

Lenguajes de Programación - Examen 2

Integrantes

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Ejercicios

1. Evalua la siguiente expresion usando representacion de ambientes en todos los casos:

```
{with {x {+ 3 2}}
  {with {y {+ 1 2}}
    {with {z 7}
      {with {foo {fun{x} {+ x {+ y z}}}}
        {with {x 3}
          {with {y {+ 2 2}}
            {with z {+ 1 1}}
              {with {mas-foo {fun {y} {* 1 {* x y}}}}
                {with {x 2}
                  {with {y 1}
                    {foo 1}}}}}}}}}}}}
```

- Evaluacion perezosa y alcance estatico.

Solución:

Evaluación	Ambiente
<pre>{with {x {+ 3 2}} {with {y {+ 1 2}} {with {z 7} {with {foo {fun{x} {+ x {+ y z}}}} {with {x 3} {with {y {+ 2 2}} {with z {+ 1 1}} {with {mas-foo {fun {y} {* 1 {* x y}}}} {with {x 2}</pre>	

```
      {with {y 1}
        {foo 1}}}}}}}}}}}}}
```

```
{with {y {+ 1 2}}
  {with {z 7}
    {with {foo {fun{x} {+ x {+ y z}}}}
      {with {x 3}
        {with {y {+ 2 2}}
          {with {z {+ 1 1}}
            {with {mas-foo {fun {y} {* 1 {* x y}}}}
              {with {x 2}
                {with {y 1}
                  {foo 1}}}}}}}}}}}}}
```

x		{+ 3 2}
---	--	---------

```
{with {foo {fun{x} {+ x {+ y z}}}}
  {with {x 3}
    {with {y {+ 2 2}}
      {with {z {+ 1 1}}
        {with {mas-foo {fun {y} {* 1 {* x y}}}}
          {with {x 2}
            {with {y 1}
              {foo 1}}}}}}}}}}
```

z		7
---	--	---

y		{+ 1 2}
---	--	---------

x		{+ 3 2}
---	--	---------

```
{with {x 3}
  {with {y {+ 2 2}}
    {with {z {+ 1 1}}
```

```
{with {mas-foo {fun {y} {* 1 {* x y}}}}
  {with {x 2}
    {with {y 1}
      {foo 1}}}}}}
```

foo		{fun{x} {+ x {+ y z}}}
z		7
y		{+ 1 2}
x		{+ 3 2}

```
{with {y {+ 2 2}}
  {with z {+ 1 1}}
    {with {mas-foo {fun {y} {* 1 {* x y}}}}
      {with {x 2}
        {with {y 1}
          {foo 1}}}}}}
```

x		3
foo		{fun{x} {+ x {+ y z}}}
z		7
y		{+ 1 2}
x		{+ 3 2}

```
{with z {+ 1 1}}
  {with {mas-foo {fun {y} {* 1 {* x y}}}}
    {with {x 2}
      {with {y 1}
        {foo 1}}}}}}
```

y		{+ 2 2}
---	--	---------

```
-----  
x   |      3  
-----  
foo  | {fun{x} {+ x {+ y z}}}  
-----  
z   |      7  
-----  
y   |    {+ 1 2}  
-----  
x   |    {+ 3 2}  
-----
```

```
{with {mas-foo {fun {y} {* 1 {* x y}}}}  
  {with {x 2}  
    {with {y 1}  
      {foo 1}}}}
```

```
-----  
z   |    {+ 1 1}  
-----  
y   |    {+ 2 2}  
-----  
x   |      3  
-----  
foo  | {fun{x} {+ x {+ y z}}}  
-----  
z   |      7  
-----  
y   |    {+ 1 2}  
-----  
x   |    {+ 3 2}  
-----
```

```
{with {x 2}  
  {with {y 1}  
    {foo 1}}}}
```

```
-----  
mas-foo | {fun {y} {* 1 {* x y}}  
-----  
z   |    {+ 1 1}  
-----  
y   |    {+ 2 2}  
-----  
x   |      3  
-----
```

```
-----  
foo   | {fun{x} {+ x {+ y z}}}  
-----  
z     |      7  
-----  
y     |    {+ 1 2}  
-----  
x     |    {+ 3 2}  
-----
```

```
{with {y 1}  
  {foo 1}}
```

```
-----  
x     |      2  
-----  
mas-foo | {fun {y} {* 1 {* x y}}  
-----  
z     |    {+ 1 1}  
-----  
y     |    {+ 2 2}  
-----  
x     |      3  
-----  
foo   | {fun{x} {+ x {+ y z}}}  
-----  
z     |      7  
-----  
y     |    {+ 1 2}  
-----  
x     |    {+ 3 2}  
-----
```

```
{foo 1}
```

```
-----  
y     |      1  
-----  
x     |      2  
-----  
mas-foo | {fun {y} {* 1 {* x y}}  
-----  
z     |    {+ 1 1}  
-----  
y     |    {+ 2 2}
```

```
-----  
x   |      3  
-----  
foo  | {fun{x} {+ x {+ y z}}}  
-----  
z   |      7  
-----  
y   |    {+ 1 2}  
-----  
x   |    {+ 3 2}  
-----
```

{{fun{x} {+ x {+ y z}}}
1}

```
-----  
y   |      1  
-----  
x   |      2  
-----  
mas-foo | {fun {y} {* 1 {* x y}}  
-----  
z   |    {+ 1 1}  
-----  
y   |    {+ 2 2}  
-----  
x   |      3  
-----  
> foo  | {fun{x} {+ x {+ y z}}}  
-----  
z   |      7  
-----  
y   |    {+ 1 2}  
-----  
x   |    {+ 3 2}  
-----
```

{+ 1 {+ y z}}

```
-----  
y   |      1  
-----  
x   |      2  
-----  
mas-foo | {fun {y} {* 1 {* x y}}  
-----
```

z		{+ 1 1}

y		{+ 2 2}

x		3

> foo		{fun{x} {+ x {+ y z}}}

z		7

y		{+ 1 2}

x		{+ 3 2}

{+ 1 {+ {+ 1 2} z}}

y		1

x		2

mas-foo		{fun {y} {* 1 {* x y}}}

z		{+ 1 1}

y		{+ 2 2}

x		3

foo		{fun{x} {+ x {+ y z}}}

z		7

> y		{+ 1 2}

x		{+ 3 2}

{+ 1 {+ {+ 1 2} 7}}

y		1

x		2

```
-----
mas-foo | {fun {y} {* 1 {* x y}}}
-----
      z  |      {+ 1 1}
-----
      y  |      {+ 2 2}
-----
      x  |      3
-----
      foo | {fun{x} {+ x {+ y z}}}}
-----
>      z  |      7
-----
      y  |      {+ 1 2}
-----
      x  |      {+ 3 2}
-----
```

{+ 1 {+ 3 7}}

```
-----
      y  |      1
-----
      x  |      2
-----
mas-foo | {fun {y} {* 1 {* x y}}}
-----
      z  |      {+ 1 1}
-----
      y  |      {+ 2 2}
-----
      x  |      3
-----
      foo | {fun{x} {+ x {+ y z}}}}
-----
>      z  |      7
-----
      y  |      {+ 1 2}
-----
      x  |      {+ 3 2}
-----
```

{+ 1 10}

	y		1
	x		2
	mas-foo		{fun {y} {* 1 {* x y}}}
	z		{+ 1 1}
	y		{+ 2 2}
	x		3
	foo		{fun{x} {+ x {+ y z}}}
>	z		7
	y		{+ 1 2}
	x		{+ 3 2}

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	y		1
	x		2
	mas-foo		{fun {y} {* 1 {* x y}}}
	z		{+ 1 1}
	y		{+ 2 2}
	x		3
	foo		{fun{x} {+ x {+ y z}}}
>	z		7
	y		{+ 1 2}
	x		{+ 3 2}

- Evaluacion perezosa y alcance dinámico.

Solución:

Evaluación	Ambiente
<pre>{with {x {+ 3 2}} {with {y {+ 1 2}} {with {z 7} {with {foo {fun{x} {+ x {+ y z}}}} {with {x 3} {with {y {+ 2 2}} {with z {+ 1 1}} {with {mas-foo {fun {y} {* 1 {* x y}}}} {with {x 2} {with {y 1} {foo 1}}}}}}}}}}}}</pre>	

<pre>{with {y {+ 1 2}} {with {z 7} {with {foo {fun{x} {+ x {+ y z}}}} {with {x 3} {with {y {+ 2 2}} {with z {+ 1 1}} {with {mas-foo {fun {y} {* 1 {* x y}}}} {with {x 2} {with {y 1} {foo 1}}}}}}}}}}}}</pre>	
----- x {+ 3 2} -----	
<pre>{with {foo {fun{x} {+ x {+ y z}}}} {with {x 3} {with {y {+ 2 2}} {with z {+ 1 1}} {with {mas-foo {fun {y} {* 1 {* x y}}}} {with {x 2}</pre>	

```
      {with {y 1}
        {foo 1}}}}}}}}}
```

z		7

y		{+ 1 2}

x		{+ 3 2}

```
{with {x 3}
  {with {y {+ 2 2}}
    {with z {+ 1 1}}
      {with {mas-foo {fun {y} {* 1 {* x y}}}}
        {with {x 2}
          {with {y 1}
            {foo 1}}}}}}}}
```

foo		{fun{x} {+ x {+ y z}}}

z		7

y		{+ 1 2}

x		{+ 3 2}

```
{with {y {+ 2 2}}
  {with z {+ 1 1}}
    {with {mas-foo {fun {y} {* 1 {* x y}}}}
      {with {x 2}
        {with {y 1}
          {foo 1}}}}}}
```

x		3

foo		{fun{x} {+ x {+ y z}}}

z		7

y | {+ 1 2}

x | {+ 3 2}

```
{with z {+ 1 1}}  
  {with {mas-foo {fun {y} {* 1 {* x y}}}}}  
    {with {x 2}  
      {with {y 1}  
        {foo 1}}}}}
```

y | {+ 2 2}

x | 3

foo | {fun{x} {+ x {+ y z}}}

z | 7

y | {+ 1 2}

x | {+ 3 2}

```
{with {mas-foo {fun {y} {* 1 {* x y}}}}  
  {with {x 2}  
    {with {y 1}  
      {foo 1}}}}
```

z | {+ 1 1}

y | {+ 2 2}

x | 3

foo | {fun{x} {+ x {+ y z}}}

z | 7

y | {+ 1 2}

```
x      |      {+ 3 2}  
-----
```

```
{with {x 2}  
  {with {y 1}  
    {foo 1}}}}
```

```
-----  
mas-foo | {fun {y} {* 1 {* x y}}  
-----  
z      |      {+ 1 1}  
-----  
y      |      {+ 2 2}  
-----  
x      |      3  
-----  
foo    | {fun{x} {+ x {+ y z}}}  
-----  
z      |      7  
-----  
y      |      {+ 1 2}  
-----  
x      |      {+ 3 2}  
-----
```

```
{with {y 1}  
  {foo 1}}
```

```
-----  
x      |      2  
-----  
mas-foo | {fun {y} {* 1 {* x y}}  
-----  
z      |      {+ 1 1}  
-----  
y      |      {+ 2 2}  
-----  
x      |      3  
-----  
foo    | {fun{x} {+ x {+ y z}}}  
-----  
z      |      7  
-----  
y      |      {+ 1 2}  
-----
```

```
x      |      {+ 3 2}  
-----
```

```
{foo 1}
```

```
-----  
y      |      1  
-----  
x      |      2  
-----  
mas-foo | {fun {y} {* 1 {* x y}}  
-----  
z      |      {+ 1 1}  
-----  
y      |      {+ 2 2}  
-----  
x      |      3  
-----  
foo     | {fun{x} {+ x {+ y z}}}  
-----  
z      |      7  
-----  
y      |      {+ 1 2}  
-----  
x      |      {+ 3 2}  
-----
```

```
{{fun{x} {+ x {+ y z}} } 1}
```

```
-----  
y      |      1  
-----  
x      |      2  
-----  
mas-foo | {fun {y} {* 1 {* x y}}  
-----  
z      |      {+ 1 1}  
-----  
y      |      {+ 2 2}  
-----  
x      |      3  
-----  
> foo   | {fun{x} {+ x {+ y z}}}  
-----  
z      |      7  
-----
```

```
-----
y   |      {+ 1 2}
-----
x   |      {+ 3 2}
-----
```

{+ 1 {+ y z}}

```
-----
y   |      1
-----
x   |      2
-----
mas-foo | {fun {y} {* 1 {* x y}}}
-----
z   |      {+ 1 1}
-----
y   |      {+ 2 2}
-----
x   |      3
-----
> foo   | {fun{x} {+ x {+ y z}}}}
-----
z   |      7
-----
y   |      {+ 1 2}
-----
x   |      {+ 3 2}
-----
```

{+ 1 {+ 1 z}}

```
-----
> y   |      1
-----
x   |      2
-----
mas-foo | {fun {y} {* 1 {* x y}}}
-----
z   |      {+ 1 1}
-----
y   |      {+ 2 2}
-----
x   |      3
-----
```

```
foo    | {fun{x} {+ x {+ y z}}}  
-----  
z      |      7  
-----  
y      |    {+ 1 2}  
-----  
x      |    {+ 3 2}  
-----
```

```
{+ 1 {+ 1 {+ 1 1}}}
```

```
-----  
y      |      1  
-----  
x      |      2  
-----  
mas-foo | {fun {y} {* 1 {* x y}}  
-----  
> z     |    {+ 1 1}  
-----  
y      |    {+ 2 2}  
-----  
x      |      3  
-----  
foo     | {fun{x} {+ x {+ y z}}}  
-----  
z      |      7  
-----  
y      |    {+ 1 2}  
-----  
x      |    {+ 3 2}  
-----
```

```
{+ 1 {+ 1 2}}
```

```
-----  
y      |      1  
-----  
x      |      2  
-----  
mas-foo | {fun {y} {* 1 {* x y}}  
-----  
> z     |    {+ 1 1}  
-----  
y      |    {+ 2 2}
```



```
-----  
x   |      3  
-----  
foo  | {fun{x} {+ x {+ y z}}}  
-----  
z   |      7  
-----  
y   |    {+ 1 2}  
-----  
x   |    {+ 3 2}  
-----
```

{+ 1 3}

```
-----  
y   |      1  
-----  
x   |      2  
-----  
mas-foo | {fun {y} {* 1 {* x y}}  
-----  
> z   |    {+ 1 1}  
-----  
y   |    {+ 2 2}  
-----  
x   |      3  
-----  
foo  | {fun{x} {+ x {+ y z}}}  
-----  
z   |      7  
-----  
y   |    {+ 1 2}  
-----  
x   |    {+ 3 2}  
-----
```

4

```
-----  
y   |      1  
-----  
x   |      2  
-----  
mas-foo | {fun {y} {* 1 {* x y}}  
-----
```

>	z		{+ 1 1}

	y		{+ 2 2}

	x		3

	foo		{fun{x} {+ x {+ y z}}}

	z		7

	y		{+ 1 2}

	x		{+ 3 2}

- Evaluacion glotona y alcance estático.

Solución:

Evaluación	Ambiente
<pre>{with {x {+ 3 2}} {with {y {+ 1 2}} {with {z 7} {with {foo {fun{x} {+ x {+ y z}}}} {with {x 3} {with {y {+ 2 2}} {with z {+ 1 1}} {with {mas-foo {fun {y} {* 1 {* x y}}}} {with {x 2} {with {y 1} {foo 1}}}}}}}}}}}</pre>	

<pre>{with {y {+ 1 2}} {with {z 7} {with {foo {fun{x} {+ x {+ y z}}}} {with {x 3} {with {y {+ 2 2}} {with z {+ 1 1}} {with {mas-foo {fun {y} {* 1 {* x y}}}} {with {x 2} {with {y 1} {foo 1}}}}}}}}}}}</pre>	

x | 5

```
{with {foo {fun{x} {+ x {+ y z}}}}  
  {with {x 3}  
    {with {y {+ 2 2}}  
      {with z {+ 1 1}}  
        {with {mas-foo {fun {y} {* 1 {* x y}}}}  
          {with {x 2}  
            {with {y 1}  
              {foo 1}}}}}}}}}
```

z | 7

y | 3

x | 5

```
{with {x 3}  
  {with {y {+ 2 2}}  
    {with z {+ 1 1}}  
      {with {mas-foo {fun {y} {* 1 {* x y}}}}  
        {with {x 2}  
          {with {y 1}  
            {foo 1}}}}}}}
```

foo | {fun{x} {+ x {+ y z}}}

z | 7

y | 3

x | 5

```
{with {y {+ 2 2}}  
  {with z {+ 1 1}}
```

```
{with {mas-foo {fun {y} {* 1 {* x y}}}}
  {with {x 2}
    {with {y 1}
      {foo 1}}}}}}
```

x		3
foo		{fun{x} {+ x {+ y z}}}
z		7
y		3
x		5

```
{with z {+ 1 1}}
{with {mas-foo {fun {y} {* 1 {* x y}}}}
  {with {x 2}
    {with {y 1}
      {foo 1}}}}}}
```

y		4
x		3
foo		{fun{x} {+ x {+ y z}}}
z		7
y		3
x		5

```
{with {mas-foo {fun {y} {* 1 {* x y}}}}
  {with {x 2}
    {with {y 1}
      {foo 1}}}}}}
```

z		2
y		4
x		3
foo		{fun{x} {+ x {+ y z}}}
z		7
y		3
x		5

```
{with {x 2}
  {with {y 1}
    {foo 1}}}}
```

mas-foo		{fun {y} {* 1 {* x y}}}
z		2
y		4
x		3
foo		{fun{x} {+ x {+ y z}}}
z		7
y		3
x		5

```
{with {y 1}
  {foo 1}}
```

x		2
---	--	---

```
mas-foo | {fun {y} {* 1 {* x y}}
-----
      z |          2
-----
      y |          4
-----
      x |          3
-----
foo     | {fun{x} {+ x {+ y z}}
-----
      z |          7
-----
      y |          3
-----
      x |          5
-----
```

{foo 1}

```
-----
      y |          1
-----
      x |          2
-----
mas-foo | {fun {y} {* 1 {* x y}}
-----
      z |          2
-----
      y |          4
-----
      x |          3
-----
foo     | {fun{x} {+ x {+ y z}}
-----
      z |          7
-----
      y |          3
-----
      x |          5
-----
```

{{fun{x} {+ x {+ y z}} 1}

```
-----
      y |          1
-----
```

	x		2

	mas-foo		{fun {y} {* 1 {* x y}}}

	z		2

	y		4

	x		3

>	foo		{fun{x} {+ x {+ y z}}}

	z		7

	y		3

	x		5

{+ 1 {+ y z}}

	y		1

	x		2

	mas-foo		{fun {y} {* 1 {* x y}}}

	z		2

	y		4

	x		3

>	foo		{fun{x} {+ x {+ y z}}}

	z		7

	y		3

	x		5

{+ 1 {+ 3 z}}

```
-----
  y   |           1
-----
  x   |           2
-----
mas-foo | {fun {y} {* 1 {* x y}}}
-----
  z   |           2
-----
  y   |           4
-----
  x   |           3
-----
foo    | {fun{x} {+ x {+ y z}}}}
-----
  z   |           7
-----
>  y   |           3
-----
  x   |           5
-----
```

{+ 1 {+ 3 7}}

```
-----
  y   |           1
-----
  x   |           2
-----
mas-foo | {fun {y} {* 1 {* x y}}}
-----
  z   |           2
-----
  y   |           4
-----
  x   |           3
-----
foo    | {fun{x} {+ x {+ y z}}}}
-----
>  z   |           7
-----
  y   |           3
-----
  x   |      {+ 3 2}
-----
```


{+ 1 {+ 3 7}}

```
-----
  y   |           1
-----
  x   |           2
-----
mas-foo | {fun {y} {* 1 {* x y}}}
-----
  z   |           2
-----
  y   |           4
-----
  x   |           3
-----
foo    | {fun{x} {+ x {+ y z}}}}
-----
>  z   |           7
-----
  y   |           3
-----
  x   |      {+ 3 2}
-----
```

{+ 1 10}

```
-----
  y   |           1
-----
  x   |           2
-----
mas-foo | {fun {y} {* 1 {* x y}}}
-----
  z   |           2
-----
  y   |           4
-----
  x   |           3
-----
foo    | {fun{x} {+ x {+ y z}}}}
-----
>  z   |           7
-----
  y   |           3
-----
```

```
x | {+ 3 2}
-----
```

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```
-----
y | 1
-----
x | 2
-----
mas-foo | {fun {y} {* 1 {* x y}}}
-----
z | 2
-----
y | 4
-----
x | 3
-----
foo | {fun{x} {+ x {+ y z}}}}
-----
> z | 7
-----
y | 3
-----
x | {+ 3 2}
-----
```

- Evaluacion glotona y alcance dinámico.

Solución:

Evaluación	Ambiente
<pre>{with {x {+ 3 2}} {with {y {+ 1 2}} {with {z 7} {with {foo {fun{x} {+ x {+ y z}}}}} {with {x 3} {with {y {+ 2 2}} {with z {+ 1 1}} {with {mas-foo {fun {y} {* 1 {* x y}}}}} {with {x 2} {with {y 1} {foo 1}}}}}}}}}}}}</pre>	

```
{with {y {+ 1 2}}
  {with {z 7}
    {with {foo {fun{x} {+ x {+ y z}}}}
      {with {x 3}
        {with {y {+ 2 2}}
          {with z {+ 1 1}}
            {with {mas-foo {fun {y} {* 1 {* x y}}}}
              {with {x 2}
                {with {y 1}
                  {foo 1}}}}}}}}}}}
```

x | 5

```
{with {foo {fun{x} {+ x {+ y z}}}}
  {with {x 3}
    {with {y {+ 2 2}}
      {with z {+ 1 1}}
        {with {mas-foo {fun {y} {* 1 {* x y}}}}
          {with {x 2}
            {with {y 1}
              {foo 1}}}}}}}}}
```

z | 7

y | 3

x | 5

```
{with {x 3}
  {with {y {+ 2 2}}
    {with z {+ 1 1}}
      {with {mas-foo {fun {y} {* 1 {* x y}}}}
        {with {x 2}
          {with {y 1}
            {foo 1}}}}}}}
```

```
-----  
foo   | {fun{x} {+ x {+ y z}}}  
-----  
z     |           7  
-----  
y     |           3  
-----  
x     |           5  
-----
```

```
{with {y {+ 2 2}}  
  {with z {+ 1 1}}  
    {with {mas-foo {fun {y} {* 1 {* x y}}}}  
      {with {x 2}  
        {with {y 1}  
          {foo 1}}}}}}
```

```
-----  
x     |           3  
-----  
foo   | {fun{x} {+ x {+ y z}}}  
-----  
z     |           7  
-----  
y     |           3  
-----  
x     |           5  
-----
```

```
{with z {+ 1 1}}  
  {with {mas-foo {fun {y} {* 1 {* x y}}}}  
    {with {x 2}  
      {with {y 1}  
        {foo 1}}}}}
```

```
-----  
y     |           4  
-----  
x     |           3  
-----  
foo   | {fun{x} {+ x {+ y z}}}  
-----
```

z		7

y		3

x		5

```
{with {mas-foo {fun {y} {* 1 {* x y}}}}
  {with {x 2}
    {with {y 1}
      {foo 1}}}}
```

z		2

y		4

x		3

foo		{fun{x} {+ x {+ y z}}}

z		7

y		3

x		5

```
{with {x 2}
  {with {y 1}
    {foo 1}}}}
```

mas-foo		{fun {y} {* 1 {* x y}}}

z		2

y		4

x		3

foo		{fun{x} {+ x {+ y z}}}

z		7

y		3

x		5

```
{with {y 1}
  {foo 1}}
```

x		2

mas-foo		{fun {y} {* 1 {* x y}}}

z		2

y		4

x		3

foo		{fun{x} {+ x {+ y z}}}

z		7

y		3

x		5

```
{foo 1}
```

y		1

x		2

mas-foo		{fun {y} {* 1 {* x y}}}

z		2

y		4

x		3

foo		{fun{x} {+ x {+ y z}}}

```
z | 7
-----
y | 3
-----
x | 5
-----
```

{{fun{x} {+ x {+ y z}}} 1}

```
-----
y | 1
-----
x | 2
-----
mas-foo | {fun {y} {* 1 {* x y}}
-----
z | 2
-----
y | 4
-----
x | 3
-----
> foo | {fun{x} {+ x {+ y z}}}
-----
z | 7
-----
y | 3
-----
x | 5
-----
```

{+ 1 {+ y z}}

```
-----
> y | 1
-----
x | 2
-----
mas-foo | {fun {y} {* 1 {* x y}}
-----
z | 2
-----
y | 4
-----
x | 3
-----
```

```
-----
foo    | {fun{x} {+ x {+ y z}}}  
-----  
z      |          7  
-----  
y      |          3  
-----  
x      |          5  
-----
```

{+ 1 {+ 1 z}}

```
-----  
y      |          1  
-----  
x      |          2  
-----  
mas-foo | {fun {y} {* 1 {* x y}}  
-----  
z      |          2  
-----  
y      |          4  
-----  
x      |          3  
-----  
> foo    | {fun{x} {+ x {+ y z}}}  
-----  
z      |          7  
-----  
y      |          3  
-----  
x      |          5  
-----
```

{+ 1 {+ 1 2}}

```
-----  
y      |          1  
-----  
x      |          2  
-----  
mas-foo | {fun {y} {* 1 {* x y}}  
-----  
> z      |          2  
-----
```



```

y | 4
-----
x | 3
-----
foo | {fun{x} {+ x {+ y z}}}
-----
z | 7
-----
y | 3
-----
x | 5
-----
```

{+ 1 3}

```

-----
y | 1
-----
x | 2
-----
mas-foo | {fun {y} {* 1 {* x y}}}
-----
> z | {+ 1 1}
-----
y | {+ 2 2}
-----
x | 3
-----
foo | {fun{x} {+ x {+ y z}}}
-----
z | 7
-----
y | {+ 1 2}
-----
x | {+ 3 2}
-----
```

4

```

-----
y | 1
-----
x | 2
-----
mas-foo | {fun {y} {* 1 {* x y}}}
```

>	z		{+ 1 1}
	y		{+ 2 2}
	x		3
	foo		{fun{x} {+ x {+ y z}}}
	z		7
	y		{+ 1 2}
	x		{+ 3 2}

Es necesario expresar el ambiente final (stack) para evaluacion glotona y perezosa; ademas de la expresion completa a evaluar en cada uno de los incisos anteriores, antes de dar el resultado final de tales evaluaciones.

2. Evalua las siguientes expresiones usando cada uno de los pasos de parametros que se solicitan, debes de poner la ultima expresion a evaluar antes de dar el resultado final de la misma, usando:
- Paso de parametros por valor.

Solución:

Evaluación	Ambiente	Store
<pre>{with* { {i -1} {j -1} {swap {fun {x y} {seqn {set tmp x} {set x y} {set y tmp}}}}} } {seqn {swap i j} {- j i}}}</pre>		

```
{with*
{
  {i -1}
  {j -1}
  {swap {fun {x y}
    {seqn
      {set tmp x}
      {set x y}
      {set y tmp}}}}}
}
{seqn
  {swap i j}
  {- j i}}}
```

swap		2

j		1

i		0

2		{fun {x y} {seqn ...}}

1		-1

0		-1

```
{seqn
  {swap i j}
  {- j i}}
```

swap		2

j		1

```
      i |      0
-----
```

```
-----
      2 | {fun {x y} {seqn ...}}
-----
      1 |      -1
-----
      0 |      -1
-----
```

```
{swap i j}
```

```
-----
swap |      2
-----
      j |      1
-----
      i |      0
-----
```

```
-----
      2 | {fun {x y} {seqn ...}}
-----
      1 |      -1
-----
      0 |      -1
-----
```

```
{- -1 i}
```

```
-----
swap |      2
-----
>      j |      1
-----
      i |      0
-----
```

```
-----  
      2 | {fun {x y} {seqn ...}}  
-----  
> 1 |      -1  
-----  
      0 |      -1  
-----
```

{- -1 -1}

```
-----  
swap |      2  
-----  
      j |      1  
-----  
> i |      0  
-----
```

```
-----  
      2 | {fun {x y} {seqn ...}}  
-----  
      1 |      -1  
-----  
> 0 |      -1  
-----
```

0

```
-----  
swap |      2  
-----  
      j |      1  
-----  
> i |      0  
-----
```

```
-----  
      2 | {fun {x y} {seqn ...}}  
-----
```

1		-1

> 0		-1

- Paso de parametros por referencia.

Solución:

Evaluación	Ambiente	Store
<pre>{with {x {+ 3 2}} {with {y {+ 1 2}} {with {z 7} {with {foo {fun{x} {+ x {+ y z}}}} {with {x 3} {with {y {+ 2 2}} {with z {+ 1 1}} {with {mas-foo {fun {y} {* 1 {* x y}}}} {with {x 2} {with {y 1} {foo 1}}}}}}}}}}}}}</pre>		

<pre>{with {y {+ 1 2}} {with {z 7} {with {foo {fun{x} {+ x {+ y z}}}} {with {x 3} {with {y {+ 2 2}} {with z {+ 1 1}} {with {mas-foo {fun {y} {* 1 {* x y}}}} {with {x 2} {with {y 1} {foo 1}}}}}}}}}}}</pre>		
<pre>----- x 5 -----</pre>		
<pre>{with {foo {fun{x} {+ x {+ y z}}}} {with {x 3}</pre>		

```
{with {y {+ 2 2}}
  {with z {+ 1 1}}
    {with {mas-foo {fun {y} {* 1 {* x y}}}}
      {with {x 2}
        {with {y 1}
          {foo 1}}}}}}}
```

z		7
y		3
x		5

```
{with {x 3}
  {with {y {+ 2 2}}
    {with z {+ 1 1}}
      {with {mas-foo {fun {y} {* 1 {* x y}}}}
        {with {x 2}
          {with {y 1}
            {foo 1}}}}}}}
```

foo		{fun{x} {+ x {+ y z}}}
z		7
y		3
x		5

```
{with {y {+ 2 2}}
  {with z {+ 1 1}}
    {with {mas-foo {fun {y} {* 1 {* x y}}}}
      {with {x 2}
        {with {y 1}
          {foo 1}}}}}}
```

x		3
---	--	---

```
-----  
foo  | {fun{x} {+ x {+ y z}}}  
-----  
z    |          7  
-----  
y    |          3  
-----  
x    |          5  
-----
```

```
{with z {+ 1 1}}  
  {with {mas-foo {fun {y} {* 1 {* x y}}}}  
    {with {x 2}  
      {with {y 1}  
        {foo 1}}}}}
```

```
-----  
y    |          4  
-----  
x    |          3  
-----  
foo  | {fun{x} {+ x {+ y z}}}  
-----  
z    |          7  
-----  
y    |          3  
-----  
x    |          5  
-----
```

```
{with {mas-foo {fun {y} {* 1 {* x y}}}}  
  {with {x 2}  
    {with {y 1}  
      {foo 1}}}}}
```

```
-----  
z    |          2  
-----  
y    |          4  
-----  
x    |          3  
-----  
foo  | {fun{x} {+ x {+ y z}}}  
-----  
z    |          7  
-----
```



```
-----  
  y |      3  
-----  
  x |      5  
-----
```

```
{with {x 2}  
  {with {y 1}  
    {foo 1}}}}
```

```
-----  
mas-foo | {fun {y} {* 1 {* x y}}  
-----  
  z |      2  
-----  
  y |      4  
-----  
  x |      3  
-----  
foo    | {fun{x} {+ x {+ y z}}}  
-----  
  z |      7  
-----  
  y |      3  
-----  
  x |      5  
-----
```

```
{with {y 1}  
  {foo 1}}
```

```
-----  
  x |      2  
-----  
mas-foo | {fun {y} {* 1 {* x y}}  
-----  
  z |      2  
-----  
  y |      4  
-----  
  x |      3  
-----  
foo    | {fun{x} {+ x {+ y z}}}  
-----  
  z |      7  
-----
```

```
-----  
y   |      3  
-----  
x   |      5  
-----
```

{foo 1}

```
-----  
y   |      1  
-----  
x   |      2  
-----  
mas-foo | {fun {y} {* 1 {* x y}}  
-----  
z   |      2  
-----  
y   |      4  
-----  
x   |      3  
-----  
foo   | {fun{x} {+ x {+ y z}}}  
-----  
z   |      7  
-----  
y   |      3  
-----  
x   |      5  
-----
```

{{fun{x} {+ x {+ y z}}}
1}

```
-----  
y   |      1  
-----  
x   |      2  
-----  
mas-foo | {fun {y} {* 1 {* x y}}  
-----  
z   |      2  
-----  
y   |      4  
-----  
x   |      3  
-----
```

```
> foo | {fun{x} {+ x {+ y z}}}  
-----  
  z |      7  
-----  
  y |      3  
-----  
  x |      5  
-----
```

```
{+ 1 {+ y z}}
```

```
-----  
> y |      1  
-----  
  x |      2  
-----  
mas-foo | {fun {y} {* 1 {* x y}}  
-----  
  z |      2  
-----  
  y |      4  
-----  
  x |      3  
-----  
foo | {fun{x} {+ x {+ y z}}}  
-----  
  z |      7  
-----  
  y |      3  
-----  
  x |      5  
-----
```

```
{+ 1 {+ 1 z}}
```

```
-----  
  y |      1  
-----  
  x |      2  
-----  
mas-foo | {fun {y} {* 1 {* x y}}  
-----  
  z |      2  
-----  
  y |      4
```

	x		3
> foo		{fun{x} {+ x {+ y z}}}	
	z		7
	y		3
	x		5

{+ 1 {+ 1 2}}

	y		1
	x		2
mas-foo		{fun {y} {* 1 {* x y}}}	
> z		2	
	y		4
	x		3
foo		{fun{x} {+ x {+ y z}}}	
	z		7
	y		3
	x		5

{+ 1 3}

	y		1
	x		2
mas-foo		{fun {y} {* 1 {* x y}}}	

```

>  z  |      {+ 1 1}
-----
    y  |      {+ 2 2}
-----
    x  |          3
-----
foo  | {fun{x} {+ x {+ y z}}}}
-----
    z  |          7
-----
    y  |      {+ 1 2}
-----
    x  |      {+ 3 2}
-----

```

4

```

-----
    y  |          1
-----
    x  |          2
-----
mas-foo | {fun {y} {* 1 {* x y}}}
-----
>  z  |      {+ 1 1}
-----
    y  |      {+ 2 2}
-----
    x  |          3
-----
foo  | {fun{x} {+ x {+ y z}}}}
-----
    z  |          7
-----
    y  |      {+ 1 2}
-----
    x  |      {+ 3 2}
-----

```

Es necesario expresar el ambiente final (stack) para evaluación glotona y perezosa; además de la expresión completa a evaluar en cada uno de los incisos anteriores, antes de dar el resultado final de tales evaluaciones.

2. Evalua las siguientes expresiones usando cada uno de los pasos de parametros que se solicitan, debes de poner la ultima expresion a evaluar antes de dar el resultado final de la misma, usando:
- Paso de parametros por valor.

Solución:

Evaluación	Ambiente	Store
<pre>{with* { {i -1} {j -1} {swap {fun {x y} {seqn {set tmp x} {set x y} {set y tmp}}}}} } {seqn {swap i j} {- j i}}}</pre>		

<pre>{with* { {i -1} {j -1} {swap {fun {x y} {seqn {set tmp x} {set x y} {set y tmp}}}}} } {seqn {swap i j} {- j i}}}</pre>		

swap 2		

```
-----  
  j  |      1  
-----  
  i  |      0  
-----
```

```
-----  
  2  | {fun {x y} {seqn ...}}  
-----  
  1  |      -1  
-----  
  0  |      -1  
-----
```

```
{seqn  
  {swap i j}  
  {- j i}}
```

```
-----  
swap |      2  
-----  
  j  |      1  
-----  
  i  |      0  
-----
```

```
-----  
  2  | {fun {x y} {seqn ...}}  
-----  
  1  |      -1  
-----  
  0  |      -1  
-----
```

```
{swap i j}
```

```
-----  
swap |      2  
-----  
  j  |      1
```

```
-----  
i | 0  
-----
```

```
-----  
2 | {fun {x y} {seqn ...}}  
-----  
1 | -1  
-----  
0 | -1  
-----
```

```
{- -1 i}
```

```
-----  
swap | 2  
-----  
> j | 1  
-----  
i | 0  
-----
```

```
-----  
2 | {fun {x y} {seqn ...}}  
-----  
> 1 | -1  
-----  
0 | -1  
-----
```

```
{- -1 -1}
```

```
-----  
swap | 2  
-----  
j | 1  
-----  
> i | 0  
-----
```



```
-----
      2 | {fun {x y} {seqn ...}}
-----
      1 |          -1
-----
>    0 |          -1
-----
```

0

```
-----
swap  |          2
-----
      j |          1
-----
>    i |          0
-----
```

```
-----
      2 | {fun {x y} {seqn ...}}
-----
      1 |          -1
-----
>    0 |          -1
-----
```

- Paso de parámetros por referencia.

Solución:

Evaluación	Ambiente	Store
<pre>{with* { {i -1} {j -1} {swap {fun {x y} {seqn {set tmp x} {set x y} {set y tmp}}}}}</pre>		

```
}
{seqn
  {swap i j}
  {- j i}}}
```

```
{with*
{
  {i -1}
  {j -1}
  {swap {fun {x y}
    {seqn
      {set tmp x}
      {set x y}
      {set y tmp}}}}
}
{seqn
  {swap i j}
  {- j i}}}
```

swap		2

j		1

i		0

2		{fun {x y} {seqn ...}}

1		-1

0		-1

```
{seqn
  {swap i j}
  {- j i}}
```

swap		2
j		1
i		0

2		{fun {x y} {seqn ...}}
1		-1
0		-1

```
{swap i j}
```

swap		2
j		0
i		1

2		{fun {x y} {seqn ...}}
1		-1
0		-1

```
{- -1 i}
```

```
-----
swap |      2
-----
>  j  |      0
-----
    i  |      1
-----
```

```
-----
    2  | {fun {x y} {seqn ...}}
-----
    1  |      -1
-----
>  0  |      -1
-----
```

{- -1 -1}

```
-----
swap |      2
-----
    j  |      0
-----
>  i  |      1
-----
```

```
-----
    2  | {fun {x y} {seqn ...}}
-----
>  1  |      -1
-----
    0  |      -1
-----
```

0

```
-----
swap |      2
-----
```

```

-----
      j   |           0
-----
>   i   |           1
-----

```

```

-----
      2   | {fun {x y} {seqn ...}}
-----
>   1   |           -1
-----
>   0   |           -1
-----

```

3. ¿Da dos ejemplos en el lenguaje *RCFWAE* de transparencia referencial?

◦ Ejemplo 1:

```

{with {x {+ 2 2}}
  {with {y {+ 1 3}}
    {+ x y}}} ;; -> 8

{with {x {* 2 2}}
  {with {y {add1 3}}
    {+ x y}}} ;; -> 8

```

◦ Ejemplo 2:

```

{with {c {+ 1 5}}
  {if0 {- c 6}
    {and true true false}
    true}} ;; -> false

{with {c 6}
  {if0 {- {* 2 c} 12}
    {and true true false}
    true}} ;; -> false

```

4. Dentro del Calculo Lambda, evalua cada una de las siguientes expresiones usando β -reducciones. Si alguna tiene forma normal, especificala.

◦ $(\lambda x. x)(\lambda x. xxx)$

$$(\lambda x. x)(\lambda x. xxx)$$

$$\rightarrow_{\beta} (\lambda x. xxx)$$

$$\rightarrow_{\beta} (\lambda x. xxx)$$

$$\circ (\lambda x. (\lambda y. yxw)z)u$$

$$(\lambda x. (\lambda y. yxw)z)u$$

$$\rightarrow_{\beta} (\lambda y. yuw)z$$

$$\rightarrow_{\beta} zuw$$

$$\circ (\lambda x. \lambda y. \lambda z. x)(yz)$$

$$(\lambda x. \lambda y. \lambda z. x)(yz)$$

$$\rightarrow_{\beta} (\lambda y. \lambda z. yz)$$

5. ¿Da un ejemplo en Cálculo Lambda (distintos a los vistos en clase) donde se aplique el **teorema de confluencia**? Haz la reducción completa en cada caso.

$$(\lambda x. (\lambda y. (\lambda z. zx)y)xz)v \rightarrow_{\beta} (\lambda y. (\lambda z. zx)y) vz$$

$$(\lambda x. (\lambda y. (\lambda z. zx)y)xz)v \rightarrow_{\beta} (\lambda x. (\lambda y. yx)xz)v$$

6. Da un ejemplo en Racket, donde uses la estructura de cajas y expongas el concepto de **estado** y **SPS**. En el ejemplo se debe reflejar el cambio de estado de una variable definida como una caja, cuyo valor dentro de la caja sea inicialmente 0 (cero) y termine con valor de 2, teniendo un valor de 1 de forma intermedia.

Solución:

Evaluación	Ambiente	Store
<pre>{with {b {newbox 0}} {seqn {setbox b 1} {setbox b 2} {openbox b}}}</pre>		

```
{seqn
  {setbox b 1}
  {setbox b 2}
  {openbox b}}
```

b		0
---	--	---

>	1		0
---	---	--	---

0		1	
---	--	---	--

```
{setbox b 1}
```

b		0
---	--	---

>	1		1
---	---	--	---

1		0
---	--	---

0		1	
---	--	---	--

```
{setbox b 2}
```

b		0
---	--	---

> 1 | 2

1 | 1

1 | 0

0 | | 1 |

{openbox b}

> b | 0

1 | 2

1 | 1

1 | 0

> 0 | | 1 |

2

> b | 0

> 1 | 2

1 | 1

1 | 0

0 | | 1 |

7. Del siguiente código en Racket:

```
(define (filter-neg l)
  (cond
    ((empty? l) empty)
    (else
     (if (< (nfirst l) 0)
         (cons (nfirst l) (filter-neg (nrest l)))
         (filter-neg (nrest l))))))
```

- Convierte el código anterior usando recursión de cola.

```
(define (filter-neg l acc)
  (cond
    ((empty? l) acc)
    (else
     (if (< (nfirst l) 0)
         (filter-neg (nrest l) (snoc acc (nfirst l)))
         (filter-neg (nrest l) acc)))))
```

- ¿Cuántos registros de activación se crean usando recursión de cola cuando recibe la lista '(0 1 -1 0 -4 1 -2)? Explica cómo se va creando el stack de ejecución.

Solución:

Stack de ejecución

```
(filter-neg '(0 1 -1 0 -4 1 -2) '())
```

```
(filter-neg '(1 -1 0 -4 1 -2) '())
```

```
(filter-neg '(-1 0 -4 1 -2) '())
```

```
(filter-neg '(0 -4 1 -2) '(-1))
```

```
(filter-neg '(-4 1 -2) '(-1))
```

```
(filter-neg '(1 -2) '(-1 -4))
```

```
(filter-neg '(-2) '(-1 -4))
```

```
(filter-neg '() '(-1 -4 -2))
```

```
'(-1 -4 -2)
```

- ¿Cuántos registros de activación se crean usando la implementación de recursión con la misma instancia que en el inciso anterior? Explica como es que se va creando el stack de ejecución.

Solución:

Stack de ejecución

```
(filter-neg '(0 1 -1 0 -4 1 -2))
```

```
-----
(filter-neg '(1 -1 0 -4 1 -2))
-----
(filter-neg '(0 1 -1 0 -4 1 -2))
```

```
-----
(filter-neg '(-1 0 -4 1 -2))
-----
(filter-neg '(1 -1 0 -4 1 -2))
-----
(filter-neg '(0 1 -1 0 -4 1 -2))
```

```
-----
(filter-neg '(0 -4 1 -2))
```

```

-----
(filter-neg '(-1 0 -4 1 -2))
-----
(filter-neg '(1 -1 0 -4 1 -2))
-----
(filter-neg '(0 1 -1 0 -4 1 -2))

```

```

-----
(filter-neg '(-4 1 -2))
-----
(filter-neg '(0 -4 1 -2))
-----
(filter-neg '(-1 0 -4 1 -2))
-----
(filter-neg '(1 -1 0 -4 1 -2))
-----
(filter-neg '(0 1 -1 0 -4 1 -2))

```

```

-----
(filter-neg '(1 -2))
-----
(filter-neg '(-4 1 -2))
-----
(filter-neg '(0 -4 1 -2))
-----
(filter-neg '(-1 0 -4 1 -2))
-----
(filter-neg '(1 -1 0 -4 1 -2))
-----
(filter-neg '(0 1 -1 0 -4 1 -2))

```

```

-----
(filter-neg '(-2))
-----
(filter-neg '(1 -2))
-----
(filter-neg '(-4 1 -2))
-----
(filter-neg '(0 -4 1 -2))
-----
(filter-neg '(-1 0 -4 1 -2))
-----
(filter-neg '(1 -1 0 -4 1 -2))
-----
(filter-neg '(0 1 -1 0 -4 1 -2))

```

```
-----  
'()  
-----  
(filter-neg '(-2))  
-----  
(filter-neg '(1 -2))  
-----  
(filter-neg '(-4 1 -2))  
-----  
(filter-neg '(0 -4 1 -2))  
-----  
(filter-neg '(-1 0 -4 1 -2))  
-----  
(filter-neg '(1 -1 0 -4 1 -2))  
-----  
(filter-neg '(0 1 -1 0 -4 1 -2))
```

```
-----  
'()  
-----  
(cons -2 (filter-neg '())) = '(-2)  
-----  
(filter-neg '(-2)) = '(-2)  
-----  
(cons -4 (filter-neg '(1 -2))) = '(-4 -2)  
-----  
(filter-neg '(-4 1 -2)) = '(-4 -2)  
-----  
(cons -1 (filter-neg '(0 -4 1 -2))) = '(-1 -4 -2)  
-----  
(filter-neg '(-1 0 -4 1 -2)) = '(-1 -4 -2)  
-----  
(filter-neg '(1 -1 0 -4 1 -2)) = '(-1 -4 -2)  
-----  
(filter-neg '(0 1 -1 0 -4 1 -2)) = '(-1 -4 -2)
```