SaUCy

ANONYMOUS AUTHOR(S)

Text of abstract

Additional Key Words and Phrases: keyword1, keyword2, keyword3

1 INTRODUCTION

Proving that a cryptographic protocol carries out a given task securely is an essential component in cryptography. Traditionally, such a protocol is analyzed in the *standalone* setting, in which a single execution takes place in isolation. In reality, however, the protocol may be running concurrently with arbitrary other protocols, and indeed, security guarantees in the standalone setting do not always translate into security guarantees in the concurrent setting. In order to provide meaningful security guarantees in the concurrent setting, the Universal Composability (UC) framework by Canetti [Canetti 2001] allows the security properties of a protocol to be defined in such a way that security is maintained under general concurrent composition with arbitrary other protocols. In other words, a UC-secure protocol maintains its security when dropped into *any context*. Importantly, this allows for complex cryptographic protocols to be designed and analyzed in a modular fashion from simpler building blocks.

Since universally composable security is such a powerful guarantee, it is perhaps not surprising that elaborating such proofs can be quite involved, and thus, error-prone. However, as UC proofs are primarily "pen-and-paper" proofs, this makes verifying them an unwieldy task. In addition, the numerous variations of UC (e.g., guc [Canetti et al. 2007], juc [Canetti and Rabin 2003], symbolic UC [Böhl and Unruh 2016], RSIM [Backes et al. 2007], GNUC [Hofheinz and Shoup 2015]) make it hard to keep track of the precise semantics of security claims. In this paper, we design and implement a specialized programming language called the Interactive Lambda Calculus (ILC) for building a concrete implementation of the UC framework, and for elaborating algorithmic entities (i.e., ideal functionalities and simulators) used in UC proofs. In particular, the type system of ILC enforces that well-typed programs are confluent, i.e., they either diverge or evaluate to a single unique value, which makes it easier to reason about the *indistinguishability* of two programs in ILC.

2 OVERVIEW

In order to prove that a cryptographic protocol carries out a given task securely, we first formalize the protocol, henceforth referred to as the real protocol, and its execution in the presence of an adversary and in a given computational environment. We then formalize an ideal protocol that is secure by definition for carrying out the task. In the ideal protocol, parties do not communicate with each other, rather, they rely on an incorruptible trusted party called the *ideal functionality* to meet the requirements of the task at hand. Finally, to show that the real protocol carries out the task securely, we show that running it "emulates" running the ideal protocol for that task, in the sense that an outside observer called the *environment*, which interacts with both the real and ideal protocols, cannot distinguish them apart.

As in [Goldwasser et al. 1989], a protocol is represented as a system of interactive Turing machines (ITMs), in which each ITM represents the program to be run within each party. Each ITM has an

input and output tapes to model inputs received from and outputs given to other ITMs. Additionally, each ITM has a communication tape to model messages sent to and received from the network.

Let π denote the real protocol followed by a set of parties, and let $\mathcal A$ denote an adversary that aims to break the security of π . If $\mathcal A$ is a passive (or semi-honest) adversary, then it can listen to all communications between the parties, and can observe the internal state of corrupted parties. If $\mathcal A$ is an active (or malicious) adversary, then it can additionally take full control of parties and alter messages en route arbitrarily. The adversary communicates with the environment $\mathcal Z$ to provide details of what it observes, and also to receive instructions on how to proceed. Note that parties cannot directly communicate with each other, rather, all communication passes through $\mathcal A$. If the network is synchronous, then $\mathcal A$ is not allowed to interfere with network traffic. If the network if asynchronous, $\mathcal A$ is allowed to delay and reorder messages arbitrarily.

Let ϕ denote the ideal protocol followed by a set of parties relying on the ideal functionality \mathcal{F} , and let \mathcal{S} denote an ideal adversary, also known as a *simulator*, that aims to break the security of ϕ . Here, the parties are *dummy parties*, since they hand received inputs directly to \mathcal{F} for processing, and output whatever is directly returned by \mathcal{F} . Clearly, since the dummy parties do nothing, and \mathcal{F} is secure by definition, it makes sense to define ϕ as secure.

The goal of the environment $\mathcal Z$ is to distinguish between the real protocol and the ideal protocol. Since in the real protocol, $\mathcal Z$ interacts with the adversary $\mathcal A$, in the ideal protocol, $\mathcal Z$ interacts with the simulator $\mathcal S$. The job of $\mathcal S$ is to pretend to be $\mathcal A$ with the aid of $\mathcal F$. The amount of help $\mathcal F$ is able to provide is specified in $\mathcal F$ itself.

3 ILC

 Definition 3.1 (Protocol Emulation). Let π and ϕ be probabilistic polynomial time (p.p.t) protocols. We say that π UC-emulates ϕ if for any p.p.t. adversary $\mathcal A$ there exists a p.p.t. ideal-process adversary $\mathcal S$ such that for any balanced PPT environment $\mathcal Z$ we have:

$$\text{Exec}_{\phi, S, Z} \approx \text{Exec}_{\pi, \mathcal{A}, Z}$$
.

Definition 3.2 (Protocol Emulation w.r.t. the Dummy Adversary). Let π and ϕ be probabilistic polynomial time (p.p.t) protocols. We say that π UC-emulates ϕ if for the dummy adversary $\mathcal D$ there exists a p.p.t. ideal-process adversary $\mathcal S$ such that for any balanced PPT environment $\mathcal Z$ we have:

$$\text{Exec}_{\phi, S, Z} \approx \text{Exec}_{\pi, \mathcal{D}, Z}$$
.

Definition 3.3 (Probability Distribution Ensemble). An ensemble of probability distributions is a family of probability distributions $\{X_{\lambda,z}\}_{\lambda\in\mathbb{N},z\in\{0,1\}^*}$ with index set $\mathbb{N}\times\{0,1\}^*$. The ensembles considered in this work are binary probability distribution ensembles, which describe single bit outputs of computations, where $\lambda\in\mathbb{N}$ represents the security parameter, and $z\in\{0,1\}^*$ represents input.

Definition 3.4 (Indistinguishability). Let X and Y be two binary probability distribution ensembles. We say that X and Y are indistinguishable (written $X \approx Y$) if for any $c, d \in \mathbb{N}$, there exists $\lambda_0 \in \mathbb{N}$ such that for all $\lambda > \lambda_0$ and all $z \in \bigcup_{\lambda < \lambda^d} \{0, 1\}^{\lambda}$,

$$|\Pr[X_{\lambda,z} = 1] - \Pr[Y_{\lambda,z} = 1]| < \lambda^{-c}.$$

Definition 3.5 (Bit Producing ILC Term). Let τ be an ILC term. We say that τ is bit producing if it is closed except for an infinite bitstream free variable σ :Inf and σ :Inf $\vdash \tau$:Bit.

The denotation $[\![\tau]\!]\sigma$, in which a particular σ is given, evaluates to a value of type Bit, and the denotation $[\![\tau]\!]$, in which no σ is specified, evaluates to a binary probability distribution ensemble over types or values?

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Definition 3.6 (Indistinguishability of Bit Producing ILC Terms). Let τ_1 and τ_2 be bit producing ILC terms. We say that τ_1 and τ_2 are indistinguishable terms if the binary probability distribution ensembles $[\![\tau_1]\!]$ and $[\![\tau_2]\!]$ are indistinguishable.

Definition 3.7 (Protocol Emulation in ILC). Let (π_1, \mathcal{F}_1) and (π_2, \mathcal{F}_2) be two protocol-functionality pairs. We say that (π_1, \mathcal{F}_1) UC-emulates (π_2, \mathcal{F}_2) iff for all adversaries \mathcal{F} , there exists an ideal-process adversary \mathcal{S} such that for any environment \mathcal{Z} , ExecUC $_{\mathcal{Z},\mathcal{F},\pi_1,\mathcal{F}_1}$ and ExecUC $_{\mathcal{Z},\mathcal{S},\pi_2,\mathcal{F}_2}$ are bit producing and indistinguishable terms.

Definition 3.8 (Protocol Emulation in ILC). Let π and ϕ be probabilistic polynomial time (p.p.t.) protocols. We say that π UC-emulates ϕ if for any p.p.t. adversary $\mathcal R$, there exists a p.p.t. ideal-process adversary $\mathcal S$ such that for any balanced p.p.t. environment $\mathcal Z$, $\operatorname{Execuc}_{\phi,\mathcal S,\mathcal Z}$ and $\operatorname{Execuc}_{\pi,\mathcal R,\mathcal Z}$ are indistinguishable bit producing terms.

We say that an adversary $\mathcal A$ is valid for a protocol π if $\mathcal A \cup \pi$

Definition 3.9 (Protocol Emulation in ILC). Let π and ϕ be protocols. We say that π UC-emulates ϕ iff for all adversaries \mathcal{A} , there exists an ideal-process adversary \mathcal{S} such that for any environment \mathcal{Z} , EXECUC[π , \mathcal{A} , \mathcal{Z} , λ , σ] and EXECUC[ϕ , \mathcal{S} , \mathcal{Z} , λ , σ] are bit producing and indistinguishable terms.

Definition 3.10 (Balanced Environment). An environment \mathcal{Z} is balanced if the overall length of inputs given by \mathcal{Z} to the parties of the main instance π is at most k times the length of the input to the adversary.

Environment should activate the adversary to allow sending of messages.

4 METATHEORY

- (1) Type soundness
- (2) Confluence

5 IMPLEMENTATION

- (1) Bidirectional type checker
- (2) Replication

6 EXPERIMENTS

- (1) Impossibility of UC commitments using standard assumptions [Canetti and Fischlin 2001].
- (2) UC commitments construction using CRS

Functionality \mathcal{F}_{COM}

 \mathcal{F}_{COM} proceeds as follows, running with parties P_1, \ldots, P_n and an adversary S.

- (1) Upon receiving a value (Commit, sid, P_i , P_j , b) from P_i , where $b \in \{0, 1\}$, record the value b and send the message (Receipt, sid, P_i , P_j) to P_j and S. Ignore any subsequent Commit messages.
- (2) Upon receiving a value (Open, sid, P_i , P_j) from P_i , proceed as follows: If some value b was previously recorded, then send the message (Open, sid, P_i , P_j , b) to P_j and S and halt. Otherwise halt.

```
let F_com = lam S .
let ('Commit, sid, P_i, P_j, b) = rd ?p2f in
req mem b {0,1} in
```

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148
                                                                 execUC(\mathcal{E}, \pi, \mathcal{A}, \mathcal{F})
149
            v z2p z2f z2a p2f p2a a2f.
150
            // The environment chooses SID, conf, and corrupted parties
            let (Corrupted, SID, conf) = \mathcal{E}\{\underline{z2p}, \underline{z2a}, \underline{z2f}\}
151
            // The protocol determines conf'
            let conf' = \pi.cmap(SID, conf)
153
            | \mathcal{A}\{SID, conf, Corrupted, a2z, a2p, a2f\}
            | \mathcal{F}\{SID, conf', Corrupted, f2z, f2p, f2a\}
155
            // Create instances of parties on demand
            let partyMap = ref empty
157
            let newPartyPID = do
               \nu f2pp z2pp.
159
               @partyMap[PID].f2p := f2pp
               @partyMap[PID].z2p := z2pp
161
               | forever do \{m \leftarrow pp2f; (PID, m) \rightarrow f2p\}
               | forever do \{m \leftarrow pp2z; (PID, m) \rightarrow z2p\}
               |\pi\{SID, conf, \underline{p2f}/\underline{pp2z}, \underline{p2z}/\underline{pp2z}\}
163
            let getParty PID =
               if PID ∉ partyMap then newParty PID
165
               return @partyMap[PID]
            | forever do
167
               (PID, m) \leftarrow z2p
               if PID \in Corrupted then Z2P(PID, m) \rightarrow p2a
169
               else m \rightarrow (\text{getParty PID}).\underline{z2p}
170
            | forever do
171
               (PID, m) \leftarrow f2p
172
               if PID \in Corrupted then F2P(PID, m) \rightarrow p2a
               else m \rightarrow (getParty PID).f2p
173
            | forever do
174
               \mid A2P2F(PID, m) \leftarrow a2p
175
                 if PID \in Corrupted then (PID, m) \rightarrow p2f
176
               \mid A2P2Z(PID, m) \leftarrow a2p
177
                 if PID \in Corrupted then (PID, m) \rightarrow p2z
178
```

Fig. 1. Definition of the SaUCy execution model. The environment, are run as concurrent processes. A new instance of the protocol π is created, on demand, for each party PID. Messages sent to honest parties are routed according to their PID; messages sent to corrupted parties are instead diverted to the adversary.

```
wr (('Receipt, sid, P_i, P_j), {P_j, S}) → ?f2p;
let ('Open, sid, P_i, P_j) = rd ?p2f in
wr (('Open, sid, P_i, P_j, b), {P_j, S}) → ?f2p
in
nu f2p, p2f.
| ▷ (F com S)
```

7 RELATED WORK

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195 196 EasyCrypt [Barthe et al. 2011], CertiCrypt [Barthe et al. 2009], CryptoVerif [Blanchet 2007], ProVerif [Blanchet 2005], RF* [Barthe et al. 2014], Cryptol [Lewis and Martin 2003], code-based game-playing proofs [Bellare and Rogaway 2006], symbolic UC [Böhl and Unruh 2016]

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8 CONCLUSION

9 FUTURE WORK

REFERENCES

 Michael Backes, Birgit Pfitzmann, and Michael Waidner. 2007. The reactive simulatability (RSIM) framework for asynchronous systems. *Information and Computation* 205, 12 (2007), 1685–1720.

Gilles Barthe, Cédric Fournet, Benjamin Grégoire, Pierre-Yves Strub, Nikhil Swamy, and Santiago Zanella-Béguelin. 2014. Probabilistic relational verification for cryptographic implementations. In *ACM SIGPLAN Notices*, Vol. 49. ACM, 193–205.

Gilles Barthe, Benjamin Grégoire, Sylvain Heraud, and Santiago Zanella Béguelin. 2011. Computer-aided security proofs for the working cryptographer. In *Annual Cryptology Conference*. Springer, 71–90.

Gilles Barthe, Benjamin Grégoire, and Santiago Zanella Béguelin. 2009. Formal certification of code-based cryptographic proofs. ACM SIGPLAN Notices 44, 1 (2009), 90–101.

Mihir Bellare and Phillip Rogaway. 2006. The security of triple encryption and a framework for code-based game-playing proofs. In *Annual International Conference on the Theory and Applications of Cryptographic Techniques*. Springer, 409–426.

Bruno Blanchet. 2005. ProVerif automatic cryptographic protocol verifier user manual. CNRS, Departement dInformatique, Ecole Normale Superieure, Paris (2005).

Bruno Blanchet. 2007. CryptoVerif: Computationally sound mechanized prover for cryptographic protocols. In *Dagstuhl seminar åÄIJFormal Protocol Verification Applied*. 117.

Florian Böhl and Dominique Unruh. 2016. Symbolic universal composability. *Journal of Computer Security* 24, 1 (2016), 1–38.

Ran Canetti. 2001. Universally composable security: A new paradigm for cryptographic protocols. In Foundations of Computer Science, 2001. Proceedings. 42nd IEEE Symposium on. IEEE, 136–145.

Ran Canetti, Yevgeniy Dodis, Rafael Pass, and Shabsi Walfish. 2007. Universally composable security with global setup. In *Theory of Cryptography Conference*. Springer, 61–85.

Ran Canetti and Marc Fischlin. 2001. Universally composable commitments. In *Annual International Cryptology Conference*. Springer, 19–40.

Ran Canetti and Tal Rabin. 2003. Universal composition with joint state. In *Annual International Cryptology Conference*. Springer, 265–281.

Shafi Goldwasser, Silvio Micali, and Charles Rackoff. 1989. The knowledge complexity of interactive proof systems. SIAM Journal on computing 18, 1 (1989), 186–208.

Dennis Hofheinz and Victor Shoup. 2015. GNUC: A new universal composability framework. *Journal of Cryptology* 28, 3 (2015), 423–508.

Jeffrey R Lewis and Brad Martin. 2003. Cryptol: High assurance, retargetable crypto development and validation. In *Military Communications Conference*, 2003. MILCOM'03. 2003 IEEE, Vol. 2. IEEE, 820–825.

Value variable

Δ R ... ~

A APPENDIX

Value Types

value Types	A, D ::= X	value variable
	unit	Unit value
	nat	Natural number
	$\mid A \times B$	Product
	A+B	Sum type
	! A	Intuitionistic type
	$\mid \mathbf{Rd} A$	Read channel
	$ \mathbf{Wr}A $	Write channel
	U <i>C</i>	Thunk type
Computation Types	$C, D := A \rightarrow C$	Value-consuming computation
1 71	F A	Value-producing computation
Linear Typing Contexts	$\Delta := \cdot \mid \Delta, x : A$	
Intuitionisitic Typing Contexts	$\Gamma ::= \cdot \mid \Gamma, x : A$	

Fig. 2. Syntax of types and typing contexts

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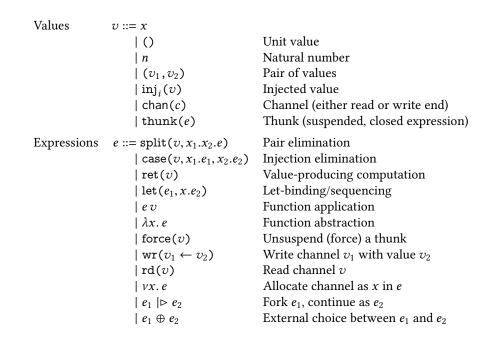


Fig. 3. Syntax of values and expressions

Modes $m, n, p := W \mid R \mid V$ (Write, Read and Value)

 $m \parallel n \Rightarrow p$ The parallel composition of modes m and n is mode p.

$$\frac{m \parallel n \Rightarrow p}{n \parallel m \Rightarrow p} \text{ sym} \qquad \frac{W \parallel V \Rightarrow W}{W \parallel V \Rightarrow W} \text{ wv} \qquad \frac{W \parallel R \Rightarrow W}{W \parallel R \Rightarrow W} \text{ wr} \qquad \frac{R \parallel R \Rightarrow R}{R \parallel R \Rightarrow R} \text{ rr}$$

 $m : n \Rightarrow p$ The sequential composition of modes m and n is mode p.

$$\overline{V: n \Rightarrow n}$$
 v* $\overline{W: V \Rightarrow W}$ WV $\overline{R: n \Rightarrow R}$ r* $\overline{W: R \Rightarrow W}$ WI

Note that in particular, the following mode compositions are *not derivable*:

• W | W \Rightarrow p is not derivable for any mode p

• W; W \Rightarrow p is not derivable for any mode p

Fig. 4. Syntax of modes; sequential and parallel mode composition.

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 Δ ; $\Gamma \vdash e : C \rhd m$ Under Δ and Γ , expression e has type C and mode m.

$$\begin{array}{c} m_1 \; ; \; m_2 \Rightarrow m_3 \\ \Delta_1; \; \Gamma \vdash e_1 : \; \mathbf{F} \; A \rhd m_1 \\ \Delta_2; \; \Gamma \vdash e_2 : \; C \rhd m_2 \\ \hline \Delta_1; \; \Gamma \vdash e_2 : \; C \rhd m_2 \\ \hline \Delta_1; \; \Gamma \vdash e_2 : \; C \rhd m_2 \\ \hline \Delta_1; \; \Delta_2; \; \Gamma, x : \; A \vdash \operatorname{let}(e_1, x.e_2) : \; C \rhd m_3 \end{array} \text{ let } \\ \\ \vdots; \; \Gamma \vdash \operatorname{ret}(v) : \; \mathbf{F} \; (!A) \rhd \mathsf{V} \\ \hline \frac{\Delta_1; \; \Gamma \vdash v : !A \qquad \Delta_2; \; \Gamma, x : \; A \vdash e : \; C \rhd m}{\Delta_1; \; \Gamma \vdash v : !A \qquad \Delta_2; \; \Gamma, x : \; A \vdash \operatorname{let}! \; (v, x.e) : \; C \rhd m} \text{ let!} \\ \hline \frac{\Delta_1; \; \Gamma \vdash v : A \qquad \Delta_2; \; \Gamma, x : \; A \vdash \operatorname{let}! \; (v, x.e) : \; C \rhd m}{\Delta_1; \; \Gamma \vdash v : A \qquad \Delta_2; \; \Gamma \vdash e : \; A \to C \rhd m} \text{ app} \\ \hline \Delta_1; \; \Gamma \vdash v : A \qquad \Delta_2; \; \Gamma \vdash e : \; C \rhd m \end{array} \text{ app}$$

$$\frac{\Delta, x : (\mathbf{Rd} \, A \times !(\mathbf{Wr} \, A)); \Gamma \vdash e : C \rhd m}{\Delta : \Gamma \vdash \nu x, e : C \rhd m} \text{ nu}$$

$$\frac{\Delta; \Gamma \vdash \upsilon : \mathbf{Rd} A}{\Delta \vdash \mathrm{rd}(\upsilon) : \mathbf{F} (A \times (\mathbf{Rd} A)) \rhd R} \operatorname{rd} \qquad \qquad \frac{\Delta_1; \Gamma \vdash \upsilon_1 : \mathbf{Wr} A \qquad \Delta_2; \Gamma \vdash \upsilon_2 : A}{\Delta_1, \Delta_2 \vdash \mathrm{wr}(\upsilon_1 \leftarrow \upsilon_2) : \mathbf{Funit} \rhd W} \operatorname{wr}$$

$$m_{1} \parallel m_{2} \Rightarrow m_{3}$$

$$\Delta_{1}; \Gamma \vdash e_{1} : C \rhd m_{1}$$

$$\Delta_{2}; \Gamma \vdash e_{2} : D \rhd m_{2}$$

$$\Delta_{1}; \Gamma \vdash e_{1} : C \rhd R$$

$$\Delta_{2}; \Gamma \vdash e_{2} : C \rhd R$$

$$\Delta_{1}; \Gamma \vdash e_{1} : C \rhd R$$

$$\Delta_{2}; \Gamma \vdash e_{2} : C \rhd R$$

$$\Delta_{1}; \Gamma \vdash e_{1} : C \rhd R$$

$$\Delta_{2}; \Gamma \vdash e_{2} : C \rhd R$$

$$\Delta_{1}; \Gamma \vdash e_{1} : C \rhd R$$

$$\Delta_{2}; \Gamma \vdash e_{2} : C \rhd R$$

$$\Delta_{1}; \Gamma \vdash e_{1} : C \rhd R$$

$$\Delta_{2}; \Gamma \vdash e_{2} : C \rhd R$$

$$\Delta_{1}; \Gamma \vdash e_{1} : C \rhd R$$

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Channels $\Sigma := \varepsilon \mid \Sigma, c$ Process pool $\pi := \varepsilon \mid \pi, e$ $C ::= \langle \Sigma; \pi \rangle$ Configurations Evaluation contexts E := let(E, x.e) $\mid E \upsilon$ Read contexts $R ::= rd(chan(c)) \oplus R$ $| R \oplus rd(chan(c))$ • $e \longrightarrow e'$ Expression e_1 reduces to e_2 . $\frac{}{\operatorname{let}(\operatorname{ret}(v),x.e)\longrightarrow [v/x]e}\operatorname{let}\frac{}{(\lambda x.e)\,v\longrightarrow [v/x]e}\operatorname{app}\frac{}{\operatorname{force}(\operatorname{thunk}(e))\longrightarrow e}\operatorname{force}$ $\frac{1}{\operatorname{split}((v_1, v_2), x.y.e) \longrightarrow [v_1/x][v_2/y]e} \operatorname{split} \frac{1}{\operatorname{case}(\operatorname{inj}_i(v), x_1.e_1, x_2.e_2) \longrightarrow e_i[v/x_i]} \operatorname{case} \frac{1}{\operatorname{case}(\operatorname{inj}_i(v), x_1.e_2, x_2.e_2)} \longrightarrow e_i[v/x_i]} \operatorname{case} \frac{$ $\overline{C_1} \equiv \overline{C_2}$ Configurations C_1 and C_2 are equivalent. $\frac{\pi_1 \equiv_{\mathsf{perm}} \pi_2}{\langle \Sigma; \pi_1 \rangle \equiv \langle \Sigma; \pi_2 \rangle} \text{ permProcs}$ $C_1 \longrightarrow C_2$ Configuration C_1 reduces to C_2 . $\frac{e \longrightarrow e'}{\langle \Sigma; \pi, E[e] \rangle \longrightarrow \langle \Sigma; \pi, E[e]' \rangle} \text{ local } \frac{}{\langle \Sigma; \pi, E[e_1 \mid \triangleright e_2] \rangle \longrightarrow \langle \Sigma; \pi, e_1, E[e_2] \rangle} \text{ fork}$ $\frac{C_1 \equiv C_1' \qquad C_1' \longrightarrow C_2 \qquad C_2 \equiv C_2'}{C_1 \longrightarrow C_2'} \text{ congr}$ $\frac{\zeta \not \Sigma \Sigma}{\langle \Sigma; \pi, E[\nu x. e] \rangle \longrightarrow \langle \Sigma, c; \pi, E[[(\mathsf{chan}(c), \mathsf{chan}(c))/x]e] \rangle} \text{ nu}$ $\frac{}{\langle \Sigma; \pi, E_1[R[\mathsf{rd}(\mathsf{chan}(c))]], E_2[\mathsf{wr}(\mathsf{chan}(c) \leftarrow v)] \rangle \longrightarrow \langle \Sigma; \pi, E_1[v], E_2[v] \rangle} \text{ rw}$