Proposition: Finite Geometric Sum Finite Geometric sum, for any $x \geq 0$:

Let
$$S = \sum_{i=0}^{k} x^{i}$$
, then we have

therefore

$$xS - S$$

$$xS - S = \sum_{i=0}^{k} x^{i+1} - \sum_{i=0}^{k} x^{i} = x^{k+1} - x^{0} = x^{k+1} - 1$$

$$-\sum_{i=1}^{k}x^{i}$$

 $S = \frac{x^{k+1} - 1}{x - 1}$

 $\sum_{i=0}^{k} x^i = \frac{x^{k+1} - 1}{x - 1}$



