

# Dijkstra Algorithm (Single source shortest path problem)

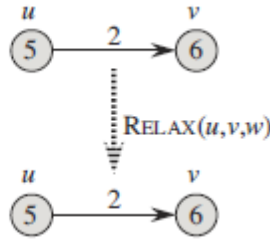
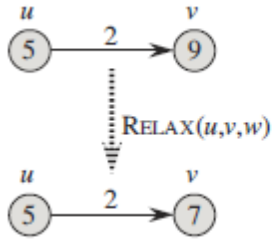
$G$  contains all non-negative edge weight.  
Weighted, directed graph.

## ✓ INITIALIZE-SINGLE-SOURCE( $G, s$ )

- 1 for each vertex  $v \in G.V$
- 2  $v.d = \infty$
- 3  $v.\pi = \text{NIL}$
- 4  $s.d = 0$

## ✓ RELAX( $u, v, w$ )

- 1 if  $v.d > u.d + w(u, v)$
- 2  $v.d = u.d + w(u, v) \rightarrow \text{DECREASE-KEY}$
- 3  $v.\pi = u$



## DIJKSTRA( $G, w, s$ ) $\rightarrow$ Source vertex

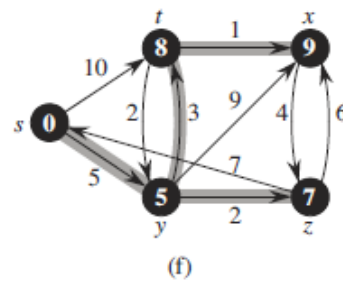
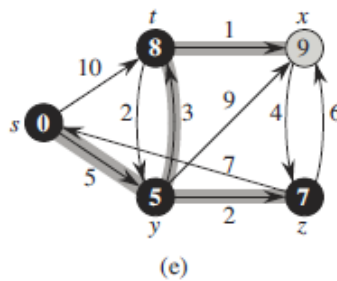
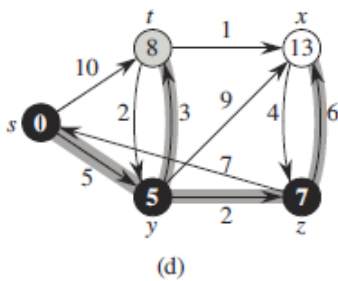
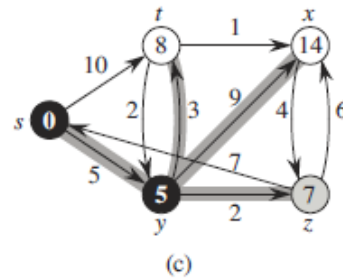
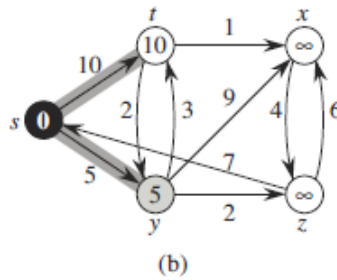
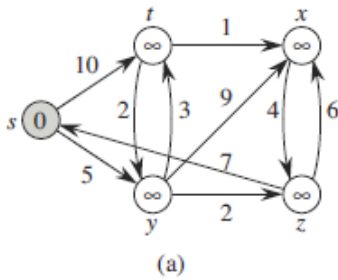
- 1 INITIALIZE-SINGLE-SOURCE( $G, s$ )
- 2  $S = \emptyset$
- 3  $Q = G.V \rightarrow \text{INSERT (Const. time)}$
- 4 while  $Q \neq \emptyset \rightarrow v$  times  $\rightarrow O(V)$
- 5  $u = \text{EXTRACT-MIN}(Q)$
- 6  $S = S \cup \{u\}$
- 7 for each vertex  $v \in G.\text{Adj}[u] \rightarrow E$  no. of times
- 8 RELAX( $u, v, w$ )  $\rightarrow \text{DECREASE-KEY } O(1)$

$Q \rightarrow$  min-priority queue  
 $S \rightarrow$  Set of vertices whose final shortest path weight from source  $s$  have already been determined.

$$S = \{s, y, z, t, x\}$$

$$\frac{O(V^2 + E)}{O(V^2)}$$

$|V|^2 > |E|$   
 $\rightarrow$  Time complexity



	Cost	Path
$s \rightarrow y$	5	$s \rightarrow y$
$s \rightarrow z$	7	$s \rightarrow y \rightarrow z$
$s \rightarrow t$	8	$s \rightarrow y \rightarrow t$
$s \rightarrow x$	9	$s \rightarrow y \rightarrow t \rightarrow x$

