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% Curran Robertson
% Lagrangian Equations of Motion of a Cart, Pendulum, Pulley System
% No Dissipative Forces.
% April 16, 2023
clear all; clc; close all
% Symbols
syms m1 m2 m3 r theta dtheta x dx g l ddtheta ddx
% Constants
% Lagrangian ( L = T - V )
L = (1/2)*m1*r^2*dtheta^2 + (1/2)*m1*(dx+r*cos(theta))^2 +
 (1/2)*m1*(r*cos(theta))^2 + (1/2)*m2*dx^2 + (1/2)*m3*dx^2 -
m1*g*r*cos(theta) - m3*g*(1-x);
L = expand(L);
L = simplify(L);
disp('L = ')
pretty(L)
% Partial Derivatives
   % DOF 1 : theta
d1 = diff(L, dtheta) ;
d2 = diff(L, theta);
    % DOF 2 : x
d4 = diff(L, dx);
d5 = diff(L, x);
% Time Derivatives
    % DOF 1 : theta
syms dtheta(t)
d3 = diff(subs(d1, dtheta, dtheta(t)), t);
    % DOF 2 : x
syms dx(t)
d6 = diff(subs(d4, dx, dx(t)), t);
% Eans of Motion
    % DOF 1 : theta
eqn1 = d3 - d2 == 0;
    % DOF 2 : x
eqn2 = d6 - d5 == 0;
% Solutions
    % DOF 1 : theta
ddtheta = solve(subs(eqn1, diff(dtheta(t), t), ddtheta);
disp('ddtheta = ')
pretty(ddtheta)
    % DOF 2 : x
ddx = solve(subs(eqn2, diff(dx(t), t), ddx), ddx);
disp('ddx = ')
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