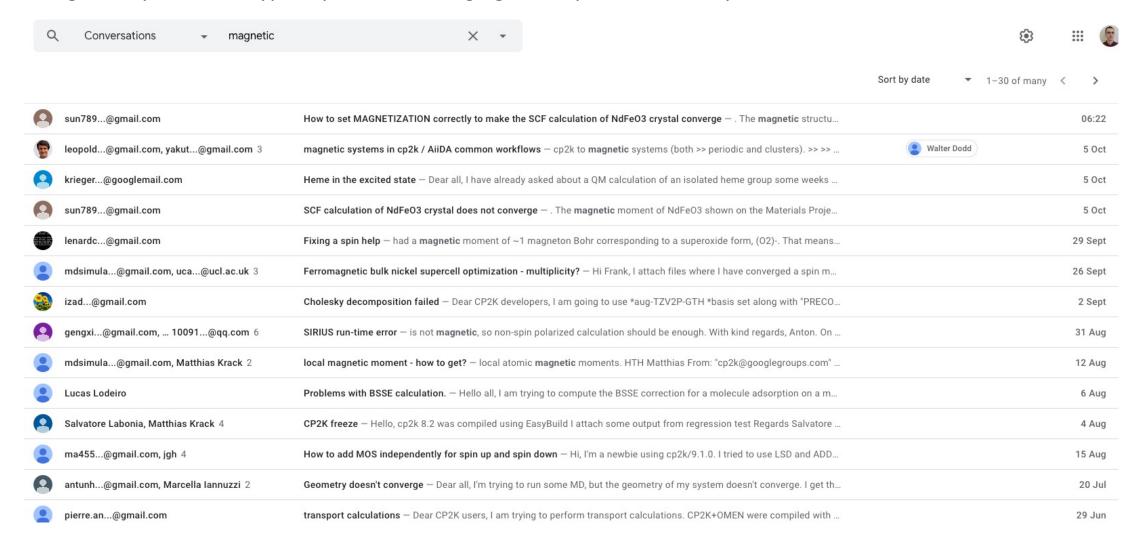
Imperial College London

Converging magnetic systems: from bulk Ni to a Ni slab in vacuum

Christian Ahart

Motivation

- Magnetic systems are common in nature (Fe, Ni, Co etc.)
- Magnetic systems are typically more challenging and expensive to study



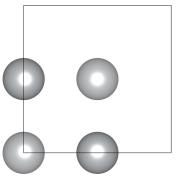
From electronic configuration [Ar] 3d8 4s2 Ni should be ferromagnetic with spin moment of 2

&END FORCE_EVAL

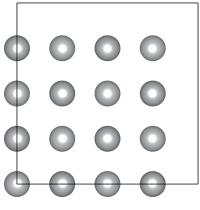
Consider a 2x2x2 supercell of Ni with 32 atoms and 576 electrons (32*18=576):

```
&FORCE_EVAL
        METHOD Quickstep
        STRESS_TENSOR ANALYTICAL
        &DFT
                BASIS_SET_FILE_NAME BASIS_MOLOPT
                POTENTIAL_FILE_NAME GTH_POTENTIALS
                CHARGE 0
                MULTIPLICITY 1
                UKS .TRUE.
                &QS
                        EPS_DEFAULT 1.0E-12
                        EXTRAPOLATION ASPC
            &END QS
                &MGRID
                        NGRIDS 5
                        CUTOFF 600.0
                        REL_CUTOFF 60.0
                &END MGRID
                &SCF
                        SCF GUESS ATOMIC
                        EPS_SCF 1.0E-8
                        MAX_SCF 500
                        ADDED_MOS 1000
                        &DIAGONALIZATION
                                ALGORITHM STANDARD
                        &END DIAGONALIZATION
                        &MIXING
                                METHOD BROYDEN_MIXING
                                ALPHA 0.1
                                NBUFFER 10
                        &END MIXING
                        &SMEAR
                                ELECTRONIC_TEMPERATURE [K] 500.0
                                METHOD FERMI DIRAC
                        &END SMEAR
                &END SCF
```

```
&XC
                &XC_FUNCTIONAL PBE
                &END XC_FUNCTIONAL
        &END XC
        &PRINT
          &E_DENSITY_CUBE ON
          &END E_DENSITY_CUBE
          &HIRSHFELD
             SHAPE_FUNCTION DENSITY
          &END HIRSHFELD
        &END PRINT
    &END DFT
&SUBSYS
        &CELL
                ABC 3.50579800 3.50579800 3.50579800
                ALPHA_BETA_GAMMA 90.000 90.000 90.000
                MULTIPLE_UNIT_CELL 2 2 2
        &END CELL
        &TOPOLOGY
                COORD_FILE_FORMAT XYZ
                COORD_FILE_NAME ${INPUT_COORD_FILE_NAME}
                MULTIPLE_UNIT_CELL 2 2 2
        &END TOPOLOGY
        &KIND Ni
                ELEMENT Ni
                BASIS_SET DZVP-MOLOPT-SR-GTH
                POTENTIAL GTH-PBE
        &END KIND
&END SUBSYS
```



FCC unit cell



2x2x2 supercell

From electronic configuration [Ar] 3d⁸ 4s² Ni should be ferromagnetic with spin moment of 2

Consider a 2x2x2 supercell of Ni with 32 atoms and 576 electrons (32*18=576):

```
Electronic structure
   Total number of core electrons
                                                                          10.00
   Total number of valence electrons
                                                                          18.00
   Total number of electrons
                                                                          28.00
  Multiplicity
                                                                  not specified
        2.00 2.00] 2.00 2.00
         6.001 6.00
          8.00
   D
 Spin 1
 Re-scaling the density matrix to get the right number of electrons for spin 1
                  # Electrons
                                           Trace(P)
                                                                   Scaling factor
                           288
                                             288.033
                                                                            1.000
 Spin 2
 Re-scaling the density matrix to get the right number of electrons for spin 2
                  # Electrons
                                           Trace(P)
                                                                   Scaling factor
                          288
                                             288.033
                                                                            1.000
```

*** SCF run converged in

25 steps ***

Spin 1 Re-scal	ling the density mat	rix to ge	t the right numbe	er of electrons for	spin 1				Hirshfeld	d Charges			
500	# Electron		Trace(P)		ing factor				D (6)				
		88	288.033	56462	1.000	#Atom	Element			Popul		Spin moment	_
			2001033		21000	1	Ni	1	18.000	9.000	9.000	-0.000	-0.000
Spin 2						2	Ni	1	18.000	9.000	9.000	-0.000	-0.000
	ling the density mat	rix to ge	t the right numbe	er of electrons for	spin 2	3	Ni	1	18.000	9.000	9.000	0.000	-0.000
	# Electron		Trace(P)		ing factor	4	Ni	1	18.000	9.000	9.000	-0.000	-0.000
		88	288.033		1.000	5	Ni	1	18.000	9.000	9.000	-0.000	0.000
						6	Ni	1	18.000	9.000	9.000	-0.000	-0.000
						7	Ni	1	18.000	9.000	9.000	-0.000	0.000
SCF WAV	VEFUNCTION OPTIMIZAT:	ION				8	Ni	1	18.000	9.000	9.000	-0.000	0.000
						9	Ni	1	18.000	9.000	9.000	-0.000	0.000
Step	Update method	Time	Convergence	Total energy	Change	10	Ni	1	18.000	9.000	9.000	-0.000	-0.000
	·					11	Ni	1	18.000	9.000	9.000	0.000	-0.000
1 N	NoMix/Diag. 0.10E+00	0.4	0.80171411	-5429.7560153866	-5.43E+03	12	Ni	1	18.000	9.000	9.000	0.000	-0.000
2 E	Broy./Diag. 0.10E+00	0.6	0.02588730	-5335.8096605085	9.39E+01	13	Ni	1	18.000	9.000	9.000	-0.000	-0.000
3 E	Broy./Diag. 0.10E+00	0.6	0.04784139	-5376.5137410802	-4.07E+01	14	Ni	1	18.000	9.000	9.000	-0.000	-0.000
4 E	Broy./Diag. 0.10E+00	0.6	0.00924909	-5457.1568627918	-8.06E+01	15	Ni	1	18.000	9.000	9.000	0.000	-0.000
5 E	Broy./Diag. 0.10E+00	0.6	0.02124621	-5458.3145504847	-1.16E+00	16	Ni	1	18.000	9.000	9.000	-0.000	0.000
6 E	Broy./Diag. 0.10E+00	0.6	0.01756844	-5434.4301411166	2.39E+01	17	Ni	1	18.000	9.000	9.000	-0.000	0.000
	Broy./Diag. 0.10E+00		0.00206891	-5415.3312463523		18	Ni	1	18.000	9.000	9.000	-0.000	0.000
8 E	Broy./Diag. 0.10E+00	0.6	0.00044585	-5418.7667399029	-3.44E+00	19	Ni	1	18.000	9.000	9.000	0.000	-0.000
	Broy./Diag. 0.10E+00		0.00013968	-5418.0821093648	6.85E-01	20	Ni	1	18.000	9.000	9.000	0.000	-0.000
	Broy./Diag. 0.10E+00		0.00006977	-5418.2285997701		21	Ni	1	18.000	9.000	9.000	-0.000	0.000
	Broy./Diag. 0.10E+00	0.7	0.00003185	-5418.2033048944		22	Ni	1	18.000	9.000	9.000	-0.000	-0.000
	Broy./Diag. 0.10E+00		0.00000965	-5418.2400190922		23	Ni Ni	1	18.000	9.000	9.000	0.000	0.000
	Broy./Diag. 0.10E+00		0.00002667	-5418.2281566399									
	Broy./Diag. 0.10E+00		0.00002834	-5418.2101435214		24	Ni	1	18.000	9.000	9.000	-0.000	-0.000
	Broy./Diag. 0.10E+00	0.6	0.00000462	-5418.1881007901		25	Ni	1	18.000	9.000	9.000	0.000	0.000
	Broy./Diag. 0.10E+00	0.6	0.00000071	-5418.1824488938		26	Ni	1	18.000	9.000	9.000	-0.000	0.000
	Broy./Diag. 0.10E+00		0.00000122	-5418.1824658980		27	Ni	1	18.000	9.000	9.000	0.000	0.000
	Broy./Diag. 0.10E+00		0.00000135	-5418.1824690107		28	Ni	1	18.000	9.000	9.000	0.000	0.000
	Broy./Diag. 0.10E+00		0.00000113	-5418.1824976251		29	Ni	1	18.000	9.000	9.000	-0.000	-0.000
	Broy./Diag. 0.10E+00		0.00000014	-5418.1824933141		30	Ni	1		9.000	9.000	-0.000	0.000
	Broy./Diag. 0.10E+00		0.00000008	-5418.1824664816		31	Ni	1		9.000	9.000	0.000	-0.000
	Broy./Diag. 0.10E+00		0.00000009	-5418.1824768989		32	Ni	1	18.000	9.000	9.000	-0.000	-0.000
	Broy./Diag. 0.10E+00		0.00000005	-5418.1824777986									
	Broy./Diag. 0.10E+00		0.00000002	-5418.1824779812									
25 E	Broy./Diag. 0.10E+00	0.6	3.7035E-09	-5418.1824782140	-2.33E-07								

From electronic configuration [Ar] 3d8 4s2 Ni should be ferromagnetic with spin moment of 1

2 unpaired electrons per atom -> total multiplicity 2S+1: 2*1*32+1=65

```
Electronic structure
  Total number of core electrons
                                                                           10.00
  Total number of valence electrons
                                                                           18.00
  Total number of electrons
                                                                           28.00
  Multiplicity
                                                                   not specified
         2.00 2.00] 2.00 2.00
      [ 6.00] 6.00
         8.00
  Spin 1
  Re-scaling the density matrix to get the right number of electrons for spin 1
                   # Electrons
                                             Trace(P)
                                                                    Scaling factor
                            320
                                              288.033
                                                                              1.111
  Spin 2
  Re-scaling the density matrix to get the right number of electrons for spin 2
                   # Electrons
                                             Trace(P)
                                                                    Scaling factor
                            256
                                              288.033
                                                                              0.889
```

36 Broy./Diag. 0.10E+00

*** SCF run converged in

5.3291E-09

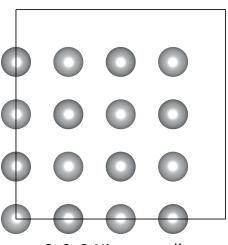
36 steps ***

-5418.2988130264 -1.33E-07

Spin 2 Re-scaling the density matrix to get the right number of electrons for spin 2 #Atom Element Kind Ref Charge Population Spin moment N	0.000 0.000 -0.000 0.000 0.000
Re-scaling the density matrix to det the right number of electrons for spin 2	0.000 0.000 -0.000 0.000 0.000
# Electrons Trace(P) Scaling factor 1 Ni 1 18.000 9.344 8.656 0.687	0.000 -0.000 0.000 0.000
256 288.033 0.889 2 Ni 1 18.000 9.344 8.656 0.687	-0.000 0.000 0.000
3 Ni 1 18.000 9.344 8.656 0.687	0.000
	0.000
SCF WAVEFUNCTION OPTIMIZATION 4 Ni 1 18.000 9.344 8.656 0.687	
5 Ni 1 18.000 9.344 8.656 0.687	0 000
Step Update method Time Convergence Total energy Change 6 Ni 1 18.000 9.344 8.656 0.687	0.000
1 NoMix/Diag. 0.10E+00 0.4 0.90450672 -5430.9290286363 -5.43E+03 7 Ni 1 18.000 9.344 8.656 0.687	-0.000
2 Broy./Diag. 0.10E+00 0.6 0.01963244 -5360.9174089422 7.00E+01 8 Ni 1 18.000 9.344 8.656 0.687	-0.000
3 Broy./Diag. 0.10E+00 0.6 0.03786641 -5391.3474411346 -3.04E+01 9 Ni 1 18.000 9.344 8.656 0.687	-0.000
4 Broy./Diag. 0.10E+00 0.6 0.01643672 -5405.2813195731 -1.39E+01	-0.000
5 Bioy./biag. 6.102+00 6.0 6.0105/305 -5306.1051012054 1./12+01	-0.000
8 Broy /Diag 8 185499 8 6 8 88601562 -5/28 562608825/ -2 /75-81	-0.000
9 Broy./Diag. 0.10E+00 0.6 0.00073849 -5420.3611606832 2.02E-01 13 N1 1 18.000 9.344 8.656 0.68/	-0.000
10 Broy./Diag. 0.10E+00 0.6 0.00082272 -5419.8704837172 4.91E-01 14 Ni 1 18.000 9.344 8.656 0.687	-0.000
11 Broy./Diag. 0.10E+00 0.6 0.00103204 -5419.1493765569 7.21E-01 15 Ni 1 18.000 9.344 8.656 0.687	-0.000
12 Broy./Diag. 0.10E+00	-0.000
13 Broy./Diag. 0.10E+00 0.6 0.00020785 -5418.2998409068 1.21E-01 10 N1 1 18.000 9.344 8.656 0.687	-0.000
15 Broy./Diag. 0.10E+00 0.6 0.00004969 -5418.2863691706 -2.12E-03 18 Ni 1 18.000 9.344 8.656 0.687	0.000
1/ Prov. (Pi 0 405:00 0 / 0 0000000 5/40 005405000 0 7/5 00	
16 Broy./Diag. 0.10E+00 0.6 0.00023052 -5418.2951055282 -8.74E-03 19 Ni 1 18.000 9.344 8.656 0.687 17 Broy./Diag. 0.10E+00 0.6 0.00078318 -5418.3069846198 -1.19E-02	-0.000
18 Broy./Diag. 0.10E+00 0.6 0.00002694 -5418.3257565653 -1.88E-02 20 Ni 1 18.000 9.344 8.656 0.687	0.000
19 Broy./Diag. 0.10E+00	-0.000
20 Broy./Diag. 0.10E+00 0.6 0.00000274 -5418.3208987916 -4.82E-03 22 Ni 1 18.000 9.344 8.656 0.687	-0.000
22 Broy./Diag. 0.10E+00 0.6 0.00001005 -5418.3093980076 8.04E-03 23 Ni 1 18.000 9.344 8.656 0.687	-0.000
23 Broy./Diag. 0.10E+00 0.6 0.000000298 -5418.3033214071 6.08E-03 24 Ni 1 18.000 9.344 8.656 0.687	-0.000
24 Broy./Diag. 0.10E+00 0.6 0.00000164 -5418.3010164987 2.30E-03 25 Ni 1 18.000 9.344 8.656 0.687	-0.000
25 Broy./Diag. 0.10E+00 0.7 0.00000002 -5418.2998/594/1 1.14E-03	-0.000
20 Didy1/Didgi 01102/00 017 010000004 041012/70002024 01702 04	
27 Broy./Diag. 0.10E+00 0.6 0.00000031 -5418.2989713234 3.29E-04 27 Ni 1 18.000 9.344 8.656 0.687 28 Broy./Diag. 0.10E+00 0.6 0.00000007 -5418.2987449650 2.26E-04 28 Ni 1 18.000 9.344 8.656 0.687	-0.000
29 Brov./Diag. 0.10F+00 0.6 0.00000004 -5418.2988038120 -5.88F-05	0.000
30 Broy./Diag. 0.10E+00 0.7 0.00000004 -5418.2988106371 -6.83E-06 29 Ni 1 18.000 9.344 8.656 0.687	-0.000
31 Broy./Diag. 0.10E+00 0.7 0.00000000 -5418.2988164482 -5.81E-06 30 Ni 1 18.000 9.344 8.656 0.687	-0.000
32 Broy./Diag. 0.10E+00 0.8 0.00000010 -5418.2988162648 1.83E-07 31 Ni 1 18.000 9.344 8.656 0.687	-0.000
33 Broy./Diag. 0.10E+00 0.6 0.00000003 -5418.2988136581 2.61E-06 22 NJ 1 10.000 0.244 0.454 0.407	-0.000
34 Broy./Diag. 0.10E+00 0.6 0.00000002 -5418.2988129024 7.56E-07 32 NI I 10.000 9.344 0.050 0.007 35 Broy./Diag. 0.10E+00 0.6 0.00000002 -5418.2988128930 9.37E-09	0.000

- Energy for bulk Ni is 3 eV lower with a ferromagnetic solution
- Correct choice of multiplicity is essential to converge magnetic solution

Multiplicity	Energy / Ha	SCF steps	Spin moment
1	-5418.1825	25	0.00
65	-5418.2988	36	0.69



2x2x2 Ni supercell

&BS section defines the atomic orbital occupation assigned in initialization of the density matrix

N: Principal quantum number

L: Angular momentum quantum number

NEL: Orbital occupation number

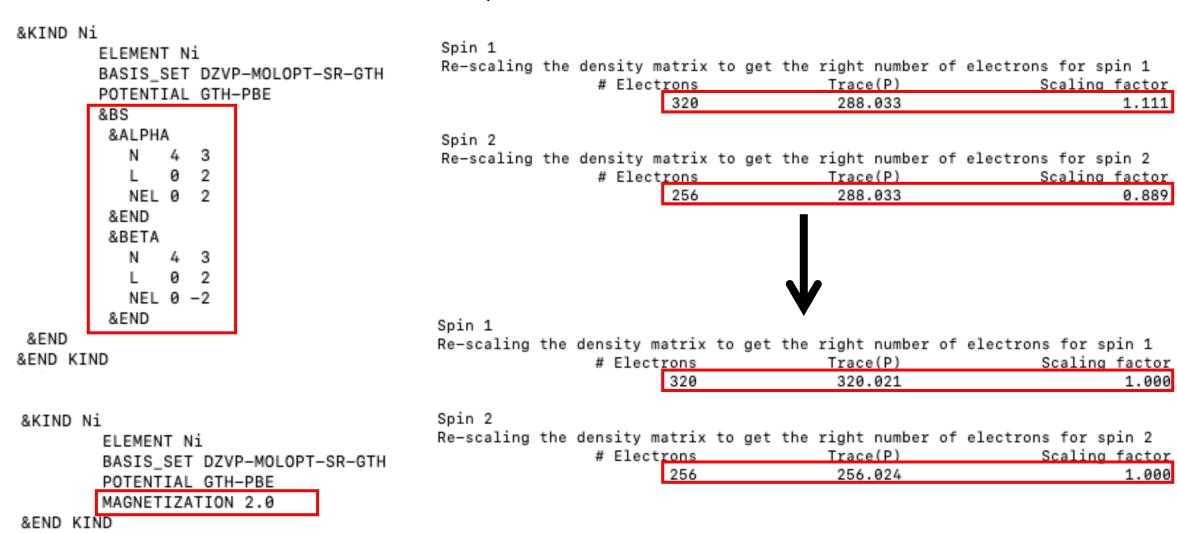
```
&KIND Ni
        ELEMENT Ni
        BASIS_SET DZVP-MOLOPT-SR-GTH
        POTENTIAL GTH-PBE
        &BS
         &ALPHA
                  3
           NEL 0
         &END
         &BETA
           NEL 0 -2
         &END
 &END
&END KIND
```

```
Electronic structure
  Total number of core electrons
                                                                           10.00
  Total number of valence electrons
                                                                           18.00
  Total number of electrons
                                                                           28.00
  Multiplicity
                                                                   not specified
          2.00 2.00] 2.00
                            2.00
         6.001 6.00
          8.00
Electronic structure
   Total number of core electrons
                                                                         10.00
   Total number of valence electrons
                                                                         18.00
   Total number of electrons
                                                                         28.00
   Multiplicity
                                                                       triplet
   Alpha Electrons
       [ 1.00 1.00] 1.00 1.00
       [ 3.00] 3.00
          5.00
   Beta Electrons
          1.00 1.00 1.00 1.00
          3.00] 3.00
          3.00
```

Alternative to &BS section is MAGNETIZATION keyword

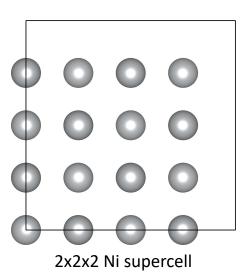
```
&KIND Ni
         ELEMENT Ni
                                               Electronic structure
         BASIS_SET DZVP-MOLOPT-SR-GTH
                                                  Total number of core electrons
                                                                                                                        10.00
         POTENTIAL GTH-PBE
                                                  Total number of valence electrons
                                                                                                                        18.00
         &BS
                                                  Total number of electrons
                                                                                                                        28.00
                                                  Multiplicity
          &ALPHA
                                                                                                                not specified
                                                         2.00 2.00] 2.00 2.00
                                                        6.001 6.00
                                                         8.00
            NEL 0 2
          &END
          &BETA
            NEL 0 -2
          &END
                                               Electronic structure
                                                  Total number of core electrons
 &END
                                                                                                                      10.00
                                                  Total number of valence electrons
                                                                                                                      18.00
&END KIND
                                                  Total number of electrons
                                                                                                                      28.00
                                                  Multiplicity
                                                                                                                    triplet
                                                  Alpha Electrons
&KIND Ni
                                                      [ 1.00 1.00] 1.00 1.00
         ELEMENT Ni
                                                      [ 3.00] 3.00
         BASIS_SET DZVP-MOLOPT-SR-GTH
                                                         5.00
         POTENTIAL GTH-PBE
                                                  Beta Electrons
         MAGNETIZATION 2.0
                                                        1.00 1.001 1.00 1.00
&END KIND
                                                      [ 3.00] 3.00
                                                         3.00
```

Alternative to &BS section is MAGNETIZATION keyword



- Energy for bulk Ni is 3 eV lower with a ferromagnetic solution
- &BS section or MAGNETIZATION lowers energy of first SCF step, however leads to slower convergence
- Multiplicity can be optimised with knowledge of calculated spin moment (starting guess s=0.5 is faster than s=1)

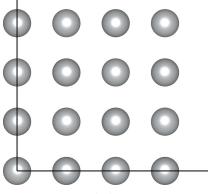
Multiplicity	Energy / Ha	SCF steps	Spin moment
1	-5418.1825	25	0.00
65	-5418.2988	36	0.69
65 (MAGNETIZATION 2)	-5418.2988	46	0.69
33	-5418.2988	19	0.69
33 (MAGNETIZATION 1)	-5418.2988	23	0.69



Ni slab in vacuum

- Energy for Ni slab in vacuum is 2 eV lower with a ferromagnetic solution
- SCF convergence is very slow (SCF steps shown for EPS_SCF: 1e-5, 1e-7)

Multiplicity	Energy / Ha	SCF steps	Spin moment
1	-5417.5516	45, 73	0.00
65 (MAGNETIZATION 2)	-5414.6756	285, 374	0.68 bulk 0.74 interfacial
33	-5417.6242	564, 616	0.68 bulk 0.75 interfacial



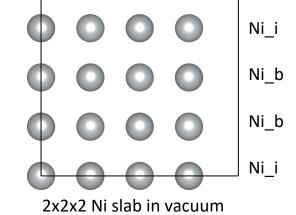
2x2x2 Ni slab in vacuum

- 1. Define MAGNETIZATION for each unique atomic environment
- 2. Choose non-integer magnetizations which sum to integer multiplicity (16*0.7+16*0.8)+1=25

```
&KIND Ni_b
ELEMENT Ni
BASIS_SET DZVP-MOLOPT-SR-GTH
POTENTIAL GTH-PADE-q18
MAGNETIZATION 0.7
&END KIND
```

&KIND Ni_i
ELEMENT Ni
BASIS_SET DZVP-MOLOPT-SR-GTH
POTENTIAL GTH-PADE-q18
MAGNETIZATION 0.8
&END KIND

Multiplicity	Energy / Ha	SCF steps	Spin moment
1	-5417.5516	45, 73	0.00
65 (MAGNETIZATION 2)	-5414.6756	285, 374	0.68 bulk 0.74 interfacial
25 (MAGNETIZATION 0.7, 0.8)	-5414.6756	57, 139	0.68 bulk 0.74 interfacial



General workflow

- 1. Converge bulk crystal with multiplicity according to Hund's rule
- 2. Converge interface with multiplicity according to Hund's rule
- 3. Define MAGNETIZATION for each unique atomic environment
- 4. Optimise MAGNETIZATION (real number) and MULTIPLICITY (integer)

Thank you for listening

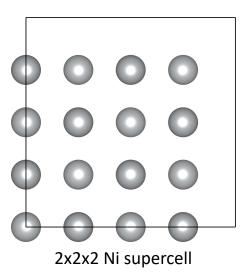
Supporting Information

Defining MAGNETIZATION increases number of SCF steps for bulk Ni

```
Multiplicity 65, MAX SCF 1
1 NoMix/Diag. 0.10E+00
                       0.5 0.90450672
                                          -5430.9290286363 -5.43E+03
       Νi
                    18.000 9.482 8.518
             1
                                                   0.964
                                                            -0.000
Multiplicity 65, MAX SCF 1, MAGNETIZATION 2
1 NoMix/Diag. 0.10E+00
                       0.4
                              0.80945817
                                           -5430.9700952423 -5.43E+03
       Νi
             1
                   18.000 9.479 8.521
                                                   0.957
                                                            -0.000
Multiplicity 65, MAX SCF 1
1 NoMix/Diag. 0.10E+00
                       0.4 0.87189090
                                           -5430.0490174185 -5.43E+03
       Νi
                   18.000 9.227 8.773
                                                   0.453
             1
                                                            -0.000
1
Multiplicity 65, MAX SCF 1, MAGNETIZATION 1
1 NoMix/Diag. 0.10E+00
                       0.4
                                          -5430.0597589981 -5.43E+03
                              0.82500894
       Νi
                    18.000 9.223 8.777
1
             1
                                                   0.446
                                                            -0.000
```

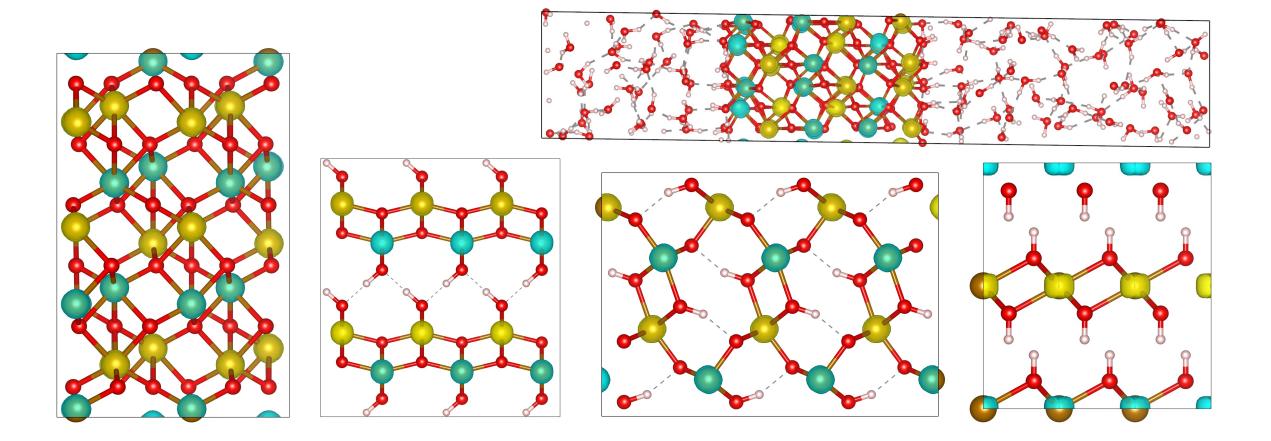
- Energy for bulk Ni is 3 eV lower with a ferromagnetic solution
- Correct choice of multiplicity is essential to converge magnetic solution
- &BS section or MAGNETIZATION lowers energy of first SCF step, however leads to slower convergence

Multiplicity	Energy / Ha	SCF steps	Spin moment
1	-5418.1825	25	0.00
65	-5418.2988	36	0.69
65 (MAGNETIZATION 2)	-5418.2988	46	0.69
33	-5418.2988	19	0.69
33 (MAGNETIZATION 1)	-5418.2988	23	0.69



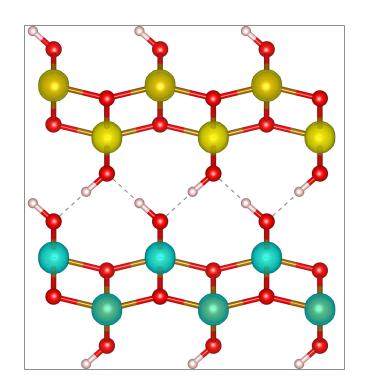
My background

- PhD research involved converging antiferromagnetic iron oxides
- No previous experience with Ni or pure metals

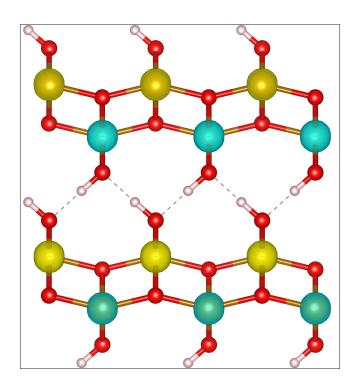


Lepidocrocite

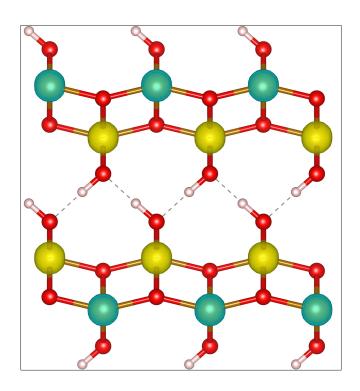
• Multiple magnetic solutions may exist for the same multiplicity, these must be checked manually



 $uudd \ \text{-}5623.8244 \ \text{Ha} \\ \text{Spin moment } 4.37 \ \mu_{\text{B}}$



udud -5623.8403 Ha Spin moment 4.29 μ_{B}



uddu~-5623.8383~Ha Spin moment 4.29 μ_{B}