

Theorem: 0 Times Vector is Identity

$$0v = 0 \text{ for every } v \in V$$

Proof

$$0v = (0 + 0)v = 0v + 0v$$

by distributivity, then adding the inverse of $0v$ to both sides tells us that

$$0 = 0v$$

