

Theorem: Scalar Multiple of Identity is Identity

$$a0 = 0 \text{ for every } a \in \mathbb{F}$$

Proof

$$a0 = a(0 + 0) = a0 + a0$$

So by adding the inverse of $a0$ to each side, you get $0 = a0$, as needed. ■