

Sensory and Motor

Class 2

Announcements

- Remember to find a partner and submit a topic with your group!
- Bring a Calculator!
- Be cognizant of quiz dates, presentation dates, and test dates.

Goals for class today

- Learn how cells (not just neurons) set a resting membrane potential.
- Introduction to ion channels
- The action potential

The neuron - a specialized cell type that can signal over long distances

There are 3 main
regions of the neuron:

Dendrites

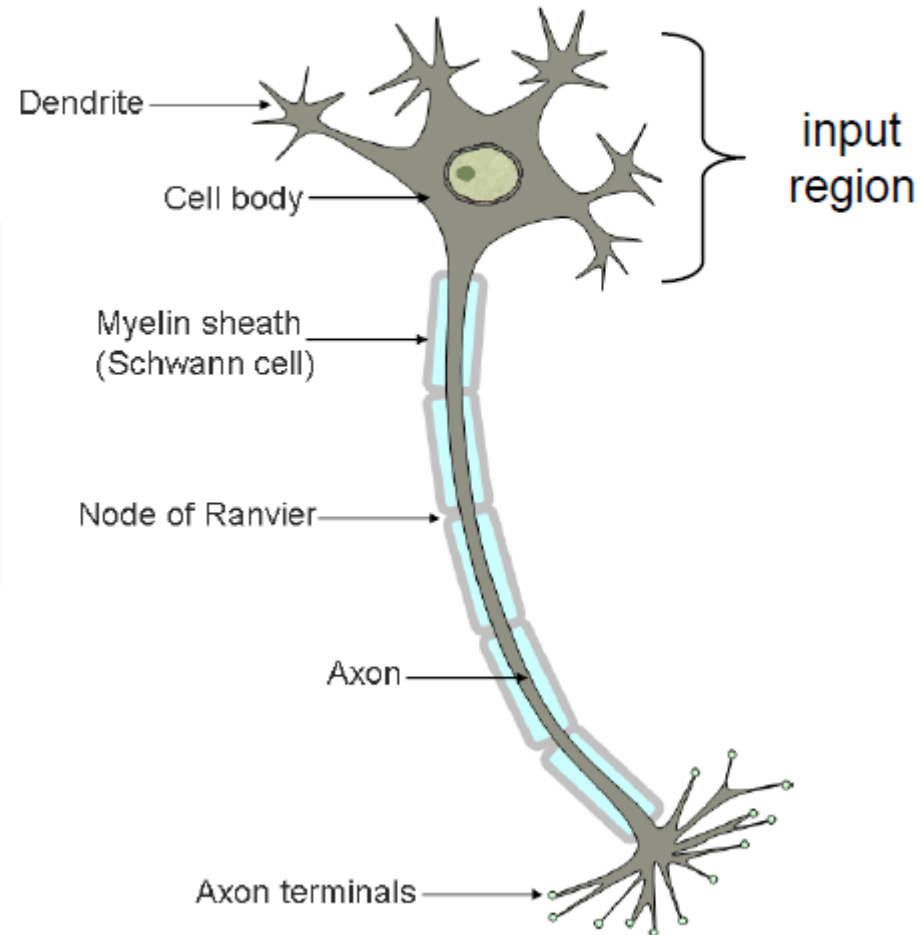
Cell body (or soma)

Axon

Terminology

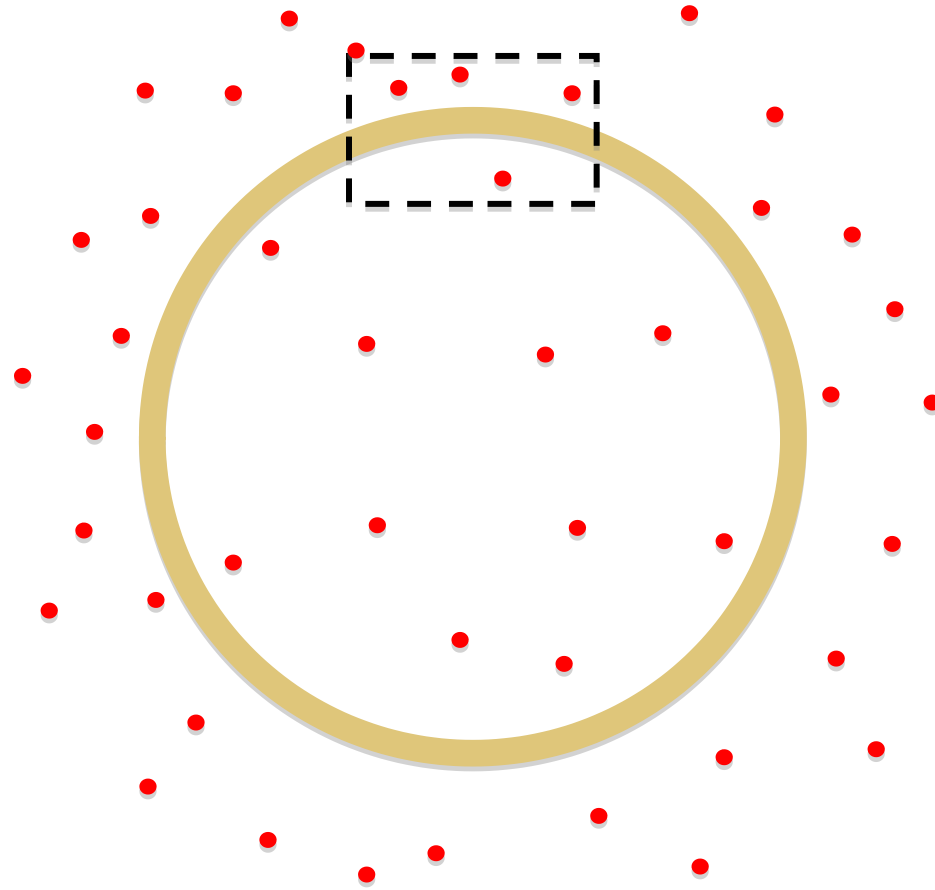
axon

dendrite



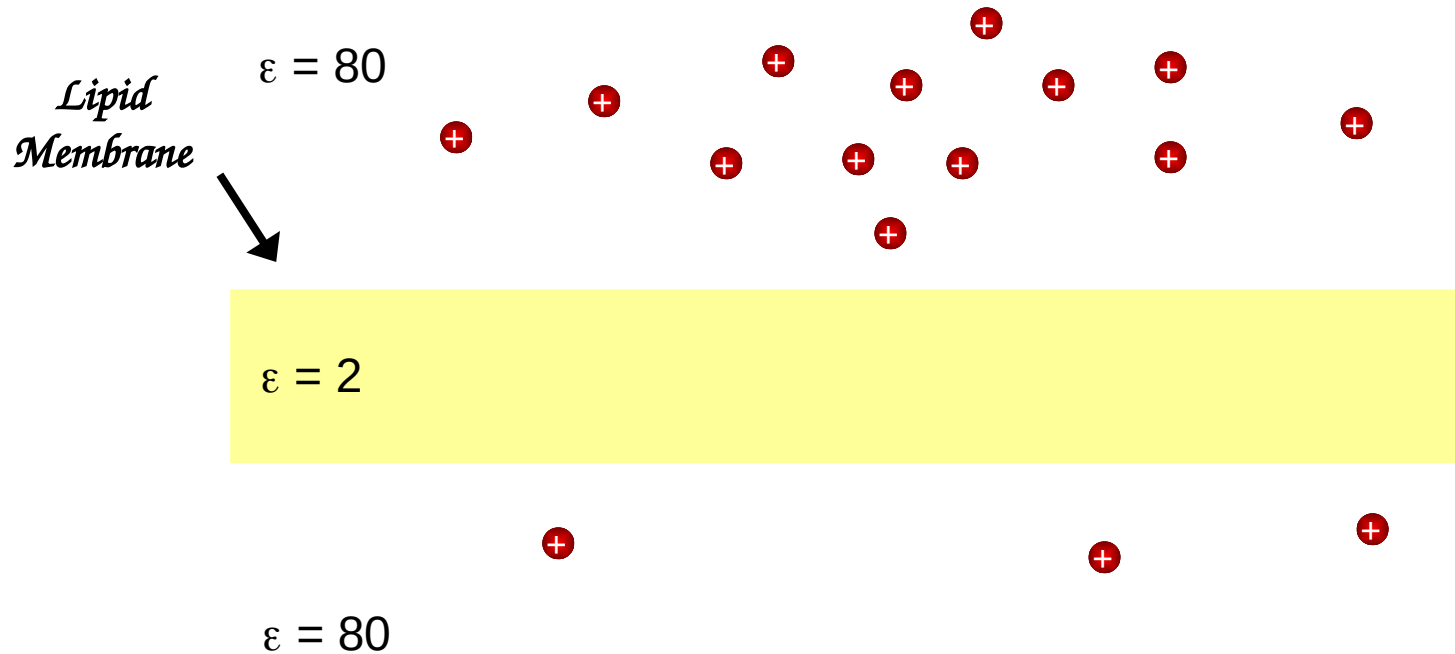
Understanding what dictates the membrane potential across a biological membrane is one of the most fundamental concepts in neuroscience!!

Biological Cell Membrane
Conceptual Model



Biological Cell Membrane

Conceptual Model



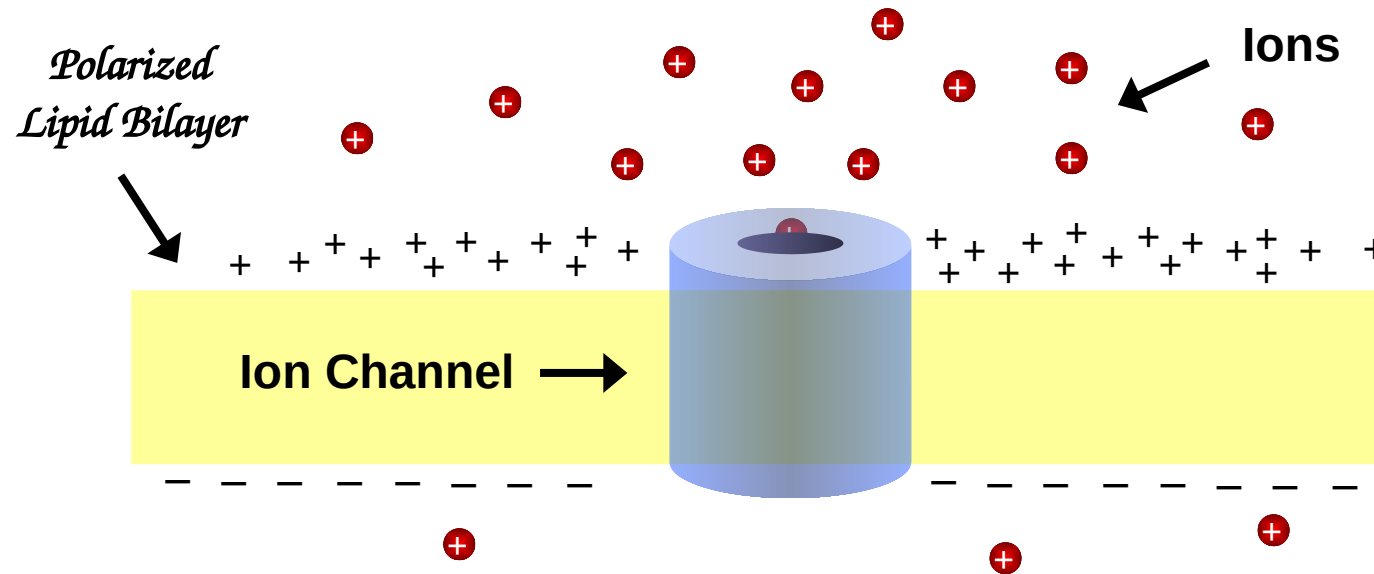
*The lipid bilayer of biological membranes are oily barriers that cannot solvate ions
(i.e., the dielectric constant of the membrane is very low)*

*Thus, the lipid bilayer represents an insurmountable energy barrier for ions
How do cell membranes lower this energy barrier?*

Permittivity (dielectric constant) is a material property that affects the Coulomb force between two point charges in the material.

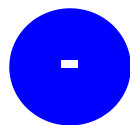
Biological Cell Membrane

Conceptual Model

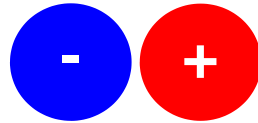


Ion channels are membrane-spanning proteins containing aqueous pores that reduce the lipid bilayer energy barrier by providing an alternate pathway for ions to cross the membrane. Thus, ion channels are catalytic membrane proteins.

Attraction between two opposite charges



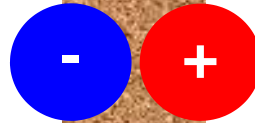
Attraction between two opposite charges



Low Energy

(charges cannot do work)

Charges separated by an insulator



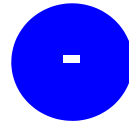
Work was done to separate the charges. Now there is a voltage across the insulator.*

The insulator is “energized”

How is this done in biological cell membranes?

** 1 Volt = 1 Joule / 1 Coulomb*

Charges separated by an insulator



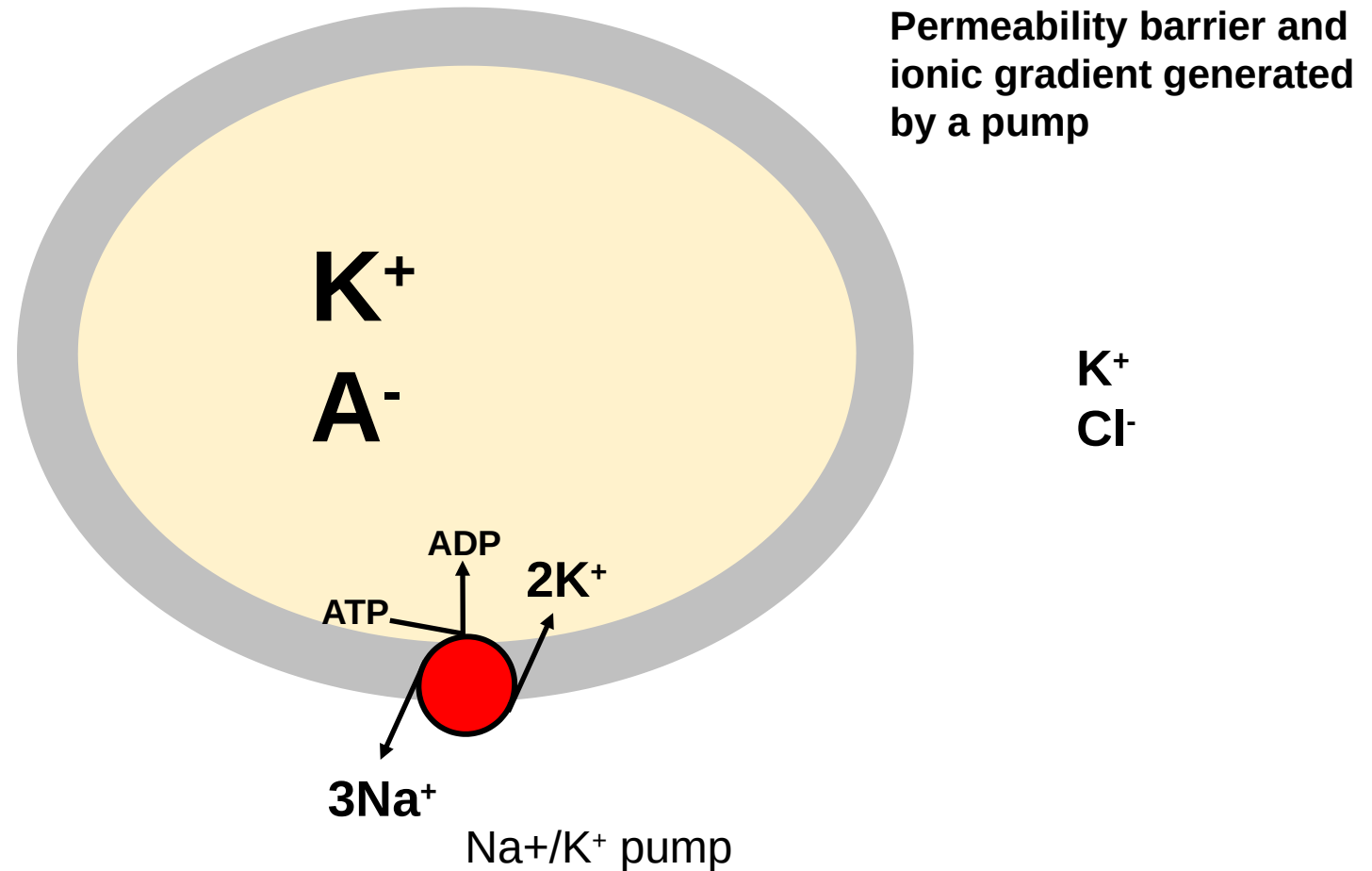
Work was done to separate the charges. Now there is a voltage across the insulator.*

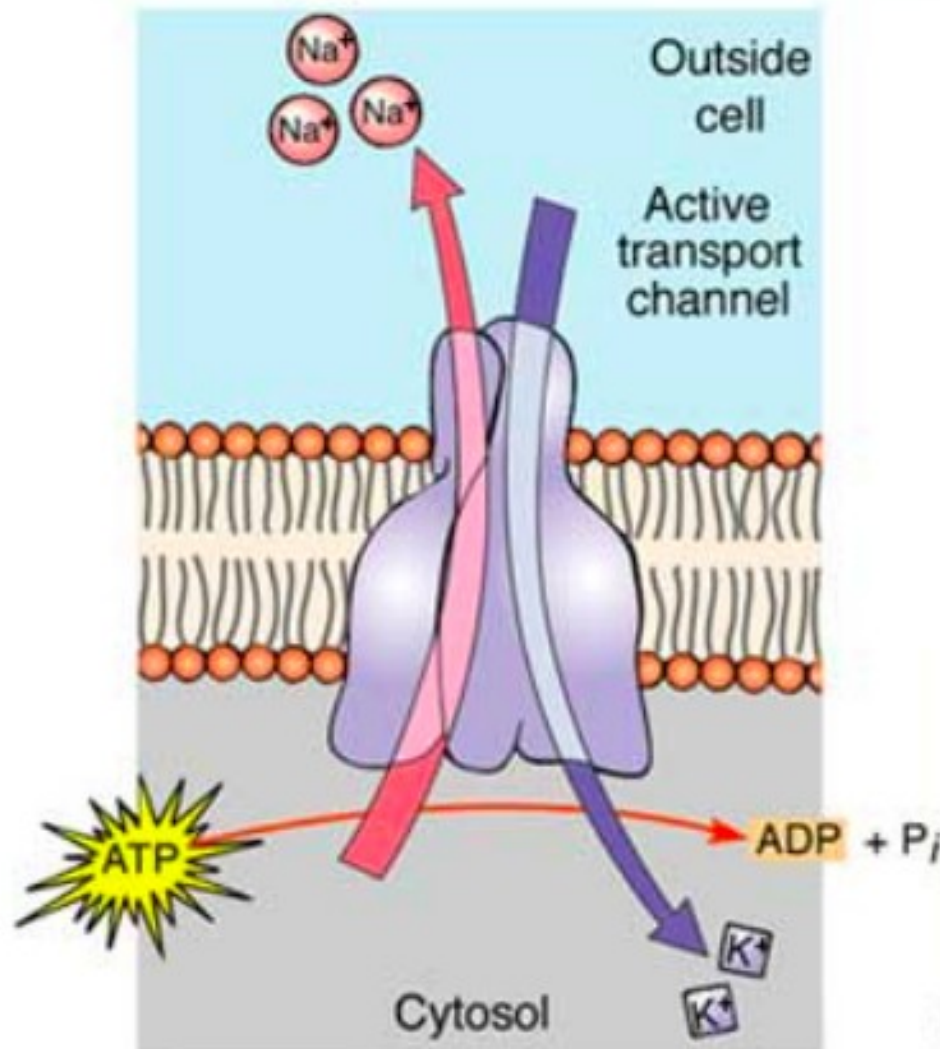
The insulator is “energized”

How is this done in biological cell membranes?

** 1 Volt = 1 Joule / 1 Coulomb*

Generation of the Membrane Potential (V_m)





<http://163.16.28.248/bio/activelearner/05/ch5c4.html>
Thomson Learning, Inc.

The sodium-potassium pump uses ATP to actively exchange extracellular K⁺ for intracellular Na⁺. (aka "Na-K ATPase")

3 Na⁺ ions are removed for every 2 K⁺ ions that are pumped into the cell.

This requires an enormous amount of energy in the brain (70% of all ATP → ADP).

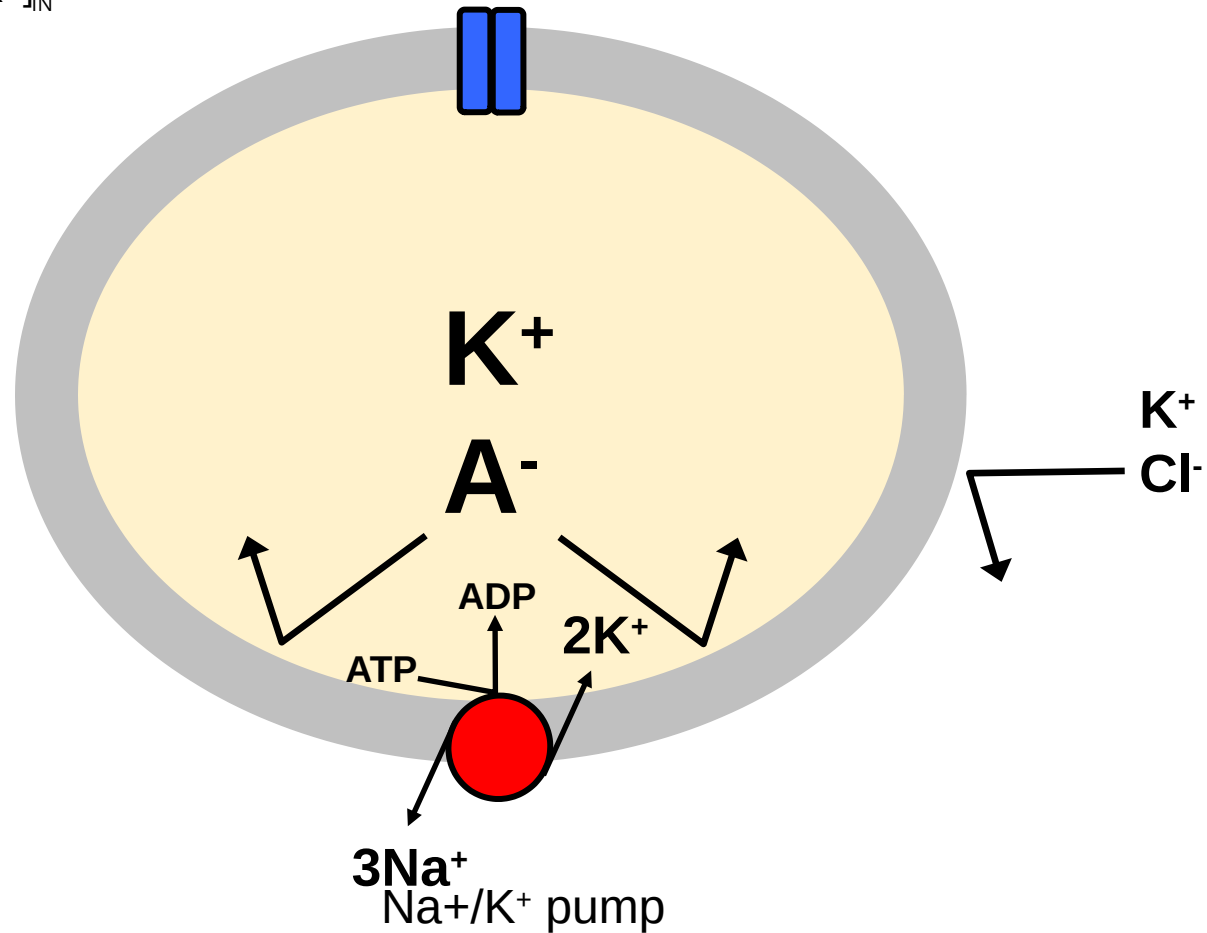
The pump is "electrogenic" - helping contribute to V_m (net 1⁺ out)


If the Na⁺/K⁺ pump stops working, a neuron slowly loses its concentration gradient, membrane potential, and dies.

K⁺– selective pore: 

$$\text{Diffusional work} = RT \ln \frac{[K^+]_{\text{OUT}}}{[K^+]_{\text{IN}}}$$

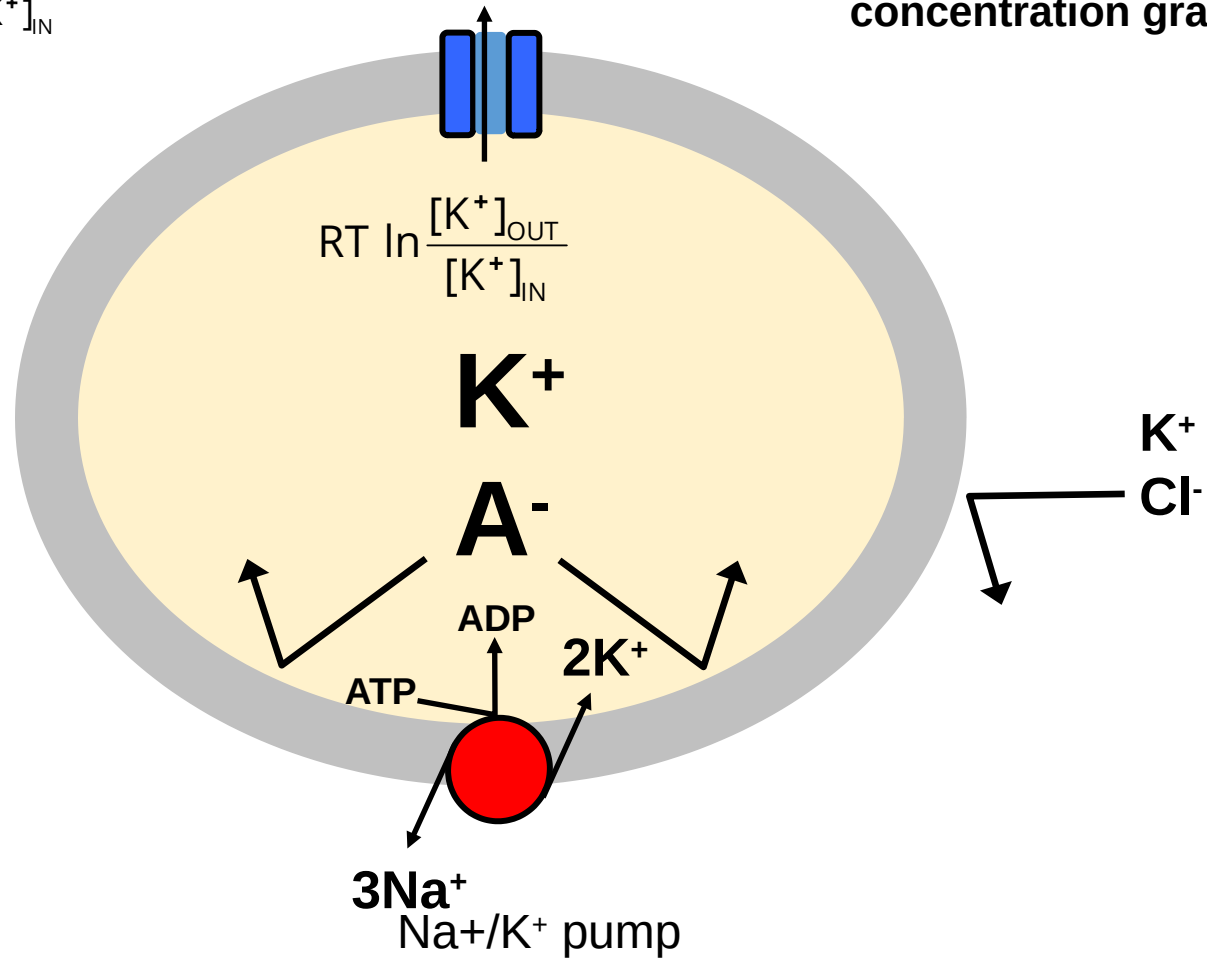
Membrane is doped with a
K⁺ –selective ion channel



K⁺– selective pore: 

$$\text{Diffusional work} = RT \ln \frac{[K^+]_{\text{OUT}}}{[K^+]_{\text{IN}}}$$

Once the K⁺ –selective ion channel opens, K⁺ starts diffusing down the concentration gradient

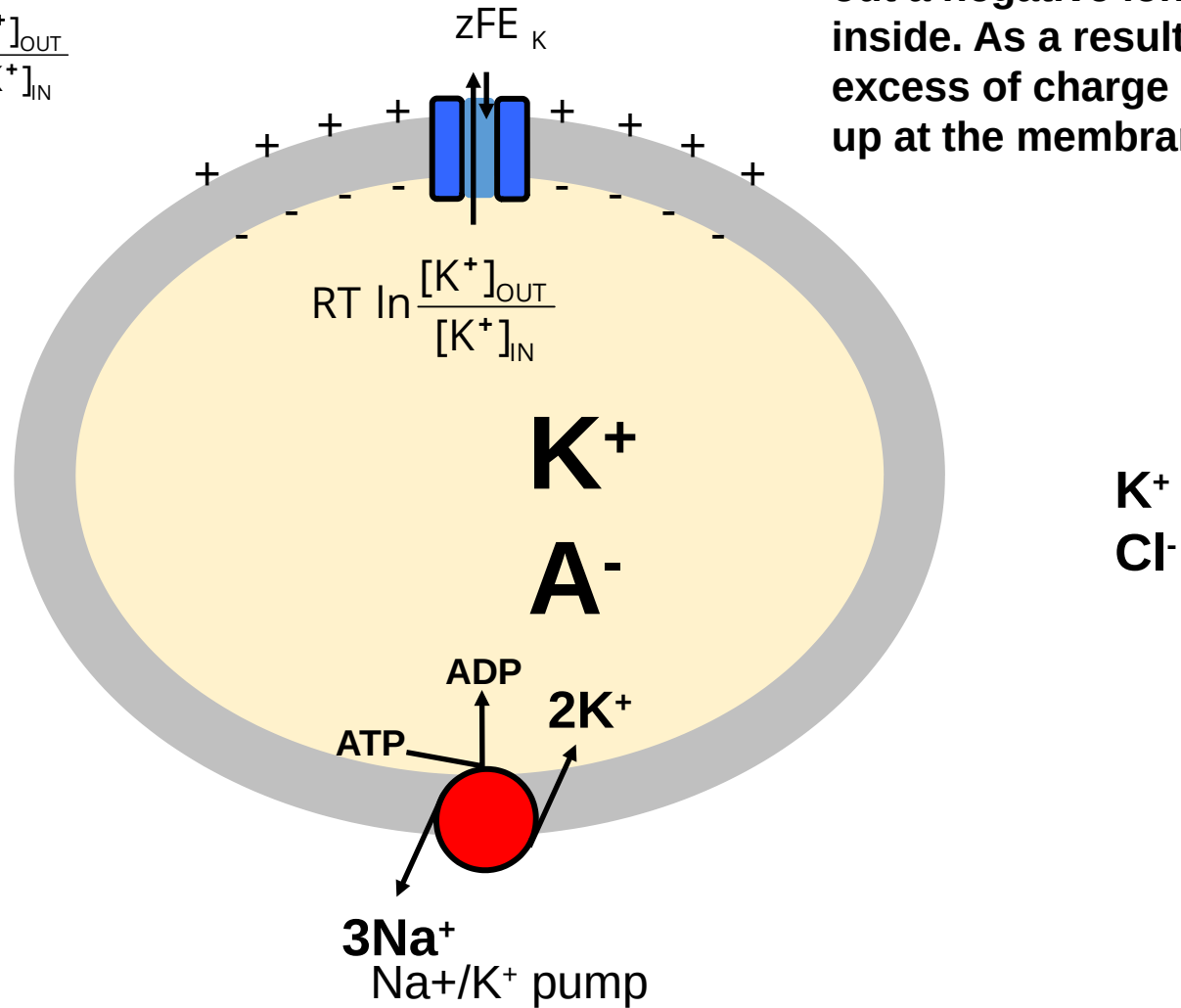


K⁺- selective pore: 

$$\text{Diffusional work} = RT \ln \frac{[K^+]_{\text{OUT}}}{[K^+]_{\text{IN}}}$$

$$\text{Electrical work} = zFE_K$$

For every K⁺ that moves out a negative ion is left inside. As a result an excess of charge builds up at the membrane

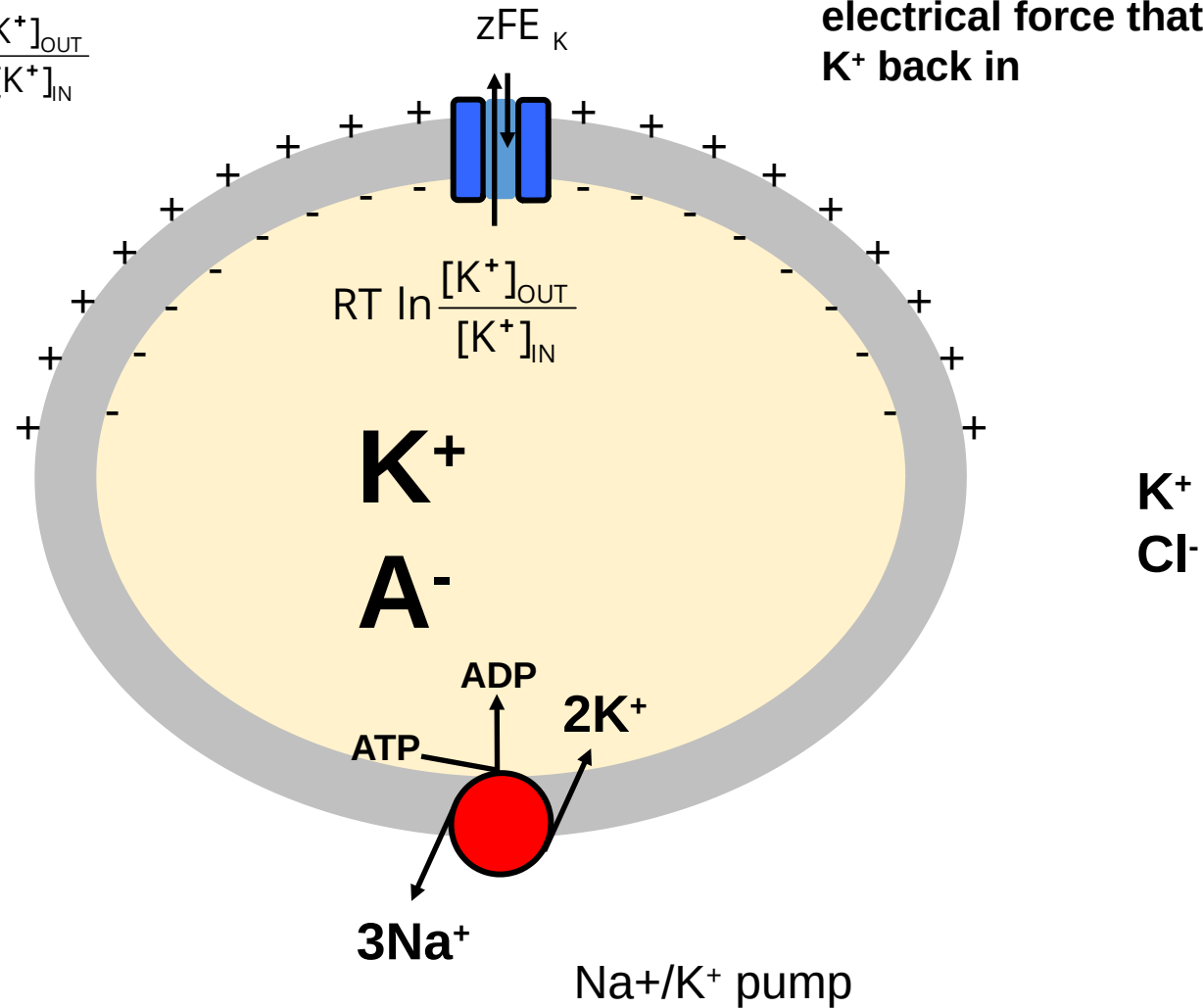



K⁺- selective pore: 

$$\text{Diffusional work} = RT \ln \frac{[K^+]_{\text{OUT}}}{[K^+]_{\text{IN}}}$$

$$\text{Electrical work} = zFE_K$$

The separation of charge at the membrane generates an electrical force that pushes K⁺ back in



K⁺- selective pore: 

$$\text{Diffusional work} = RT \ln \frac{[K^+]_{\text{OUT}}}{[K^+]_{\text{IN}}}$$

$$\text{Electrical work} = zFE_K$$

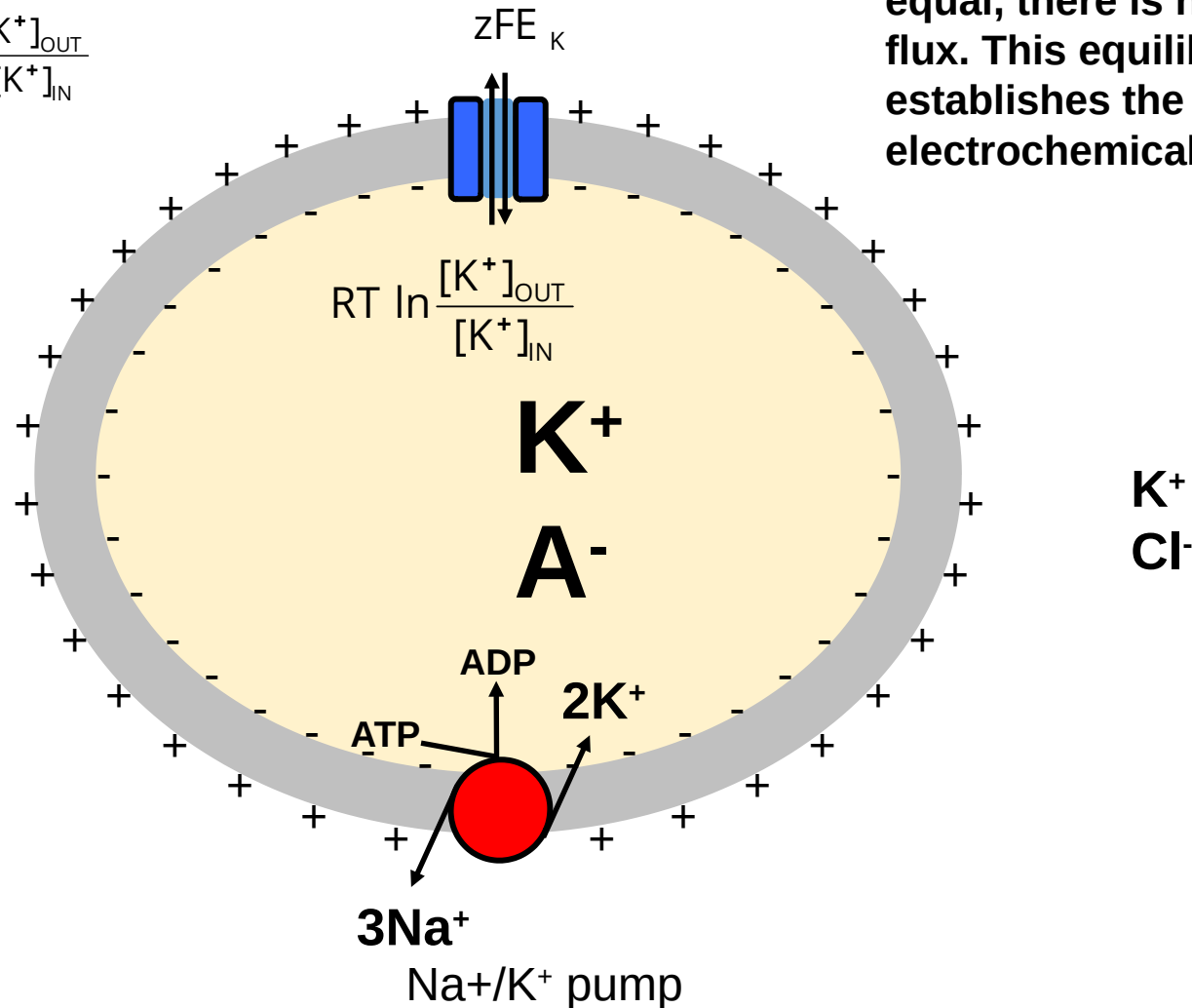
Equilibrium:

$$zFE_K = RT \ln \frac{[K^+]_{\text{OUT}}}{[K^+]_{\text{IN}}}$$

$$E_K = \frac{RT}{zF} \ln \frac{[K^+]_{\text{OUT}}}{[K^+]_{\text{IN}}}$$

The Nernst Eq.

When the electrical and diffusional forces are equal, there is not net K⁺ flux. This equilibrium establishes the electrochemical potential



Calculating Equilibrium Potentials

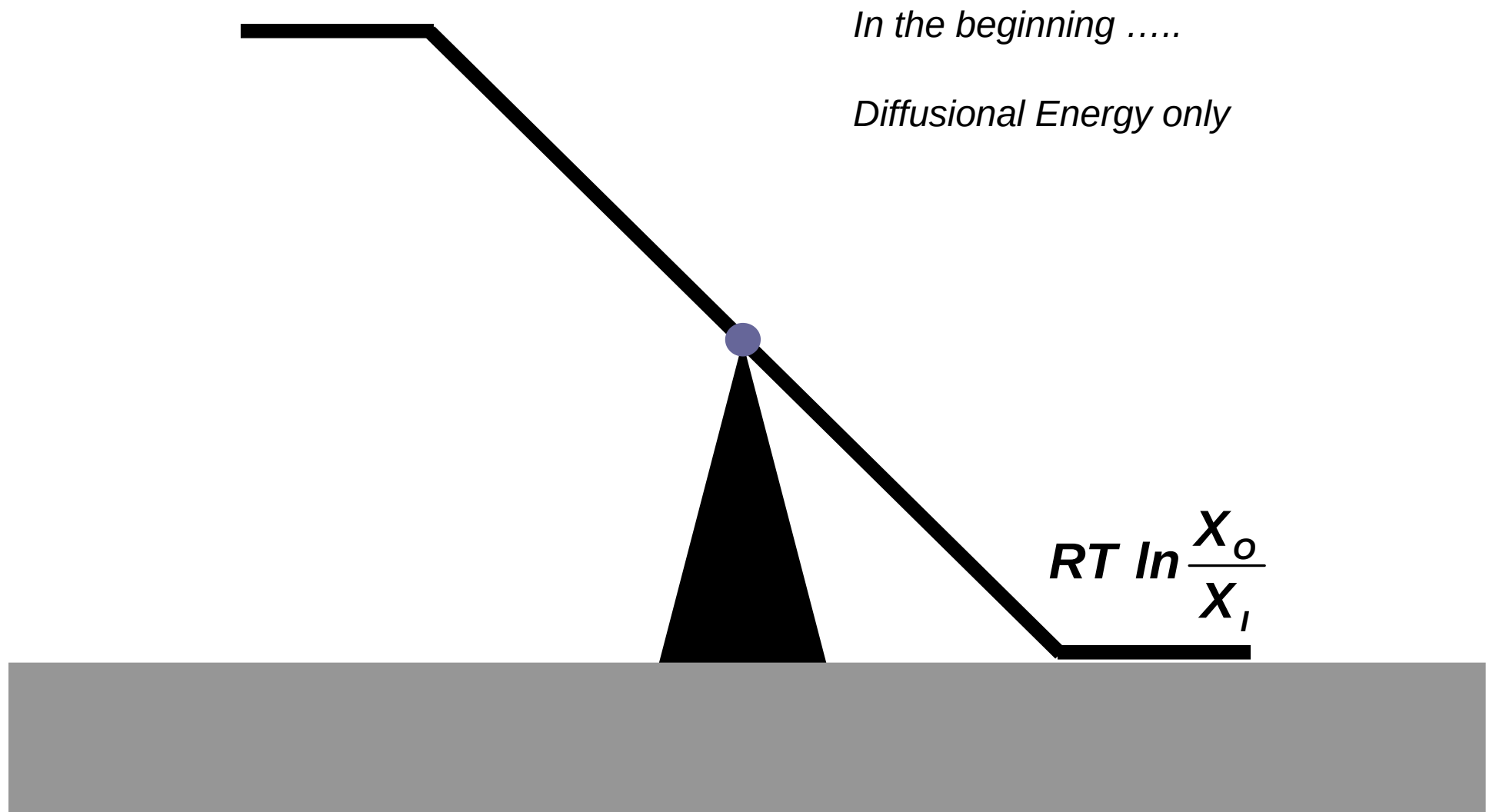
If a cell membrane is *preferentially* permeable to ion X, the Equilibrium Potential of ion X approximates V_m , and is calculated by applying the *Nernst Equation*:

$$E_X = \frac{RT}{zF} \ln \frac{[X]_{OUT}}{[X]_{IN}}$$

R = gas constant
T = abs. temperature
F = Faraday constant
z = valence of ion

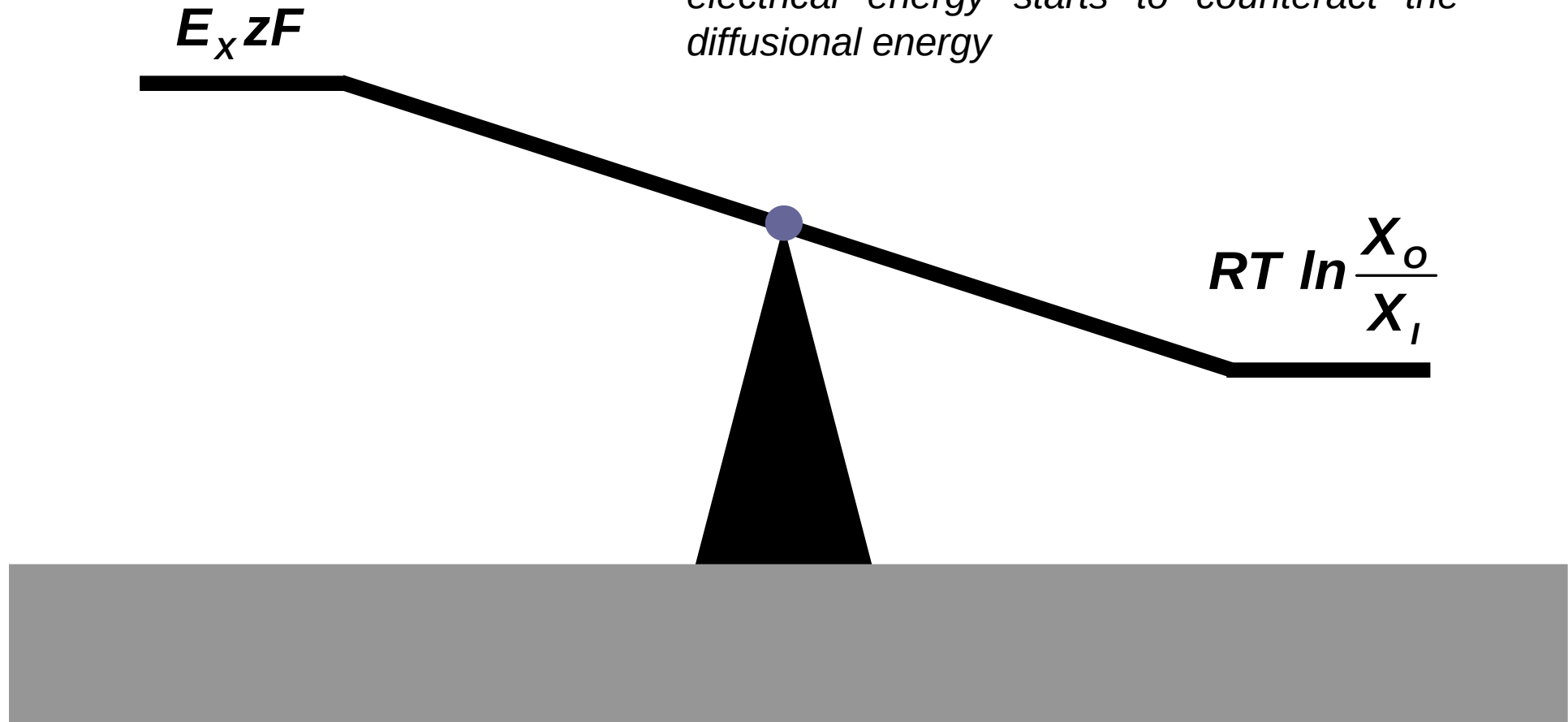
$$E_X = 2.303 \frac{RT}{zF} \log_{10} \frac{[X]_{OUT}}{[X]_{IN}} = 58 \log_{10} \frac{[X]_{OUT}}{[X]_{IN}} \quad \text{at } 22^\circ\text{C}$$

$$E_X = 62 \log_{10} \frac{[X]_{OUT}}{[X]_{IN}} \quad \text{at } 37^\circ\text{C}$$

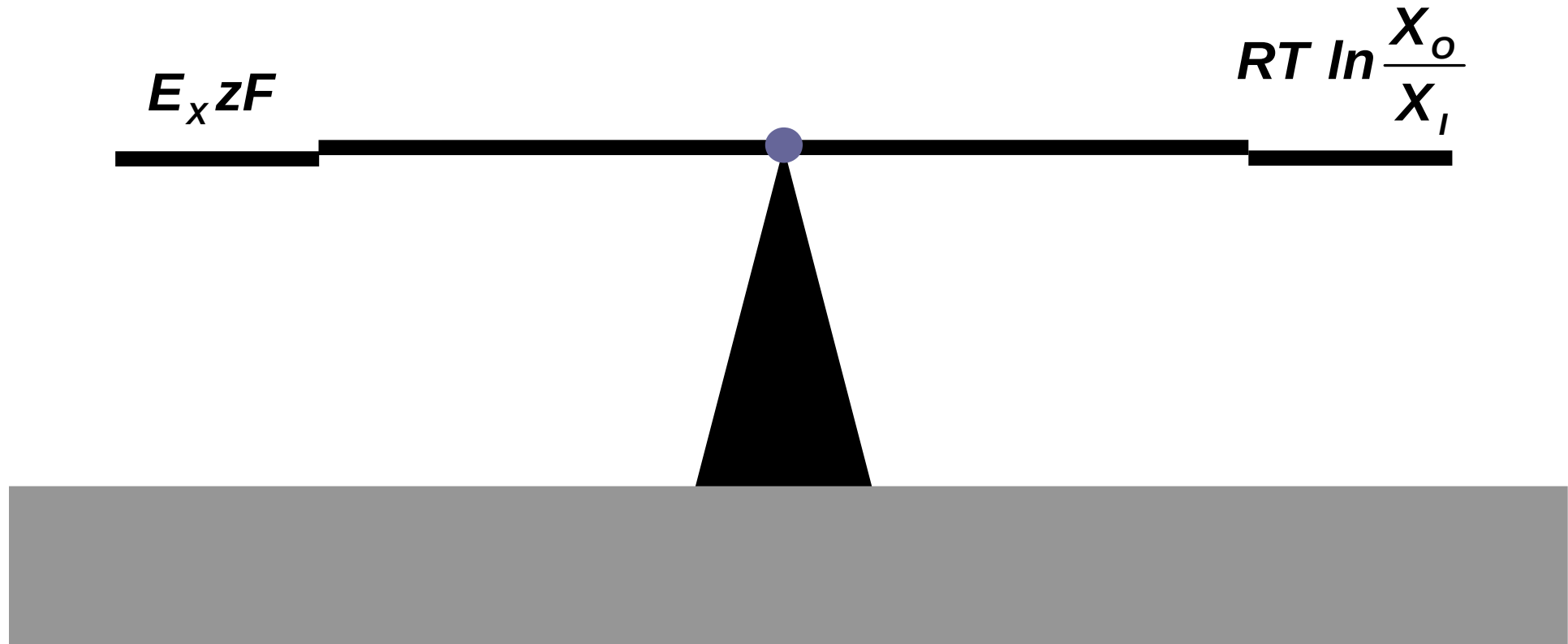


Separation of charge

Using the diffusional energy, ions flow down the concentration gradient through ion-selective channels and the separation of charge across the membrane begins. Thus, electrical energy starts to counteract the diffusional energy



When the tendency of ions to flow down the concentration gradient (diffusional energy) is exactly balanced by the tendency of ions to flow back under the influence of an electrical potential (electrical energy), the system has reach an electrochemical equilibrium



Calculating Equilibrium Potentials

If a cell membrane is *preferentially* permeable to ion X, the Equilibrium Potential of ion X approximates V_m , and is calculated by applying the *Nernst Equation*:

$$E_X = \frac{RT}{zF} \ln \frac{[X]_{OUT}}{[X]_{IN}}$$

R = gas constant

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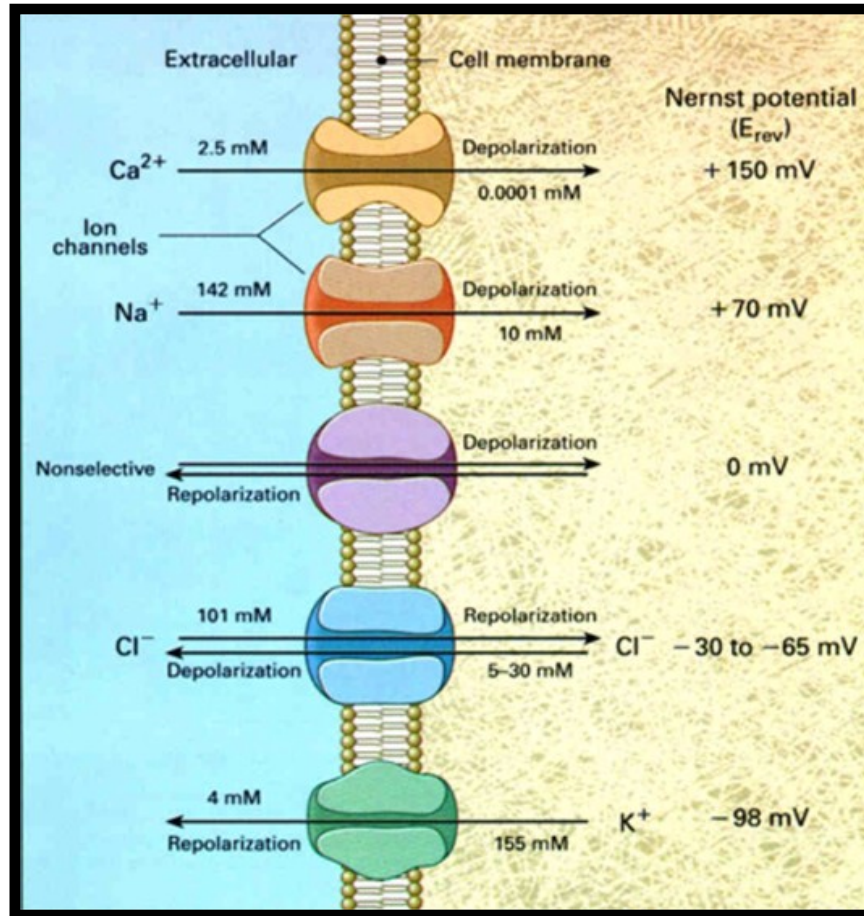
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$$E_X = 62 \log_{10} \frac{[X]_{OUT}}{[X]_{IN}} \quad \text{at } 37^\circ\text{C}$$

Applications of the Nernst Equation

if only one ion-selective channel is open at a given time,
the Nernst Equation can calculate the V_m of a cell



Sodium:

$$E_{Na} = 58 [\log (142 / 10)] = +66 \text{ mV}$$

Potassium:

$$E_K = 58 [\log (4 / 155)] = -91 \text{ mV}$$

Chloride:

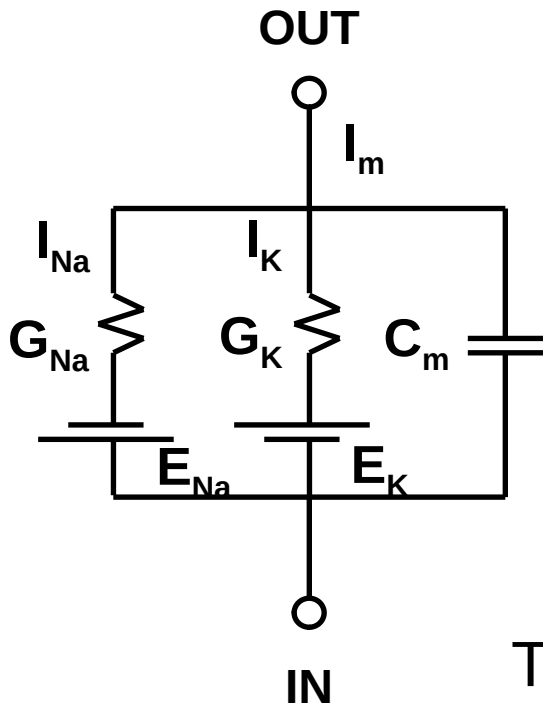
$$E_{Cl} = 58 [\log (30 / 101)] = -30 \text{ mV}$$

Calcium:

$$E_{Ca} = 29 [\log (2.5 / 0.0001)] = +127 \text{ mV}$$

Calculating the Membrane Potential

a more realistic scenario- Multiple ions involved



Steady-state: $I_m = I_{Na} + I_K = 0$. Then, applying Ohm's Law it is easy to show that:

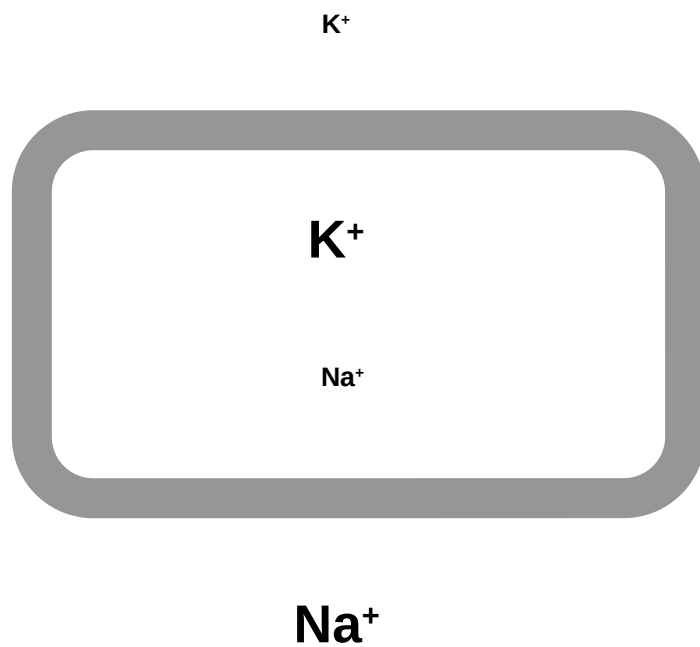
$$V_m = E_{Na} (G_{Na}/G_m) + E_K (G_K/G_m)$$

where the total conductance is

$$G_m = G_{Na} + G_K$$

Thus, V_m is the *weighted average* of the E_x

Three-branch Model

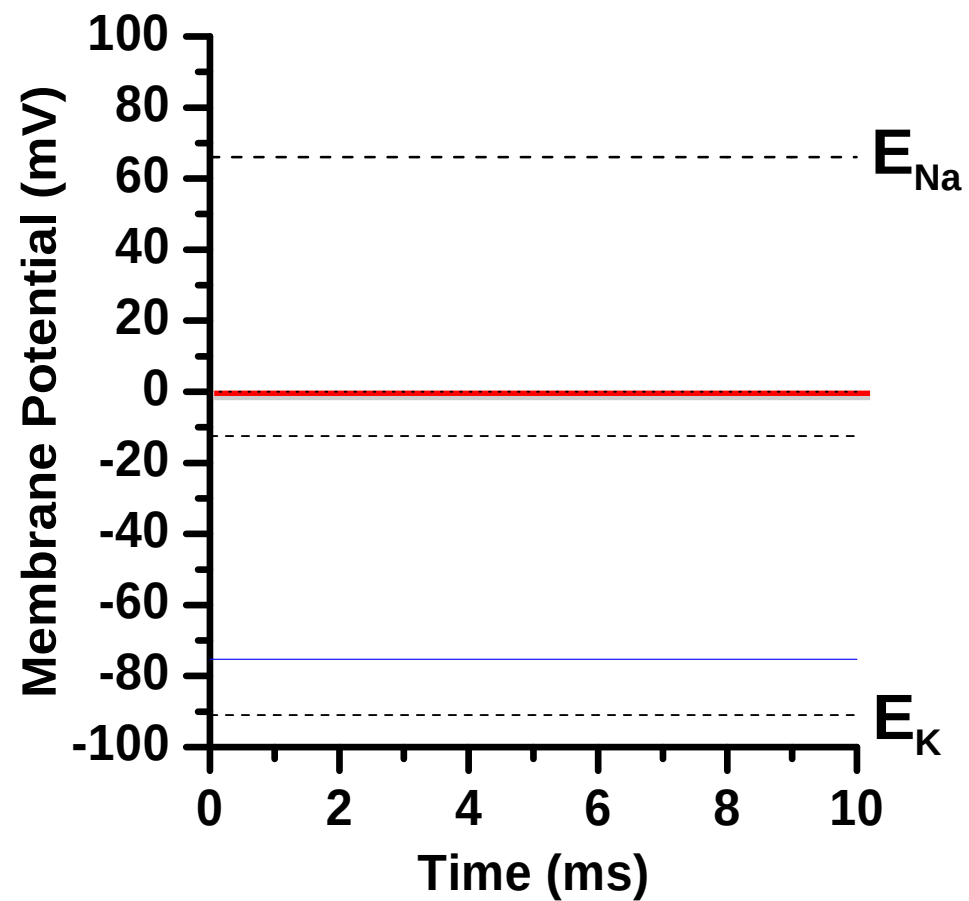


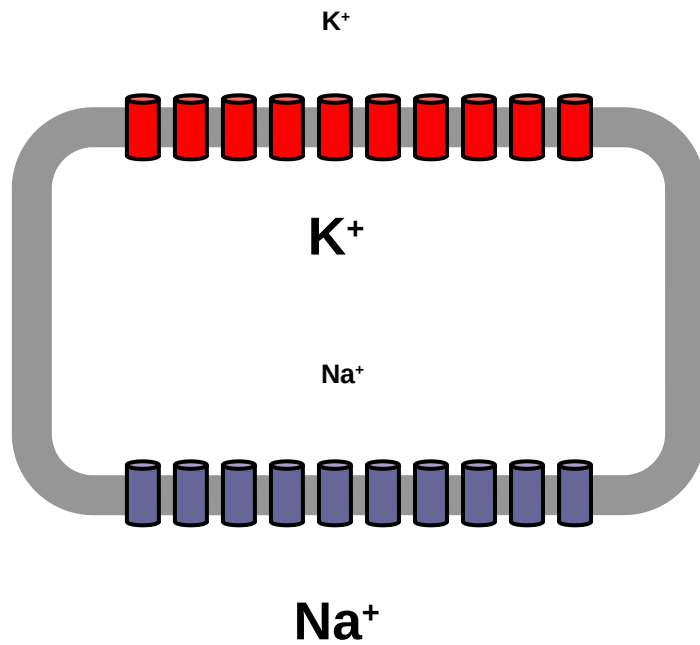
No ion channels

$$V_m = E_{Na} (G_{Na}/G_m) + E_K (G_K/G_m)$$

$$G_{Na}/G_m = 0 \quad G_K/G_m = 0$$

$$V_m = 0 \text{ mV}$$





ion channels are closed



K^+ channel



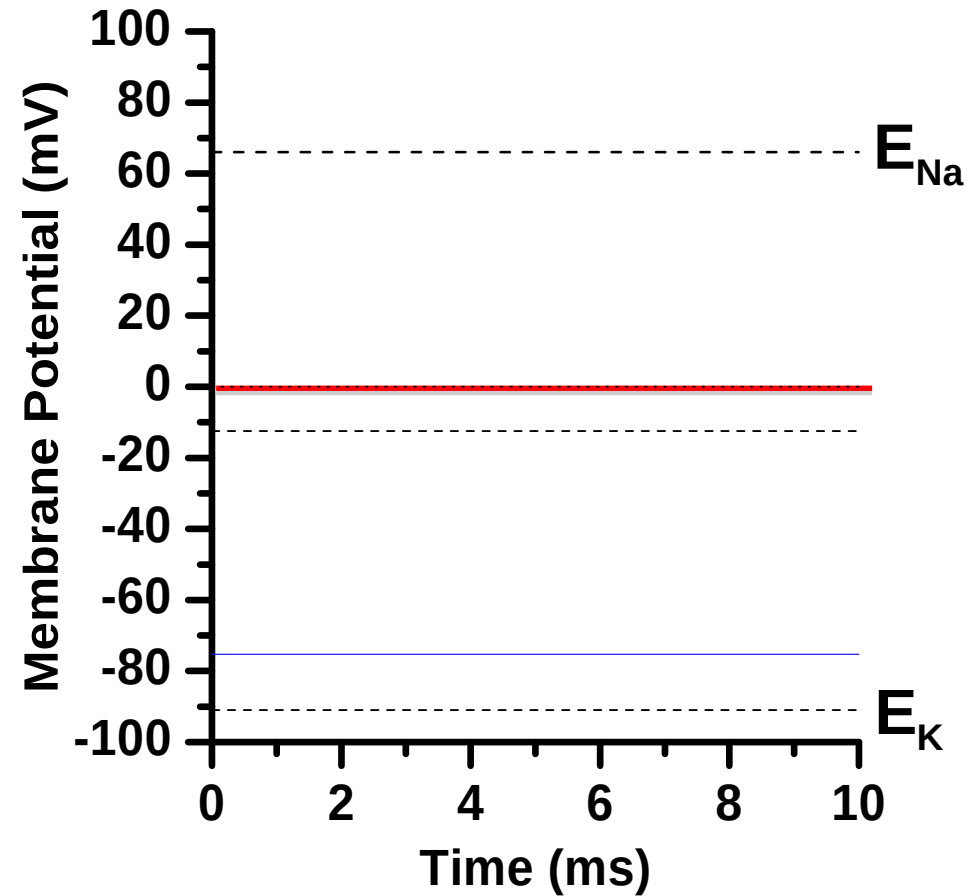
Na^+ channel

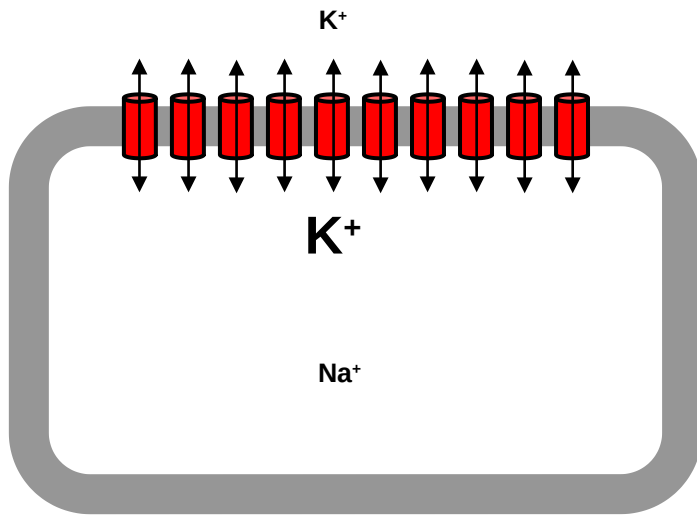
$G_x \propto \# \text{ open channels}$

$$V_m = E_{Na} (G_{Na}/G_m) + E_K (G_K/G_m)$$

$$G_{Na}/G_m = 0 \quad G_K/G_m = 0$$

$$V_m = 0 \text{ mV}$$





Na⁺

K⁺ channels are open



K⁺ channel



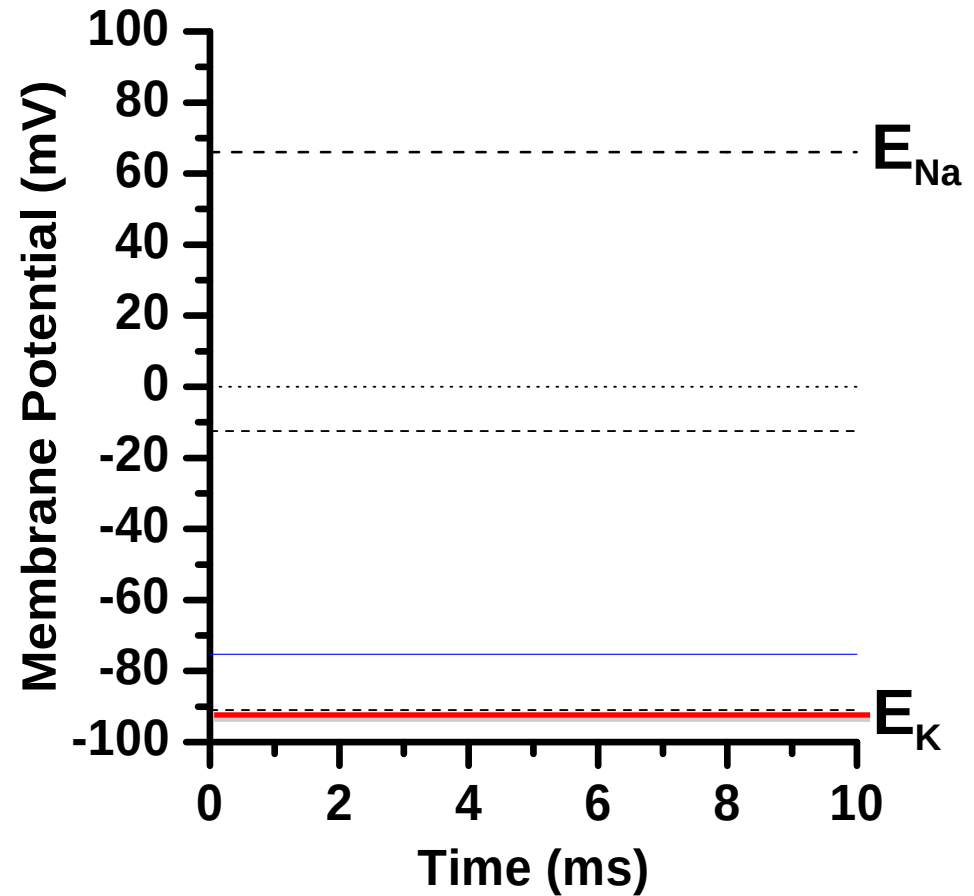
Na⁺ channel

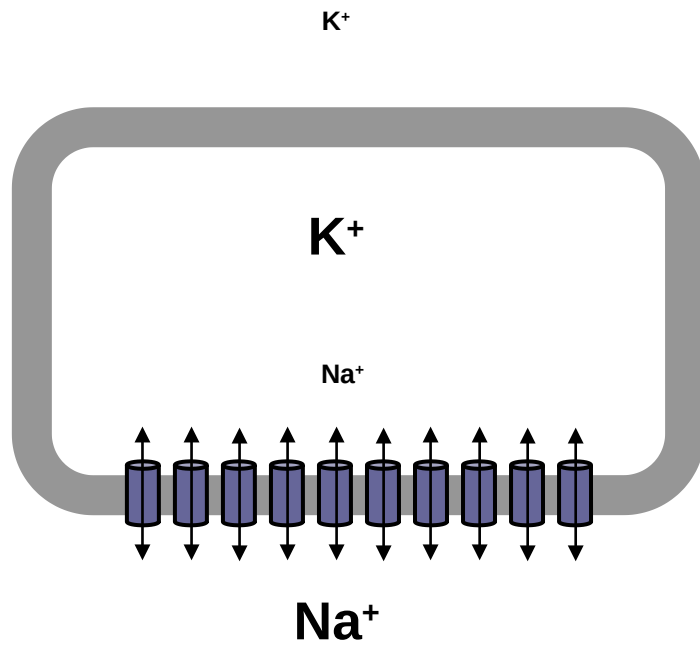
$G_x \propto \# \text{ open channels}$

$$V_m = E_{\text{Na}} (G_{\text{Na}}/G_m) + E_{\text{K}} (G_{\text{K}}/G_m)$$

$$G_{\text{Na}}/G_m = 0 \quad G_{\text{K}}/G_m = 1$$

$$V_m = (+66)(0) + (-91)(1) = -91 \text{ mV}$$





Na^+ channels are open



K^+ channel



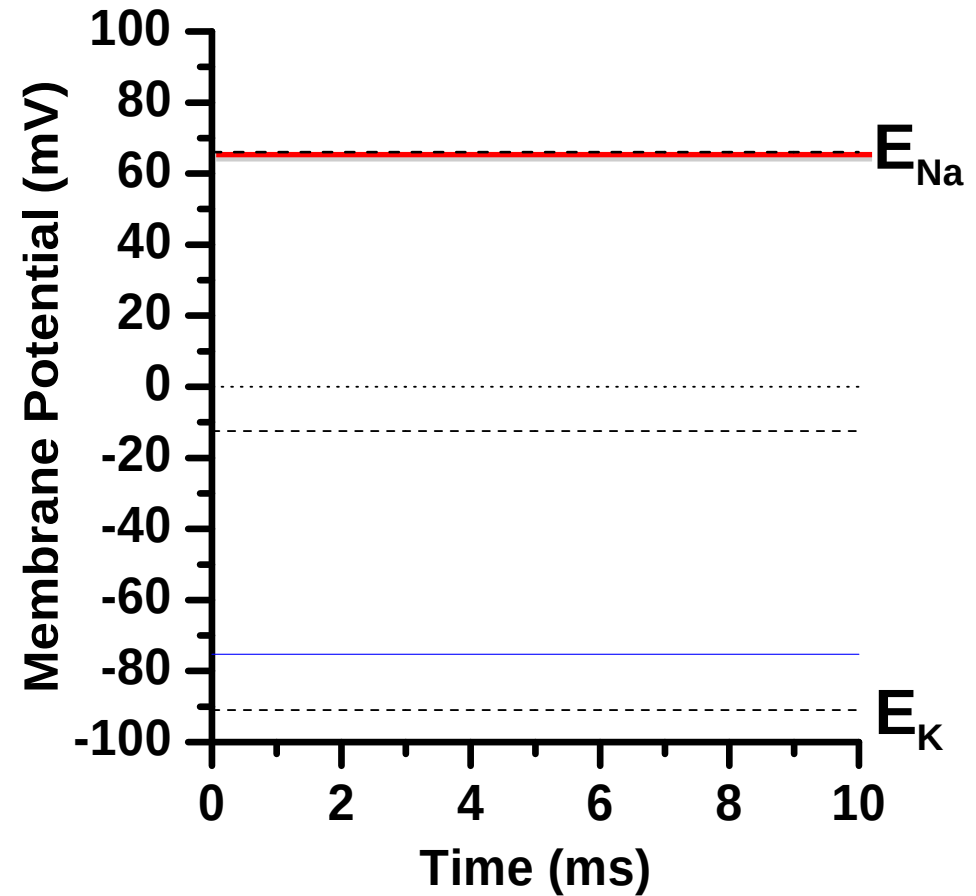
Na^+ channel

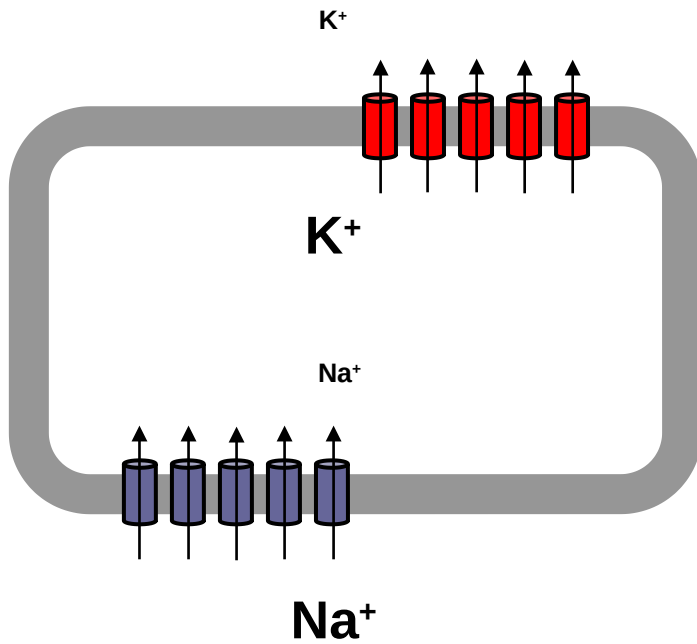
$G_x \propto \# \text{ open channels}$

$$V_m = E_{Na} (G_{Na}/G_m) + E_K (G_K/G_m)$$

$$G_{Na}/G_m = 1 \quad G_K/G_m = 0$$

$$V_m = (+66)(1) + (-91)(0) = +66 \text{ mV}$$





Na^+ & K^+ channels are open



K^+ channel



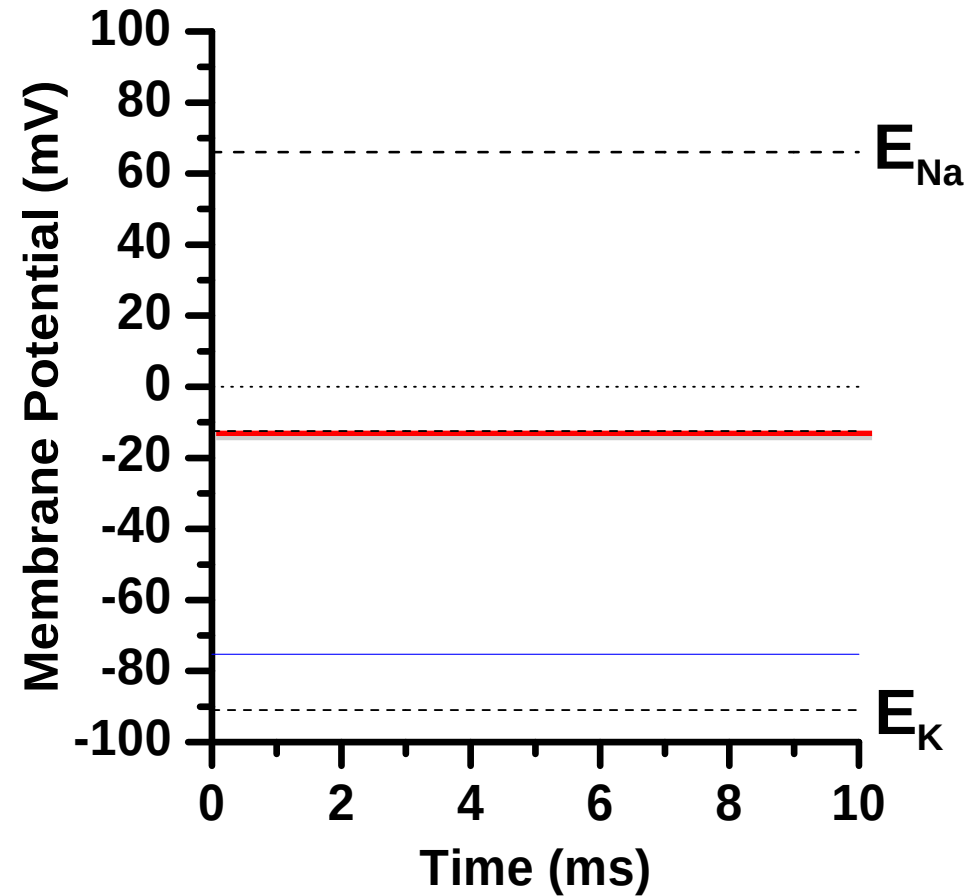
Na^+ channel

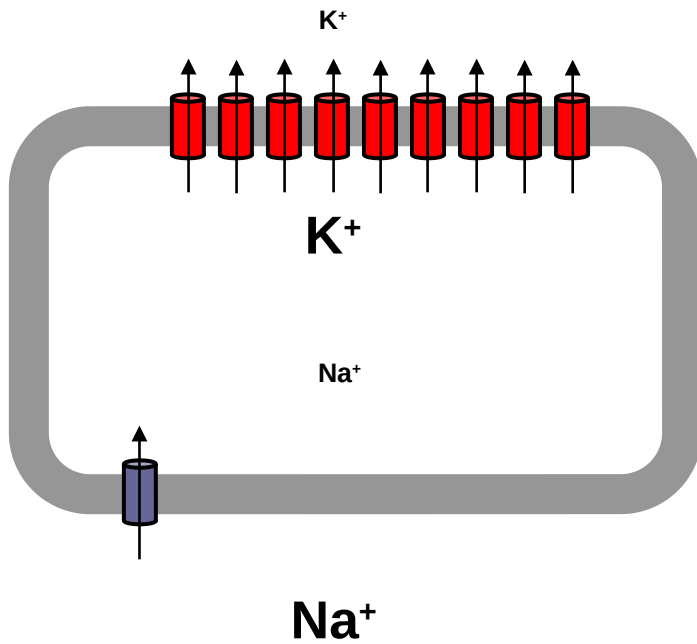
$G_x \propto \# \text{ open channels}$

$$V_m = E_{Na} (G_{Na}/G_m) + E_K (G_K/G_m)$$

$$G_{Na}/G_m = 0.5 \quad G_K/G_m = 0.5$$

$$V_m = (E_{Na} + E_K) / 2 = -12.5 \text{ mV}$$





Na^+ & K^+ channels are open



K^+ channel



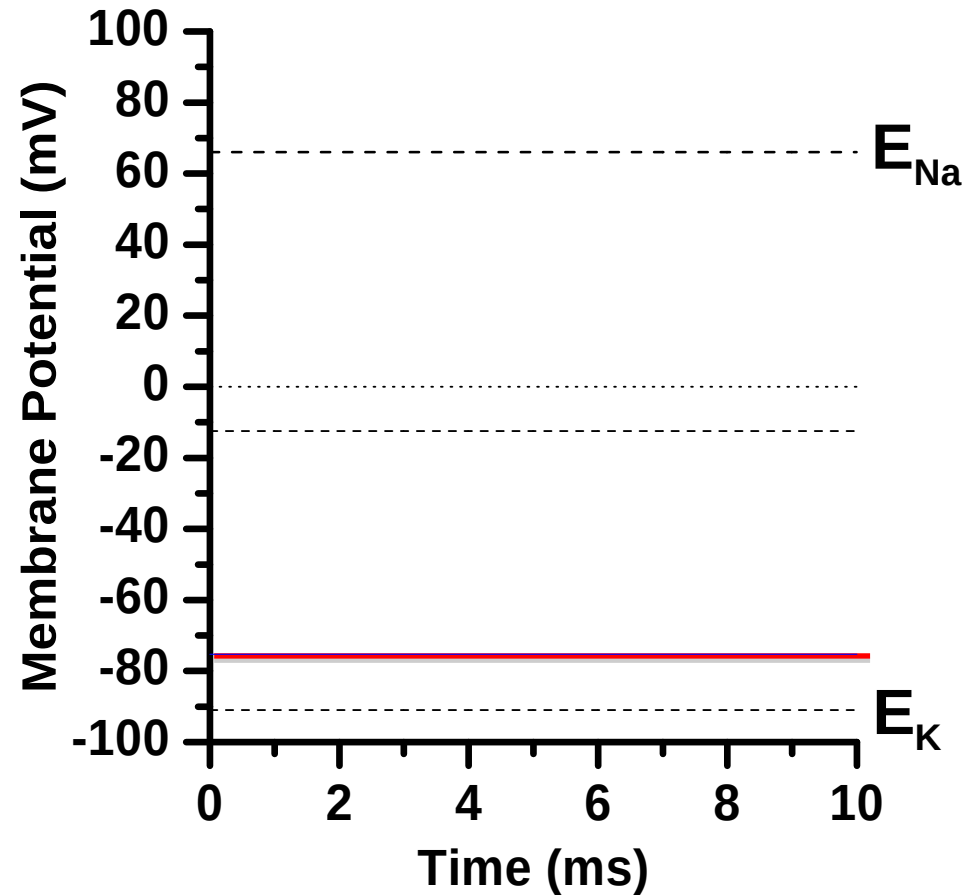
Na^+ channel

$G_x \propto \# \text{ open channels}$

$$V_m = E_{Na} (G_{Na}/G_m) + E_K (G_K/G_m)$$

$$G_{Na}/G_m = 0.1 \quad G_K/G_m = 0.9$$

$$V_m = (+66)(0.1) + (-91)(0.9) = -75.3 \text{ mV}$$



Calculating the Membrane Potential

another method

The Goldman-Hodgkin-Katz (GHK)
Equation

$$V_m = 62 \log_{10} \left(\frac{P_{Na} [Na^+]_{OUT} + P_K [K^+]_{OUT}}{P_{Na} [Na^+]_{IN} + P_K [K^+]_{IN}} \right)$$

$$P_x = \text{relative permeability} = P_x / P_K$$

The Goldman-Hodgkin-Katz Equation

$$V_m = \frac{RT}{F} \ln \left(\frac{P_{Na^+}[Na^+]_{out} + P_{K^+}[K^+]_{out} + P_{Cl^-}[Cl^-]_{in}}{P_{Na^+}[Na^+]_{in} + P_{K^+}[K^+]_{in} + P_{Cl^-}[Cl^-]_{out}} \right)$$

Where:

V_m = membrane potential at steady state

P = permeability

Please note the
solid line

R = gas constant = 8.314 J/Kmol

T = absolute temperature in kelvin = $^{\circ}\text{C} + 273$

z = valence of the ion

F = Faraday constant = 96,485 C/mol

$$\frac{RT}{F} \text{ at } 37^{\circ}\text{C} = 0.0267 \text{ V} = 26.7 \text{ mV}$$

Permeability

Can be thought of as the number of open ion channels.

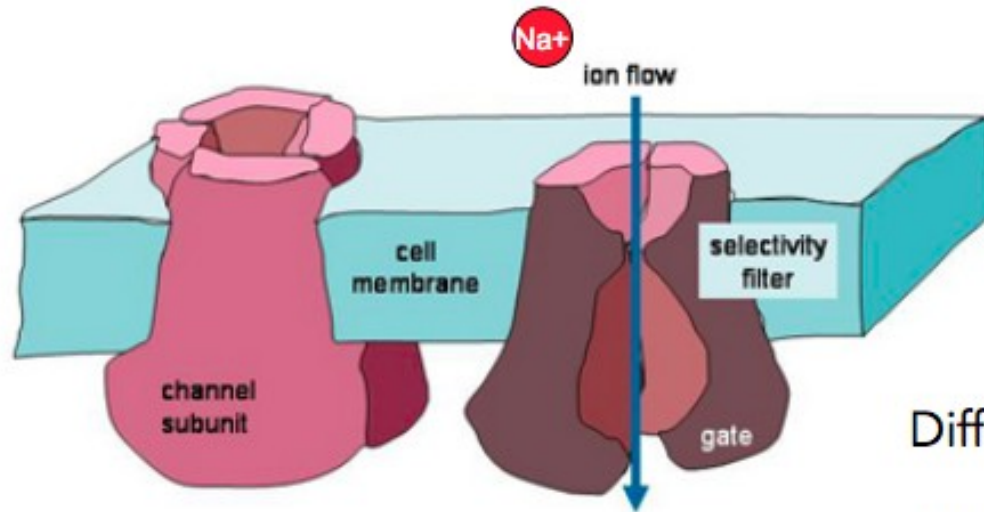
To simplify for GHK, P is usually written as a ratio, for example:

$$P_{\text{Na}^+}:P_{\text{K}^+}:P_{\text{Cl}^-} = \sim 1:100:10$$

Now that we have learned how to measure the equilibrium potential (E) for individual ions and V_m when multiple ionic conductances are present we must learn about the proteins that make this possible:

Ion Channels

Charge moving over time = current



Difference in voltage is a potential

Movement of charge = current (I)
(eg. across voltage separation)

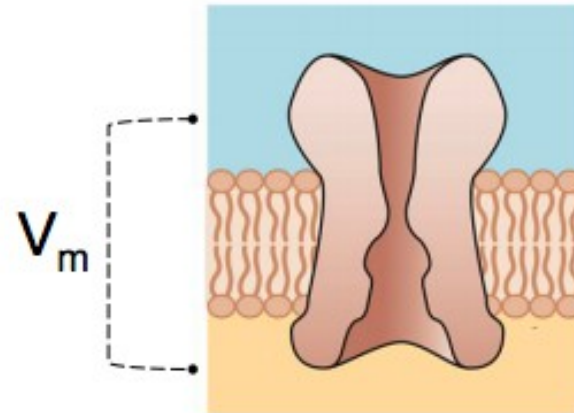
Current is abbreviated " I "
and is measured in amps

(Usually nA or pA for
neurons)

Units: Charge/time = current

Coulombs/sec = amperes

Think of a battery



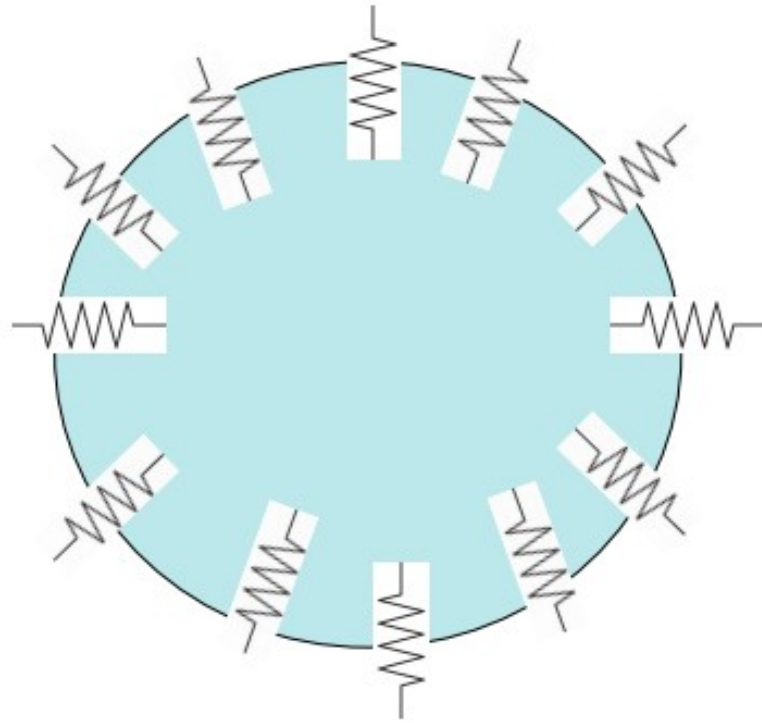
Current follows the path of least resistance



Colourbox.com



In a three dimensional cell with many channels, many resistors combine to make up the overall “membrane resistance”



Because there is a simple way to relate voltage to current, neuronal recordings can easily monitor either

Voltage difference across the membrane
OR
Current flow across the membrane

$$\Delta V = IR$$

Voltage = Current x Resistance

How can we describe this process mathematically???

$$\Delta V = IR$$

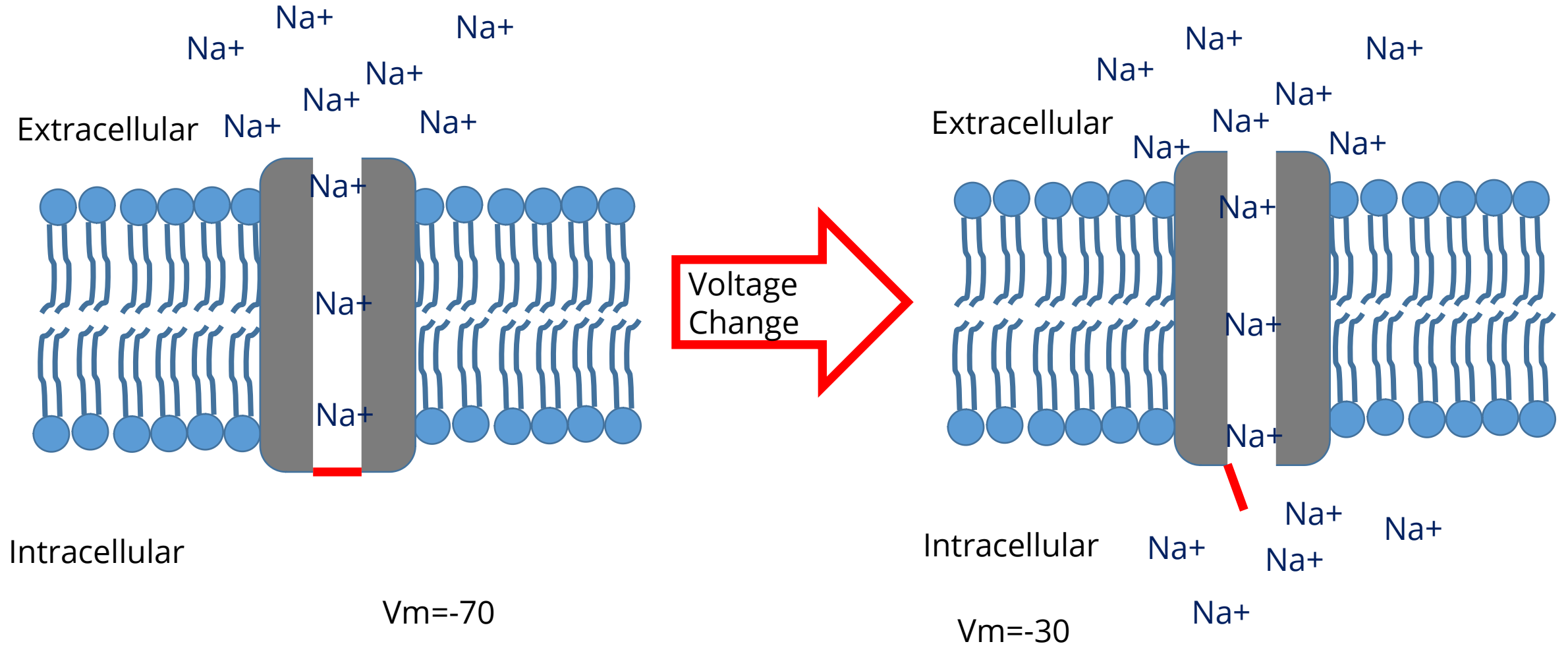
$$\Delta V = (V_m - E_{ion}) = \text{Driving Force}$$

Current in the form of moving ions (charged) through a resistor (permeation pore) across a voltage (V_m) is described by Ohm's Law.

$V = IR$ $R = 1/G$
 $R = \text{Resistance}$
 $G = \text{Conductance}$

- Not all channels are leak channels (always “open”)
- Some channels have GATES that keep them closed in the ABSENCE of a stimulus
- Three major groups of gated channels in neurons are 1) Voltage gated, 2) Ligand (chemically) gated, 3) and Mechanically gated ion channels

Voltage gated ion channels

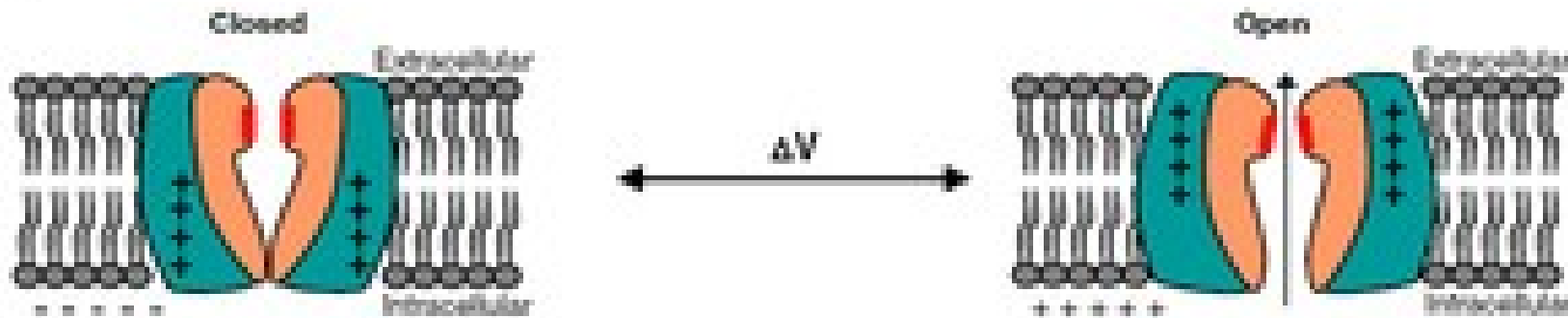


How do voltage gated channels gate??

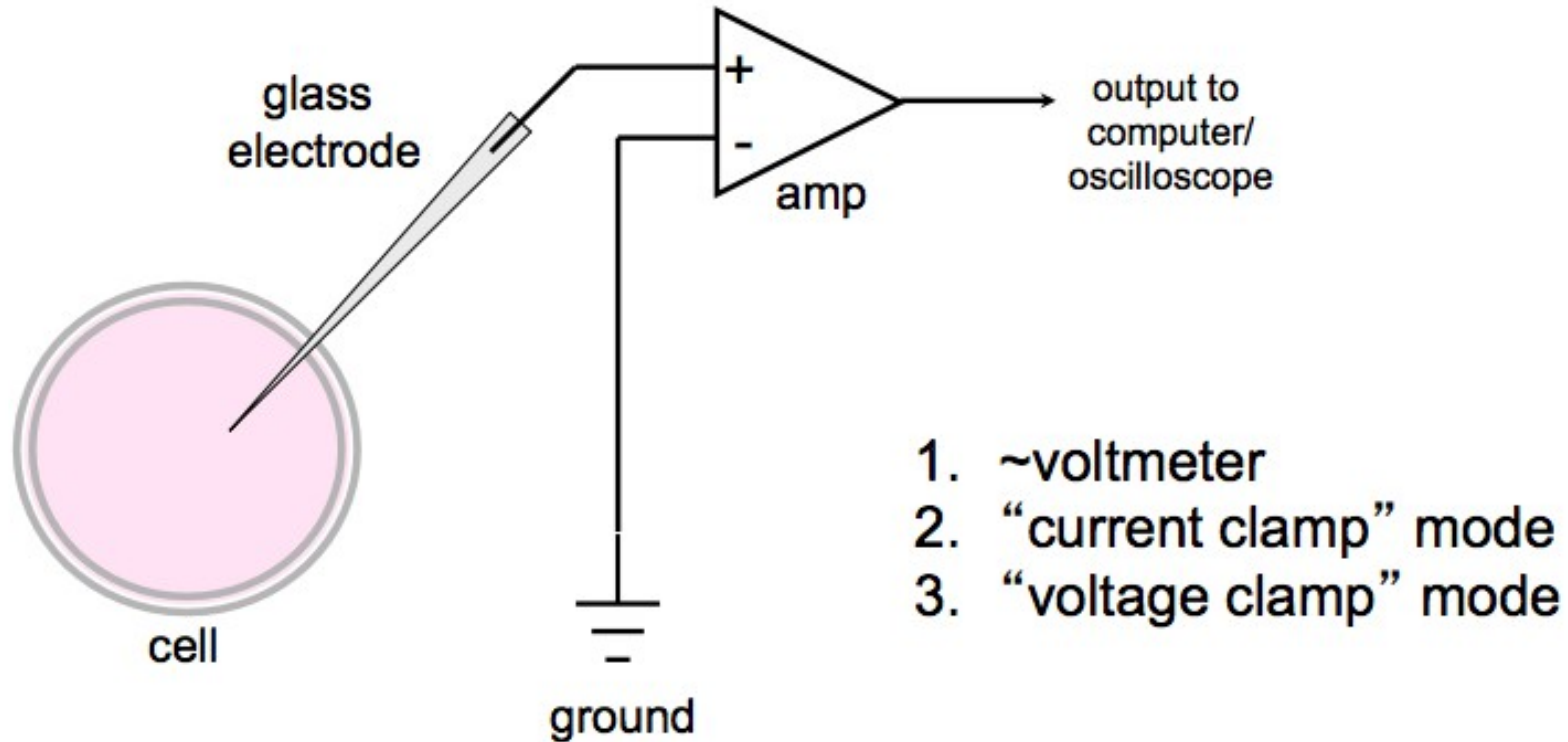
Although this differs among different classes of voltage gated ion channels (K^+ , Na^+ , Ca^{2+}), there are many more similarities.

A change in voltage across a membrane moves parts of ion channels containing charged amino

- A net positive change on the inner leaflet of the plasma membrane induces an electrostatic repulsion of positively charged amino acids on the channel.
- This induces a conformational change of the tetramer that opens the “activation gate” and allows ions to flow.



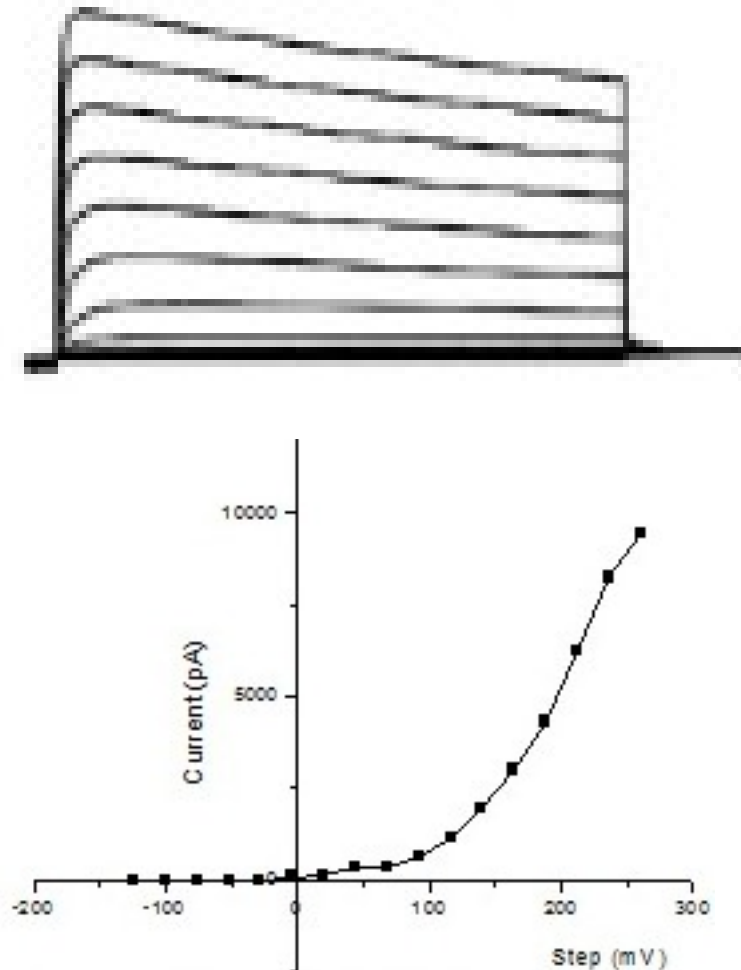
Different methods for recording from cells



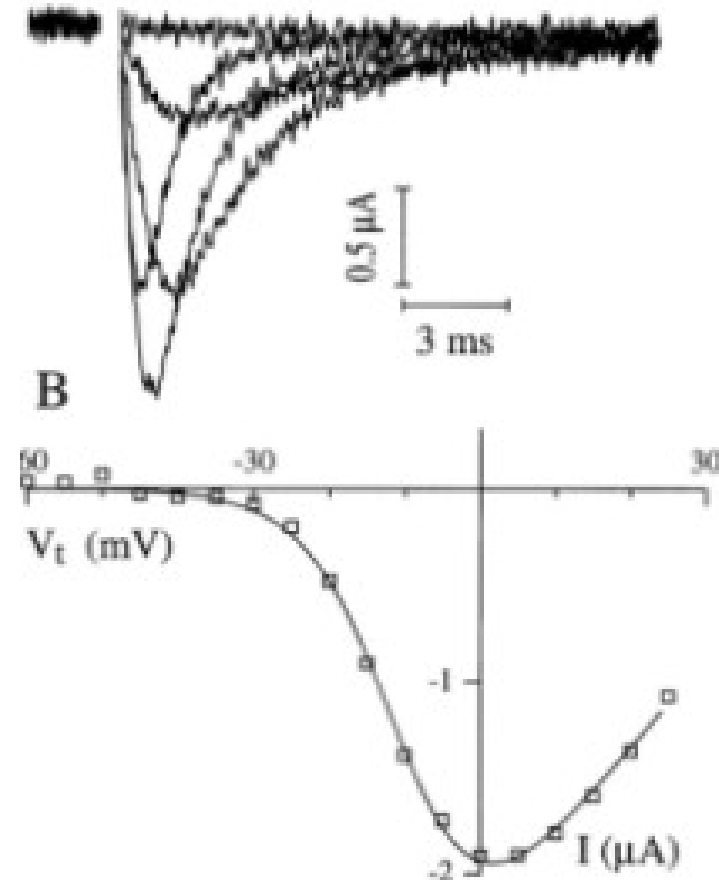
Terminology
current clamp
voltage clamp

What do typical voltage gated Na^+ (Nav) and K^+ (Kv) currents look like at in voltage clamp?

- Kv



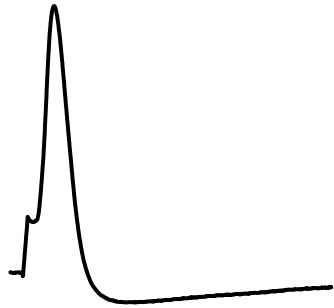
- Nav



Lets take a break- 10 min

What do different action potentials look like in current clamp?

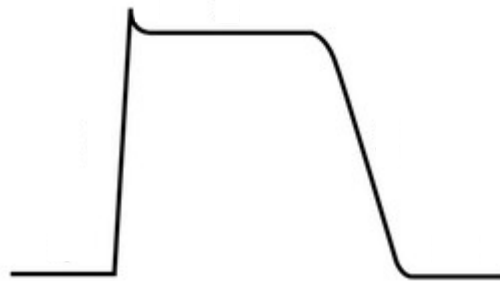
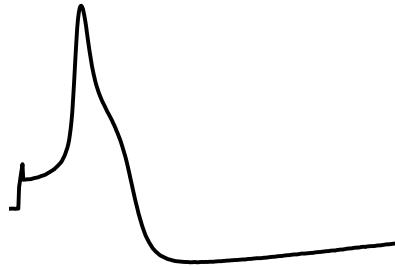
Spinal Cord – Dorsal Horn



Squid Giant Axon



Dorsal Root Ganglion



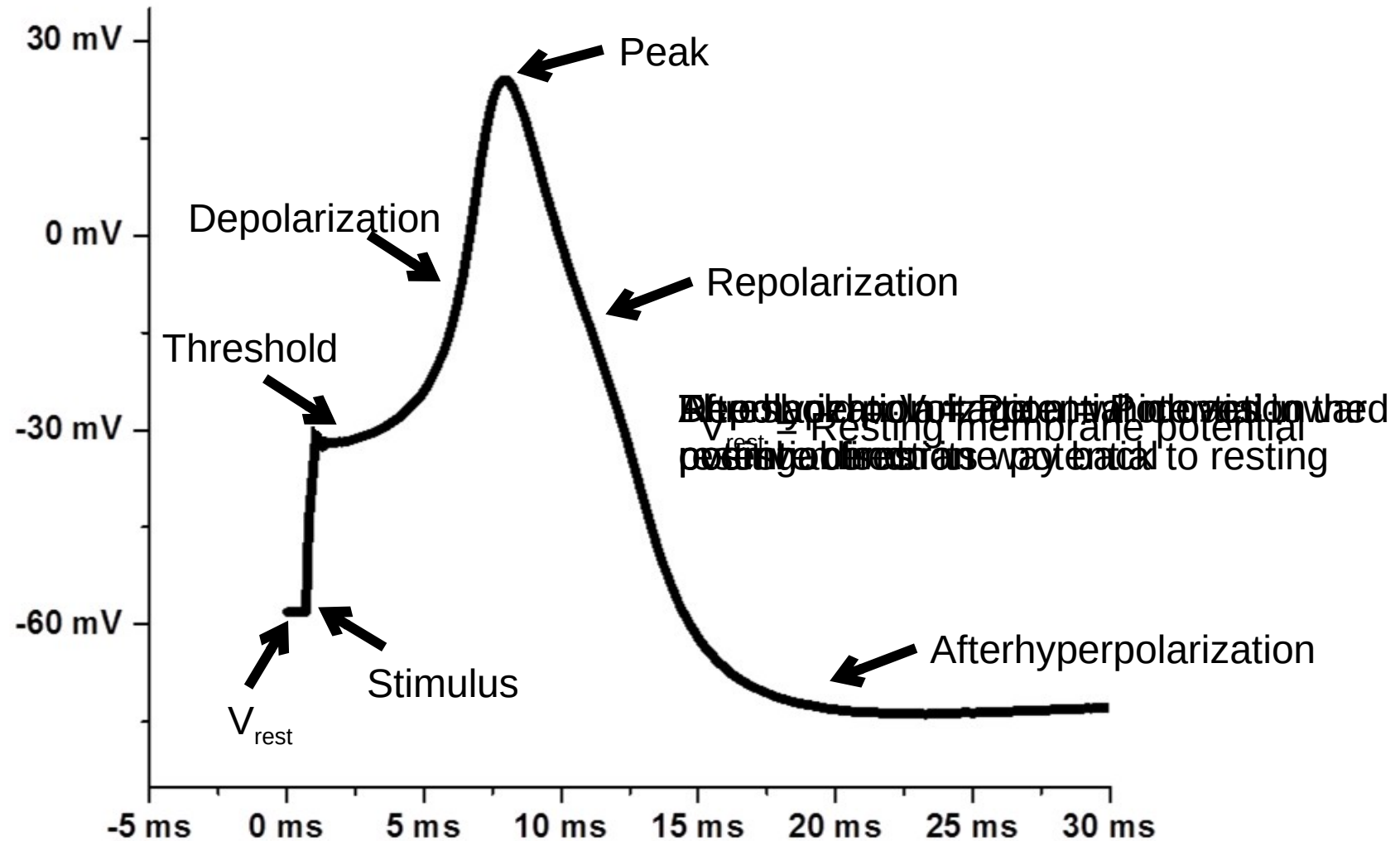
Cardiac Muscle



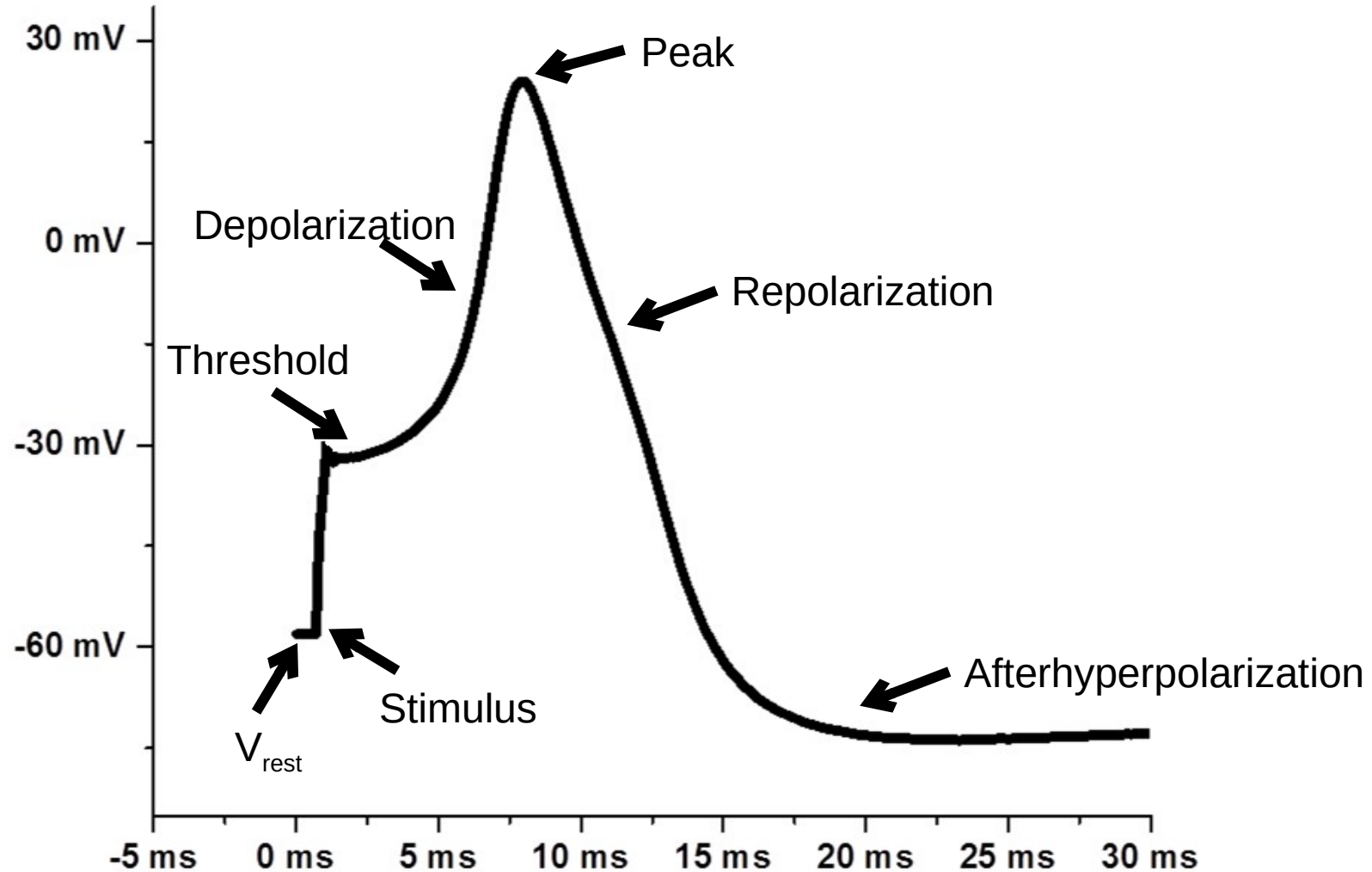
Skeletal Muscle

How do we use this information to understand the generation of Action Potentials in the nervous system?

The Action Potential Waveform



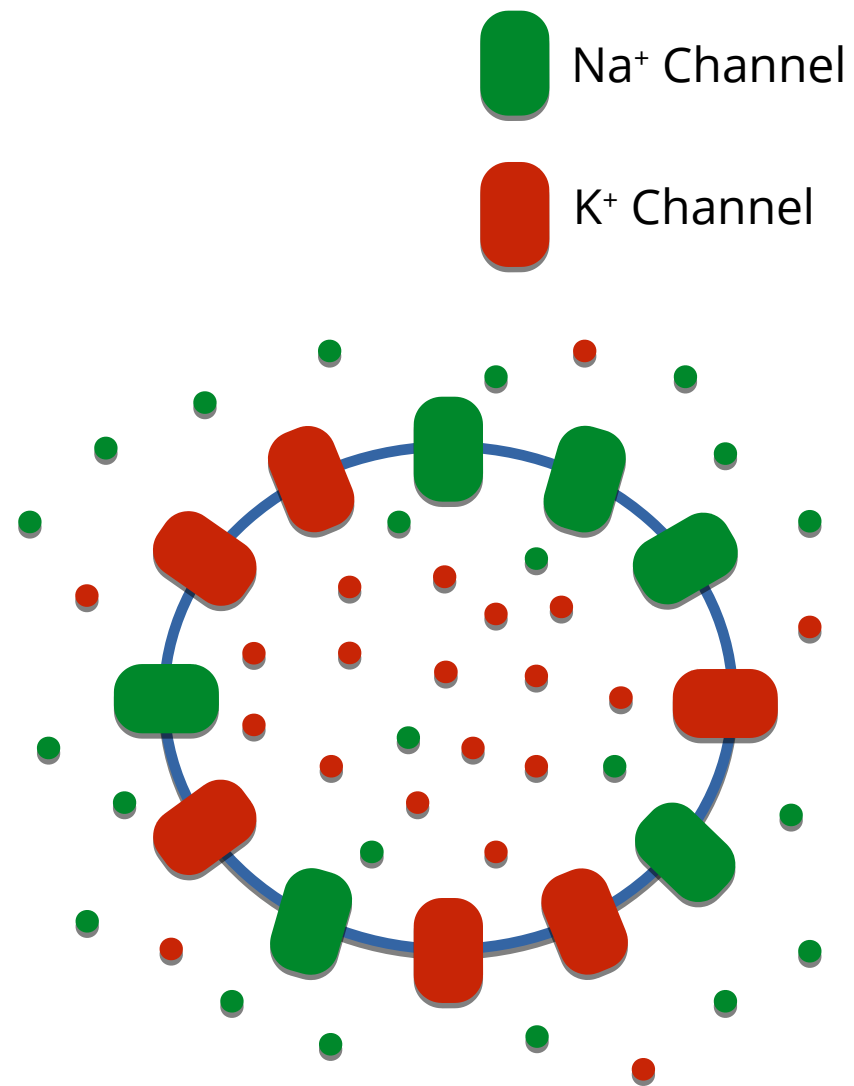
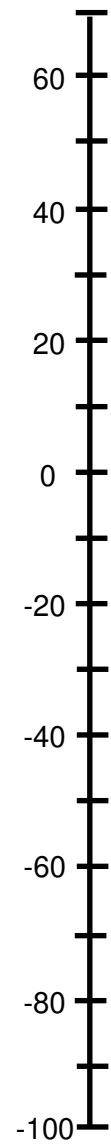
The Action Potential Waveform



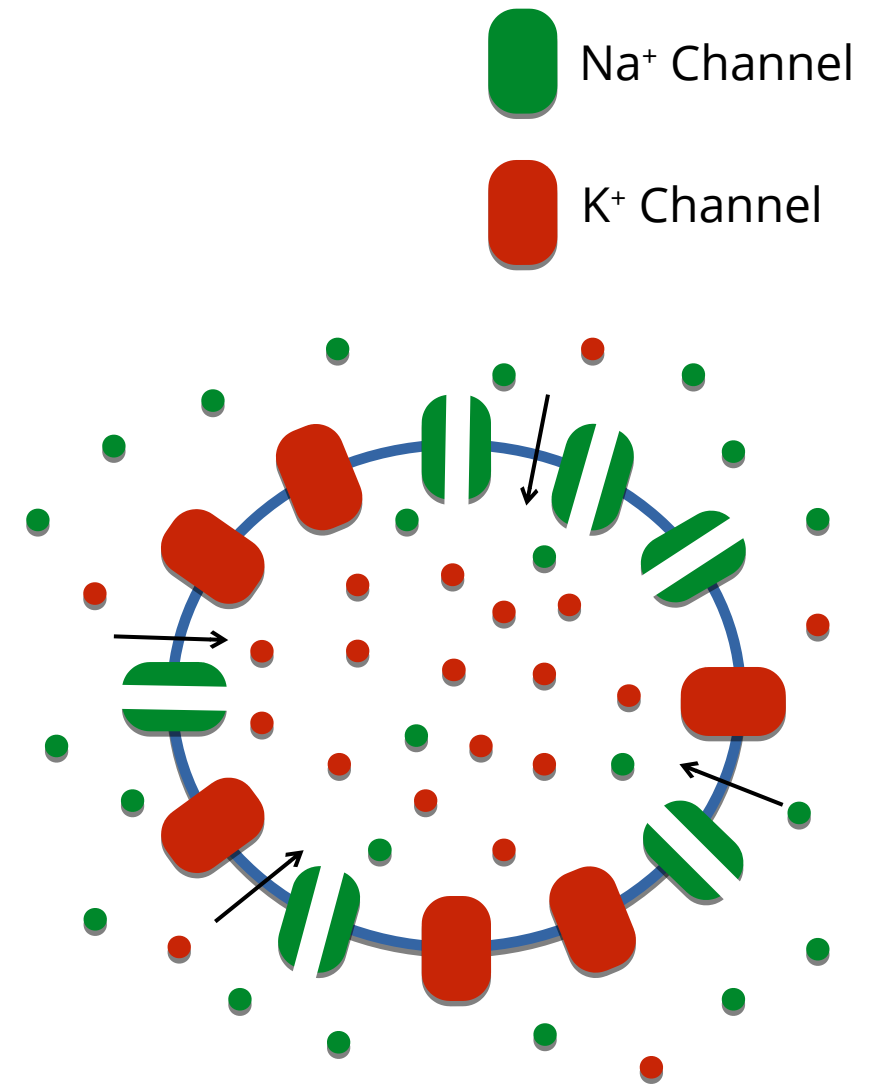
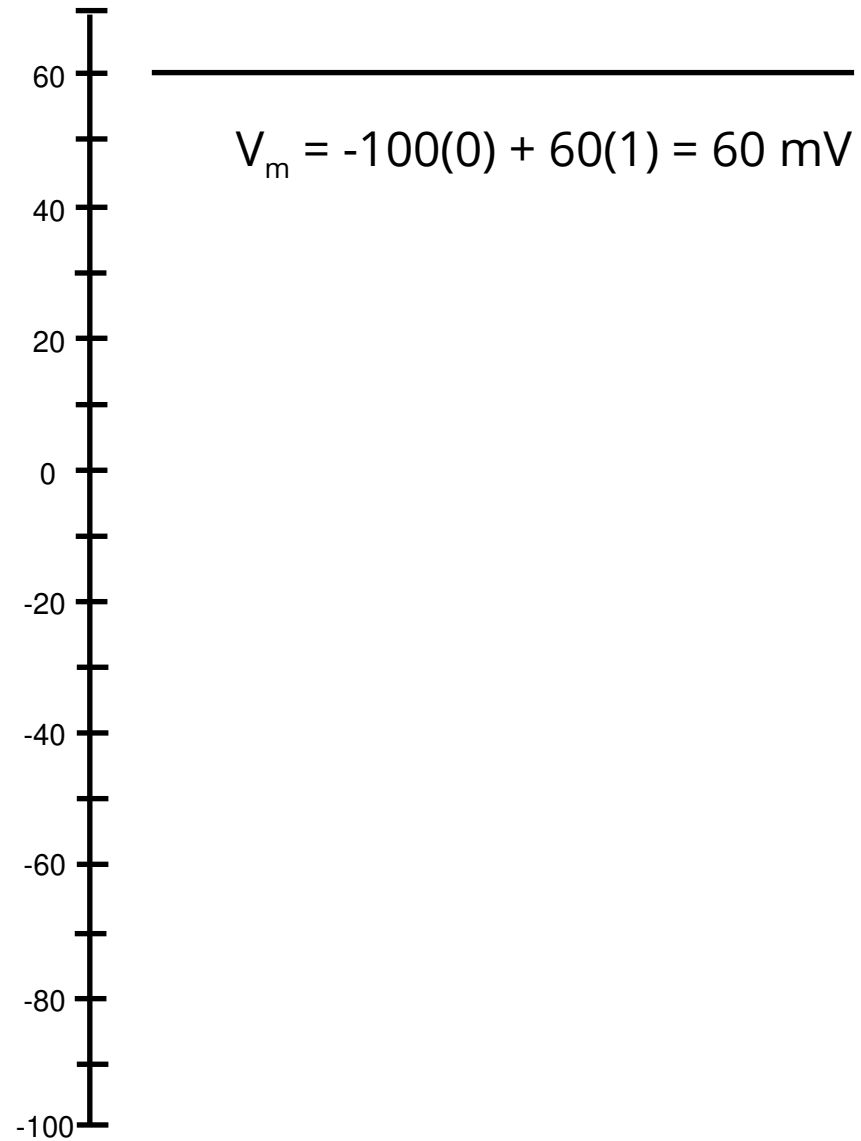
Defining terms

- V_{rest} = Resting membrane potential
- Threshold = Voltage at which action potential fires (point of no return)
- Depolarization = Potential moves in the positive direction
- Repolarization = Potential moves toward resting membrane potential
- Afterhyperpolarization = Potential overshoots on its way back to resting

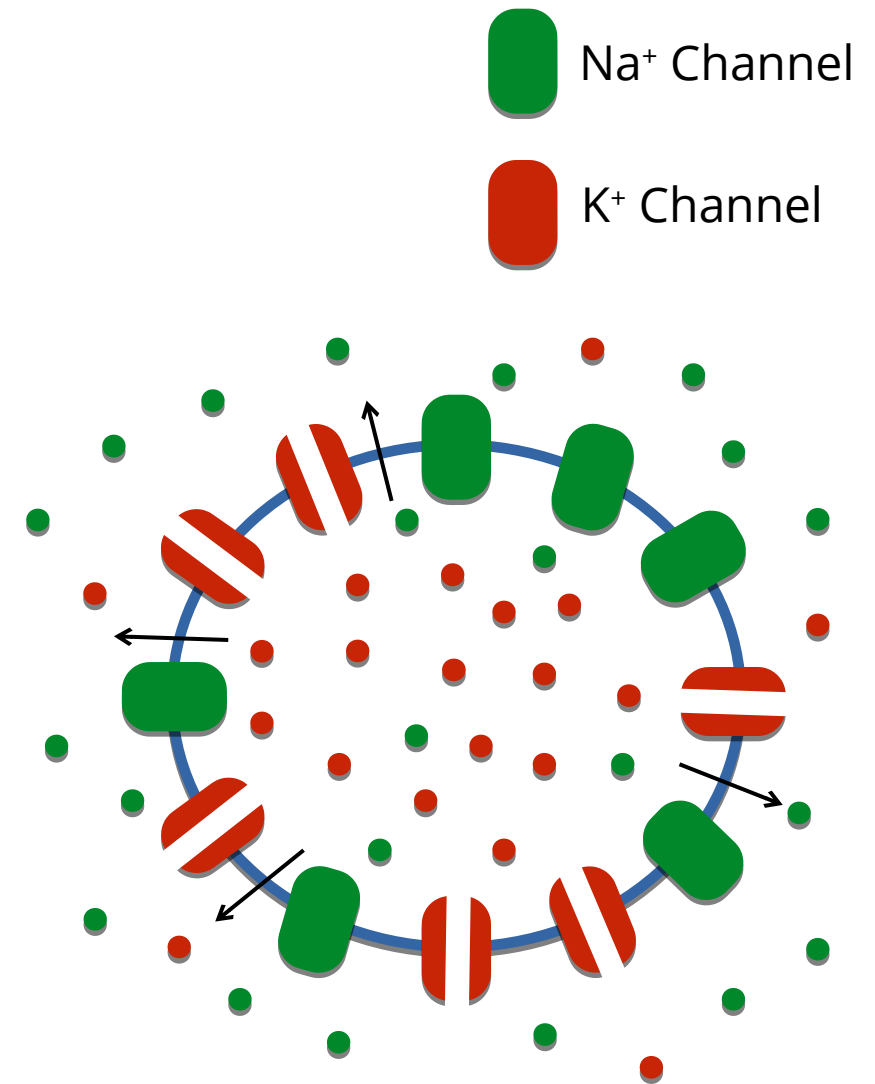
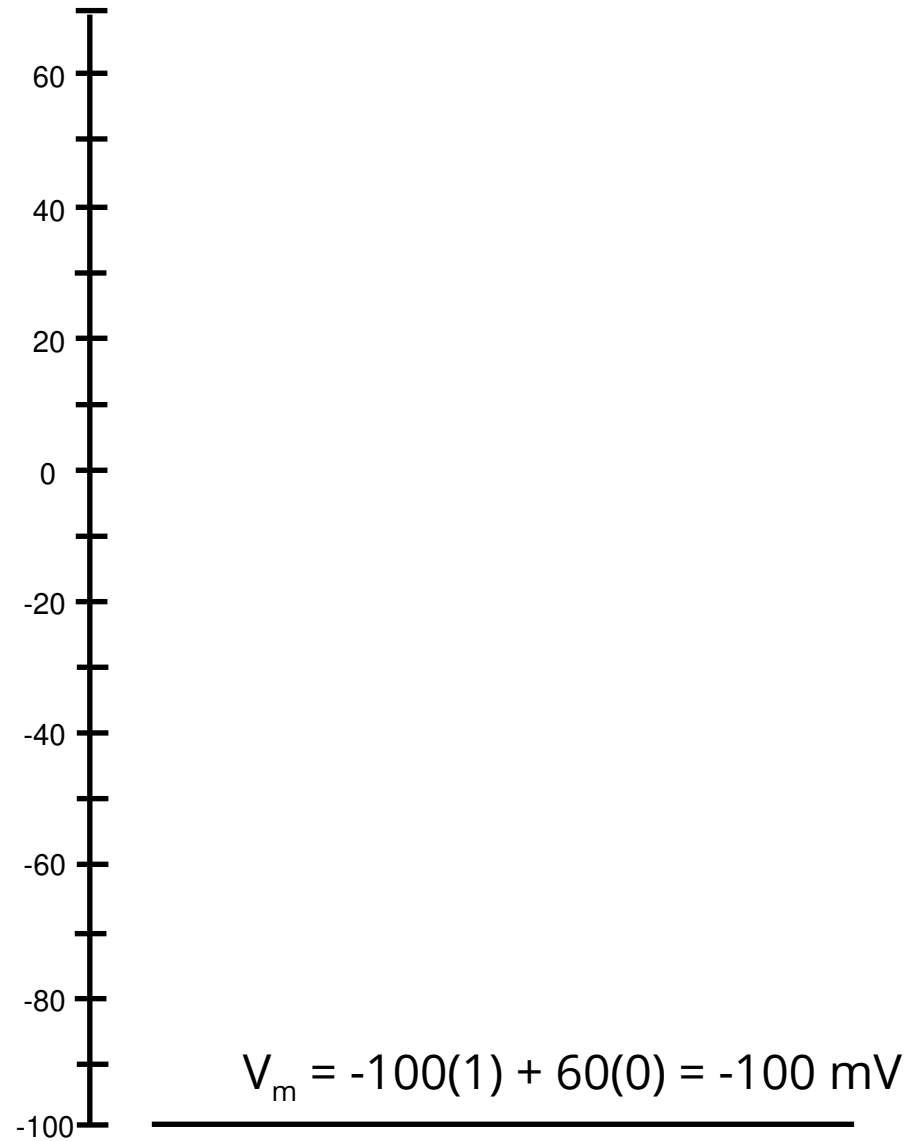
Membrane Potential



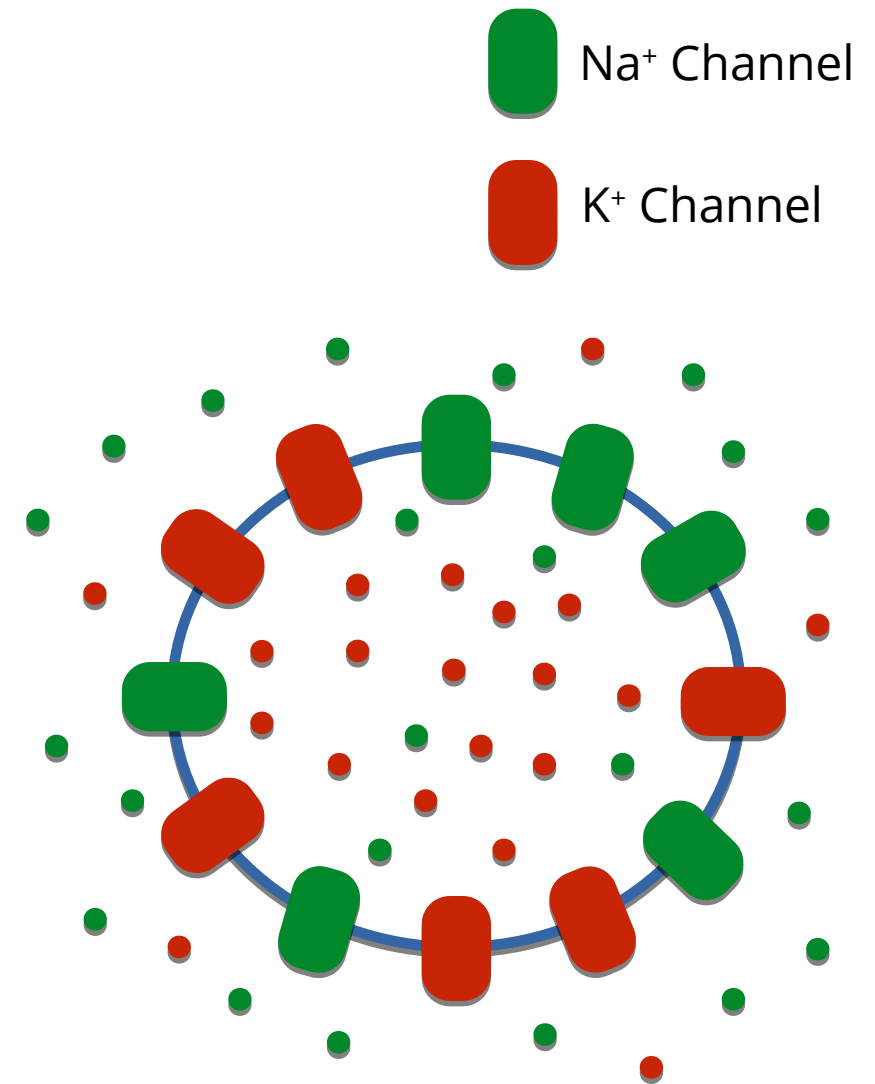
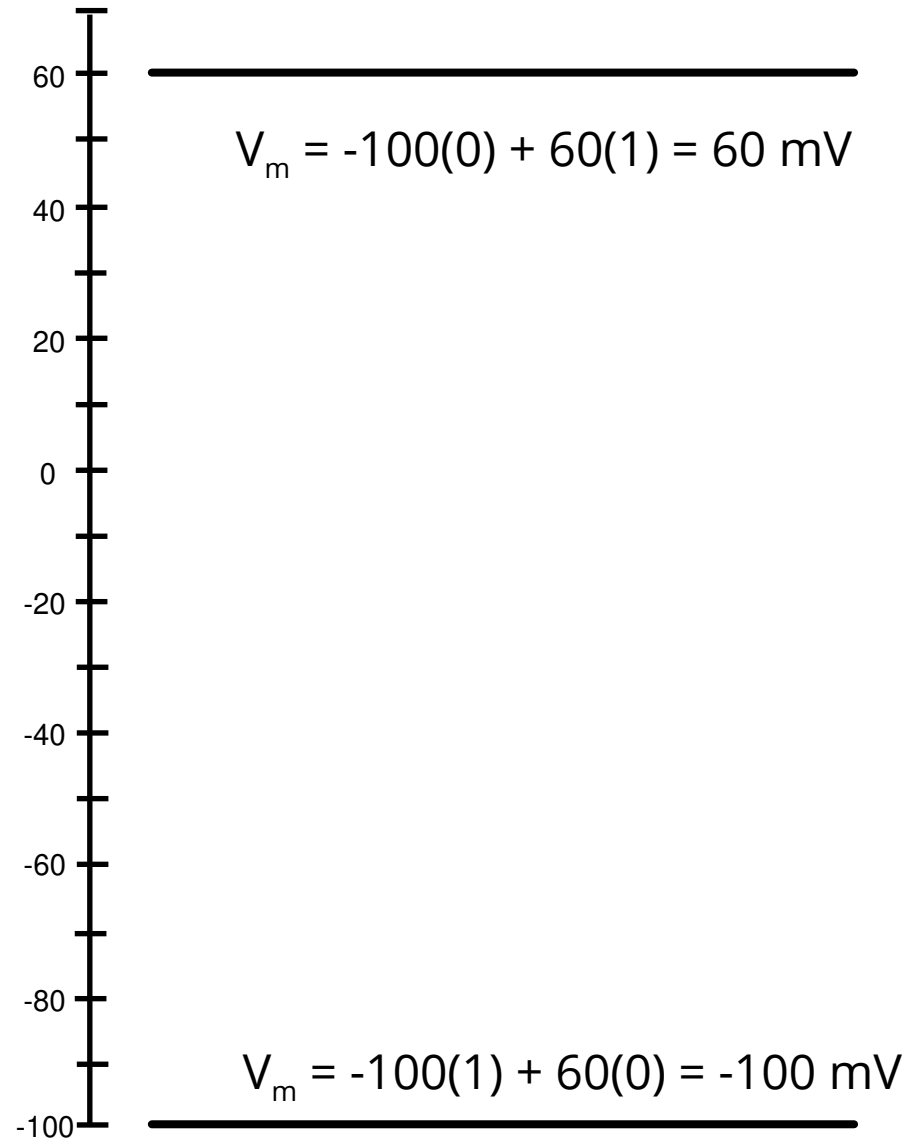
Membrane Potential



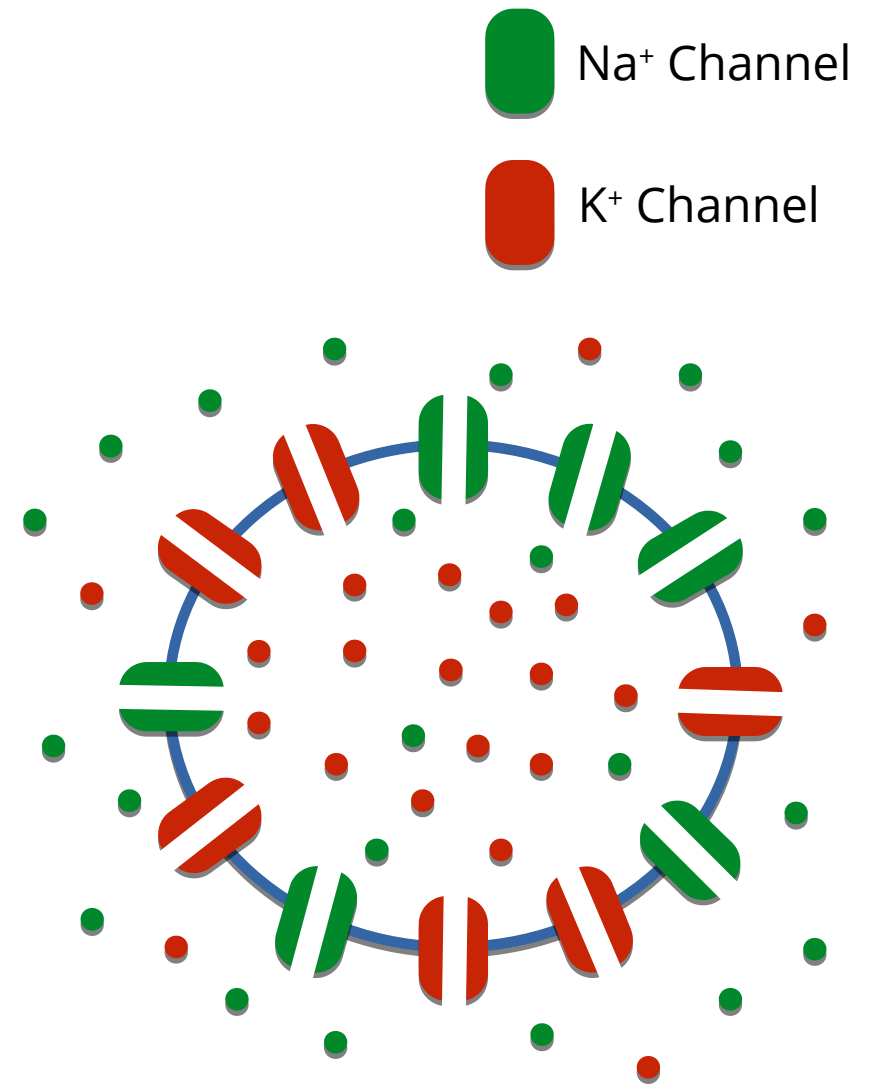
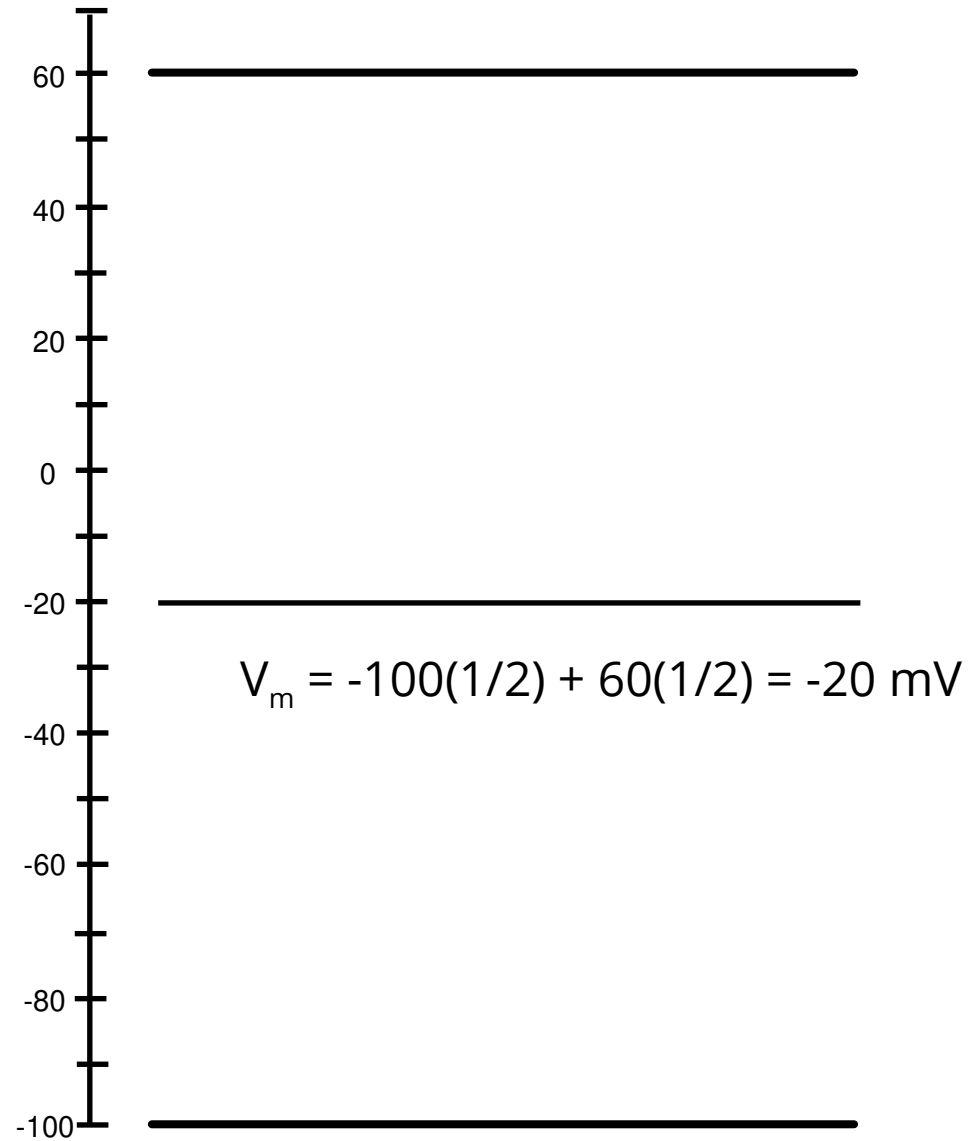
Membrane Potential



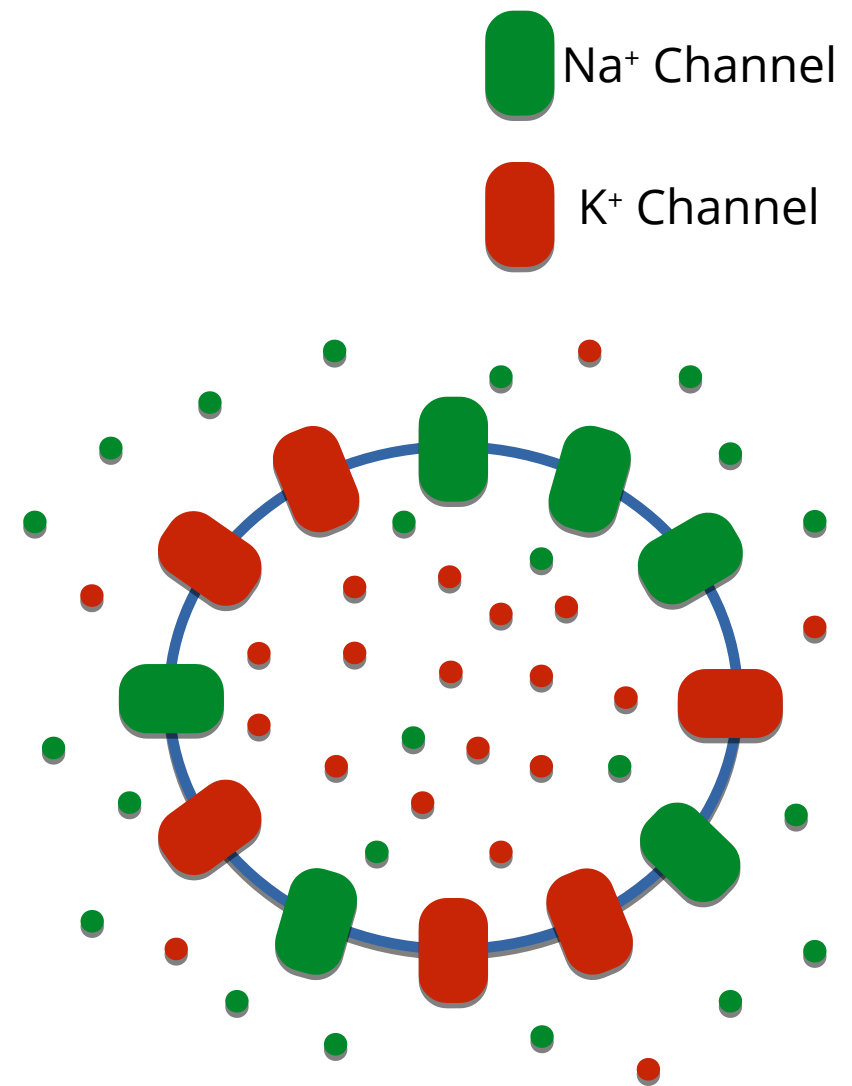
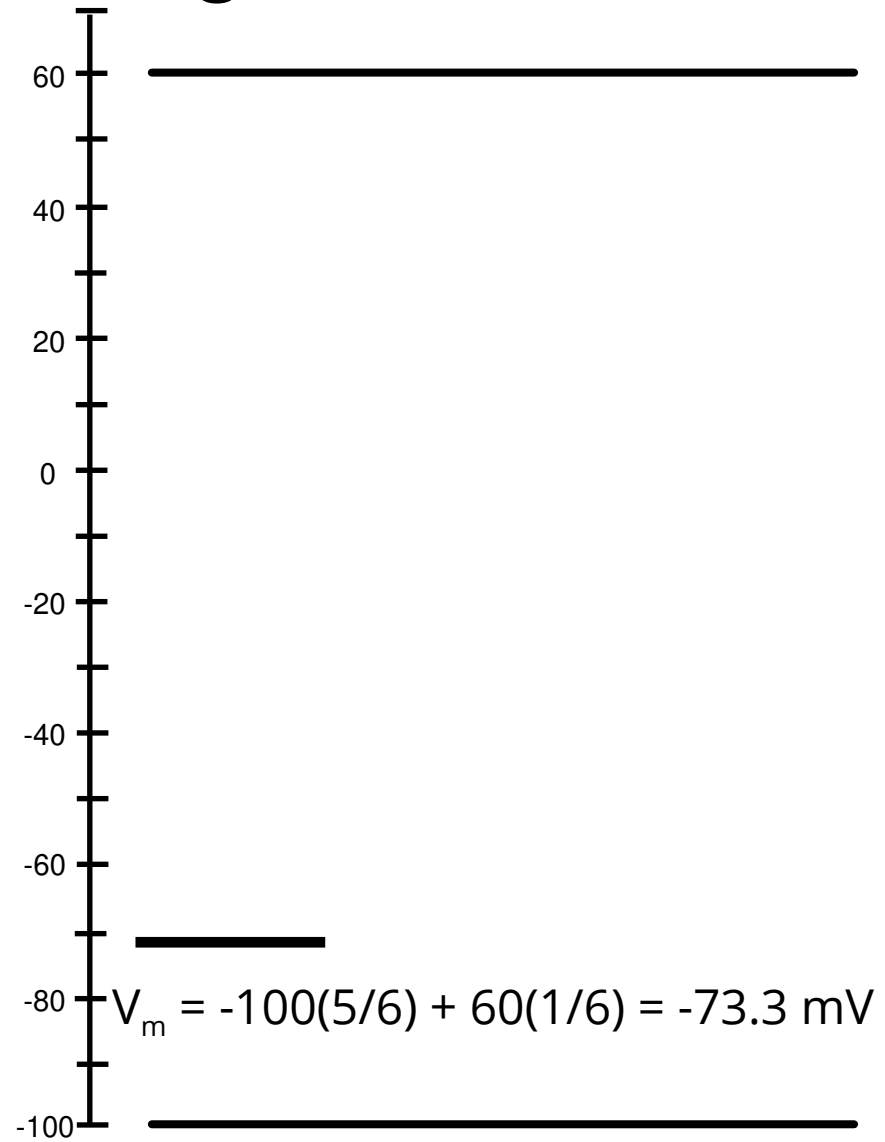
Membrane Potential



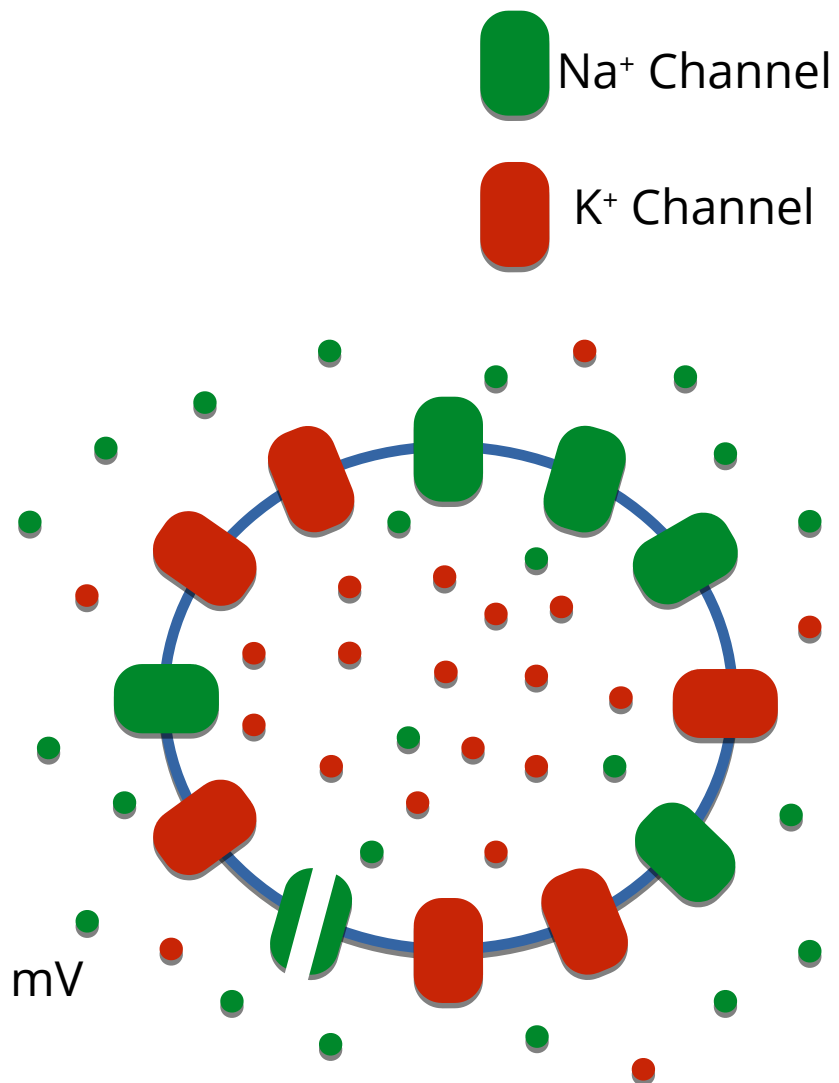
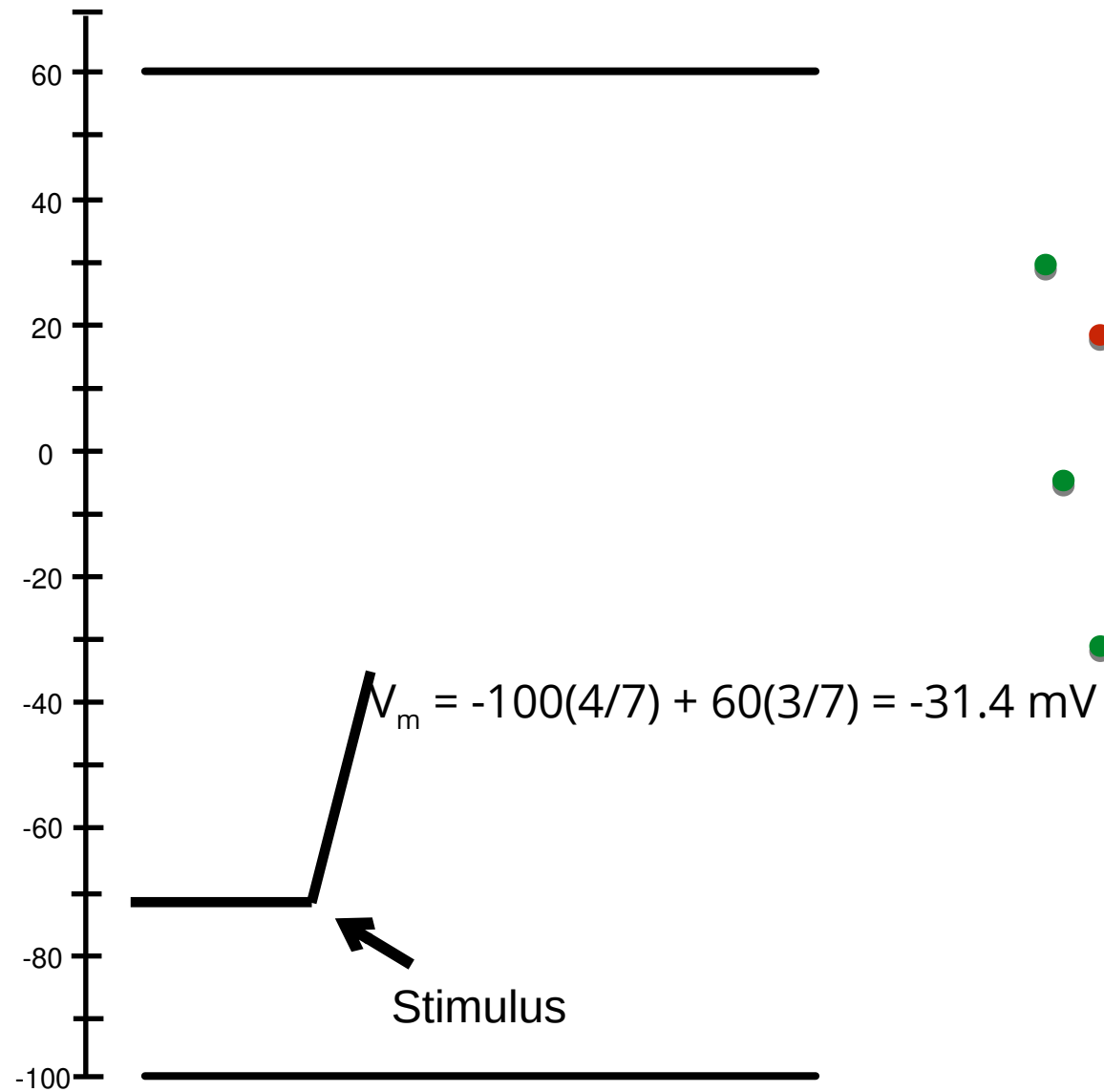
Membrane Potential



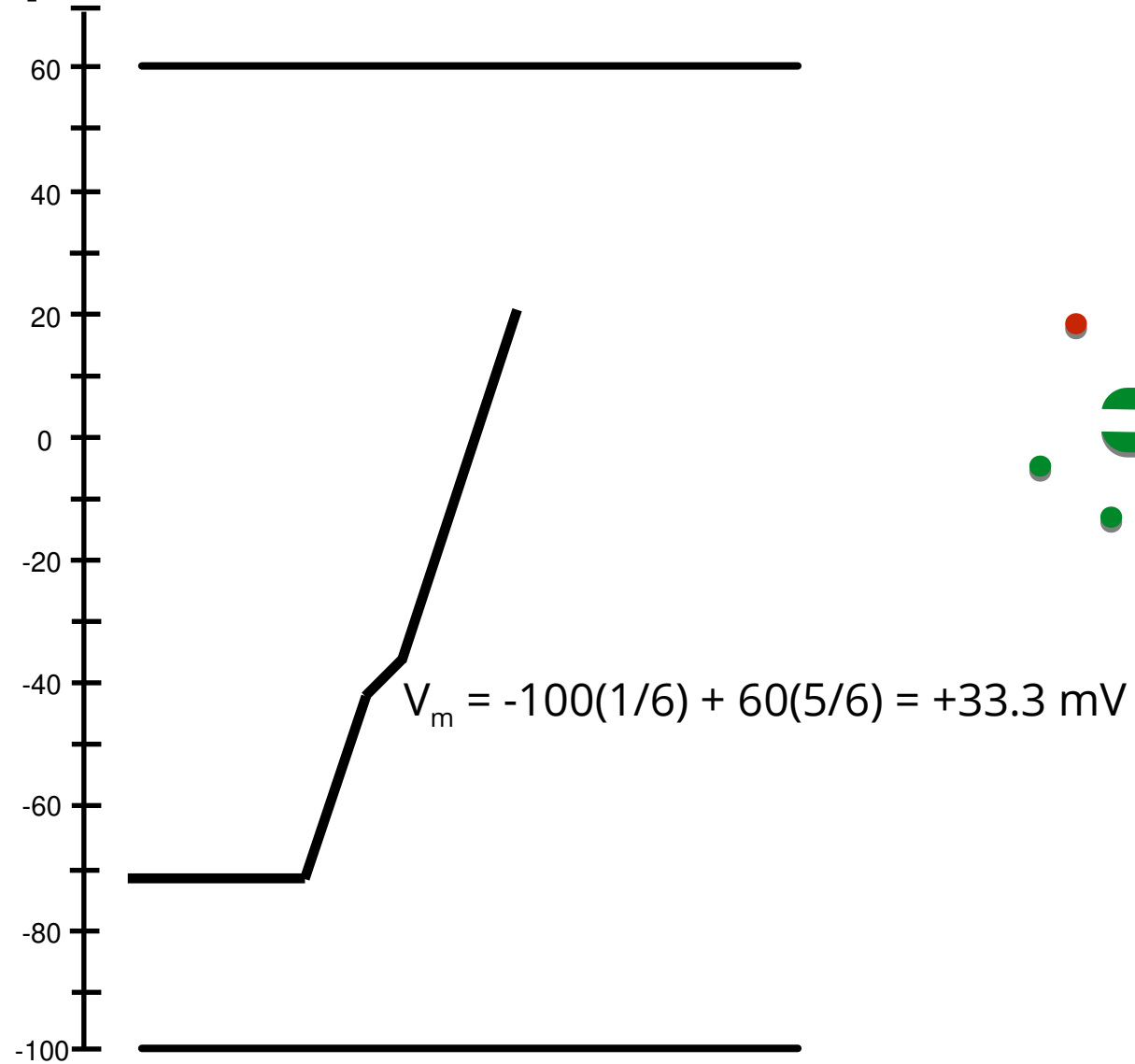
Resting



Threshold

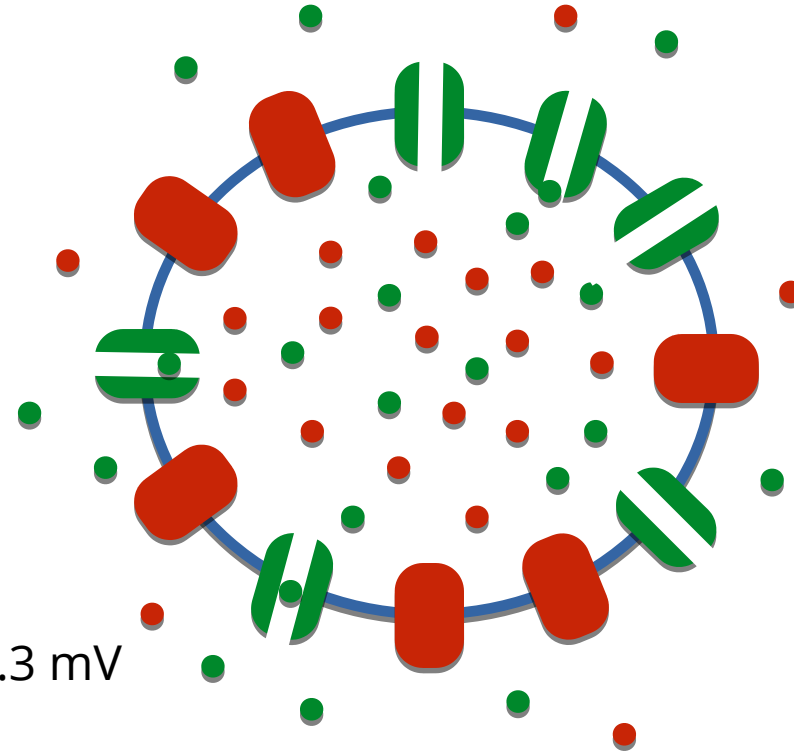


Depolarization

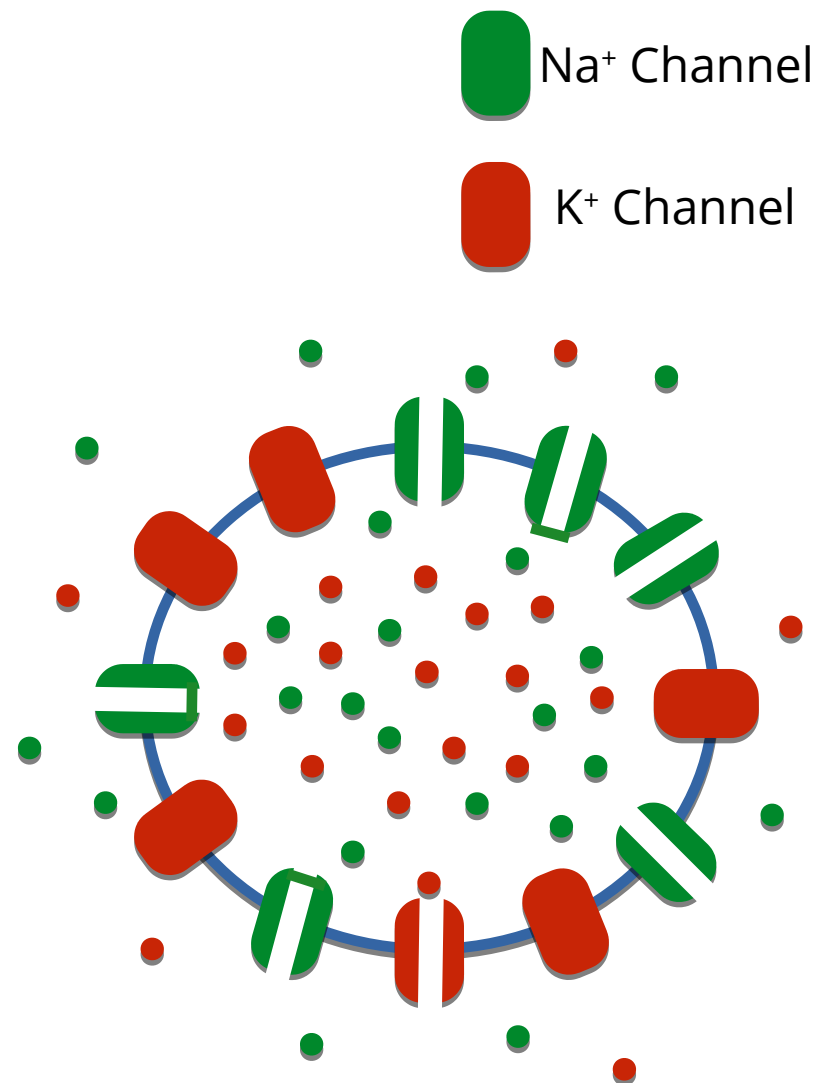
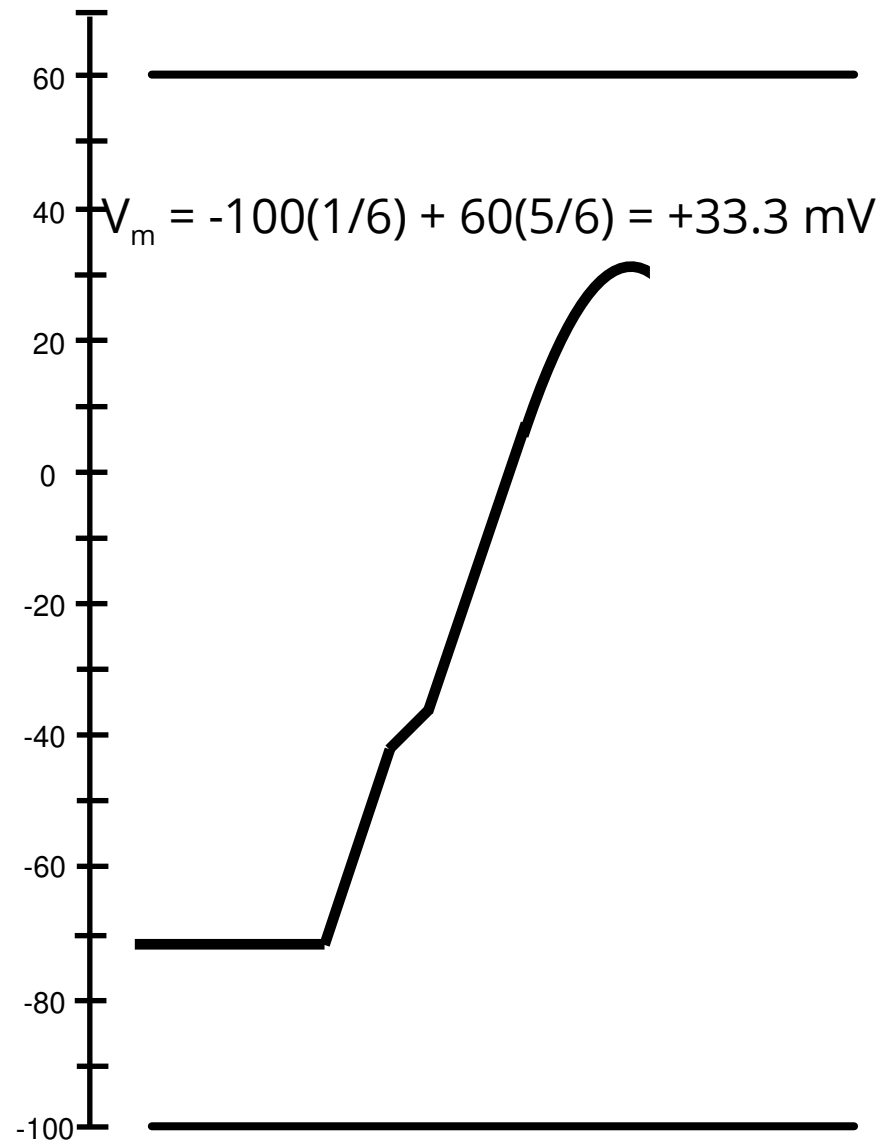


Na⁺ Channel

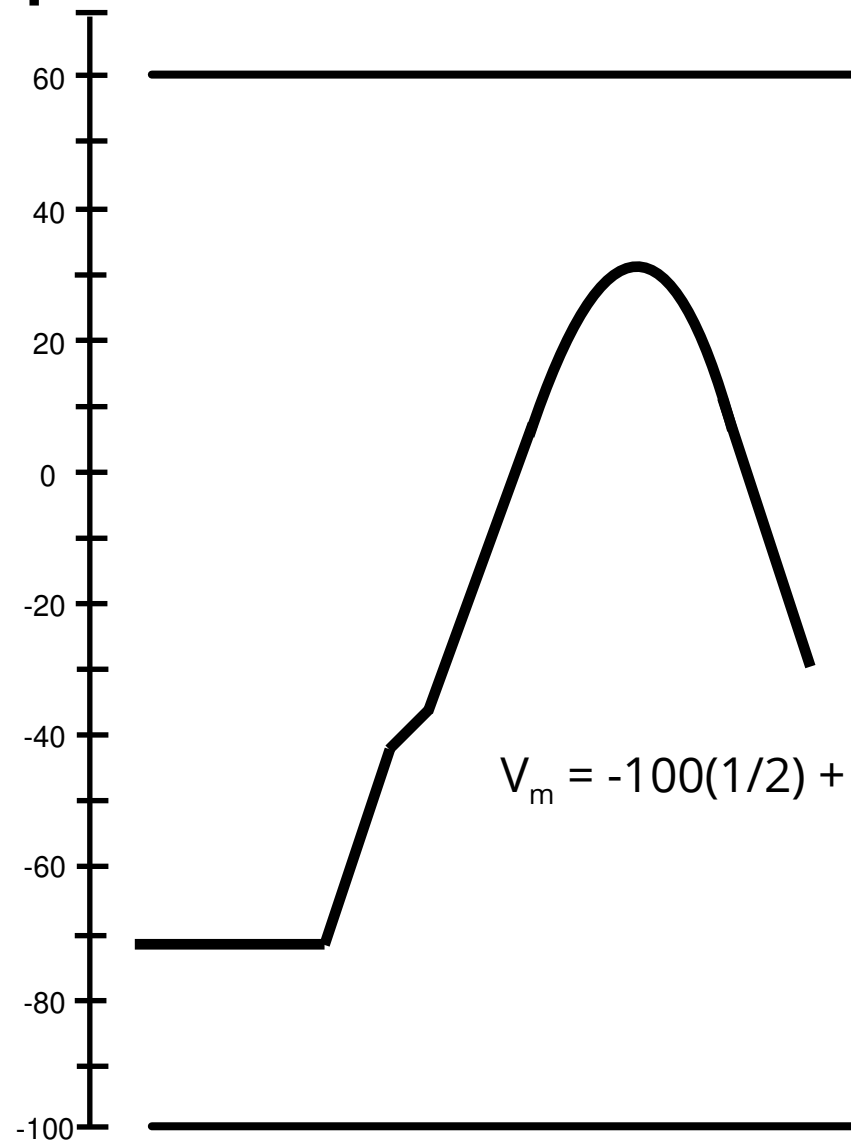
K⁺ Channel



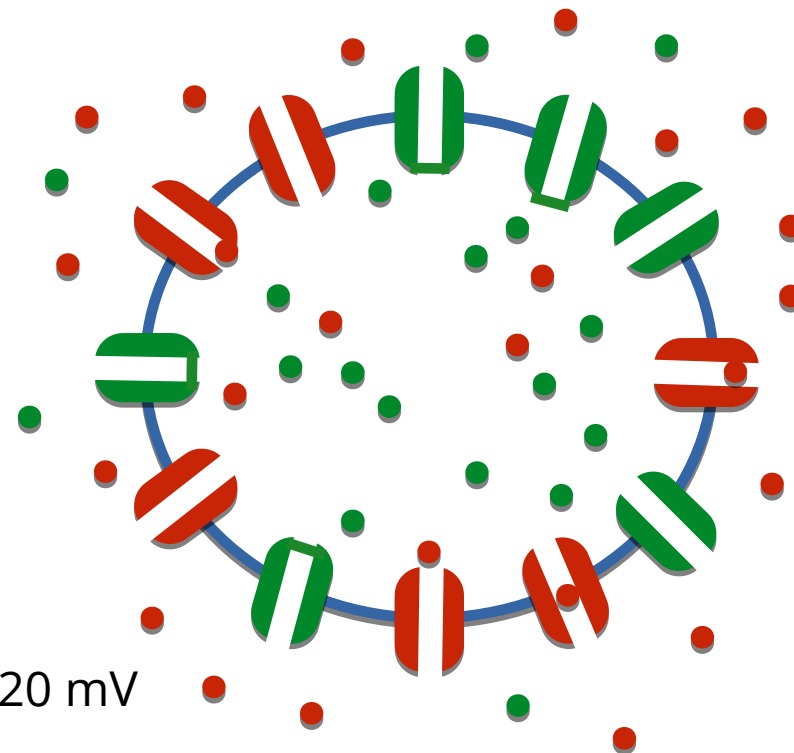
Peak



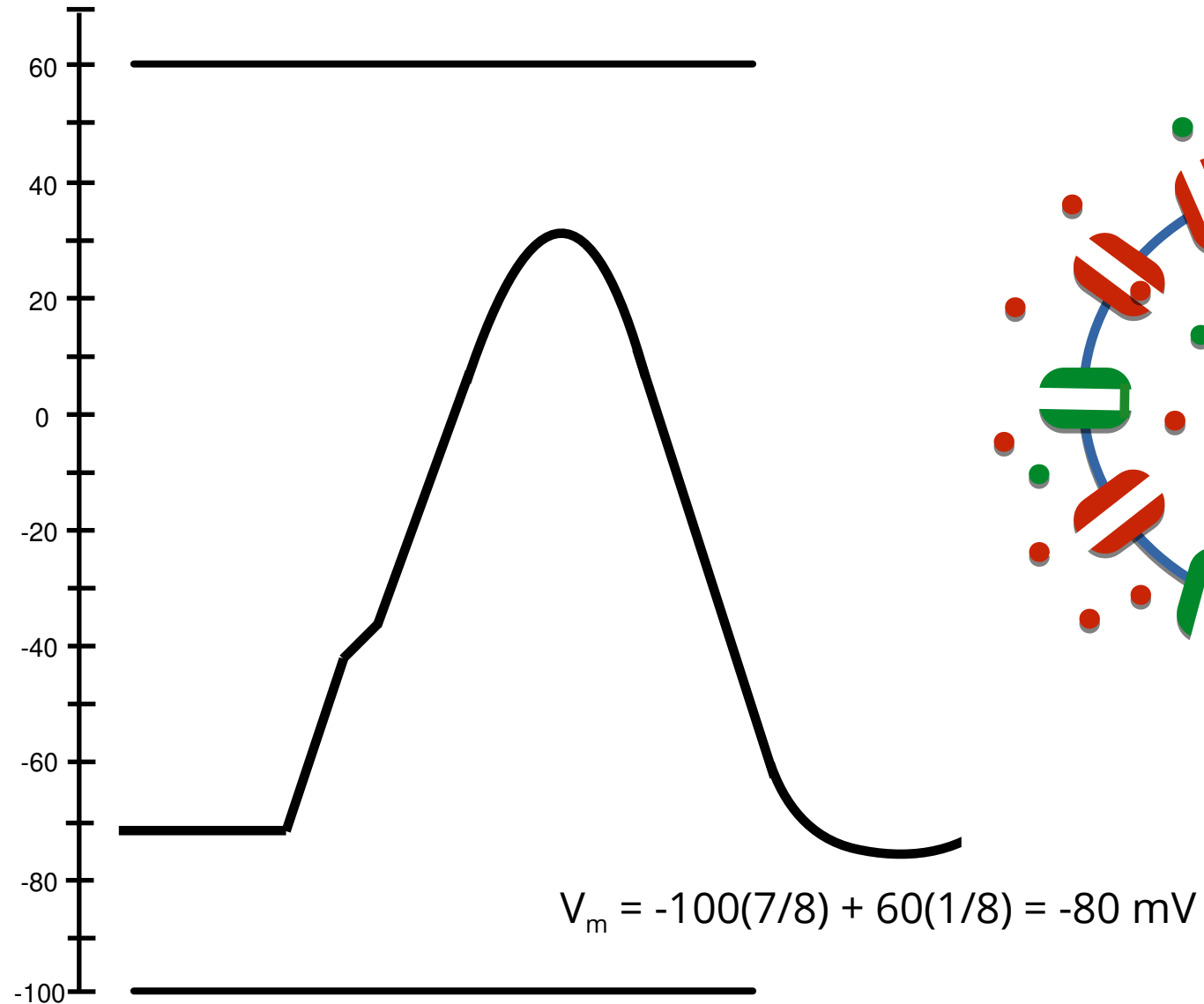
Repolarization



$$V_m = -100(1/2) + 60(1/2) = -20 \text{ mV}$$

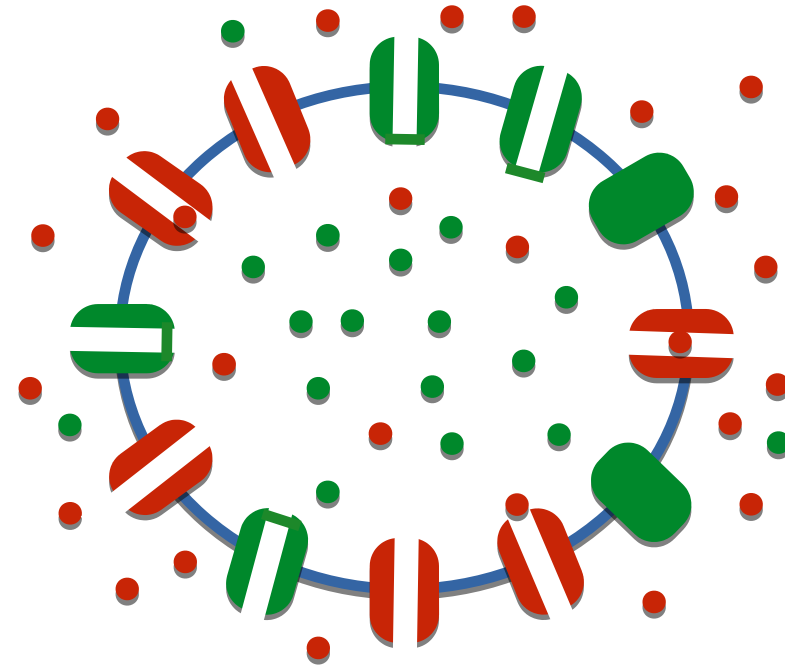


Afterhyperpolarization

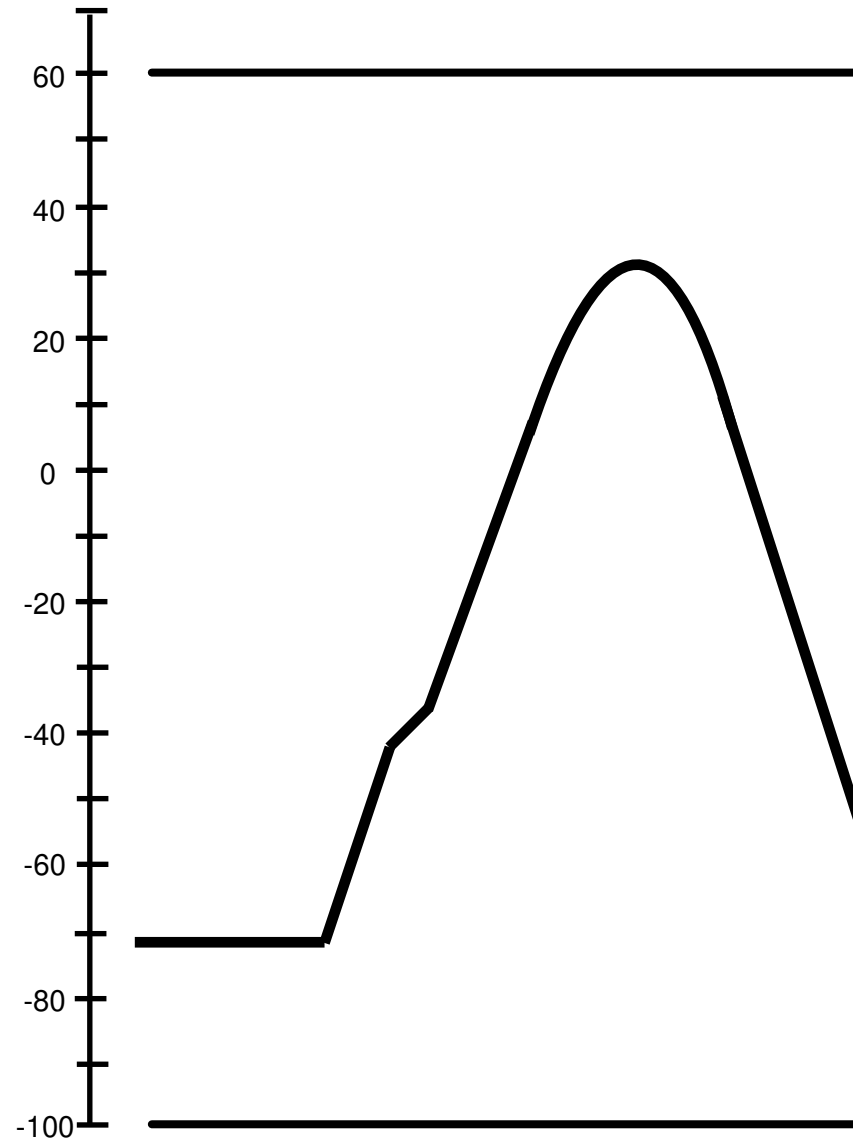


Na⁺ Channel

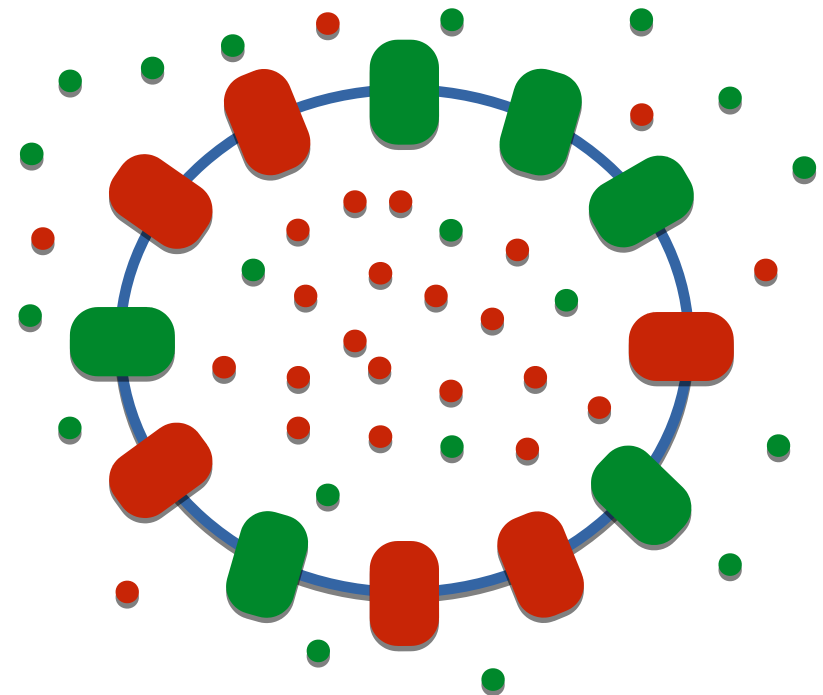
K⁺ Channel



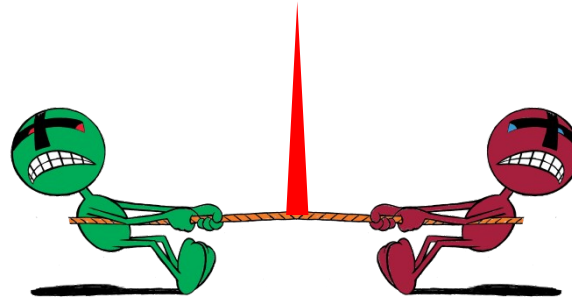
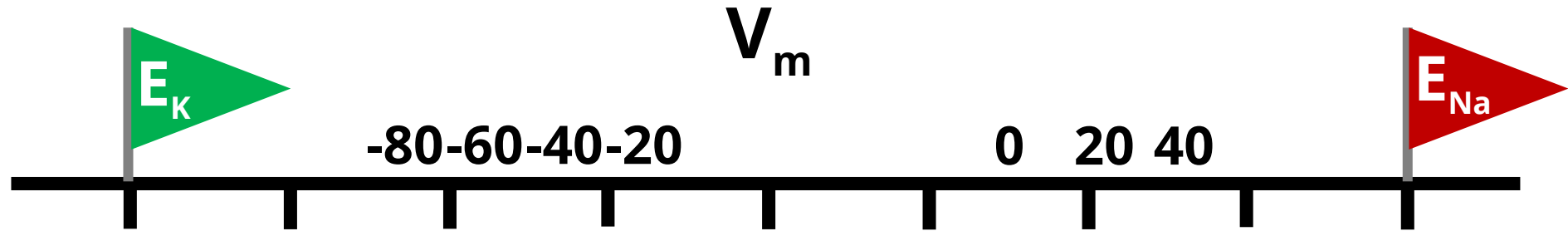
Return to Rest



$$V_m = -100(5/6) + 60(1/6) = -73.3 \text{ mV}$$

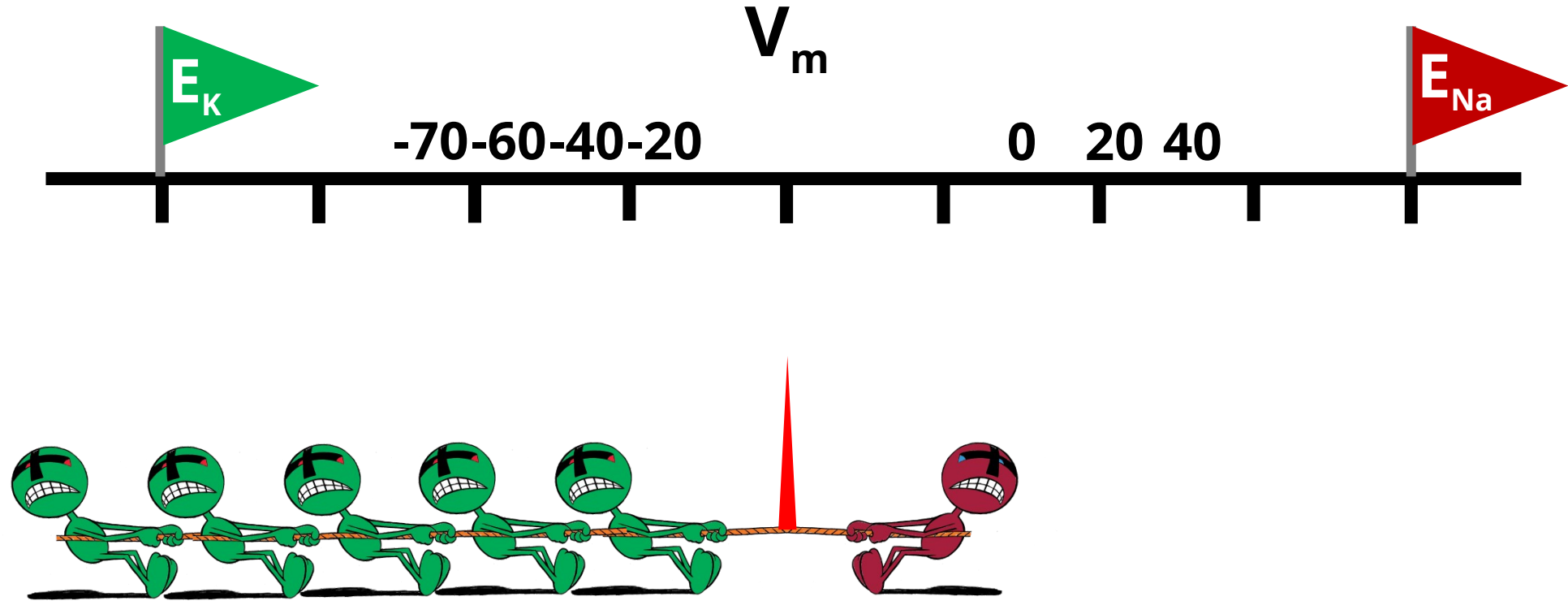


Conductance Tug-of-War Games



MC13

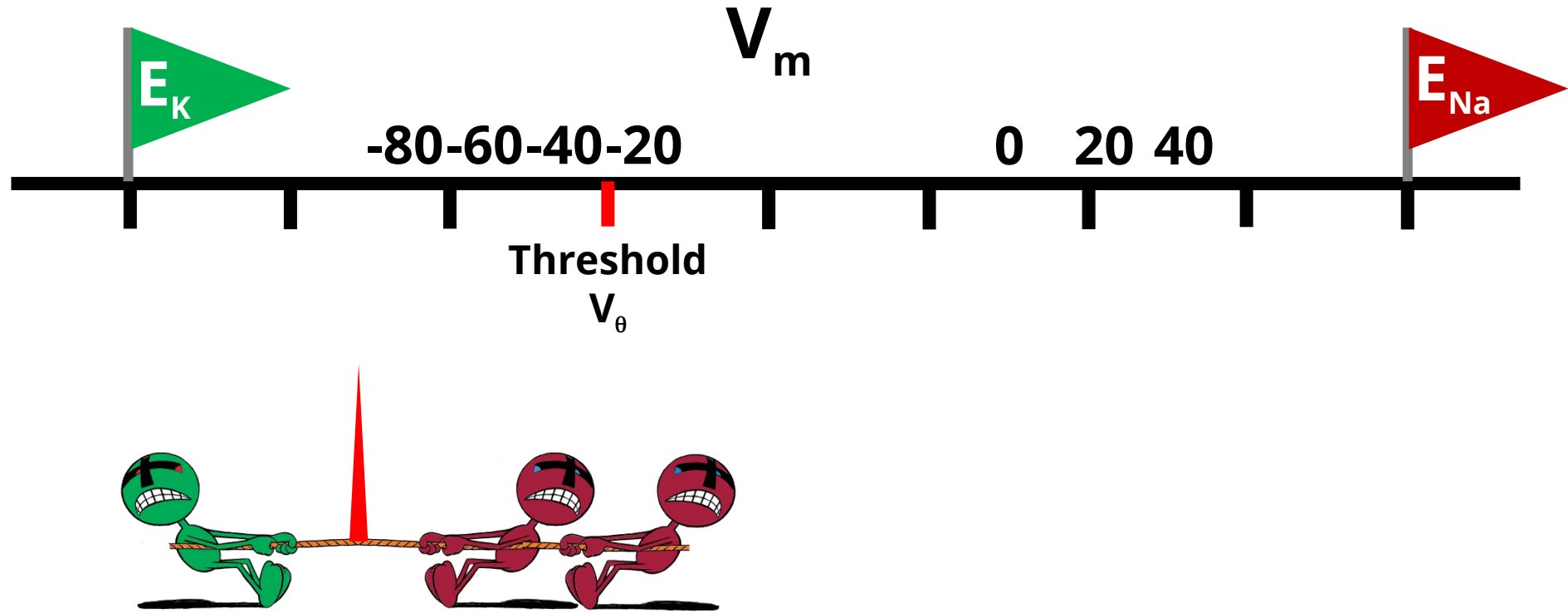
Conductance Tug-of-War Games



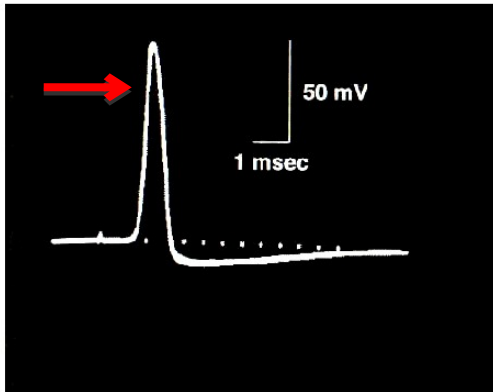
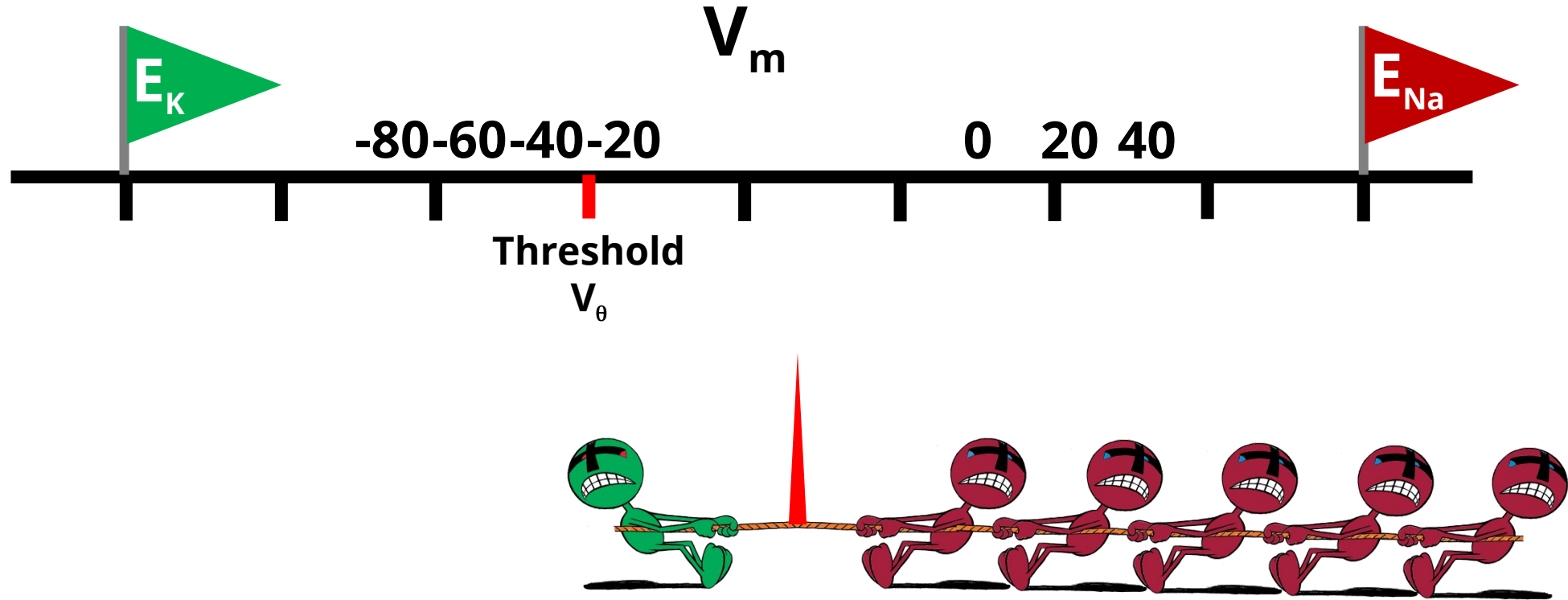
$$V_m = -100(5/6) + 60(1/6) = -73.3 \text{ mV}$$

MC13

Conductance Tug-of-War Games

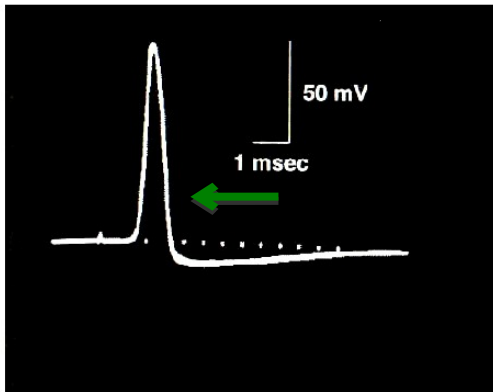
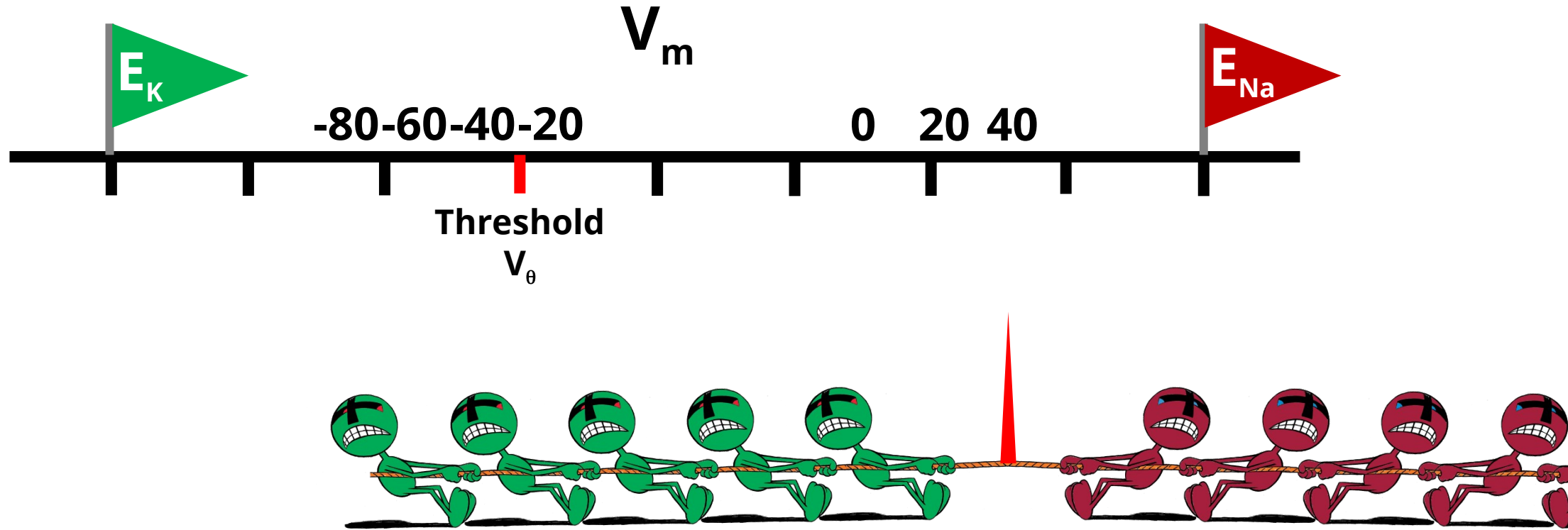


Conductance Tug-of-War Games



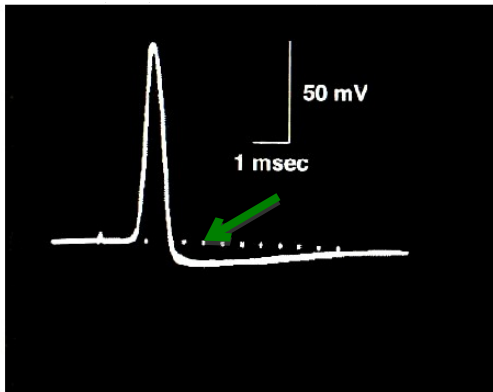
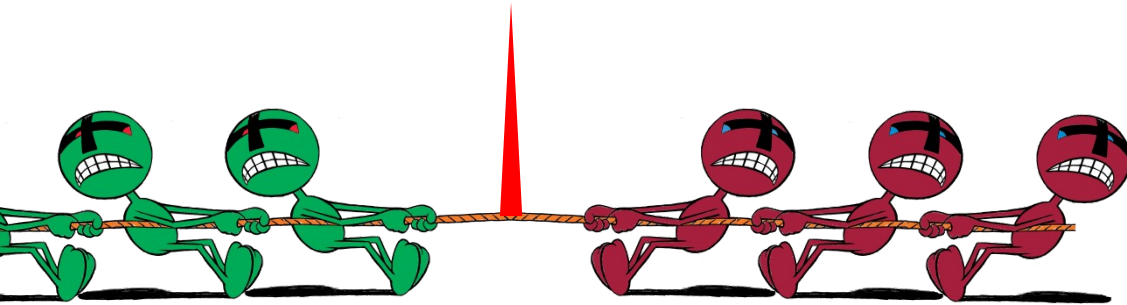
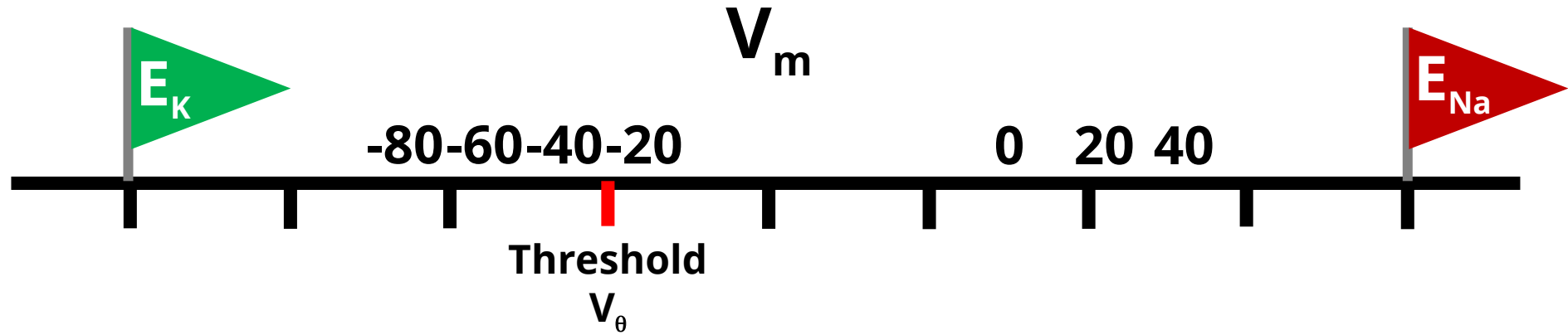
$$V_m = -100(1/6) + 60(5/6) = +33.3 \text{ mV} \quad M_{G13}$$

Conductance Tug-of-War Games



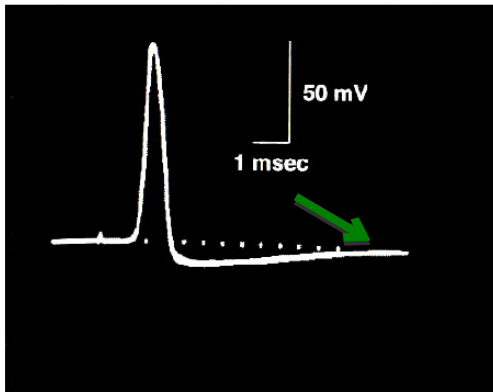
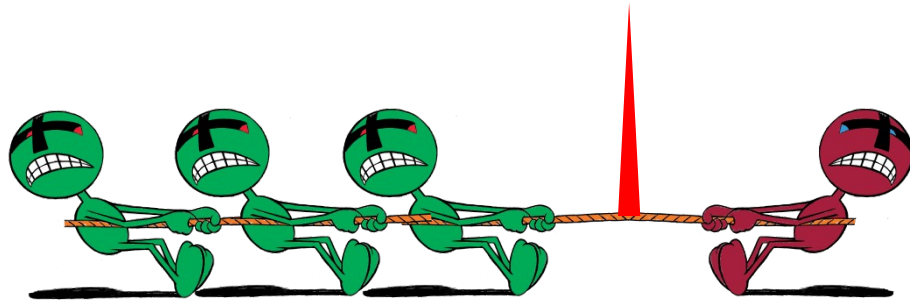
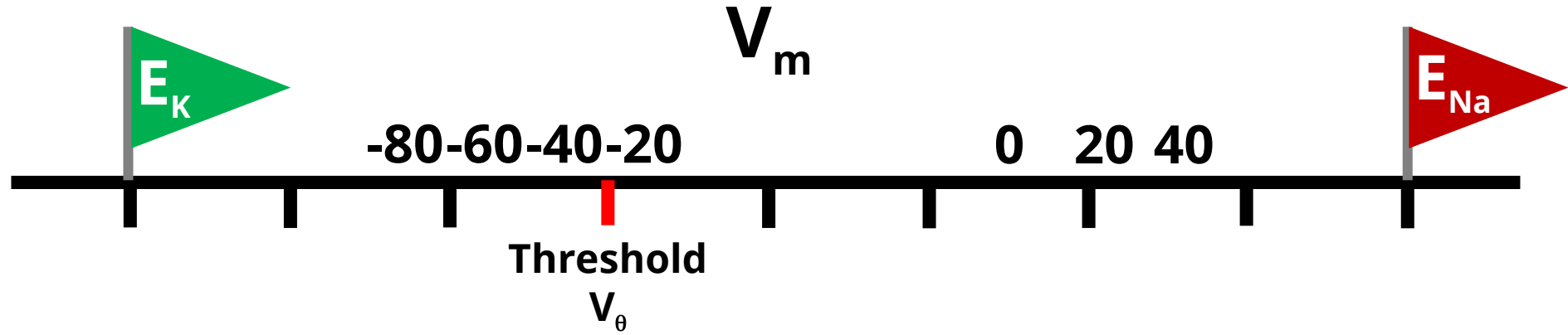
$$V_m = -100(2/3) + 60(1/3) = -46.7 \text{ mV} \quad \text{MCG13}$$

Conductance Tug-of-War Games



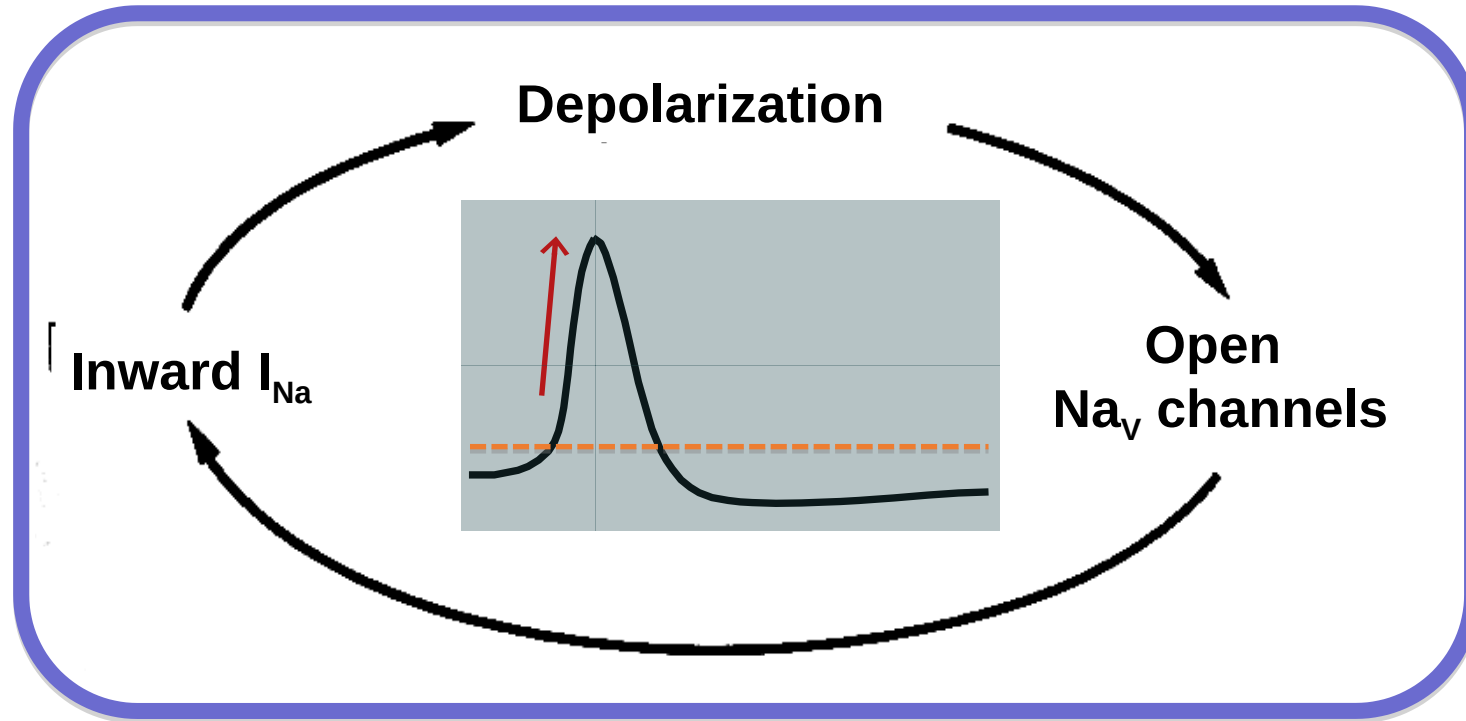
$$V_m = -100(6/6) + 60(0/6) = -100 \text{ mV} \quad M_{G13}$$

Conductance Tug-of-War Games

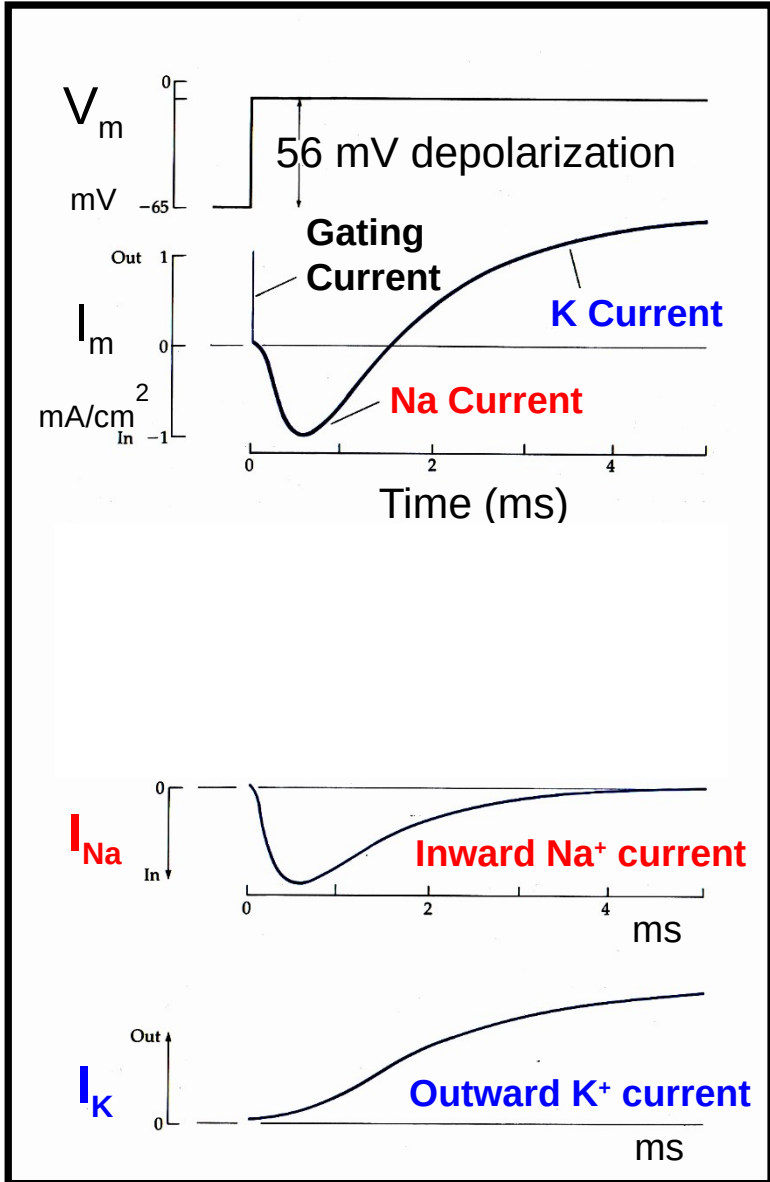


$$V_m = -100(5/6) + 60(1/6) = -73.3 \text{ mV} \quad M_{G13}$$

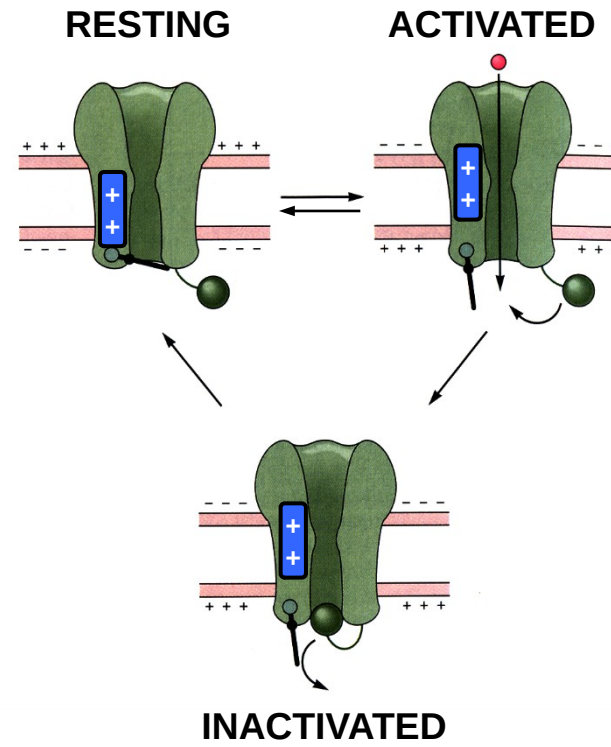
The positive feedback loop of the action potential (regenerative property of the AP)



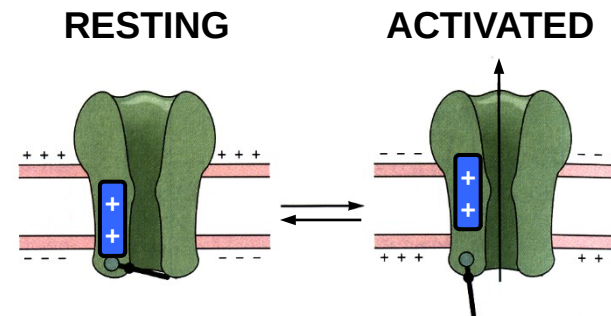
The Voltage-Clamp Perspective of the AP



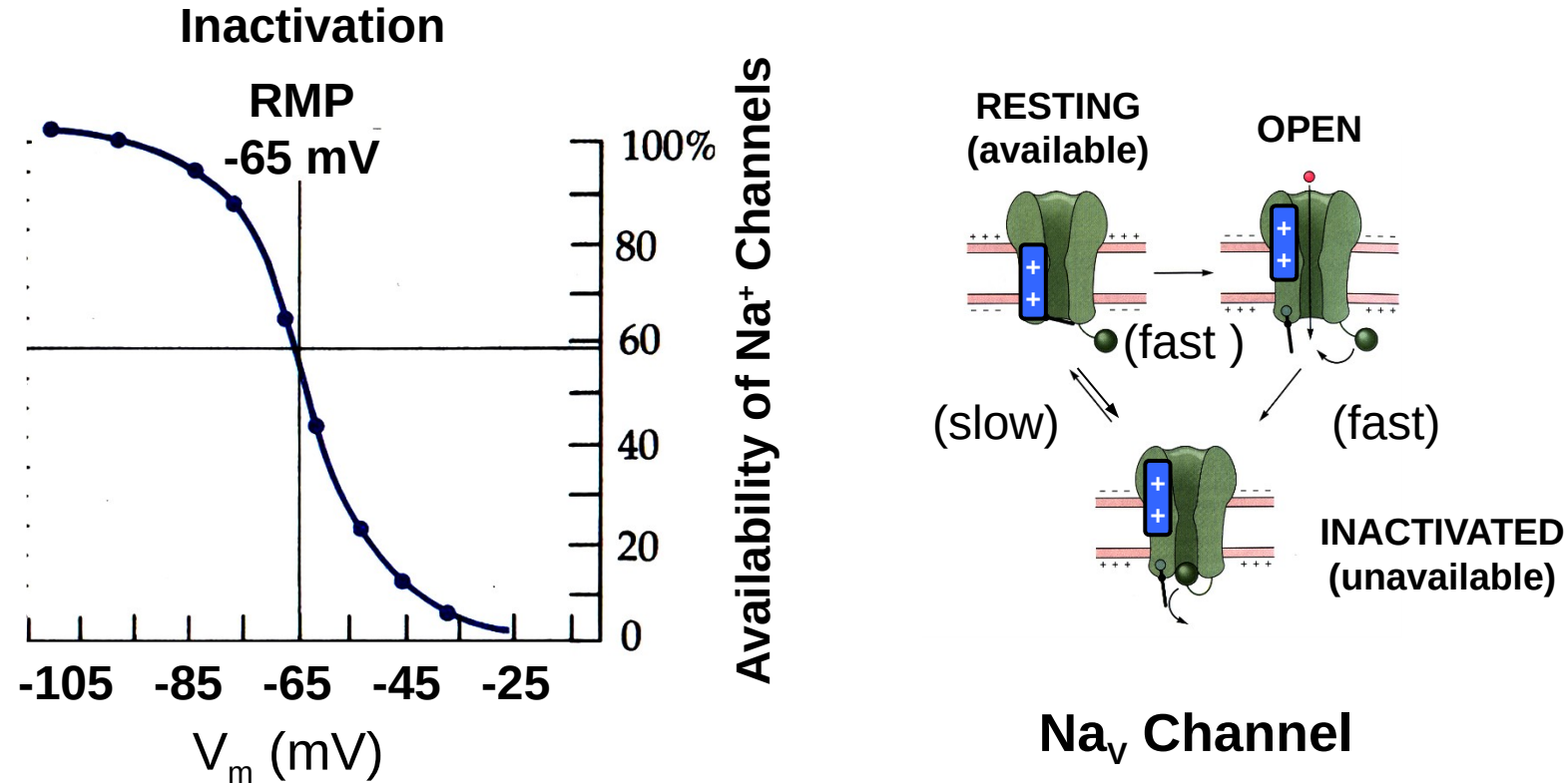
Na_v Channel



K_v Channel



Voltage-dependent Inactivation of Na⁺ Channels

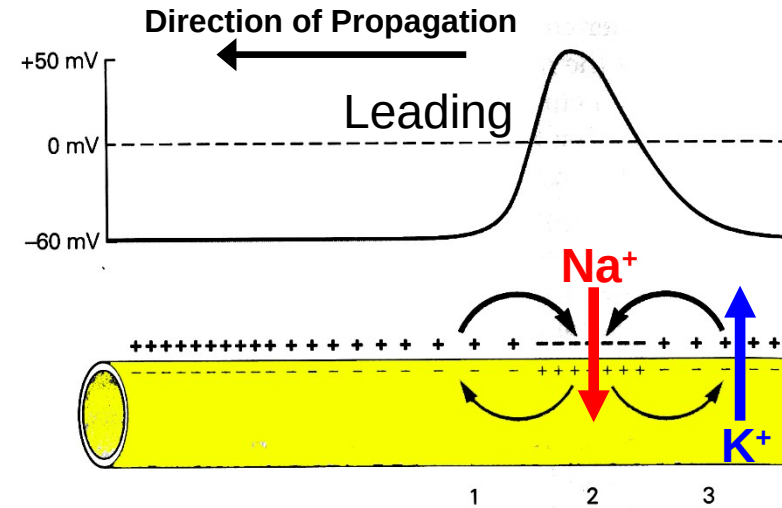


Na⁺ channels can inactivate slowly without opening. Thus, a small sustained depolarization that does not reach threshold may be sufficient prevent AP firing. This may happen as a result of modest hyperkalemia (external K⁺ is elevated)

Active propagation in un-myelinated axons

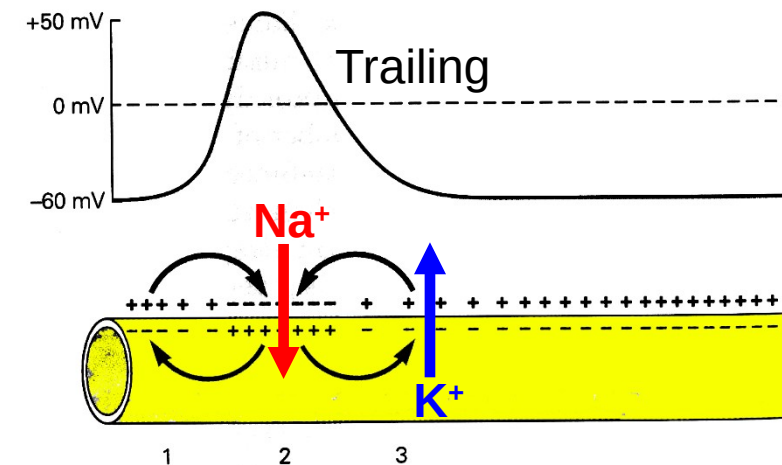
Local Circuits

Active depolarization and repolarization at the leading and trailing edges of the AP, respectively



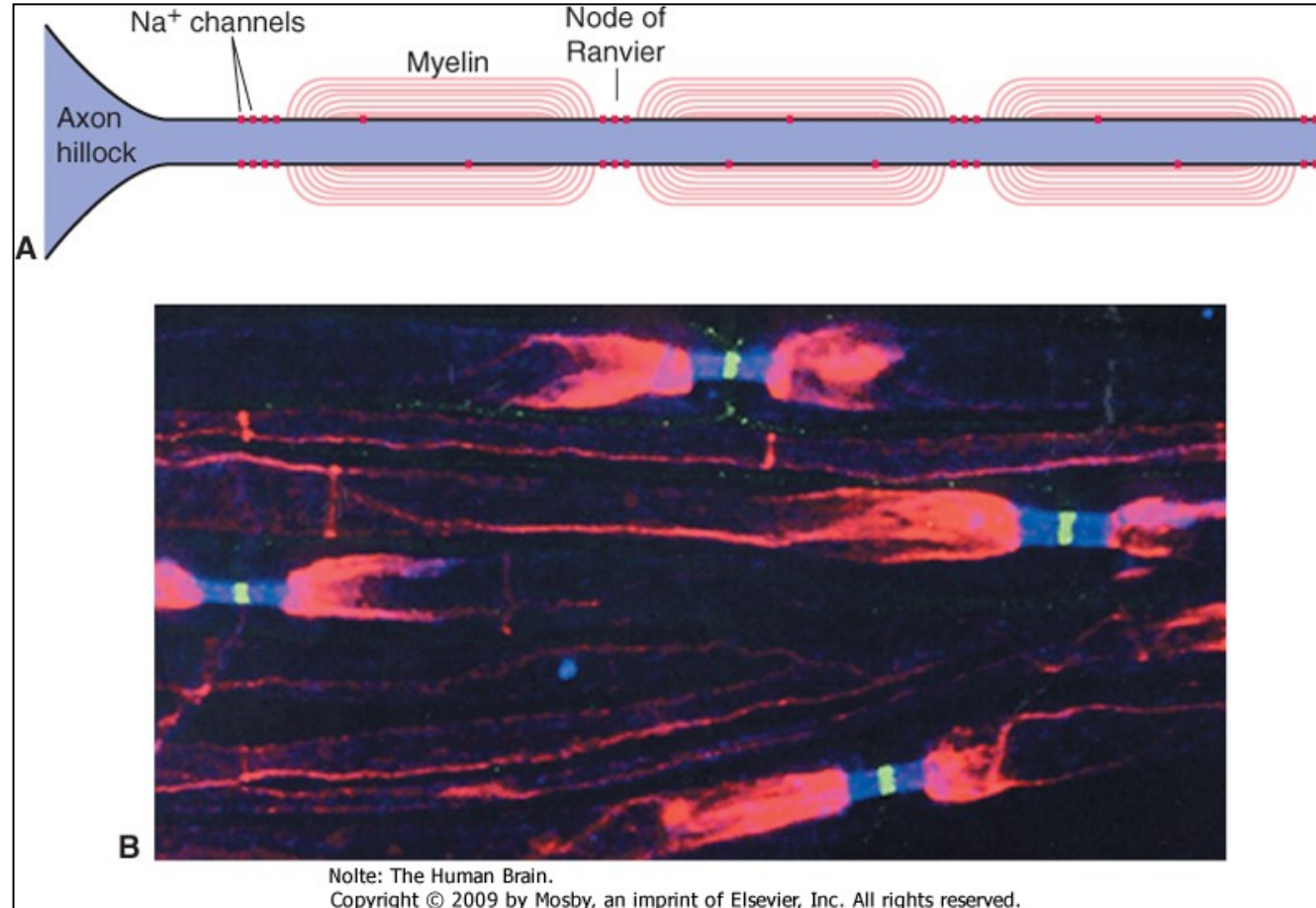
A short time later.....

Unidirectional AP propagation



Myelination

myelin sheaths at intervals of ~ 1 mm



Immunofluorescence: Node of Ranvier marker (blue);
Na_v channels (green); K_v channels (red)