

Reg. No. 2021054011

# Indian Institute of Information Technology Ranchi

Department of Electronics & Communication Engineering  
B. Tech End Semester Examination – Spring Semester 2022-23

Semester: IV

Course Code: EC-2006/EI-2006

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Course Name: Signal and Systems

QUESTION PAPER

Max Marks: 100

Duration: 3 Hrs.

- Instructions:
- (1) Number in [ ] indicates marks.
  - (2) Any missing data can be assumed suitably.
  - (3) Symbols have their usual meaning.
  - (4) Non-Programmable Scientific Calculator are allowed

## Section A: Answer any ten questions.

- Consider an aperiodic signal  $x(t) = e^{-at}$ ,  $a > 0$ , for  $t \geq 0$  and zero otherwise. Find the energy and the power of this signal and determine whether the signal is finite energy, finite power, or both. [4]
- Plot the following signal: [4]
 
$$y(t) = 3r(t + 3) - 6r(t + 1) + 3r(t) - 3u(t - 3)$$
- Find the even and odd components of [4]
 
$$x(t) = e^{-2t} \cos t$$
- Evaluate the following integral [4]
 
$$f(t) = \int_0^{10} ((t-1)^3 - 3(t-6) + 1)\delta(t-3)dt$$
- Show that the system described by the differential equation [4]
 
$$\frac{dy(t)}{dt} + 4y(t) + 1 = x(t)$$
 is nonlinear.
- Check whether the following system is time-invariant. [4]

$$y(t) = tx(t) + 5$$

- Consider the Rectangular Pulse or gate function  $x(t) = u(t) - u(t-1)$ . Obtain  $y(t) = x(t) * x(t)$ , that is, the convolution of rectangular pulse with itself. [4]
- Find the Fourier transform of following function [4]
 
$$x(t) = \sin \omega t$$
- Find the Fourier transform of  $y(t) = u(t) - u(t-1)$ . [4]
- Discuss the properties of Fourier Transform. [4]
- Obtain the Laplace transform of  $x(t) = e^{-at} \cos 4t u(t)$  [4]
- Obtain the inverse Laplace transform of  $X(S) = \frac{4}{(s+1)(s+3)}$  [4]

## Section B: Answer any three questions

- A continuous-time signal is shown in figure 1. Sketch each of the following signal. [10]
 

$y_1(t) = x\left(\frac{t}{2} + 1\right)$

$y_2(t) = -1 + 2x(t)$
- Express the signals shown in figure 2 in terms of unit step functions. Calculate its derivative and sketch it. [6]

Figure 1: Signal  $x(t)$ .





Figure 2: The input signal  $x(t)$ .

4. Write down the difference between the following
- Continuous-time and Discrete-time Signals
  - Causal and Non-Causal Systems

5. What is convolution? Explain LTI systems.

6. If the durations of  $x(t)$  and  $h(t)$  are  $T_1$  and  $T_2$ , respectively, then the duration of  $y(t) = x(t) * h(t)$  is \_\_\_\_\_.

If the areas under  $x(t)$  and  $h(t)$  are  $A_1$  and  $A_2$ , respectively, then the area under  $y(t) = x(t) * h(t)$  is \_\_\_\_\_.

7. Obtain the convolution of these two signals

$$x(t) = 2u(t)$$

$$h(t) = e^{-2t}u(t)$$

8. Consider  $x[n]$  and  $h[n]$  as shown in figure 3, respectively. (The signals are all zero outside the ranges indicated.) Evaluate  $y[n] = x[n] * h[n]$ .

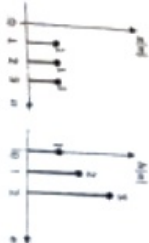


Figure 3: The input signal  $x[n]$  and impulse response  $h[n]$ .

9. What is the difference between Fourier series and Fourier transform?

10. Given the periodic train of pulses shown in figure 4, obtain Fourier coefficients  $a_0$ ,  $a_n$ , and  $b_n$ . Find the Fourier Series Expansion for the waveform.



Figure 4: Periodic train of pulses  $x(t)$ .

11. Determine the Fourier transform of the signum function, that is
- $$x(t) = \text{sgn}(t) = \begin{cases} 1 & t > 0 \\ -1 & t < 0 \end{cases}$$

12. Obtain the Laplace Transform of  $x(t) = e^{-10t}u(t)$  and establish the ROC.

13. Determine the Laplace transform of  $x(t) = t u(t - 2)$

14. Find the initial and final values of  $X(s) = \frac{4}{s} + \frac{5s+8}{s^2+6s+10}$

15. Consider the system characterized by

$$\frac{d^2y}{dt^2} + 3\frac{dy}{dt} - 4y = e^{-t}u(t)$$

Use the Laplace transform to solve the differential equation subject to

$$y(0) = 1, \frac{dy(0)}{dt} = 0.$$

\*\*\*End\*\*\*