Monday, October 18, 2021 12:18 PI

- Alex (2) aslying

5.4 (a) The resistivity of a p-type GaAs material at T=300 K is required to be $\rho=0.35\,(\Omega\text{-cm})$. Determine the acceptor impurity concentration that is required. What is the hole mobility corresponding to this impurity concentration? (b) An n-type GaAs material is required to have a conductivity of $\sigma=120\,(\Omega\text{-cm})^{-1}$. What donor impurity concentration is required and what is the corresponding electron mobility?

$$\rho = \frac{1}{e \mu_1 N_0} \times = \mu_1 N_0$$

$$0.35 = \frac{1}{(16 \times 10^{17}) \times} \times = 1.786 \times 10^{17}$$

a.) From Figure 5.2 and 5.3,
$$N_a \approx 8 \times 10^{16}/\text{cm}^3$$

$$\mu_P = \frac{1.786 \times 10^{17}}{8 \times 10^{16}} = 220 \text{ cm}^2/\text{N.s}$$

b.)
$$\sigma = e \mu_n N_d = 120 / \Omega cm$$
 $7.5 \times 10^{20} = \mu_n N_d \text{ where } N_d \approx Z \times 10^{17} / \text{cm}^3$
 $\mu_n = \frac{7.5 \times 10^{20}}{7 \times 10^{17}} = \frac{3800 \text{ cm}^2 / \text{N.s}}{3800 \text{ cm}^2 / \text{N.s}}$

5.14 In a particular semiconductor material, $\mu_n = 1000 \text{ cm}^2/\text{V-s}$, $\mu_p = 600 \text{ cm}^2/\text{V-s}$, and $N_C = N_V = 10^{19} \text{ cm}^{-3}$. These parameters are independent of temperature. The measured conductivity of the intrinsic material is $\sigma = 10^{-6} (\Omega - \text{cm})^{-1}$ at T = 300 K. Find the conductivity at T = 500 K.

$$\sigma = e \left(\mu_n + \mu_p \right) n_i \left| n_i^2 - N_c N_V \exp \left(- \frac{\epsilon_g}{n_i} \right) \right|$$
Conductivity

$$\begin{aligned}
& = \frac{6}{e(\mu_{1} + 4)} = \frac{10^{-6}}{(1.6 \times 10^{3})(1000 + 600)} = 3.1 \times 10^{3} \text{ cm}^{3} \\
& = \text{ int } \ln\left(\frac{N_{c}N_{V}}{n_{1}^{12}}\right) = \left(\frac{26 \times 10^{-3}}{3}\right) \ln\left(\frac{(10^{9})(10^{9})}{(3.9 \times 10^{3})^{2}}\right) = 1.122 \text{ eV} \\
& = \frac{26 \times 10^{-3}}{300} = \frac{500}{300} = 0.432 \text{ eV} \\
& = \frac{1.122}{0.432} = 2.29 \times 10^{13} / \text{cm}^{3} \\
& = \frac{1.122}{0.432} = 2.29 \times 10^{13} / \text{cm}^{3}
\end{aligned}$$

$$\sigma = \left(\frac{1.6 \times 10^{-19}}{300}\right) \left(\frac{1.000 + 600}{0.432}\right) \left(\frac{2.29 \times 10^{13}}{300}\right) = \frac{5.86 \times 10^{-3}}{300} \cdot \frac{1.122}{300} = \frac{1.122}{0.432} =$$

5.16 An n-type silicon material at T = 300 K has a conductivity of 0.25 (Ω -cm)⁻¹. (a) What is the donor impurity concentration and the corresponding electron mobility? (b) Determine the expected conductivity of the material at (i) T = 250 K and (ii) T = 400 K.

o.)
$$\sigma = e \mu_n N_d$$

o.25 = $(1.6 \times 10^{-19}) \mu_n N_d$
From Figure 5.3, $N_d \approx 1.2 \times 10^{15} / \text{cm}^3$
 $\frac{0.25}{16 \times 10^{15}} = \mu_n = \frac{1300 \text{ cm}^2}{1300 \text{ cm}^2} = \frac{13$

5.1 yields
$$\mu_{n} \approx 1800 \text{ cm}^{2}/v.s$$

$$\sigma = (1.6 \times 10^{-19})(1800)(1.2 \times 10^{15}) = 0.346/\Omega \cdot cm$$

$$\text{[ii]} \quad T = 400 \text{ K} = 127 ° \text{C}$$
5.1 yields $\mu_{n} \approx 670 \text{ cm}^{2}/v.s$

$$\sigma = (1.6 \times 10^{-19})(670)(1.2 \times 10^{15}) = 0.129/\Omega \cdot cm$$

5.32 The hole concentration in p-type GaAs is given by $p(x) = 10^{16}(1 + x/L)^2$ cm⁻³ for $-L \le x \le 0$ where $L = 12 \mu m$. The hole diffusion coefficient is $D_p = 10$ cm²/s. Calculate the hole diffusion current density at (a) x = 0, $(b) x = -6 \mu m$, and $(c) x = -12 \mu m$.

$$J_{p} = -e D_{p} \frac{dp}{dx} = -e D_{p} \frac{d}{dx} \left[10^{16} \left(1 + \frac{x}{L} \right)^{2} \right]$$

$$= -e D_{p} \left[\frac{10^{16}}{L} \left(\frac{2(1 + \frac{x}{L})}{L} \right) \right]$$

or.)
$$x = 0 \, \mu M$$

$$J_p = \frac{-(1.6 \times 10^{-17})(10)(10^{16})(2)}{12 \times 10^{-4}} = \frac{-26.7 \, \text{A/cm}^2}{12 \times 10^{-4}}$$

$$J_{p} = \frac{-(1.6 \times 10^{-12})(10)(10^{16})(2)(1-\frac{6}{12})}{12 \times 10^{-4}} = \frac{-13.3 \, \text{A/cm}^{2}}{12 \times 10^{-4}}$$

$$J_{p} = \frac{-(1.6 \times 10^{-12})(10)(10)(10)(1-\frac{12}{12})}{12 \times 10^{-4}} = \frac{0.4}{12}$$

5.38 In n-type silicon, the Fermi energy level varies linearly with distance over a short range. At x = 0, $E_F - E_{Fi} = 0.4$ eV and, at $x = 10^{-3}$ cm, $E_F - E_{Fi} = 0.15$ eV. (a) Write the expression for the electron concentration over the distance. (b) If the electron diffusion coefficient is $D_n = 25$ cm²/s, calculate the electron diffusion current density at (i) x = 0 and $(ii) x = 5 \times 10^{-4}$ cm.

$$n = n \cdot \exp\left(\frac{E_F - E_{F_f}}{nT}\right)$$

E_f =
$$E_{f_i} = ax + b$$

 $E_f - E_{f_i} = a(0) + b$
 $b = 0.4$

$$E_{F} = e_{F} = a(10^{-3}) + 0.4 = 0.15$$

 $a = -2.5 \times 10^{2} \text{ eV/cm}$

$$E_F - E_{F_i} = 0.4 - 2.5 \times 10^2 x$$
 $n = n_i \exp\left(\frac{0.4 - 2.5 \times 10^2 x}{nT}\right)$

T= 300H

6.)
$$J_n = eD_n \frac{dn}{dx} = eD_n n_i \left[\frac{-2.5 \times 10^2}{hT} \right] exp \left[\frac{0.4 - 2.5 \times 10^2 \times 10^2}{hT} \right]$$

$$J_{n} = \frac{-(1.6 \times 10^{-19})(25)(1.5 \times 10^{10})(2.5 \times 10^{2})}{0.0259} \exp \left[\frac{0.4 - 2.5 \times 10^{2} \times 10^{2}}{kT}\right]$$

$$J_n = -5.79 \times 10^4 \text{ exp} \left[\frac{0.4 - 2.5 \times 10^2 \text{ X}}{\text{ht}} \right]$$

[i]
$$x = 0_{pm}$$

$$J_n = -5.79 \times 10^4 \exp \left[\frac{0.4 - 2.5 \times 10^3 (0)}{ht} \right]$$

$$J_n = -2.95 \times 10^3 A/cm^2$$

[ii]
$$x = 5 \mu m$$

$$J_n = -5.79 \times 10^4 \text{ exp} \left[\frac{0.4 - 2.5 \times 10^5 (5)}{\text{hT}} \right]$$

$$J_n = -23.7 \text{ A/cm}^2$$

6.2 GaAs, at T = 300 K, is uniformly doped with acceptor impurity atoms to a concentration of $N_a = 2 \times 10^{16}$ cm⁻³. Assume an excess carrier lifetime of 5×10^{-7} s.

(a) Determine the electron-hole recombination rate if the excess electron concentration is $\delta n = 5 \times 10^{14}$ cm⁻³. (b) Using the results of part (a), what is the lifetime of holes?

$$P_{0} = N_{o} = \frac{2 \times 10^{16} / \text{cm}^{3}}{(1.8 \times 10^{6})^{2}} = \frac{(1.8 \times 10^{6})^{2}}{2 \times 10^{16}} = 1.62 \times 10^{-7} / \text{cm}^{3}$$

(a.)
$$R' = \frac{4n}{2n\delta} = \frac{5 \times 10^{14}}{5 \times 10^{-7}} = \frac{10^{27}}{\text{cm} \cdot \text{s}}$$

6.)
$$R_{p} = \frac{P_{0}}{\tau_{pt}} = \frac{n_{0}}{\tau_{nt}} = \frac{n_{0}}{\tau_{no}}$$

$$\gamma_{pt} = \frac{P_{0}}{n_{0}} (\gamma_{no}) = \frac{(2 \times 10^{18})}{(1.62 \times 10^{-4})} (S \times 10^{-7})$$

Consider a silicon sample at T = 300 K that is uniformly doped with acceptor impurity atoms at a concentration of $N_a = 10^{16}$ cm⁻³. At t = 0, a light source is turned on generating excess carriers uniformly throughout the sample at a rate of $g' = 8 \times 10^{20}$ cm⁻³ s⁻¹. Assume the minority carrier lifetime is $\tau_{n0} = 5 \times 10^{-7}$ s, and assume mobility values of $\mu_n = 900$ cm² /V-s and $\mu_p = 380$ cm² /V-s. (a) Determine the conductivity of the silicon as a function of time for $t \ge 0$. (b) What is the value of conductivity at (i) t = 0 and (ii) $t = \infty$?

$$P_0 = N_0 = 10^{6} \text{ cm}^3$$

$$n_0 = \frac{m_i^2}{P_0} = \frac{(1.5 \times 10)^2}{10^{16}} = 2.25 \times 10^{6} \text{ cm}^3$$

α.)
$$\sigma = e\mu_{n} (n_{0} + \Delta n) + e\mu_{p} (p_{0} + \Delta p)$$

$$= e\mu_{p}p_{0} + e(\mu_{n} + \mu_{p}) \Delta n$$

$$\Delta n = \Delta p = q' r_{n_{0}} (1 - e^{-t/r_{n_{0}}})$$

$$= (8 \times 10^{20}) (5 \times 10^{-7}) (1 - e^{-t/r_{n_{0}}})$$

$$= 4 \times 10^{15} (1 - e^{-t/r_{n_{0}}})$$

$$\sigma = (1.6 \times 10^{-17}) (380) (10^{16}) + (16 \times 10^{-17}) (900 + 380) [4 \times 10^{15} (1 - e^{-t/r_{n_{0}}})]$$

$$\sigma = 0.61 + 0.082 (1 - e^{-t/r_{n_{0}}}) / \Omega. cm$$

6.)
[ii]
$$6(\infty) = 0.61/\Omega.cm$$
[iii]
 $6(\infty) = 0.69/\Omega.cm$

6.14 A bar of silicon at T = 300 K has a length of L = 0.05 cm and a cross-sectional area of $A = 10^{-5}$ cm². The semiconductor is uniformly doped with $N_d = 8 \times 10^{15}$ cm⁻³ and $N_a = 2 \times 10^{15}$ cm⁻³. A voltage of 10 V is applied across the length of the material. For t < 0, the semiconductor has been uniformly illuminated with light, producing an excess carrier generation rate of $g' = 8 \times 10^{20}$ cm⁻³ s⁻¹. The minority carrier lifetime is $\tau_{p0} = 5 \times 10^{-7}$ s. At t = 0, the light source is turned off. Determine the current in the semiconductor as a function of time for $t \ge 0$.

$$V = IR$$

$$I = \frac{V}{R} \qquad R = \frac{L}{6A}$$

$$I = \frac{6A}{L} (V)$$

$$N_{s} = N_{s} + N_{o} = 8 \times 10^{18} + 2 \times 10^{18} = 10^{16} / \text{cm}^{3}$$

$$u_{n} \approx 1300 \quad \text{cm}^{2}/V.5 \qquad \mu_{p} \approx 400 \quad \text{cm}^{2}/V.5$$

$$\sigma = e \mu_{n} n_{o} + e \left(M_{n} + M_{f}\right) \Delta p$$

$$\Delta p = g' \quad \chi_{po} e^{-t/\chi_{po}} = \left(8 \times 10^{10}\right) \left(5 \times 10^{-7}\right) e^{-t/\chi_{po}}$$

$$\Delta p = 4 \times 10^{14} e^{-t/\chi_{po}} / \text{cm}^{3}$$

$$\sigma = (16 \times 10^{-17}) \left(1300\right) \left(8 \times 10^{15} - 2 \times 10^{19}\right) + \left(16 \times 10^{-17}\right) \left(1300 + 400\right) \left(t \times 10^{19} e^{-t/\chi_{po}}\right)$$

$$\sigma = 1. \quad 25 + 0.11 e^{-t/\chi_{po}} \left(10^{-5}\right) \left(10\right)$$

$$I = \frac{\left(125 + 0.11 e^{-t/\chi_{po}}\right) \left(10^{-5}\right) \left(10\right)}{0.05}$$

6.20 The x = 0 end of an $N_a = 1 \times 10^{14}$ cm⁻³ doped semi-infinite ($x \ge 0$) bar of silicon maintained at T = 300 K is attached to a "minority carrier digester" which makes $n_p = 0$ at x = 0 (n_p is the minority carrier electron concentration in a p-type semiconductor). The electric field is zero. (a) Determine the thermal-equilibrium values of n_{p0} and p_{p0} . (b) What is the excess minority carrier concentration at x = 0? (c) Derive the expression for the steady-state excess minority carrier concentration as a function of x.

$$P_{p} = P_{po} + \Delta p = n_{po} + 0 = P_{po}$$

$$N_{on} = 10^{14} / \text{cm}^{3}$$

$$P_{p} = N_{on} = 10^{14} / \text{cm}^{3}$$

$$n_{po} P_{po} = n_{o}^{2}$$

$$n_{po} = \frac{n_{o}^{2}}{P_{po}} = \frac{(1.5 \times 10^{14})^{2}}{10^{14}} = \frac{2.25 \times 10^{6} / \text{cm}^{3}}{10^{14}}$$

$$\Delta n = n_{p} - n_{po}$$

$$X = 0 \quad n_{p} = 0$$

$$\Delta n = 0 - 2.25 \times 10^{6} = \frac{-2.25 \times 10^{6} / \text{cm}^{3}}{(n_{onority} \text{ corrier})}$$

$$(.) \quad x = 0 \quad E = 0 \quad g' \approx 0 \quad \frac{\delta(np)}{\Delta t} = 0$$

$$D_n \frac{\lambda'(\Delta n)}{\Delta x^2} - \frac{\Delta n}{\gamma_{n0}} = 0$$

$$L^2 = D_n \gamma_{n0}$$

n, =
$$A \exp\left(\frac{x}{L_n}\right) + B \exp\left(\frac{x}{L_n}\right)$$

$$B = 0; x > 0$$

$$A = 0$$
; $x < 0$

$$\Delta n = \Delta n (0) \exp \left(\frac{-x}{L_n}\right); \quad x \ge 0$$

$$\Delta n = \Delta n (0) \exp \left(\frac{x}{L_n}\right); \quad x \le 0$$

6.32 Consider n-type silicon doped at $N_d = 5 \times 10^{15}$ cm⁻³. It is found that $E_{Fn} - E_F = 1.02 \times 10^{-3}$ eV. (a) What is the excess carrier concentration? (b) Determine $E_{Fn} - E_{Fi}$. (c) Calculate $E_{Fi} - E_{Fp}$.

a.)
$$E_{r_n} - E_{r_n} = (E_{r_n} - E_{r_n}) - (E_{r_n} - E_{r_n})$$

$$= hT \left[ln \left(\frac{n_0 + \Delta n}{n_1} \right) \right] - kT \left[ln \left(\frac{n_0}{n_1} \right) \right]$$

$$= hT \left[ln \left(\frac{n_0 + \Delta n}{n_0} \right) \right]$$

$$1.02 \times 10^{-3} = (0.0259) ln \left[\frac{5 \times 10^{15} + \Delta n}{5 \times 10^{15}} \right]$$

$$5 \times 10^{15} + \Delta n = 5 \times 10^{15} exp \left[\frac{1.02 \times 10^{-3}}{0.0259} \right]$$

$$\Delta_n = 2 \times 10^{14} / cm^3$$

$$E_{F_{n}} - E_{F_{i}} = hT \left[ln \left(\frac{n_{0} + 4n}{n_{i}} \right) \right]$$

$$= (0.0259) l_{n} \left[\frac{5 \times 10^{15} + 2 \times 10^{17}}{1.5 \times 10^{10}} \right]$$

$$= 0.33 \text{ eV}$$

c.)
$$E_{F_i} - E_{F_p} = hT \left[ln \left(\frac{\Delta p}{n_i} \right) \right]$$

$$= \left(0.0259 \right) ln \left[\frac{2 \times 10^{17}}{1.5 \times 10^{10}} \right]$$

$$= \left[0.25 \text{ eV} \right]$$