

SaUCy

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Text of abstract

Additional Key Words and Phrases: keyword1, keyword2, keyword3

1 INTRODUCTION

UC paper [Canetti 2001]. **TODO** Lots!

2 OVERVIEW

3 ILC

Definition 3.1 (Protocol Emulation). Let π and ϕ be probabilistic polynomial time (p.p.t) protocols. We say that π UC-emulates ϕ if for any p.p.t. adversary \mathcal{A} there exists a p.p.t. ideal-process adversary \mathcal{S} such that for any balanced PPT environment \mathcal{Z} we have:

$$\text{EXEC}_{\phi, \mathcal{S}, \mathcal{Z}} \approx \text{EXEC}_{\pi, \mathcal{A}, \mathcal{Z}}.$$

Definition 3.2 (Code-Based Protocol Emulation). Let \mathcal{L}_π and \mathcal{L}_ϕ be p.p.t. program terms. We say that \mathcal{L}_π UC-emulates \mathcal{L}_ϕ if for any p.p.t. adversary term $\mathcal{L}_\mathcal{A}$ there exists a p.p.t. ideal-process term $\mathcal{L}_\mathcal{S}$ such that for any balanced p.p.t. environment term $\mathcal{L}_\mathcal{Z}$ we have:

$$\text{TRACE}_{\mathcal{L}_\phi, \mathcal{L}_\mathcal{S}, \mathcal{L}_\mathcal{Z}} \approx_\epsilon \text{TRACE}_{\mathcal{L}_\pi, \mathcal{L}_\mathcal{A}, \mathcal{L}_\mathcal{Z}}.$$

How to define \approx_ϵ relation? Observational equivalence is a stronger notion than computational equivalence [Comon-Lundh and Cortier 2008]. However, they also show that indistinguishability (based on games) is soundly abstracted by trace equivalence.

4 METATHEORY

- (1) Type soundness
- (2) Confluence

5 IMPLEMENTATION

- (1) Bidirectional type checker
- (2) Replication

6 EXPERIMENTS

- (1) Impossibility of UC commitments using standard assumptions [Canetti and Fischlin 2001].
- (2) UC commitments construction using CRS

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50                                     execUC( $\mathcal{E}, \pi, \mathcal{A}, \mathcal{F}$ )
51  $v \text{ z2p } \text{z2f } \text{z2a } \text{p2f } \text{p2a } \text{a2f}.$ 
52 // The environment chooses SID, conf, and corrupted parties
53 let (Corrupted, SID, conf) =  $\mathcal{E}\{\text{z2p}, \text{z2a}, \text{z2f}\}$ 
54 // The protocol determines conf'
55 let conf' =  $\pi.\text{cmap}(\text{SID}, \text{conf})$ 
56 |  $\mathcal{A}\{\text{SID}, \text{conf}, \text{Corrupted}, \text{a2z}, \text{a2p}, \text{a2f}\}$ 
57 |  $\mathcal{F}\{\text{SID}, \text{conf}', \text{Corrupted}, \text{f2z}, \text{f2p}, \text{f2a}\}$ 
58 // Create instances of parties on demand
59 let partyMap = ref empty
60 let newPartyPID = do
61    $v \text{ f2pp } \text{z2pp}.$ 
62   @partyMap[PID].f2p :=  $\text{f2pp}$ 
63   @partyMap[PID].z2p :=  $\text{z2pp}$ 
64   | forever do  $\{m \leftarrow \text{pp2f}; (\text{PID}, m) \rightarrow \text{f2p}\}$ 
65   | forever do  $\{m \leftarrow \text{pp2z}; (\text{PID}, m) \rightarrow \text{z2p}\}$ 
66   |  $\pi\{\text{SID}, \text{conf}, \text{p2f}/\text{pp2z}, \text{p2z}/\text{pp2z}\}$ 
67 let getParty PID =
68   if PID  $\notin$  partyMap then newParty PID
69   return @partyMap[PID]
70 | forever do
71   (PID, m)  $\leftarrow \text{z2p}$ 
72   if PID  $\in$  Corrupted then  $\text{Z2P}(\text{PID}, m) \rightarrow \text{p2a}$ 
73   else  $m \rightarrow (\text{getParty PID}).\text{z2p}$ 
74 | forever do
75   (PID, m)  $\leftarrow \text{f2p}$ 
76   if PID  $\in$  Corrupted then  $\text{F2P}(\text{PID}, m) \rightarrow \text{p2a}$ 
77   else  $m \rightarrow (\text{getParty PID}).\text{f2p}$ 
78 | forever do
79   |  $\text{A2P2F}(\text{PID}, m) \leftarrow \text{a2p}$ 
80   if PID  $\in$  Corrupted then  $(\text{PID}, m) \rightarrow \text{p2f}$ 
81   |  $\text{A2P2Z}(\text{PID}, m) \leftarrow \text{a2p}$ 
82   if PID  $\in$  Corrupted then  $(\text{PID}, m) \rightarrow \text{p2z}$ 

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Fig. 1. Definition of the SaUCy execution model. The environment, are run as concurrent processes. A new instance of the protocol π is created, on demand, for each party PID. Messages sent to honest parties are routed according to their PID; messages sent to corrupted parties are instead diverted to the adversary.

Functionality \mathcal{F}_{COM}

\mathcal{F}_{COM} proceeds as follows, running with parties P_1, \dots, P_n and an adversary S .

- (1) Upon receiving a value (Commit, sid, P_i, P_j, b) from P_i , where $b \in \{0, 1\}$, record the value b and send the message (Receipt, sid, P_i, P_j) to P_j and S . Ignore any subsequent Commit messages.
- (2) Upon receiving a value (Open, sid, P_i, P_j) from P_i , proceed as follows: If some value b was previously recorded, then send the message (Open, sid, P_i, P_j, b) to P_j and S and halt. Otherwise halt.

let $\text{F_com} = \text{lam } S .$

let (Commit, sid, P_i, P_j, b) = rd ?p2f in

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99   req mem b {0,1} in
100   wr (('Receipt, sid, P_i, P_j), {P_j, S}) → ?f2p ;
101   let ('Open, sid, P_i, P_j) = rd ?p2f in
102   wr (('Open, sid, P_i, P_j, b), {P_j, S}) → ?f2p
103 in
104   nu f2p, p2f .
105   | ▷ (F_com S)
106

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7 RELATED WORK

EasyCrypt [Barthe et al. 2011], CertiCrypt [Barthe et al. 2009], CryptoVerif [Blanchet 2007], ProVerif [Blanchet 2005], RF* [Barthe et al. 2014], Cryptol [Lewis and Martin 2003], code-based game-playing proofs [Bellare and Rogaway 2006], symbolic UC [Böhl and Unruh 2016]

8 CONCLUSION

9 FUTURE WORK

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A APPENDIX

Value Types	$A, B ::= x$	Value variable
	unit	Unit value
	nat	Natural number
	$A \times B$	Product
	$A + B$	Sum type
	!A	Intuitionistic type
	Rd A	Read channel
	Wr A	Write channel
	U C	Thunk type
Computation Types	$C, D ::= A \rightarrow C$	Value-consuming computation
	F A	Value-producing computation
Linear Typing Contexts	$\Delta ::= \cdot \mid \Delta, x : A$	
Intuitionistic Typing Contexts	$\Gamma ::= \cdot \mid \Gamma, x : A$	

Fig. 2. Syntax of types and typing contexts

Values	$v ::= x$	
	()	Unit value
	n	Natural number
	(v_1, v_2)	Pair of values
	inj_i (v)	Injected value
	chan (c)	Channel (either read or write end)
	thunk (e)	Thunk (suspended, closed expression)
Expressions	$e ::= \text{split}(v, x_1.x_2.e)$	Pair elimination
	case $(v, x_1.e_1, x_2.e_2)$	Injection elimination
	ret (v)	Value-producing computation
	let $(e_1, x.e_2)$	Let-binding/sequencing
	$e \ v$	Function application
	$\lambda x. e$	Function abstraction
	force (v)	Unsuspend (force) a thunk
	wr $(v_1 \leftarrow v_2)$	Write channel v_1 with value v_2
	rd (v)	Read channel v
	$\nu x. e$	Allocate channel as x in e
	$e_1 \triangleright e_2$	Fork e_1 , continue as e_2
	$e_1 \oplus e_2$	External choice between e_1 and e_2

Fig. 3. Syntax of values and expressions

Modes $m, n, p ::= W \mid R \mid V$ (Write, Read and Value)

$m \parallel n \Rightarrow p$ The parallel composition of modes m and n is mode p .

$$\frac{m \parallel n \Rightarrow p}{n \parallel m \Rightarrow p} \text{sym} \quad \frac{}{W \parallel V \Rightarrow W} \text{wv} \quad \frac{}{W \parallel R \Rightarrow W} \text{wr} \quad \frac{}{R \parallel R \Rightarrow R} \text{rr}$$

$m ; n \Rightarrow p$ The sequential composition of modes m and n is mode p .

$$\frac{}{V ; n \Rightarrow n} \text{v*} \quad \frac{}{W ; V \Rightarrow W} \text{wv} \quad \frac{}{R ; n \Rightarrow R} \text{r*} \quad \frac{}{W ; R \Rightarrow W} \text{wr}$$

Note that in particular, the following mode compositions are *not derivable*:

- $W \parallel W \Rightarrow p$ is *not* derivable for any mode p
- $W ; W \Rightarrow p$ is *not* derivable for any mode p

Fig. 4. Syntax of modes; sequential and parallel mode composition.

$\Delta; \Gamma \vdash e : C \triangleright m$ Under Δ and Γ , expression e has type C and mode m .

$$\begin{array}{c} \frac{m_1 ; m_2 \Rightarrow m_3}{\Delta_1; \Gamma \vdash e_1 : \mathbf{F}A \triangleright m_1} \quad \frac{\Delta_2, x : A; \Gamma \vdash e_2 : C \triangleright m_2}{\Delta_1, \Delta_2; \Gamma, x : A \vdash \text{let}(e_1, x.e_2) : C \triangleright m_3} \text{let} \\ \frac{\Delta; \Gamma \vdash v : A}{\Delta; \Gamma \vdash \text{ret}(v) : \mathbf{F}A \triangleright V} \text{ret} \quad \frac{\Delta_1; \Gamma \vdash v : !A \quad \Delta_2; \Gamma, x : A \vdash e : C \triangleright m}{\Delta_1, \Delta_2; \Gamma, x : A \vdash \text{let}!(v, x.e) : C \triangleright m} \text{let!} \\ \frac{; \Gamma \vdash v : A}{; \Gamma \vdash \text{ret}(v) : \mathbf{F}(!A) \triangleright V} \text{ret!} \quad \frac{\Delta_1; \Gamma \vdash v : A \quad \Delta_2; \Gamma \vdash e : A \rightarrow C \triangleright m}{\Delta_1, \Delta_2; \Gamma \vdash e v : C \triangleright m} \text{app} \\ \frac{\Delta; \Gamma \vdash e : C \triangleright m}{\Delta; \Gamma \vdash \lambda x. e : A \rightarrow C \triangleright m} \text{lam} \quad \frac{\Delta, x : (\mathbf{Rd}A \times !(\mathbf{Wr}A)); \Gamma \vdash e : C \triangleright m}{\Delta; \Gamma \vdash vx. e : C \triangleright m} \text{nu} \\ \frac{\Delta; \Gamma \vdash v : \mathbf{Rd}A}{\Delta \vdash \text{rd}(v) : \mathbf{F}(A \times (\mathbf{Rd}A)) \triangleright R} \text{rd} \quad \frac{\Delta_1; \Gamma \vdash v_1 : \mathbf{Wr}A \quad \Delta_2; \Gamma \vdash v_2 : A}{\Delta_1, \Delta_2 \vdash \text{wr}(v_1 \leftarrow v_2) : \mathbf{F}unit \triangleright W} \text{wr} \\ \frac{m_1 \parallel m_2 \Rightarrow m_3 \quad \Delta_1; \Gamma \vdash e_1 : C \triangleright m_1 \quad \Delta_2; \Gamma \vdash e_2 : D \triangleright m_2}{\Delta_1, \Delta_2 \vdash e_1 \mid e_2 : D \triangleright m_3} \text{fork} \quad \frac{\Delta_1; \Gamma \vdash e_1 : C \triangleright R \quad \Delta_2; \Gamma \vdash e_2 : C \triangleright R}{\Delta_1, \Delta_2 \vdash e_1 \oplus e_2 : C \triangleright R} \text{choice} \end{array}$$

Channels	$\Sigma ::= \varepsilon \mid \Sigma, c$
Process pool	$\pi ::= \varepsilon \mid \pi, e$
Configurations	$C ::= \langle \Sigma; \pi \rangle$
Evaluation contexts	$E ::= \text{let}(E, x.e)$ $\mid E v$ $\mid \bullet$
Read contexts	$R ::= \text{rd}(\text{chan}(c)) \oplus R$ $\mid R \oplus \text{rd}(\text{chan}(c))$ $\mid \bullet$

$e \longrightarrow e'$ Expression e_1 reduces to e_2 .

$$\frac{}{\text{let}(\text{ret}(v), x.e) \longrightarrow [v/x]e} \text{let} \quad \frac{}{(\lambda x. e) v \longrightarrow [v/x]e} \text{app} \quad \frac{}{\text{force}(\text{thunk}(e)) \longrightarrow e} \text{force}$$

$$\frac{}{\text{split}((v_1, v_2), x.y.e) \longrightarrow [v_1/x][v_2/y]e} \text{split} \quad \frac{}{\text{case}(\text{inj}_i(v), x_1.e_1, x_2.e_2) \longrightarrow e_i[v/x_i]} \text{case}$$

$C_1 \equiv C_2$ Configurations C_1 and C_2 are equivalent.

$$\frac{\pi_1 \equiv_{\text{perm}} \pi_2}{\langle \Sigma; \pi_1 \rangle \equiv \langle \Sigma; \pi_2 \rangle} \text{permProcs}$$

$C_1 \longrightarrow C_2$ Configuration C_1 reduces to C_2 .

$$\frac{e \longrightarrow e'}{\langle \Sigma; \pi, E[e] \rangle \longrightarrow \langle \Sigma; \pi, E[e'] \rangle} \text{local} \quad \frac{}{\langle \Sigma; \pi, E[e_1 \mid \triangleright e_2] \rangle \longrightarrow \langle \Sigma; \pi, e_1, E[e_2] \rangle} \text{fork}$$

$$\frac{C_1 \equiv C'_1 \quad C'_1 \longrightarrow C_2 \quad C_2 \equiv C'_2}{C_1 \longrightarrow C'_2} \text{congr}$$

$$\frac{c \notin \Sigma}{\langle \Sigma; \pi, E[vx.e] \rangle \longrightarrow \langle \Sigma, c; \pi, E[(\text{chan}(c), \text{chan}(c))/x]e \rangle} \text{nu}$$

$$\frac{}{\langle \Sigma; \pi, E_1[R[\text{rd}(\text{chan}(c))]], E_2[\text{wr}(\text{chan}(c) \leftarrow v)] \rangle \longrightarrow \langle \Sigma; \pi, E_1[v], E_2[()] \rangle} \text{rw}$$