## Definition: Cross Product

The cross product of two vectors  $\vec{a}, \vec{b} \in \mathbb{R}^3$  is a vector  $\vec{c}$  perpendicular to both  $\vec{a}$  and  $\vec{b}$  and whose magnitude is equal to the area of the parallelogram generated by  $\vec{a}$  and  $\vec{b}$ :  $\vec{a} \times \vec{b} \stackrel{\mathbb{D}}{=} ||a|| \, ||b|| \sin(\theta) \, \vec{n}$ 

 $\vec{a} \times \vec{b} \stackrel{\nu}{=} ||a|| \, ||b|| \sin{(\theta)} \, \vec{n}$  with  $\theta$  being the angle in the range  $[0,\pi]$  between  $\vec{a}$  and  $\vec{b}$  and  $\vec{n}$  a unit vector that is normal to both  $\vec{a}$  and  $\vec{b}$  oriented with respect to the right hand rule.