

Definition: Open Ball

Let (M, d) be a metric space, an open ball of radius $\varepsilon > 0$:

$$B(x, \varepsilon) \stackrel{\text{def}}{=} \{y : d(x, y) < \varepsilon\}$$