



$$i = \sqrt{-1}, i^2 = -1, i^3 = -i, i^4 = 1$$

$$\begin{aligned} & \Rightarrow 2 + 3i + 7i^2 + 5i^3 + 9i^4 \\ & 2 + 3i + 7(-1) + 5(-i) + 9(1) \\ & 2 + 3i - 7 - 5i + 9 \\ & \boxed{4 - 2i} \text{ — complex number} \end{aligned}$$

$$\begin{aligned} & \Rightarrow (2 - 3i) - (6 - 18i) \\ & 2 - 3i - 6 + 18i \\ & \boxed{-4 + 15i} \end{aligned}$$

$$\begin{aligned} & \Rightarrow (7 - 10i) - (3 + 30i) \\ & 7 - 10i - 3 - 30i \\ & \boxed{4 - 40i} \end{aligned}$$

$$\begin{aligned} & \Rightarrow (-10i) + (-40 + 8i) \\ & -2i - 40 \\ & \boxed{-40 - 2i} \end{aligned}$$

$$\begin{aligned} & \Rightarrow (-33 - 2i) - (50 + 9i) \\ & -33 - 2i - 50 - 9i \\ & \boxed{-83 - 11i} \end{aligned}$$

$$\begin{aligned} & \Rightarrow (35 - 23i) + (13 + 25i) \\ & \boxed{48 + 2i} \end{aligned}$$

$$\begin{aligned} & \Rightarrow 3(-2 + 10i) \\ & -6 + 30i \end{aligned}$$

$$\begin{aligned} & \Rightarrow -6i(5 + 7i) \\ & -30i - 42i^2 \\ & -30i - 42(-1) \\ & -30i + 42 \\ & \boxed{42 - 30i} \end{aligned}$$

$$\begin{aligned} & \Rightarrow (1+2i)(3+i) \\ & 3+i+6i+2i^2 \\ & 3+7i+2(-1) \\ & -2+3+7i \\ & \boxed{1+7i} \end{aligned}$$

$$\begin{aligned} & \Rightarrow (4+i)(7-3i) \\ & 28-12i+7i-3i^2 \\ & 28-5i-3(-1) \\ & 28+3-5i \\ & \boxed{31-5i} \end{aligned}$$

$$\begin{aligned} & \Rightarrow (2-i)(2+i) \\ & 4+\cancel{2i-2i}-i^2 \\ & 4-i^2 \\ & 4-(-1) \\ & 4+1 \\ & \boxed{5} \end{aligned}$$

$$\begin{aligned} & \Rightarrow (1+i)(1+i) \\ & 1+i+i+i^2 \\ & \cancel{1+2i} \\ & \boxed{2i} \end{aligned}$$

$$\begin{aligned} & \Rightarrow (a-bi)(a+bi) \\ & a^2 + \cancel{abi} - \cancel{abi} - bi^2 \\ & a^2 - b^2i^2 \\ & a^2 - b^2(-1) \\ & \boxed{a^2 + b^2} \end{aligned}$$

$$\begin{aligned} & \Rightarrow (1+3i)^2 \cdot (2+i) \\ & (1+3i)(1+3i)(2+i) \\ & 1+3i+3i+9i^2 \\ & (1+6i+9i^2)(2+i) \\ & 2+i+12i+6i^2+18i^2+9i^3 \end{aligned}$$

$$\begin{aligned} & \Rightarrow 15i(-i-1) \\ & -15i^2-15i \\ & -15(-1)-15i \\ & \boxed{15-15i} \end{aligned}$$

$$\begin{aligned} & \Rightarrow -6i(6-2i) \\ & -36i+12i^2 \\ & -36i+12(-1) \\ & \boxed{-12-36i} \end{aligned}$$

$$\begin{aligned} & 2+13i+24i^2+9i^3 \\ & 2+13i+24(-1)+9(-i) \\ & 2+13i-24-9i \\ & \boxed{-22+4i} \end{aligned}$$

$$\Rightarrow -3i(8i + 5)$$

$$-24i^2 - 15i$$

$$-24(-1) - 15i$$

$$\boxed{24 - 15i}$$

$$\Rightarrow 9i(-4 - 7i)$$

$$-36i - 63i^2$$

$$-36i - 63(-1)$$

$$\boxed{63 - 36i}$$

$$\Rightarrow -5i(5i - 5)$$

$$-25i^2 + 25i$$

$$-25(-1) + 25i$$

$$\boxed{25 + 25i}$$

$$\Rightarrow 11(6i - 9)$$

$$66i - 99$$

$$\boxed{-99 + 66i}$$

$$\Rightarrow 5i(5 + 3i)$$

$$25i + 15i^2$$

$$25i + 15(-1)$$

$$\boxed{-15 + 25i}$$

$$\Rightarrow 14(-2i + 6)$$

$$-28i + 84$$

$$\boxed{84 - 28i}$$

$$\Rightarrow (7 - 10i) - (3 + 30i)$$

$$7 - 10i - 3 - 30i$$

$$\boxed{4 - 40i}$$

$$\Rightarrow (-3 + 71i) + (9)$$

$$\boxed{6 + 71i}$$

$$\Rightarrow (21 + 2i) + (13 + 8i)$$

$$\boxed{34 + 10i}$$

$$\Rightarrow (-14 + 3i) - (14i)$$

$$-14 + 3i - 14i$$

$$\boxed{-14 - 11i}$$

$$\Rightarrow 8(11i + 2)$$

$$88i + 16$$

$$\boxed{16 + 88i}$$

$$\Rightarrow -6i(6 - 2i)$$

$$-36i + 12i^2$$

$$-36i + 12(-1)$$

$$\boxed{-12 - 36i}$$

$$\Rightarrow (1+i) \cdot (3-5i)$$

$$3 - 5i + 3i - 5i^2$$

$$3 - 2i - 5(-1)$$

$$3 - 2i + 5$$

$$\boxed{8 - 2i}$$

$$\Rightarrow (-2-3i) \cdot (-5-2i)$$

$$10 + 4i + 15i + 6i^2$$

$$10 + 19i + 6(-1)$$

$$10 - 6 + 19i$$

$$\boxed{4 + 19i}$$

$$\Rightarrow 2x^2 + 5 = 6x$$

$$2x^2 - 6x + 5 = 0$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-(-6) \pm \sqrt{(-6)^2 - 4(2)(5)}}{2(2)}$$

$$\frac{6 \pm \sqrt{36 - 40}}{4} = \frac{6 \pm \sqrt{-4}}{4} = \frac{6 \pm 2i}{4} = \boxed{\frac{3 \pm i}{2}}$$

$$\blacktriangleright -9x^2 + x + 3 = 0$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-1 \pm \sqrt{(1)^2 - 4(-9)(3)}}{2(-9)} = \frac{-1 \pm \sqrt{1 + 108}}{-18}$$

$$\frac{-1 \pm \sqrt{109}}{-18} = \frac{1 \pm \sqrt{109}}{18} = \boxed{\frac{1}{18} \pm \frac{\sqrt{109}}{18}}$$

$$\blacktriangleright 3x^2 + 9x + 17 = 0$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-9 \pm \sqrt{(9)^2 - 4(3)(17)}}{2(3)} = \frac{-9 \pm \sqrt{81 - 204}}{6}$$

$$\frac{-9 \pm \sqrt{-123}}{6} = \frac{-9 \pm 123i}{6} = -\frac{9}{6} \pm \frac{123i}{6} = \boxed{-\frac{3}{2} \pm \frac{123i}{6}}$$

$$\Rightarrow 5x^2 + 3x + 1 = 0$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-3 \pm \sqrt{(3)^2 - 4(5)(1)}}{2(5)} = \frac{-3 \pm \sqrt{9 - 20}}{10}$$



$$\frac{-3 \pm \sqrt{-11}}{10} = \frac{-3 \pm i\sqrt{11}}{10} = \left[-\frac{3}{10} \pm \frac{\sqrt{11}}{10}i \right]$$

$$\Rightarrow 2x^2 + 3x - 11 = 0$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-3 \pm \sqrt{(3)^2 - 4(2)(-11)}}{2(2)} = \frac{-3 \pm \sqrt{9 + 88}}{4}$$



$$\frac{-3 \pm \sqrt{97}}{4} = \left[-\frac{3}{4} \pm \frac{\sqrt{97}}{4} \right]$$

$$\begin{aligned} & \Rightarrow (70 + 22i) - (71 + 70i) \\ & 70 + 22i - 71 - 70i \\ & \boxed{-1 - 48i} \end{aligned} \quad \begin{aligned} & \Rightarrow 3i(3 + 2i) \\ & 9i + 6i^2 \\ & 9i + 6(-1) \\ & \boxed{-6 + 9i} \end{aligned}$$

$$\Rightarrow -9x^2 + x + 3 = 0$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-1 \pm \sqrt{(1)^2 - 4(-9)(3)}}{2(-9)} = \frac{-1 \pm \sqrt{1 + 108}}{-18}$$

$$\frac{-1 \pm \sqrt{109}}{-18} = \boxed{\frac{1}{18} \pm \frac{\sqrt{109}}{18}}$$

$$\begin{aligned} & \Rightarrow (2 - i) \cdot (-3 + 2i) \\ & -6 + 4i + 3i - 2i^2 \\ & -6 + 7i - 2(-1) \\ & -6 + 7i + 2 \\ & \boxed{-4 + 7i} \end{aligned}$$

$$\begin{aligned} & \Rightarrow (-30i) + (52 - 30i) \\ & -60i + 52 \\ & \boxed{52 - 60i} \end{aligned}$$

$$\begin{aligned}
 & \triangleright 11i(-8 + 10i) \\
 & -88i + 110i^2 \\
 & -88i + 110(-1) \\
 & \boxed{-110 - 88i}
 \end{aligned}$$

$$\begin{aligned}
 & \triangleright (-19 + 7i) - (29 + 32i) \\
 & -19 + 7i - 29 - 32i \\
 & \boxed{-48 - 25i}
 \end{aligned}$$

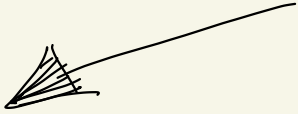
$$\begin{aligned}
 & \triangleright (5 - 5i) \cdot (-3 + 5i) \\
 & -15 + 25i + 15i - 25i^2 \\
 & -15 + 40i - 25(-1) \\
 & -15 + 25 + 40i \\
 & \boxed{10 + 40i}
 \end{aligned}$$

$$\begin{aligned}
 & \triangleright \pm \sqrt{-18} \\
 & \pm i\sqrt{18} \\
 & \quad \swarrow \searrow \\
 & \quad 9 \quad 2 \\
 & \quad \swarrow \searrow \\
 & \quad 3 \quad 3 \\
 & \boxed{\pm 3i\sqrt{2}}
 \end{aligned}$$

$$\begin{aligned}
 & \triangleright (-4 - 5i) \cdot (1 - i) \\
 & -4 + 4i - 5i + 5i^2 \\
 & -4 - i + 5(-1) \\
 & -4 - 5 - i \\
 & \boxed{-9 - i}
 \end{aligned}$$

$$\Rightarrow 3x^2 + 9x + 17 = 0$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-9 \pm \sqrt{(9)^2 - 4(3)(17)}}{2(3)}$$



$$\frac{-9 \pm \sqrt{81 - 204}}{6} = \frac{-9 \pm \sqrt{-123}}{6} = \frac{-9 \pm i\sqrt{123}}{6}$$

$$= \left[-\frac{3}{2} \pm \frac{\sqrt{123}}{6}i \right]$$