# 2 Parte-Neural Networks

# February 2, 2024

[13]: import json

```
import numpy as np
      from tensorflow import keras
      from tensorflow.keras import layers
      from math import log, sqrt
      import matplotlib.pyplot as plt
      import math
[14]: ising_tc = 1/(1/2*log(1+sqrt(2)))
      ising tc
[14]: 2.269185314213022
[15]: def abre_e_le(file_name):
          with open(file_name, 'r') as file:
              loaded_data = json.load(file)
          return loaded_data
[16]: def deixa_no_capricho(json_dict):
          arranged_dict = dict()
          for temp in json_dict.keys():
              arranged_dict[float(temp)] = list()
              for confs in json dict[temp]:
                  conf = np.array(confs[0])
                  conf class = confs[1]
                  arranged_dict[float(temp)].append((conf, conf_class))
          return arranged_dict
```

As duas funções acima leem os arquvios salvos a partir de "1\_Parte-Monte\_Carlo\_generating\_and\_saving.ipynb" e armazenam as informações nas estruturas de dados necessárias

```
[17]: def split(treino):
    arr_of_arrs = list()
    arr_of_class = list()
```

```
for temp in treino.keys():
    for confs in treino[temp]:
        arr_of_arrs.append(confs[0])
        arr_of_class.append(confs[1])

arr_of_arrs = np.asarray(arr_of_arrs)
    arr_of_class = np.asarray(arr_of_class).reshape((-1,1))

return arr_of_arrs, arr_of_class
```

'split' separa o 'lattice' de sua classificação(ferromagnético ou paramagnético)

```
[18]: treino = abre_e_le("train.txt")
    treino = deixa_no_capricho(treino)

teste = abre_e_le("test.txt")
    teste = deixa_no_capricho(teste)

x_train, y_train = split(treino)
    x_test, y_test = split(teste)
```

```
[19]: temp1 = [1.189 for i in range(0,len(teste[1.189]))]
  temp2 = [1.733 for i in range(0,len(teste[1.733]))]
  temp3 = [2.069 for i in range(0,len(teste[2.069]))]
  temp4 = [2.269 for i in range(0,len(teste[2.269]))]
  temp5 = [2.278 for i in range(0,len(teste[2.278]))]
  temp6 = [2.469 for i in range(0,len(teste[2.278]))]
  temp7 = [2.822 for i in range(0,len(teste[2.469]))]
  temp8 = [3.367 for i in range(0,len(teste[3.367]))]
temp8 = temp1+temp2+temp3+temp4+temp5+temp6+temp7+temp8
```

'temps' será usado para construirmos as visualizações

### 0.0.1 Rede simples

```
[20]: model = keras.Sequential([
    keras.layers.Dense(10, activation='relu'),
    keras.layers.Dense(1, activation='sigmoid')
])
```

Uma rede com apenas uma camada intermediária composta por 10 perceptrons.

```
[21]: model = keras.Sequential([
    keras.layers.Dense(10, activation='relu'),
    keras.layers.Dense(1, activation='sigmoid')
```

```
100/100 [============= ] - Os 1ms/step - loss: 0.4459 - binary_accuracy: 0.7994
```

# Explicação

Como temos um problema de classificação binário, a função de perda utilizada é "binary\_crossentropy" (a mais utilizada nesses cenários).

Para avaliarmos nosso modelo, iremos verificar sua acurácia.

Depois treinamos nosso modelo em um conjunto de treino e avaliamos seu desempenho em um conjunto de teste.

Salvamos ao final o modelo treinado, seu "histórico de treino" e sua avaliação no conjunto de teste.

```
[22]: print(f"Acurácia no conjunto de teste: {evaluation[1]}")
```

Acurácia no conjunto de teste: 0.7993749976158142

nossa simples rede classificou corretamente o "lattice" em 79.7% das vezes no conjunto de dados não visto durante o treino

```
[23]: def simple_net_calc_prob(teste,trained_model, temps):
    prob_0 = dict()
    prob_1 = dict()

    for temp in teste.keys():
        prob_0[temp] = list()
        prob_1[temp] = list()
        for conf in teste[temp]:
            element = np.expand_dims(conf[0],axis=0)

        prob = trained_model.predict(element, verbose=0)
        elemen_prob_1 = prob[0][0]
```

```
elemen_prob_0 = 1 - elemen_prob_1

prob_0[temp].append(elemen_prob_0)
 prob_1[temp].append(elemen_prob_1)

return prob_0, prob_1
```

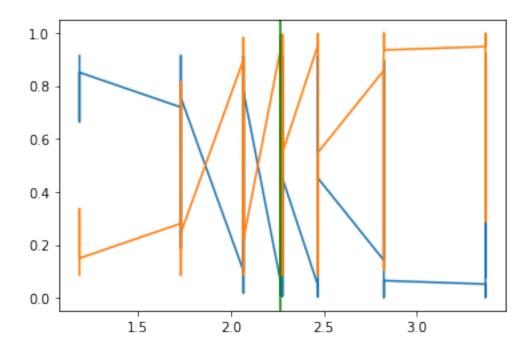
Iremos iterar novamente sobre o conjunto de testes, agora salvando cada previsão feita.

```
[24]: prob_0, prob_1 = simple_net_calc_prob(teste, model, temps)
```

#### Gráficos

```
[26]: plt.plot(temps, all_values_prob_0)
plt.plot(temps, all_values_prob_1)
plt.axvline(ising_tc, color='g')
```

[26]: <matplotlib.lines.Line2D at 0x7fc1104a2190>



Em um primeiro momento é possível observar que o grau de 'confusão' da rede aumenta no intervalo entre 2.0 graus e 2.5 graus, e sabemos que a temperatura de transição de fase encontra-se nesse intervalo.

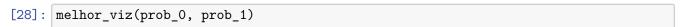
Para uma melhor visualização, vamos tirar o resultado médio para cada temperatura

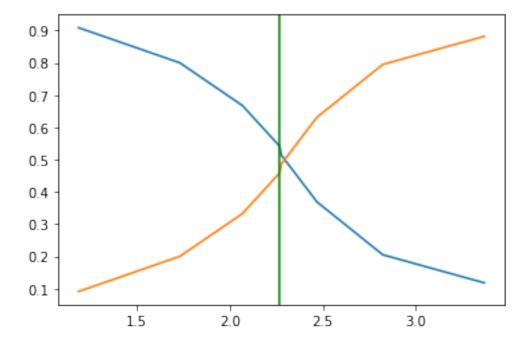
```
def melhor_viz(prob_0, prob_1):
    mean_prob_0 = list()
    mean_prob_1 = list()

for temp in prob_0.keys():
    tmp_prob_0 = sum(prob_0[temp]) / len(prob_0[temp])
    tmp_prob_1 = sum(prob_1[temp]) / len(prob_1[temp])

    mean_prob_0.append(tmp_prob_0)
    mean_prob_1.append(tmp_prob_1)

plt.plot(prob_0.keys(), mean_prob_0)
    plt.plot(prob_0.keys(), mean_prob_1)
    plt.axvline(ising_tc, color='g')
```



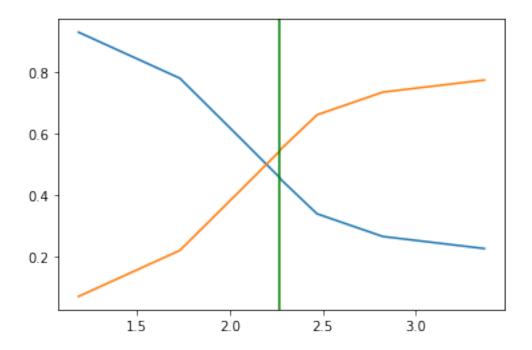


Assim percebemos que o 'ponto de confusão' máximo da rede encontra-se incrivelmente perto da

temperatura de transição de fase.

#### 0.0.2 Utilizando uma rede um pouco mais complexa

```
[29]: more_cpx_model = keras.Sequential([
        layers.Dense(4, activation='relu'),
        layers.Dense(10, activation='relu'),
        layers.Dense(4, activation='relu'),
        layers.Dense(1, activation='sigmoid'),
     ])
     more_cpx_model.
      early_stopping = keras.callbacks.EarlyStopping(
        patience=10,
        min_delta=0.001,
        restore_best_weights=True,
     )
     more_cpx_model_history = more_cpx_model.fit(
        x_train, y_train,
        validation_data=(x_test, y_test),
        batch_size=512,
        epochs=1000,
        callbacks=[early stopping],
        verbose=0, # hide the output because we have so many epochs
[30]: more_cpx model_evaluate = more_cpx_model.evaluate(x_test, y_test)
    binary_accuracy: 0.7581
[31]: print(f"Acurácia no conjunto de teste: {more_cpx_model_evaluate[1]}")
    Acurácia no conjunto de teste: 0.7581250071525574
[32]: m_prob_0, m_prob_1 = simple_net_calc_prob(teste, more_cpx_model, temps)
[33]: melhor_viz(m_prob_0, m_prob_1)
```



# 0.0.3 Redes mais complexas

#### Le Net 5

```
[34]: x_{train} = x_{train.reshape}(-1, 8, 8, 1)
      x_{test} = x_{test.reshape}(-1, 8, 8, 1)
      le_net_model = keras.models.Sequential([
          keras.layers.Input(shape=(8, 8, 1)),
          keras.layers.Conv2D(6, kernel_size=(3, 3), activation='tanh',_
       →padding='valid'),
          keras.layers.MaxPooling2D(pool_size=(2, 2)),
          keras.layers.Conv2D(16, kernel_size=(3, 3), activation='tanh',_
       →padding='valid'),
          keras.layers.Flatten(),
          keras.layers.Dense(120, activation='tanh'),
          keras.layers.Dropout(0.2),
          keras.layers.Dense(84, activation='tanh'),
          keras.layers.Dense(1, activation='sigmoid')
      ])
      le_net_model.compile(optimizer='adam', loss='binary_crossentropy',_
       →metrics=['binary_accuracy'])
      history_le_net_model = le_net_model.fit(x_train, y_train, epochs=10,_
       ⇔batch_size=32, validation_split=0.1)
```

```
Epoch 1/10
    360/360 [============= ] - 2s 2ms/step - loss: 0.4786 -
    binary_accuracy: 0.7716 - val_loss: 0.1696 - val_binary_accuracy: 0.9914
    Epoch 2/10
    binary_accuracy: 0.7833 - val_loss: 0.1257 - val_binary_accuracy: 0.9945
    Epoch 3/10
    360/360 [============ ] - 1s 2ms/step - loss: 0.4575 -
    binary_accuracy: 0.7863 - val_loss: 0.1430 - val_binary_accuracy: 0.9945
    Epoch 4/10
    360/360 [============ ] - 1s 2ms/step - loss: 0.4538 -
    binary_accuracy: 0.7869 - val_loss: 0.1068 - val_binary_accuracy: 0.9937
    Epoch 5/10
    binary_accuracy: 0.7891 - val_loss: 0.1545 - val_binary_accuracy: 0.9922
    Epoch 6/10
    360/360 [=========== ] - 1s 2ms/step - loss: 0.4536 -
    binary_accuracy: 0.7891 - val_loss: 0.1538 - val_binary_accuracy: 0.9930
    360/360 [============= ] - 1s 2ms/step - loss: 0.4543 -
    binary_accuracy: 0.7878 - val_loss: 0.1233 - val_binary_accuracy: 0.9953
    360/360 [============ ] - 1s 2ms/step - loss: 0.4502 -
    binary_accuracy: 0.7899 - val_loss: 0.1241 - val_binary_accuracy: 0.9930
    Epoch 9/10
    360/360 [============ ] - 1s 2ms/step - loss: 0.4496 -
    binary_accuracy: 0.7911 - val_loss: 0.1311 - val_binary_accuracy: 0.9945
    Epoch 10/10
    360/360 [============= ] - 1s 2ms/step - loss: 0.4501 -
    binary_accuracy: 0.7896 - val_loss: 0.1395 - val_binary_accuracy: 0.9922
    100/100 [============= ] - Os 1ms/step - loss: 0.4330 -
    binary_accuracy: 0.8019
[35]: print(f"Acurácia no conjunto de teste: {evaluation_le_net_model[1]}")
    Acurácia no conjunto de teste: 0.8018749952316284
[36]: def le_net_calc_prob(teste, model):
        prob_0 = dict()
        prob_1 = dict()
        for temp in teste.keys():
           prob_0[temp] = list()
           prob_1[temp] = list()
```

evaluation\_le net\_model = le\_net\_model.evaluate(x\_test, y\_test)

```
for conf in teste[temp]:
    element = conf[0].reshape(-1, 8, 8, 1)

prob = model.predict(element, verbose=0)

elemen_prob_1 = prob[0][0]
    elemen_prob_0 = 1 - elemen_prob_1

prob_0[temp].append(elemen_prob_0)
    prob_1[temp].append(elemen_prob_1)

return prob_0, prob_1
```

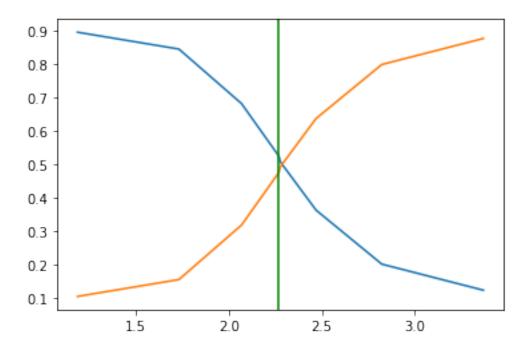
```
[37]: le_net_prob_0, le_net_prob_1 = le_net_calc_prob(teste, le_net_model)
```

```
[38]: def le_net_melhor_viz():
    mean_prob_0 = list()
    mean_prob_1 = list()

for temp in le_net_prob_0.keys():
        tmp_prob_0 = sum(le_net_prob_0[temp]) / len(le_net_prob_0[temp])
        tmp_prob_1 = sum(le_net_prob_1[temp]) / len(le_net_prob_1[temp])

        mean_prob_0.append(tmp_prob_0)
        mean_prob_1.append(tmp_prob_1)

plt.plot(prob_0.keys(), mean_prob_0)
    plt.plot(prob_0.keys(), mean_prob_1)
    plt.axvline(ising_tc, color='g')
```



#### AlexNet

```
[39]: alex_net_model = keras.models.Sequential([
          keras.layers.Input(shape=(8, 8, 1)),
          keras.layers.Conv2D(96, kernel_size=(3, 3), strides=(2, 2),
       ⇔activation='relu'),
          keras.layers.Conv2D(256, kernel_size=(5, 5), padding='same',__
       ⇒activation='relu'),
          keras.layers.Conv2D(384, kernel_size=(3, 3), padding='same',_
       ⇔activation='relu'),
          keras.layers.Conv2D(384, kernel_size=(3, 3), padding='same',_
       ⇔activation='relu'),
          keras.layers.Conv2D(256, kernel_size=(3, 3), padding='same',_
       ⇔activation='relu'),
          keras.layers.Flatten(),
          keras.layers.Dense(4096, activation='relu'),
          keras.layers.Dropout(0.5),
          keras.layers.Dense(4096, activation='relu'),
          keras.layers.Dropout(0.5),
          keras.layers.Dense(1, activation='sigmoid')
      ])
      # Compile the model
      alex_net_model.compile(optimizer='adam', loss='binary_crossentropy',__
       →metrics=['binary_accuracy'])
```

```
[40]: history_alex_net = alex_net_model.fit(x_train, y_train, epochs=10,__
      ⇒batch_size=32, validation_split=0.1)
     evaluation_alex_net = alex_net_model.evaluate(x_test, y_test)
    Epoch 1/10
    360/360 [============= ] - 142s 392ms/step - loss: 0.5174 -
    binary_accuracy: 0.7510 - val_loss: 0.1151 - val_binary_accuracy: 0.9844
    Epoch 2/10
    360/360 [============ ] - 134s 373ms/step - loss: 0.4683 -
    binary_accuracy: 0.7807 - val_loss: 0.2355 - val_binary_accuracy: 0.9945
    Epoch 3/10
    360/360 [============= ] - 134s 373ms/step - loss: 0.4665 -
    binary_accuracy: 0.7786 - val_loss: 0.2450 - val_binary_accuracy: 0.9828
    Epoch 4/10
    360/360 [============= ] - 138s 383ms/step - loss: 0.4593 -
    binary_accuracy: 0.7841 - val_loss: 0.1143 - val_binary_accuracy: 0.9953
    Epoch 5/10
    360/360 [============== ] - 140s 390ms/step - loss: 0.4442 -
    binary_accuracy: 0.7915 - val_loss: 0.1161 - val_binary_accuracy: 0.9844
    Epoch 6/10
    360/360 [============ ] - 149s 414ms/step - loss: 0.4177 -
    binary_accuracy: 0.8025 - val_loss: 0.1078 - val_binary_accuracy: 0.9711
    Epoch 7/10
    360/360 [============ ] - 149s 415ms/step - loss: 0.3869 -
    binary_accuracy: 0.8264 - val_loss: 0.1543 - val_binary_accuracy: 0.9438
    Epoch 8/10
    360/360 [=========== ] - 139s 386ms/step - loss: 0.3492 -
    binary_accuracy: 0.8484 - val_loss: 0.1307 - val_binary_accuracy: 0.9484
    Epoch 9/10
    360/360 [============= ] - 134s 372ms/step - loss: 0.3139 -
    binary_accuracy: 0.8694 - val_loss: 0.1291 - val_binary_accuracy: 0.9430
    Epoch 10/10
    360/360 [============ ] - 134s 372ms/step - loss: 0.2828 -
    binary_accuracy: 0.8905 - val_loss: 0.1743 - val_binary_accuracy: 0.9250
    binary_accuracy: 0.7713
[41]: print(f"Test Accuracy: {evaluation_alex_net[1]}")
    Test Accuracy: 0.7712500095367432
[42]: def alex_net_calc_prob(teste, model):
        prob 0 = dict()
        prob_1 = dict()
        for temp in teste.keys():
            prob_0[temp] = list()
```

```
prob_1[temp] = list()

for conf in teste[temp]:
    element = conf[0].reshape(-1, 8, 8, 1)

prob = model.predict(element, verbose=0)

elemen_prob_1 = prob[0][0]
    elemen_prob_0 = 1 - elemen_prob_1

prob_0[temp].append(elemen_prob_0)
    prob_1[temp].append(elemen_prob_1)

return prob_0, prob_1

alex_net_prob_0, alex_net_prob_1 = alex_net_calc_prob(teste, alex_net_model)
```

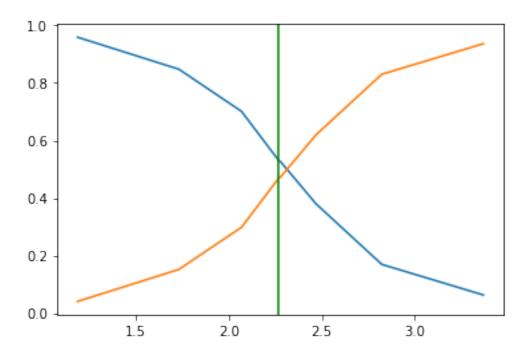
```
[43]: def alex_net_melhor_viz():
    mean_prob_0 = list()
    mean_prob_1 = list()

for temp in le_net_prob_0.keys():
    tmp_prob_0 = sum(alex_net_prob_0[temp]) / len(alex_net_prob_0[temp])
    tmp_prob_1 = sum(alex_net_prob_1[temp]) / len(alex_net_prob_1[temp])

    mean_prob_0.append(tmp_prob_0)
    mean_prob_1.append(tmp_prob_1)

plt.plot(prob_0.keys(), mean_prob_0)
    plt.plot(prob_0.keys(), mean_prob_1)
    plt.axvline(ising_tc, color='g')

alex_net_melhor_viz()
```



Vgg net Vgg net não roda no sistema utilizado. Utilizaremos o colab no futuro para tentar rodar

```
[44]:
      vgg_net_model = keras.models.Sequential([
      keras.layers.Input(shape=(8, 8, 1)),
      keras.layers.Conv2D(64, kernel_size=(3, 3), padding='same', activation='relu'),
      keras.layers.Conv2D(64, kernel_size=(3, 3), padding='same', activation='relu'),
      #layers.MaxPooling2D(pool_size=(2, 2), strides=(2, 2)),
      keras.layers.Conv2D(128, kernel_size=(3, 3), padding='same', activation='relu'),
      keras.layers.Conv2D(128, kernel_size=(3, 3), padding='same', activation='relu'),
      #layers.MaxPooling2D(pool_size=(2, 2), strides=(2, 2)),
      keras.layers.Conv2D(256, kernel_size=(3, 3), padding='same', activation='relu'),
      keras.layers.Conv2D(256, kernel_size=(3, 3), padding='same', activation='relu'),
      keras.layers.Conv2D(256, kernel_size=(3, 3), padding='same', activation='relu'),
      #layers.MaxPooling2D(pool_size=(2, 2), strides=(2, 2)),
      keras.layers.Conv2D(512, kernel size=(3, 3), padding='same', activation='relu'),
      keras.layers.Conv2D(512, kernel_size=(3, 3), padding='same', activation='relu'),
      keras.layers.Conv2D(512, kernel size=(3, 3), padding='same', activation='relu'),
      #layers.MaxPooling2D(pool_size=(2, 2), strides=(2, 2)),
      keras.layers.Conv2D(512, kernel_size=(3, 3), padding='same', activation='relu'),
      keras.layers.Conv2D(512, kernel_size=(3, 3), padding='same', activation='relu'),
      keras.layers.Conv2D(512, kernel_size=(3, 3), padding='same', activation='relu'),
      #layers.MaxPooling2D(pool_size=(2, 2), strides=(2, 2)),
      keras.layers.Flatten(),
      keras.layers.Dense(4096, activation='relu'),
```

```
keras.layers.Dropout(0.5),
keras.layers.Dense(4096, activation='relu'),
keras.layers.Dropout(0.5),
keras.layers.Dense(1, activation='sigmoid')
])
"""
```

```
[44]: "\nvgg_net_model = keras.models.Sequential([\nkeras.layers.Input(shape=(8, 8,
      1)), \nkeras.layers.Conv2D(64, kernel_size=(3, 3), padding='same',
      activation='relu'), \nkeras.layers.Conv2D(64, kernel_size=(3, 3), padding='same',
      activation='relu'), \n#layers.MaxPooling2D(pool size=(2, 2), strides=(2,
      2)), \nkeras.layers.Conv2D(128, kernel_size=(3, 3), padding='same',
      activation='relu'),\nkeras.layers.Conv2D(128, kernel size=(3, 3),
      padding='same', activation='relu'), \n#layers.MaxPooling2D(pool_size=(2, 2),
      strides=(2, 2)),\nkeras.layers.Conv2D(256, kernel size=(3, 3), padding='same',
      activation='relu'), \nkeras.layers.Conv2D(256, kernel_size=(3, 3),
      padding='same', activation='relu'), \nkeras.layers.Conv2D(256, kernel_size=(3,
      3), padding='same', activation='relu'), \n#layers.MaxPooling2D(pool_size=(2, 2),
      strides=(2, 2)),\nkeras.layers.Conv2D(512, kernel_size=(3, 3), padding='same',
      activation='relu'), \nkeras.layers.Conv2D(512, kernel_size=(3, 3),
      padding='same', activation='relu'),\nkeras.layers.Conv2D(512, kernel_size=(3,
      3), padding='same', activation='relu'), \n#layers. MaxPooling2D(pool size=(2, 2),
      strides=(2, 2)),\nkeras.layers.Conv2D(512, kernel_size=(3, 3), padding='same',
      activation='relu'), \nkeras.layers.Conv2D(512, kernel_size=(3, 3),
      padding='same', activation='relu'), \nkeras.layers.Conv2D(512, kernel_size=(3,
      3), padding='same', activation='relu'), \n#layers. MaxPooling2D(pool size=(2, 2),
      strides=(2, 2)),\nkeras.layers.Flatten(),\nkeras.layers.Dense(4096,
      activation='relu'), \nkeras.layers.Dropout(0.5), \nkeras.layers.Dense(4096,
      activation='relu'), \nkeras.layers.Dropout(0.5), \nkeras.layers.Dense(1,
      activation='sigmoid')\n])\n"
```

```
[45]: #vgg_net_model.compile(optimizer='adam',

# loss='binary_crossentropy',

# metrics=['binary_accuracy'])

#history_vgg_net = vgg_net_model.fit(x_train, y_train, epochs=10, u)

-batch_size=32, validation_split=0.1)

#evaluation_vgg_net = vgg_net_model.evaluate(x_test, y_test)
```

#### Algumas conclusões

- Arquiteturas básicas já são capazes de reconhecer as fases do sistema, especialmente as fases em temperaturas mais extremas.
- Uma rede em que o ponto máximo de confusão coincida com a solução de Onsager não necessariamente é uma rede que teve um melhor desempenho, vimos isso pois uma rede mais básica coincidiu melhor com a temperatura de transição de fase do que redes mais complexas, mesmo a rede mais básica tendo um desempenho pior na avaliação no conjunto de testes. Ainda sim a capaciadade de reconhecimento de padrões em um sistema complexo é notável.