Delta)
 \mathbf{2}
       /* Iterating shortest path tree to get next_n and next_e
      for u in NodesVisited do
3
          prev_n = Pred[u]
 4
          /* Find the next node v visited from s to u
                                                                                    */
\mathbf{5}
          while Pred[v] \neq s do
 6
            v = Pred[v]
 7
          end
8
         next\_n = v
9
10
          next_e = G[s, u]
          write(s, u, next_n, next_e, prev_n, Dist[u]) // Write output
11
12
      end
13 end
14 return
```

denoted by $Path(n_o, n_d)$, can be efficiently constructed as

$$Path(n_o, n_d) = \langle R(n_o, n_d).next_e, R(R(n_o, n_d).next_n, n_d).next_e, \cdots \rangle$$
 (5)

which recursively queries the next edge visited from n_o to n_d until the destination is reached.

Although it is enough to construct the path from $next_n$, $prev_n$ is also stored in UBODT and it is primarily used for correction of reverse movement explained later in Section 4.3. In case that the node pair (n_o, n_d) is not found in UBODT, implying that $l^N(n_o, n_d) > \Delta$, a conventional Dijkstra algorithm could be invoked, which is described in details in Section 4.2.4.

4.2. Map matching stage

In the map matching stage, HMM is integrated with precomputation to infer the path traversed by the vehicle considering both GPS error and topology constraint. The stage is divided into 4 steps: candidate search (CS), optimal path inference (OPI), complete path construction (CPC) and geometry construction (GC) as illustrated in Figure 1.

4.2.1. Candidate search (CS)

This step searches for candidate edges for each point in a trajectory. An example of candidate edge is displayed in Figure 3. When e is selected as a candidate edge of GPS

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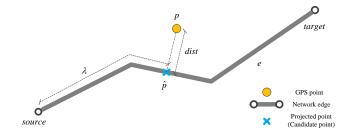


Figure 3. Example of a candidate selected for a GPS point.

point p, the location of the vehicle is estimated as the projected point of p on e.geom, denoted by \hat{p} . The point \hat{p} is also called a *candidate point* of p. A candidate C is stored as a tuple

$$C = (\hat{p}, e, dist, \lambda) \tag{6}$$

where dist is the Euclidean distance from p to \hat{p} and λ is the offset distance along e.geom from e.s to \hat{p} with $0 \le \lambda \le e.L$. The projection of a point on a polyline is solved with the linear referencing algorithm (Rahmani and Koutsopoulos 2013) by iterating through each segment in the polyline and returning the one with minimum distance.

Given a GPS point p, the set of candidates is constructed as the k-Nearest Neighbors (KNN) of road edges around p within a search radius of r, denoted by

$$CS(p) = KNN(p)_{k,r} \tag{7}$$

In this article, R-tree (Guttman 1984) is employed to accelerate candidate search. Although KNN search using R-tree has been studied in Roussopoulos et al. (1995), it is not used in FMM because of the additional constraint imposed by r. In practice, it is likely that a small r will be specified and the intersection query will return very few edges, from which KNN can be retrieved efficiently. In FMM, KNN query on R-tree is divided into the following three steps:

- (1) R-tree intersection: Create a square with center of p and side length of 2r and perform an intersection query on R-tree to export all edges whose bounding box is intersected with the square.
- (2) Candidate construction: For each edge e obtained in previous step, project p to \hat{p} on e.geom. If $dist(p, \hat{p}) \leq r$, create a candidate for e.
- (3) KNN sort: Sort all the candidates found in previous step according to $dist(p, \hat{p})$ and return the k smallest ones.

Based on the above definition, given a trajectory $tr = \langle p_1, p_2, \cdots, p_N \rangle$, a trajectory candidate set (TRCS) is constructed as

$$TRCS(tr) = \langle CS(p_1), CS(p_2), ..., CS(p_N) \rangle$$
(8)

In some areas with a low density of road network, e.g. suburb, there may be less than kedges around p_n within r. Therefore, TRCS(tr) is stored as a variable-length two dimensional array of candidates. In TRCS(tr), each candidate is indexed by C_n^i representing the i-th candidate matched to p_n where $1 \leq i \leq k$ and $1 \leq n \leq N$. For brevity, i is ignored sometimes thus C_n represents an arbitrary candidate matched to p_n in tr.

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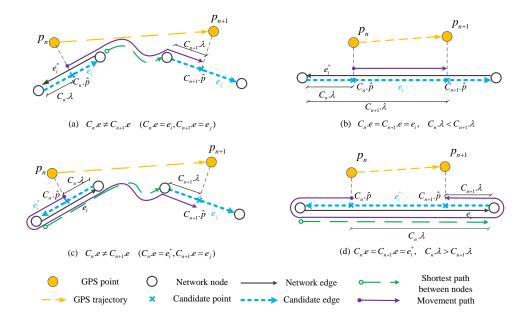


Figure 4. Illustration of querying SP distance from candidate C_n to C_{n+1} using UBODT. Edge e_i and e_i^* are two edges with reverse direction representing a bi-directional road segment.

4.2.2. Optimal path inference (OPI) integrated with UBODT

In this step, a transition graph is firstly built from the trajectory candidates based on HMM model, where the SP distances between candidates are queried. After that, an optimal path is inferred for the trajectory. In this section, acceleration of SP distance query utilizing UBODT is introduced first. After that, the definition of HMM and details of OPI are presented.

It has been demonstrated in Section 4.1 that SP distance between nodes of a graph can be retrieved directly from UBODT. However, additional processing is required for computing the SP distance from C_n to C_{n+1} , which is actually the distance between points on edges rather than nodes of a graph. Assume that a vehicle will always move along the direction of an edge, all the possible movements from p_n and p_{n+1} are illustrated in Figure 4 and listed below:

- (1) p_n and p_{n+1} are matched to different edges, namely $C_n.e \neq C_{n+1}.e$. It implies that the vehicle first leaves the edge $C_n.e$ following the path $C_n.\hat{p} \to C_n.e.t$. After that, it enters the edge $C_{n+1}.e$ along the SP from $C_n.e.t$ to $C_{n+1}.e.s$. Finally, on edge $C_{n+1}.e$, it moves to position $C_{n+1}.\hat{p}$. Therefore, the complete path traversed is $C_n.\hat{p} \to C_n.e.t \to C_{n+1}.e.s \to C_{n+1}.\hat{p}$. Two examples are illustrated in Figure 4 (a) and (c).
- (2) p_n and p_{n+1} are matched to the same edge namely $C_n.e = C_{n+1}.e = e$. It can be further divided into two conditions below:
 - a) $C_n.\lambda \leq C_{n+1}.\lambda$. It represents that the vehicle stays on edge e when moving from p_n to p_{n+1} . The path is $C_n.\hat{p} \to C_{n+1}.\hat{p}$ with length of $C_{n+1}.\lambda C_n.\lambda$. An example is shown in Figure 4 (b).
 - b) $C_n.\lambda > C_{n+1}.\lambda$. It indicates that the vehicle leaves edge e then re-enters e following the path $C_n.\hat{p} \to e.t \to e.s \to C_{n+1}.\hat{p}$. An example is demonstrated in Figure 4 (d).

Based on the above observations, the SP distance from C_n to C_{n+1} is calculated as

$$l_{n,n+1}^{C} = \begin{cases} C_{n+1}.\lambda - C_{n}.\lambda, & \text{if } C_{n}.e = C_{n+1}.e, C_{n}.\lambda \le C_{n+1}.\lambda \\ C_{n}.e.L - C_{n}.\lambda + l_{n,n+1}^{N} + C_{n+1}.\lambda, & else \end{cases}$$
(9)

where $l_{n,n+1}^N = l^N(C_n.e.t, C_{n+1}.e.s)$ is the SP distance from the node $C_n.e.t$ to $C_{n+1}.e.s$. In the literature, the definition of HMM for map matching differs primarily in three parts: transition probability, emission probability and the objective function to be maximized or minimized. A commonly used definition for transition probability is the Euclidean distance divided by SP distance (Lou et al. 2009, Yuan et al. 2010b), which can be problematic in cases of dense GPS data and large search radius. Figure 5 provides 3 examples where the Euclidean distance between p_n and p_{n+1} , denoted by $d_{n,n+1}$, is greater than $l_{n,n+1}^C$. In Figure 5 (a), after projection, the candidate points get closer than the GPS observations, resulting in a transition probability larger than 1. A more serious problem occurs in Figure 5 (b) where a large search radius is set and the two points are matched to the same place of an edge with $l_{n,n+1}^C = 0$, which would cause a division by 0 error. The same problem exists in Figure 5 (c) where they are matched to the same edge with a reverse direction. Since it is always preferred over transitions with an SP whose length is closer to the Euclidean distance, in FMM the transition probability is defined as

$$tp(C_n, C_{n+1}) = \frac{\min(d_{n,n+1}, l_{n,n+1}^C)}{\max(d_{n,n+1}, l_{n,n+1}^C)}$$
(10)

Therefore, in Figure 5 (a) tp < 1 whereas in (b) and (c) tp = 0. These paths are likely to be eliminated in later OPI.

Regarding the emission probability, the same definition used by Lou *et al.* (2009) is adopted with the assumption that the GPS point follows a zero mean gaussian distribution around the vehicle's true location. Formally, the emission probability of candidate C_n is defined as

$$C_n.ep = \frac{1}{\sqrt{2\pi}\sigma} e^{-(C_n.dist)^2/2\sigma^2}$$
(11)

where σ is the standard deviation indicating GPS error.

Based on the above definitions of transition and emission probability, TRCS(tr) can be treated as a transition graph where a node represents a candidate C_n and an edge represents the SP from C_n to C_{n+1} . A candidate path in TRCS(tr) is defined as a sequence of candidates matched for each point in tr denoted by $\langle C_1, C_2, \ldots, C_N \rangle$. Similar with Lou et al. (2009), each candidate path is assigned with a score defined as

$$score = \sum_{n=1}^{N-1} tp(C_n, C_{n+1}) \times C_{n+1}.ep$$
 (12)

By employing Viterbi algorithm (Forney 1973), an optimal path O-path can be inferred efficiently as the path with the maximum score, which is stored as a sequence of N

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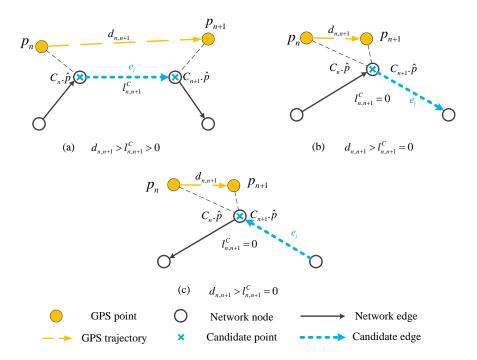


Figure 5. Degenerate cases in transition probability calculation where the shortest path distance $(l_{n,n+1}^C)$ is smaller than the Euclidean distance $(d_{n,n+1})$.

candidates matched for each point in tr, denoted by

$$O_{path} = \langle \hat{C}_1, \hat{C}_2, \cdots, \hat{C}_N \rangle \tag{13}$$

4.2.3. Complete path construction (CPC) and geometry construction (GC)

Once O-path is obtained, the last two steps are complete path construction (CPC) and geometry construction (GC). In the CPC step, a complete path C-path, which is a sequence of edges traversed by tr, is constructed by concatenating the SPs connecting consecutive candidates in O-path, denoted by

$$C_{-path} = \langle \hat{C}_{1}.e, \cdots, \hat{C}_{n}.e, Path(\hat{C}_{n}.e.t, \hat{C}_{n+1}.e.s), \hat{C}_{n+1}.e, \cdots, \hat{C}_{N}.e \rangle$$

$$(14)$$

The query of $Path(\hat{C}_{n}.e.t, \hat{C}_{n+1}.e.s)$ is also performed in UBODT as illustrated in Section 4.1. In some previous work (Chen et al. 2014, Zhe and Zhang 2015), both the SP distance and path are queried and stored for each transition of candidates, which wastes computational resources because only one of them is finally exported. FMM addresses that issue by only querying the SP path after O_{-path} is obtained. Finally, the corresponding geometry is constructed by concatenating the polyline for each edge in C_{-path} .

4.2.4. Handling of long distance routing queries

In FMM, UBODT is queried in the OPI step for SP distance and CPC step for the detailed path. In practice, it could happen that the SP distance between consecutive candidates is longer than Δ . Consequently, no SP information is returned from UBODT. To address that issue and evaluate the improvement gained by precomputation, fours modes are of FMM are designed as follows.

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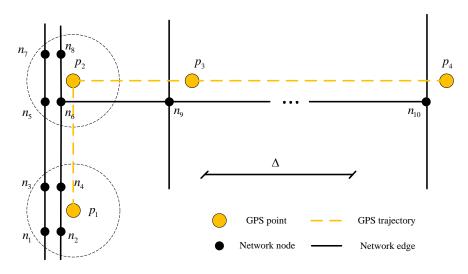


Figure 6. Illustration of unnecessary long distance routing queries. When processing candidates of p_1 and p_2 in the optimal path inference step, $l_{\{1,3\},\{6,8\}}^N$ and $l_{\{2,4\},\{5,7\}}^N$ are much larger than Δ , which needs to call Dijkstra routing queries. However, these queries are unnecessary because finally $n_4 \to n_6$ is likely to be inferred as the optimal path.

(M1) UBODT+Dijkstra (brute force): The first mode directly calls a Dijkstra algorithm whenever the SP distance is not found in UBODT in the OPI step or the SP path is not found in CPC step.

In M1 there exists a problem of false distant candidates where consecutive GPS observations p_n and p_{n+1} are close but some of their candidates are distant. As illustrated in Figure 6, p_1 and p_2 are close but the SP distances from n_1, n_3 to n_6, n_8 , namely $l_{\{1,3\},\{6,8\}}^N$ are longer than Δ . The corresponding SP queries are unnecessary because $l_{4,6}^N$ is much smaller so that the paths from $\{n_1, n_3\} \rightarrow \{n_6, n_8\}$ are likely to be pruned. These unnecessary queries can degrade the performance of OPI significantly.

(M2) UBODT+Dijkstra (optimized): To avoid the aforementioned unnecessary queries, the second mode firstly returns Δ as an estimation of the SP distance if it is not found in UBODT. When p_n and p_{n+1} are close, the correct candidates should still have a much shorter SP distance and will still be inferred as part of the optimal path. If the O-path returned in OPI still contains the distant candidates, which implies that p_n and p_{n+1} are really distant, it switches to M1 to reprocess the trajectory candidates.

Taking the same case in Figure 6 as an example, when the SP distances $l_{(1,3),(6,8)}^N$ are estimated as Δ , they are still longer than $l_{4,6}^N$ and likely to be pruned in the OPI. When p_n and p_{n+1} are really distant as shown by p_3 and p_4 in Figure 6, the candidates with estimated distance of Δ can be inferred as the optimal path, which is $n_9 \to n_{10}$. Consequently, no C-path is found in UBODT in the CPC step. According to the definition of M2, it will switch to M1 mode, where the correct distance and path can be returned.

- (M3) UBODT: The third mode also returns Δ as the distance if it is not found in UBODT in the OPI step. When a large gap still exists in O-path, the trajectory is exported as unmatched. Without invoking Dijkstra algorithm, M3 has a higher performance than M1 and M2. In practice, a trajectory containing a large gap provides less reliable information about the movement and might be useless. The large gap is likely to be generated from sparse GPS data, which would be less common in the future.
- (M4) Dijkstra: Without querying UBODT, the last mode invokes Dijkstra algorithm all the time. The performance gained by precomputation can be evaluated by comparing

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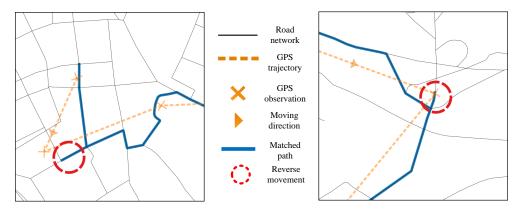


Figure 7. Two examples of reverse movement observed in matching real-world GPS data without applying penalty.

with M3.

4.3. Penalty for reverse movement in MM

When matching real-world GPS data using the HMM model defined by Equations 10 to 12, it is frequently observed in the result that the vehicle moves back and forth on the two directed edges corresponding to a single bidirectional road segment, which is called *reverse movement*. Two such examples are displayed in Figure 7. Although it could happen that the vehicle is actually moving back and forth on a road segment, a more common case is that there exists a bidirectional road segment and the error in GPS observation is large. As a consequence, the path containing reverse movement can be returned in the OPI step because it has a higher score than the correct path, as demonstrated in Figure 7.

Detailed analysis shows that reverse movement occurs between an SP and a candidate edge rather than inside an SP. When there are two reverse edges within the search region, p_n may be matched to either of them and reverse movement occurs in both cases. An example is illustrated in Figure 8 with three consecutive observations p_{n-1}, p_n and p_{n+1} . The two cases shown in Figure 8 (a) and (b) actually represent the same movement with the nodes visited in the order of $\langle 1, 2, 3, 4, 3, 5, 6 \rangle$. According to Equation 9, the row in UBODT queried by $l_{n-1,n}^C$ is $R(C_{n-1}.e.t, C_n.e.s)$ and similarly $R(C_n.e.t, C_{n+1}.e.s)$ is queried for $l_{n,n+1}^C$. In Figure 8(a), p_n is matched to the edge (3,4), i.e., $C_n.e = (3,4)$. Reverse movement occurs between $C_n.e$ and the SP from C_n to C_{n+1} , which can detected by $C_n.e.s = R(4,6).next_n = 3$. In Figure 8(b), p_n is matched to the reverse edge $C_n.e = (4,3)$. Reverse movement occurs between $C_n.e$ and the SP from C_{n-1} to C_n , which is detected by $C_n.t = R(1,4).prev_n = 3$.

Based on the two observations, reverse movements can be detected efficiently by comparing candidate edge with the SP queried from UBODT. Once reverse movement is detected from C_n to C_{n+1} , a penalized SP distance $\tilde{l}_{n,n+1}^C$ is calculated by increasing the actual SP distance controlled by a penalty factor pf, as shown below:

$$\tilde{l}_{n,n+1}^{C} = \begin{cases}
l_{n,n+1}^{C} + pf * C_{n}.L & \text{if } record.next_n = C_{n}.e.s; \\
l_{n,n+1}^{C} + pf * C_{n+1}.L & \text{else if } record.prev_n = C_{n+1}.e.t; \\
l_{n,n+1}^{C} & \text{else.}
\end{cases}$$
(15)

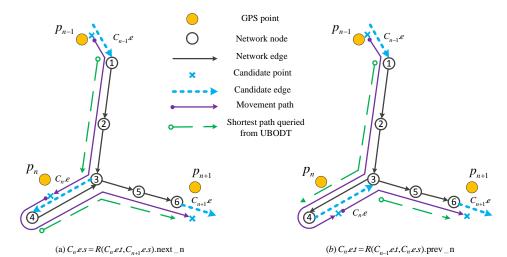


Figure 8. Detection of reverse movement by comparing the candidate edge with the SP queried from UBODT, namely checking $C_n.e.s = R(C_n.e.t, C_{n+1}.e.s).next_n$ in (a) and $C_n.e.t =$ $R(C_{n-1}.e.t, C_n.e.s).prev_n$ in (b).

where $record = R(C_n.e.t, C_{n+1}.e.s)$. The first and second condition correspond to Figure 8 (a) and (b), respectively. The penalized SP distance $\tilde{l}_{n,n+1}^C$ is used in replace of $l_{n,n+1}^C$ in Equation 10. After applying penalty, the path containing reverse movement is likely to be assigned with a lower transition probability and gets eliminated in the OPI step.

4.4. Implementation details

An open source implementation of the algorithm in C++ is provided at https://github.com/cyang-kth/fmm. Depending on the unit of processing, the algorithm can be performed in either stream mode or batch mode. The former is selected by default where a single trajectory is matched and followed by the next. In the latter, a batch of trajectories are matched step by step with intermediate results stored. The batch mode consumes more memory and is primarily designed for measuring the running time of different steps in FMM.

Case study

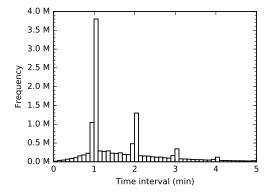
In this section, a case study is performed to evaluate FMM using a real-world GPS dataset. The input data and experiment setup are firstly introduced, followed with performance and accuracy assessment. After that, the penalty for reverse movement is evaluated.

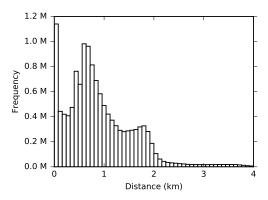
5.1. Data description and experiment setup

The taxi GPS data used in this case study was originally collected in the Mobile Millennium Project (Allström et al. 2011). The dataset covers 1 month period from 2013-03-01 to 2013-03-31 and contains about 13 million GPS observations reported by around 1,500 vehicles in Stockholm, Sweden. Each record is stored in the format of (record ID, vehicle ID, time-stamp, latitude, longitude, hired). The last attribute hired is a boolean value

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Figure 9. Histogram of time interval (left) and distance (right) between consecutive GPS observations

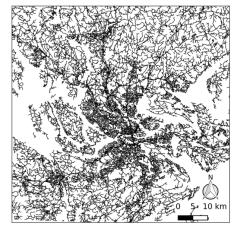


Figure 10. Study area $(6,675 \ km^2)$ of Stockholm and road network with 23,921 nodes and 57,928 directed edges

indicating whether the taxi is hired by consumers. Statistics of time interval and distance between consecutive GPS records are demonstrated in Figure 9. The GPS data is sparse with most time intervals between 1 minute to 4 minutes and a majority of distances under 2 km. From the raw GPS data, a taxi trip is extracted as a consecutive sequence of records with true hired states and stored as a polyline. Totally 673,849 trip trajectories are extracted and they are preprocessed to remove outliers according to the following criteria: (1) the trajectory contains only one point;(2) its average speed is above 150 km/h; (3) its geometry exceeds the boundary of the road network. Finally 644,695 trips (95.7%) containing 6,812,720 points are kept. The GPS error used for map matching is empirically set as 100m.

The road network used in this study is provided by Swedish National Road Database, which is displayed in Figure 10. It covers a region of 75 $km \times 89$ km with an area of 6,675 km^2 and consists of 23,921 nodes and 57,928 directed edges where each bidirectional road segment is stored as two opposite directed edges.

All the experiments in this case study are conducted on a desktop computer running Ubuntu operating system with Intel Quad Core CPU 3.00 GHz and 4GB RAM where only a single processor is used.

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Table 1. Statistics of precomputing UBODT from a road network with 23,921 nodes and 57,928 directed edges

$\Delta(km)$	Number of rows	Neighbors per node	Average Running time(second)
2	811,014	33	4.265
3	1,689,430	70	5.678
4	2,861,572	119	7.471
5	4,305,012	179	9.656

5.2. Performance assessment

5.2.1. Precomputing stage

Statistics of precomputing UBODT are presented in Table 1. As the SP distance threshold Δ increases, a larger UBODT is generated in a longer but acceptable time. When $\Delta = 5km$, it takes less than 10 seconds to generate a UBODT with about 4.3 million rows. In previous similar work (Zhe and Zhang 2015), it took 500 - 600 seconds to generate the same kind of table on a smaller road network with $\Delta = 4km$. The corresponding running time of UBODT precomputation here is 7.471 seconds, about 70-80 times faster than their work. The reason for this considerable improvement is that their algorithm creates a minimum priority queue to store all pairs of origin and destination (OD) in G then iteratively pulls the OD pair with minimum distance from the queue until all SPs shorter than Δ have been retrieved. The maintenance of the priority queue adopts a strategy similar with Floyd Warshall algorithm (Floyd 1962), which is applicable for dense graph whereas a road network graph is generally sparse. In the meanwhile, it consumes more memory to store all pairs of nodes, which is less efficient than iterating through all nodes with a single source Dijkstra algorithm adopted in FMM.

5.2.2. Map matching stage

This section evaluates various aspects of MM performance including sensitivities to configurations, different modes of routing integration and running time of all steps in FMM. No penalty for reverse movement is applied in these experiments. The performance is measured by MM speed defined as the number of GPS points matched per second.

The first experiment explores the impact of the upper bound of UBODT and routing integration on the performance of MM. Three UBODTs are generated with Δ of 3km, 4km and 5km and the four integration modes described in Section 4.2.4 are tested. In the experiment, a 1-day dataset containing 27,343 trajectories and 310,137 points is map matched with configurations of k = 8, r = 300m, H = 5,178,049, M = 30,000 and no geometry output. The results are reported in Table 2. As can be observed, M3 obtains the highest speed around 30,000 points/second among the four modes, which is 167 times of the slowest mode M4 with a speed of 179 points/second. The matched percentage of M3 is slightly lower than the rest three modes. The reason is that no Dijkstra routing is invoked so that a high performance is achieved and trajectories containing a large gap are exported as unmatched. Compared with the brute force integration of Dijkstra in M1, the optimization in M2 is effective with the number of routing queries reduced substantially. When $\Delta = 5km$, M1 calls Dijkstra queries 319,945 times while M2 calls only 13,457 times. In both M1 and M2, the MM speed increases with Δ , which is resulted from fewer Dijkstra queries. However, the speed of M3 drops from 32,215 points/second to 29,102 points/second when Δ rises from 4km to 5km. It can be explained by the fact that a larger UBODT table is read and searched but the number of points matched is slightly increased by 1%.

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Table 2. MM performance tested on a 1-day dataset containing 27,343 trajectories and 310,137 points with configurations of candidate set size k=8, search radius r=300m, hash table size H=5,178,049, node multiplier M=30,000 and no geometry output. The modes tested are (M1) UBODT+Dijkstra (brute force), (M2) UBODT+Dijkstra (optimized), (M3) UBODT and M4 (Dijkstra).

Mode	$\Delta(km)$	$\begin{array}{c} \text{Running} \\ \text{time} (\text{second}) \end{array}$	$\begin{array}{c} {\rm Match} \\ {\rm percentage}(\%) \end{array}$	$\begin{array}{c} {\rm Speed} \\ {\rm (points/second)} \end{array}$	Dijkstra queries count
M1	3	225.35	98.86	1,360.5	1,642,888
M1	4	115.95	98.86	2,644.2	692,301
M1	5	69.15	98.86	4,433.2	319,945
M2	3	83.15	98.83	3,686.2	$582,\!474$
M2	4	18.11	98.83	16,923.4	50,349
M2	5	13.91	98.83	22,027.5	13,457
M3	3	8.99	88.15	$30,\!390.5$	0
M3	4	9.31	96.80	$32,\!215.1$	0
M3	5	10.42	97.87	29,102.8	0
M4	_	1,711.07	98.86	179.18	16,644,031

Table 3. MM performance tested on the one-month dataset containing 644,695 trajectories and 6,812,720 points with the same configurations as Table 2 (No geometry output). The modes tested are (M2) UBODT+Dijkstra (optimized) and (M3) UBODT.

Mode	$\Delta(km)$	$\begin{array}{c} \text{Running} \\ \text{time} (\text{second}) \end{array}$	$\begin{array}{c} {\rm Match} \\ {\rm percentage}(\%) \end{array}$	$\begin{array}{c} {\rm Speed} \\ {\rm (points/second)} \end{array}$	Memory (Megabyte)
M2	3	2,075.07	99.69	3,272.9	146.3
M2	4	475.72	99.69	$14,\!276.4$	201.3
M2	5	315.10	99.69	$21,\!554.2$	266.2
M3	3	135.55	87.18	43,816.6	141.9
M3	4	140.49	96.77	46,929.6	195.6
M3	5	147.20	98.24	45,471.9	261.7

Based on the above findings, the second experiment takes the 1-month dataset as input using the same configurations where only M2 and M3 are tested because M1 and M4 are too slow. The results are reported in Table 3. When matching a large number of trajectories, M3 is much faster than M2 with a sacrifice of smaller number of points matched. When $\Delta = 3km$, M3 achieves a speed of 43,816 points/second, which is 14 times of M2. However, only 87% of points are matched in M3 while in M2 it is 99.69%. By setting a larger Δ , the match percentage of M3 get increased while no significant change is observed in M2. In M3, the highest speed is reported with Δ of 4km, which is similar with Table 2. On average, the speeds of M3 reported in Table 3 are higher than those in Table 2. The reason is that when tested with a small dataset, the input and output account for a larger proportion of the total running time. It can also be observed that matching a large number of trajectories does not consume a huge memory. With $\Delta = 5km$ and UBODT size of 4.3 million rows, it consumes only 261 megabytes (MB) memory, which can be explained by the fact that trajectories are matched in a stream way.

As a summary, M3 with only UBODT queried is the most suitable mode in practice. With appropriate setting of Δ , M3 achieves a high MM speed and matches a large proportion of trajectories at the same time. Therefore, it is set as the default integration mode in subsequent experiments.

The third experiment investigates the running time constitutions of FMM. The trajectories are matched in batch mode where a small buffer set are read iteratively from the input trajectories and matched step by step. The running time of each step then

Table 4. Running time of all steps in FMM (M3) tested with the one-month dataset containing 6.812,720 points with configurations of k=8. The steps are Input, Candidate Search (CS), Optimal path inference (OPI), Complete Path Construction (CPC), Geometry Construction (GC) and Output

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$\begin{array}{c} \text{Output} \\ \text{mode} \end{array}$				ınning	time (R	T) of s	teps (se	econd)	RT (second)	Match percent age (%)	~ .
			Input	CS	OPI	CPC	GC	Output	_		
No GO	5	300	17.81	90.16	31.40	5.68	_	8.04	155.43	98.24	43,043.5
No GO	4	300	7.23	89.62	28.39	5.34	_	6.49	139.38	96.77	47,186.1
No GO	5	200	11.01	61.41	26.17	5.46	_	6.61	113.17	92.56	55,717.7
GO	5	300	18.45	90.03	30.85	5.45	8.22	107.18	266.45	98.24	$25,\!105.7$

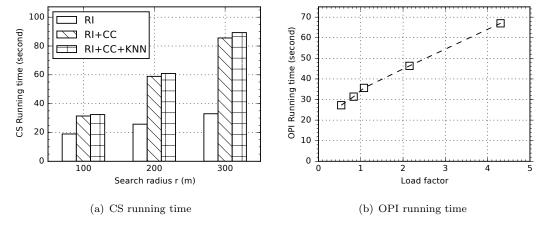


Figure 11. Investigation of running time for candidate search (CS) (a) and optimal path inference (OPI) (b) tested with the one-month data with $\Delta = 5km$. In (a), the three steps are Rtree intersection (RI), candidate construction (CC) and k = 8 nearest neighbor sort (KNN).

gets accumulated as the final result. In the experiment, the 1-month dataset is matched with k=8 and different combinations of Δ , r and output mode are explored. The results are reported in Table 4. It shows that without geometry output, the most time consuming step in FMM is CS, which occupies more than 50% of the total running time. Following CS, OPI accounts for about 20%. When r = 300m and $\Delta = 5km$, writing geometry output degrades the performance substantially from 43,043 points/second to 25,105 points/second where about 40% of the time is spent in the output step. By setting a smaller r of 200m, both CS and OPI takes a shorter time because a smaller candidate set is constructed and processed. However, a smaller r may result in a lower accuracy. The running time constitution of $\Delta = 4km$ also explains the speed improvement in Table 3 with shorter input and OPI step.

The fourth experiment investigates the bottleneck of MM by dividing CS into three steps: R-tree intersection (RI), candidate construction (CC) and KNN sort, as described in Section 4.2.1. Since the three steps are coupled with each other, CS is tested in three modes: RI, RI+CC and RI+CC+KNN. The running time is displayed in Figure 11 (a). It shows that CC is the most time-consuming step in CS, in which the linear referencing algorithm is the most complex task as the projection needs to iterate through all segments in the polyline of a road edge. Regarding the running time of OPI, it is evaluated against the load factor of UBODT lf, which is displayed in Figure 11 (b). When a smaller lf is set, there are fewer elements in each bucket of UBODT on average. Consequently, OPI

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Table 5. Performance comparison with the literature by single processor's MM speed

Study	Implementation and Hardware	GPS interval (second)	Network	Configura- tions	Performance (points/secon
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Study	Implementation and Hardware	GPS interval (second)	Network		Configura- tions	Performance (points/second)
			V	E		
Marchal et al. (2005)	Java, 4 processor 2.5GHz CPU	1	45k	15k	$N^a = 30$	2,000
Li <i>et al.</i> (2011)	Java, Amazon Elastic Compute Cloud	20-60	11k	15k	k = 5 $r = 50m$	$1,250*^{b}$
Miwa <i>et al.</i> (2012)	Fortan, Dual Core 2 GHz CPU,2 GB RAM	5-90	45k	121k	$_c$	287*
Li <i>et al.</i> (2013)	Quadcore 3.2GHz CPU	120	_	_	_	50*
Huang $et \ al.$ (2013)	Hadoop, Single core 3.0GHz CPU,4G RAM	20	106k	141k	_	900-6,000*
Chen $et al.$ (2014)	C#, Dual-core 3.1 GHz CPU, 8GB RAM	10-120	19k	46k	k = 10 $r = 40m$	5,582(No IO) 228(IO)
Zhe and Zhang (2015)	C++, Single-Core 3.4 GHZ CPU, 32 GB RAM	20	20k	47k	_	1,000-2,000
this article	C++, Quad-core 3 GHz CPU, 4GB RAM	60-240	23k	58k	k = 8 $r = 300m$	$25,000 (GO)^d$ 45,000 (No GO)

 $^{^{\}rm a}$ N denotes the size of a candidate path set maintained in the algorithm.

takes a shorter time.

Finally, the performance of FMM is compared with previous studies as summarized in Table 5. The road network used here is on a similar scale in terms of graph size while the GPS data is sparser than previous work. With k = 8 and r = 300m, FMM reports a much higher speed of around 45,000 points/second without geometry output and 25,000 points/second with geometry output. Besides, a large r of 300m is used here as opposed to 50m commonly used in previous studies due to the low accuracy of GPS data collected. When matching a high-quality dataset with smaller r and k, the speed has a potential to be higher according to the findings in Table 4.

5.3. Accuracy assessment

To evaluate the accuracy of the matched result, a ground truth dataset is collected in a similar way as Lou et al. (2009) by randomly selecting 30 trips that are diversely distributed in space, time and length, which are labeled with a true path based on human judgment. Let GT and MR denote the set of complete paths in the ground truth

^b The speed suffixed with * is not directly reported in original article but calculated with information provided by the authors. In some studies where multiple cores of CPU or nodes were used, the speed reported here is rescaled to reflect single-processor's performance.

^c The sign of – means that the information was not provided in that article.

^d GO stands for geometry output. The speed is based on Table 3.

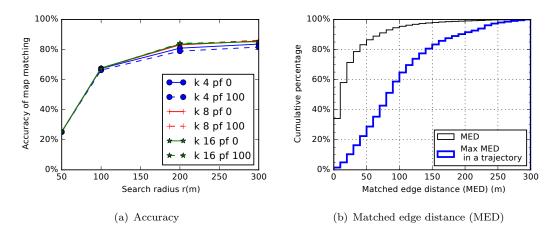


Figure 12. Accuracy of map matching for various configurations (a) and the cumulative distribution of matched edge distance obtained from matching one-month data with k = 8, r = 300m and $\Delta = 5km$.

and matched result, respectively. The accuracy of MM, denoted by A, is defined as the average of the overlapping ratio between GT and MR calculated below

$$A = \frac{1}{|GT|} \sum_{i}^{|GT|} \frac{|GT[i] \cap MR[i]|}{|GT[i] \cup MR[i]|}$$

$$\tag{16}$$

The influence of various configurations on the accuracy is displayed in Figure 12 (a). When r increases from 50m to 300m, the accuracy grows from 25% to 80%. Table 5 shows that r is set as 50m in most previous work. However, the corresponding accuracy is only 25% in this experiment, which results from the large error in GPS observations.

To prove the above hypothesis, let the distance from a GPS point p_i to its matched edge $\hat{C}_{i.e}$ be defined as matched edge distance (MED), namely $\hat{C}_{i.dist}$. Figure 12 (b) demonstrates the distribution of MED of a point and the maximum of MED within a trajectory obtained from matching the 1-month dataset with k=8, r=300m and $\Delta=5km$. It can be observed that although there are 82 % of points whose MED is smaller than 50m, only 22% of the trajectories have a maximum MED under 50m. It implies that when r is set as 50m, 78% of the trajectories are either incorrectly matched or unmatched.

It is important to emphasize that the HMM model defined by Equations 10 to 12 are designed the same as Lou et al. (2009) except that several degenerate cases are settled in FMM. Because of the large error in GPS data, the accuracy of FMM is lower than previous work. In practice, it is flexible to define a different set of emission and transition probabilities in FMM with the same performance achieved. Additionally, varying pf and k exhibits no significant impact on the accuracy. It may be explained by the selection bias that the trips affected by penalty are not included in GT. More detailed evaluation of pf is provided in the next section.

5.4. Evaluation of penalty for reverse movement

When evaluating the penalty for reverse movement, experiments are performed on the 1-month dataset with k = 8, r = 300m, $\Delta = 5km$ and pf varied from 0 to 100. Reverse

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movement in the matched result can be detected by comparing consecutive edges in the C-path. A trajectory containing reverse movement is also referred as reverse trajectory. The distribution of reverse trajectories in the matched result with respect to pf is shown in Figure 13 (a). As pf increases from 0 to 100, the number of reverse trajectories reduces rapidly from 355,000 (55%) to a lower bound of 215,000 (33%). The high percentage of reverse trajectories can be explained by the fact that a taxi is likely to change moving direction at the start of a trip after fetching a passenger. To prove that, the maximal direction change of a trajectory tr is introduced and defined as

$$\alpha = \min_{1 \le n \le N-2} (\cos(\overrightarrow{p_n, p_{n+1}}, \overrightarrow{p_{n+1}}, \overrightarrow{p_{n+1}}, \overrightarrow{p_{n+2}}))$$
 (17)

where N is the number of points in tr and $-1 \le \alpha \le 1$. When $\alpha = -1$, it implies a completely reverse movement in tr while $\alpha = 1$ corresponds to a straight line.

The distribution of α in the original and reverse trajectories in the result of pf = 0 is displayed in Figure 13 (b). A large proportion of the original and reverse trajectories are

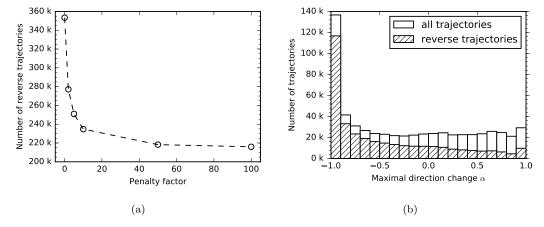


Figure 13. Distribution of reverse trajectories with respect to pf (a) and distribution of maximal distribution change α in the original and reverse trajectories with pf = 0 (b).

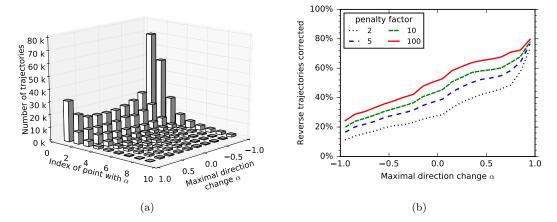


Figure 14. Distribution of maximal distribution change α and the index of point where α occurs in the original trajectories (a) and percentage of reverse trajectories being corrected with respect to α .

Reverse

(no penalty)

Matched path

(with penalty)

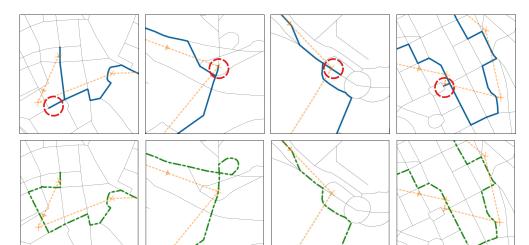


Figure 15. Examples of reverse movement corrected by applying a penalty with pf = 100.

Moving direction

concentrated in the region with α close to -1. The joint distribution of α and the index of point where α occurs in the original trajectories is displayed in Figure 14 (a). It shows that a large number of maximal direction changes occur close to the start of a trajectory, which fits with the taxi driving behavior of changing direction after fetching a passenger. Figure 14 (b) demonstrates the percentage of reverse trajectories being corrected with respect to α . As can be observed, with a larger α indicating a smaller direction change, a reverse trajectory has a higher probability of being corrected. The reason is that a trajectory with a small direction change is unlikely to contain reverse movement. Therefore, when reverse movement is generated in the matched result, there should exist another candidate path representing the true movement with a high score. Consequently, applying a penalty has a great potential to correct the result. Some examples tested with pf = 100 are displayed in Figure 15, which shows that the algorithm can correct reverse movement effectively.

6. Conclusions and future work

GPS trajectory

Road network

GPS observation

The article proposed fast map matching, an algorithm integrating hidden Markov model with precomputation and provided an open source implementation. By precomputing all pairs of shortest paths in the road network under a specific distance threshold, repeated routing queries in MM are replaced with hash table search. Additionally, several degenerate cases and a problem of reverse movement were identified in previous MM algorithms and corrected in this article. Experiments on a real-world GPS dataset demonstrate that precomputation can effectively improve the performance of MM and FMM has achieved a considerable performance in both precomputing and map matching stage. It takes less than 10 seconds to precompute a UBODT containing more than 4 million rows. Single-processor MM speeds are reported as 25,000 points/second with geometry output and 45,000 points/second without geometry output, which are much higher than previous work. Further investigation on the running time of all steps in FMM reveals that when precomputation is employed, the new bottleneck of in MM is located in candidate search and more specifically, the linear referencing function which projects a GPS point to the

polyline of a road edge. Comparison of different modes of routing integration shows that exporting the large-gap trajectories as unmatched without invoking Dijkstra is the most suitable mode in practice, which achieves a high speed and matches a large proportion of trajectories. In addition, by applying a penalty, reverse movement in the result is corrected effectively.

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The future work would be planned in the following directions. Firstly, the performance of FMM can be further improved by introducing parallel computing. The new bottleneck is identified as candidate search and how to alleviate this problem will be investigated. Besides, useful information can also be extracted and analyzed from the matched result, e.g., travel time and movement patterns.

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