



# Area and circumference of circles

$$2 \cdot \pi \cdot r = \text{Circumference}$$

$$\frac{1133.54}{2} = \frac{2\pi r}{2}$$

$$\frac{566.77}{\pi} = \frac{\cancel{\pi} r}{\cancel{\pi}}$$

$$180.5 = r$$

$$180.5 \cdot 2 = d$$

$$\boxed{361 = d}$$

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$$\frac{\cancel{2} \pi r}{\cancel{2}} = \frac{452.16}{2}$$

$$\frac{\cancel{\pi} r}{\cancel{\pi}} = \frac{226.08}{\pi}$$

$$\rightarrow \boxed{r = 72}$$

$$A = \pi r^2$$

$$\pi (1)^2$$

$$\pi(1) = \boxed{3.14}$$

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$$d = 2 \quad \pi(r)^2 = \pi(2/2)^2 = \pi(1)^2$$
$$= \pi(1)$$
$$= \boxed{3.14}$$

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$$\frac{50.24}{2} = \frac{2\pi r}{2}$$

$$\frac{25.12}{\pi} = \frac{\cancel{\pi}r}{\cancel{\pi}} \rightarrow r = 8$$

$$A = \pi r^2 \Rightarrow \pi(8)^2 \Rightarrow \pi(64) \Rightarrow \boxed{200.96}$$

$$A = \pi r^2$$

$$A = \pi(4)^2 = \pi(16) = 50.24$$

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$$D = 4 \quad r = 4/2 = 2$$

$$A = \pi r^2 \Rightarrow \pi(2)^2 = \pi(4) = \boxed{12.56}$$

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$$\frac{\cancel{2}\pi r}{\cancel{2}} = \frac{18.84}{2}$$

$$\frac{\cancel{\pi}r}{\cancel{\pi}} = \frac{9.42}{\pi} \Rightarrow r = 3$$

$$A = \pi r^2 \Rightarrow \pi(3)^2 = \pi(9) = 28.26$$

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$$r = 5 \quad A = \pi r^2 = \pi(5)^2 = \pi(25)$$

## Circumference of parts of circles

$$r=9 \quad 2 \cdot \pi \cdot r = 2 \cdot \pi \cdot 9 = 56.52$$

$$\frac{56.52}{2} = 28.26$$

$$\frac{(2 \cdot \pi \cdot 8)}{4} = \boxed{12.56}$$

$$(2 \cdot \pi \cdot 5) \cdot 0.75 = 23.55$$

$$d=10 \quad r = 10/2 = 5$$

$$\frac{(2 \cdot \pi \cdot 5)}{2} = 15.7$$

$$r=11 \quad \frac{(2 \cdot \pi \cdot 11)}{2} = \frac{69.08}{2} = \boxed{34.54}$$

Area of parts of circles

$$A = \pi r^2 = \pi (10)^2 = \pi (100) = 314$$
$$\frac{314}{4} = 78.5$$

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$$D=10 \quad r=5$$

$$A = \pi (5)^2 = \pi (25) = 78.5$$

$$\frac{78.5}{2} = \boxed{39.25}$$

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$$r=4 \quad A = \pi (r)^2 = \pi (4)^2 = \pi (16) = 50.24$$

$$50.24 \cdot 0.75 = \boxed{37.68}$$

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$$r=2 \quad A = \pi (r)^2 = \pi (2)^2 = \pi (4) = 12.56$$

$$\frac{12.56}{2} = 6.28$$

## Volume of cylinders

$$V = Bh$$

$$B = \pi(r)^2$$

$$A = \pi r^2 = \pi(2)^2 = \pi(4) = 12.56$$

$$B = 12.56 \quad h = 8$$

$$Bh = (12.56)(8) = 100.48$$

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$$A = \pi(r)^2 = \pi(6)^2 = \pi(36) = 113.04$$

$$B = 113.04 \quad h = 4$$

$$V = Bh = (113.04)(4) = \boxed{452.16}$$

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$$A = \pi r^2 = \pi(4)^2 = \pi(16) = 50.24$$

$$B = 50.24 \quad h = 10$$

$$Bh = (50.24)(10) = \boxed{502.4}$$

$$A = \pi r^2 = \pi (2)^2 = \pi (4) = 12.56$$

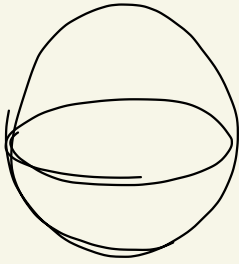
$$B = 12.56 \quad h = 5$$

$$Bh = (12.56)(5) = \boxed{62.8}$$



# Volume of spheres

Sphere



$$V = \frac{4}{3} \pi r^3$$

$$\frac{4}{3} \pi (9)^3 = 3052.08$$

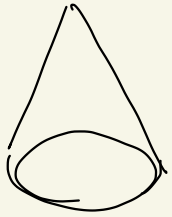
$$\frac{4}{3} \pi (7)^3 = \frac{4}{3} \pi (343) = \boxed{\frac{1372}{3} \pi}$$

$$\frac{4}{3} \pi (2)^3 = \frac{4}{3} \pi (8) = \boxed{\frac{32}{3} \pi}$$

$$\frac{4}{3} \pi r^3$$

$$\frac{4}{3} \pi (2)^3 = \frac{4}{3} \pi (8)$$

# Volume of Cones



$$V = \frac{1}{3} Bh$$

$$A = \pi r^2 = \pi(5)^2 = 25\pi$$

$$B = 25\pi \quad h = 3$$

$$V = \frac{1}{3} (25\pi)(3) = \boxed{25\pi}$$

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$$V = \frac{1}{3} Bh$$

$$A = \pi r^2 = \pi(6)^2 = \pi(36) = 36\pi$$

$$B = 36\pi \quad h = 4$$

$$V = \frac{1}{3} \cdot 36\pi \cdot 4 = \boxed{48\pi}$$

$$V = \frac{1}{3} B h$$

$$A = \pi r^2 = \pi (5)^2 = 25 \pi$$

$$B = 25 \pi \quad h = 6$$

$$\frac{1}{3} \cdot 25 \pi \cdot 6 = 50 \pi$$

$$V = \frac{1}{3} B h$$

$$A = \pi r^2 = \pi (2)^2 = 4 \pi$$

$$B = 4 \pi \quad h = 5$$

$$\frac{1}{3} \cdot 4 \pi \cdot 5 = \boxed{\frac{20}{3} \pi}$$

Volume of cylinders, spheres, and cones word problems

$$V = \frac{4}{3} \pi r^3 = \frac{4}{3} \pi (15)^3 = 4500 \pi$$

$$\frac{4500 \pi}{2} = \boxed{2250 \pi}$$

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$$V = \frac{1}{3} B h \quad \frac{3}{3} - \frac{2}{3} = \frac{1}{3}$$

$$A = \pi r^2 = \pi (3)^2 = 9 \pi$$

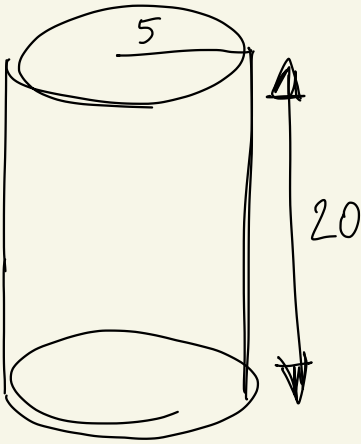
$$B = 9 \pi \quad h = 8$$

$$\frac{1}{3} \cdot 9 \pi \cdot 8 = 24 \pi$$

$$24 \pi \cdot \frac{1}{3} = \boxed{8 \pi}$$

$$V = \frac{4}{3} \pi r^3 = \frac{4}{3} \pi (30)^3 = \frac{4}{3} \pi (27000) \\ = 36000 \pi$$


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$$r = 5 \quad h = 20$$

$$V = Bh$$

$$B = \pi r^2 = \pi (5)^2 = 25\pi$$

$$B = 25\pi \quad h = 20$$

$$Bh = 500\pi$$

$$Bh = 500 \cdot 3.14$$

$$Bh = 1570$$

$$\frac{4710}{1570} = 3$$

# Unit Test

$$A = \pi r^2 = \pi (14/2 = 7)^2 = \pi (7)^2 = 49\pi$$

$$\frac{49\pi}{2} = \boxed{\frac{49}{2}\pi}$$

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$$C = 2\pi r = 2\pi(5) = 10\pi = \frac{10\pi}{2} = \boxed{5\pi}$$

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$$V = Bh$$

$$A = \pi r^2 = \pi (3)^2 = 9\pi$$

$$B = 9\pi \quad h = 2$$

$$Bh = (9\pi)(2) = \boxed{18\pi}$$

$$V = \frac{1}{3} B h$$

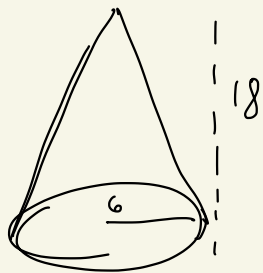
$$A = \pi r^2 = \pi (3)^2 = 9\pi$$

$$B = 9\pi \quad h = 2$$

$$\frac{1}{3} (9\pi) (2) = \boxed{6\pi}$$

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$$V = \frac{4}{3} \pi r^3 = \frac{4}{3} \pi (8)^3 = \frac{2048}{3} \pi$$



$$h = 18 \quad r = 6$$

$$V = \frac{1}{3} B h$$

$$A = \pi r^2 = \pi (6)^2 = 36\pi$$

$$B = 36\pi \quad h = 18$$

$$\frac{1}{3} \cdot 36\pi \cdot 18 = \boxed{216\pi}$$



$$2\pi r = 2\pi(8) = 16\pi = \boxed{50.24 \text{ units}}$$

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$$V = Bh$$

$$36\pi = Bh$$

$$36\pi = (\pi r^2)(h)$$

$$36\pi = (\pi(3)^2)(h)$$

$$\frac{36\pi}{9\pi} = \frac{\cancel{9\pi}(h)}{\cancel{9\pi}}$$

$$4 = h$$

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$$V = \frac{4}{3}\pi(r)^3 = \frac{4}{3}\pi(1)^3 = \frac{4}{3}\pi$$

$$= \frac{4}{3} \cdot 3.14$$

$$= \boxed{4.186}$$

$$D = 4 \quad r = 4/2 = 2$$

$$C = 2\pi r = 2\pi(2) = 4\pi = 12.56$$

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$$V = \frac{1}{3} Bh$$

$$A = \pi r^2 = \pi(3)^2 = 9\pi$$

$$B = 9\pi \quad h = 4$$

$$\frac{1}{3}(9\pi)(4) = \boxed{12\pi}$$

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$$r = 4 \quad C = 2\pi(r) = 2\pi(4) = 8\pi$$

$$8\pi \cdot \frac{3}{4} = \frac{24\pi}{4} = \boxed{6\pi}$$

$$V = \frac{4}{3} \pi r^3 = \frac{4}{3} \pi \left(\frac{1}{2}\right)^3 = \frac{4}{3} \pi \left(\frac{1}{8}\right) = \boxed{\frac{1}{6} \pi}$$

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$$r=4 \quad A = \pi r^2 = \pi (4)^2 = \pi (16) = 16\pi$$

$$\frac{16\pi}{2} = \boxed{8\pi}$$

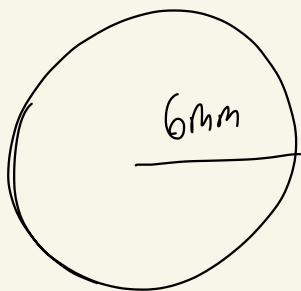
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$$V = Bh \quad A = \pi r^2 = \pi (4)^2 = \pi (16) = 16\pi$$

$$B = 16\pi \quad h = 3$$

$$Bh = 16\pi \cdot 3 = 48\pi$$

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$$V = \frac{4}{3} \pi r^3 = \frac{4}{3} \pi (6)^3$$
$$= \frac{4}{3} \pi (216)$$
$$= 288 \pi$$

$$4 \cdot 288 \pi = \boxed{1152 \pi}$$

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$$V = \frac{4}{3} \pi r^3 = \frac{4}{3} \pi (10)^3 = \frac{4}{3} \pi (1000)$$
$$= \frac{4000}{3} \pi$$

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$$C = 2 \pi r$$

$$\frac{113.04}{2} = \frac{2 \pi r}{2} \Rightarrow \frac{56.52}{\pi} = \frac{\cancel{\pi} r}{\cancel{\pi}}$$

$$18 = r$$

$$D = r \cdot 2$$

$$D = 18 \cdot 2$$

$$\boxed{D = 36}$$