Currency Engineering

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Contents

1 Introduction

We show how the process by which people drive markets to a sustained and stable equilibrium of aggregate supply and aggregate demand is constrained and destabilized by technical properties of the currency used. We identify the major technical problems with legacy currencies and present a design for an significantly improved currency that is highly likely to maintain a sustained and stable state with aggregate supply in equality with aggregate demand and full-employment.

Around 1777 David Hume observed, despite theoretical considerations to the contrary, that properties of a nation's currency had observable affects on the state of the economy,

> If we consider any one kingdom by itself, it is evident, that the greater or less plenty of money is of no consequence; since the prices of commodities are always proportioned to the plenty of money, and a crown in Harry VII.'s time served the same purpose as a pound does at present ... It is indeed evident, that money is nothing but the representation of labour and commodities, and serves only as a method of rating or estimating them. Where coin is in greater plenty; as a greater quantity of it is required to represent the same quantity of goods; it can have no effect, either good or bad, taking a nation within itself; any more than it would make an alteration on a merchant's books, if, instead of the Arabian method of notation, which requires few characters, he should make use of the Roman, which requires a great many ... **But notwithstanding this conclusion**, which must be allowed just, it is certain, that, since the discovery of the mines in America, industry has encreased in all the nations of Europe, except in the possessors of those mines; and this may justly be ascribed, amongst other reasons, to the encrease of gold and silver. Accordingly we find, that, in every kingdom, into which money begins to flow in greater abundance than formerly, every thing takes a new face: labour and industry gain life; the merchant becomes more enterprising, the manufacturer more diligent and skilful, and even the farmer follows his plough with greater alacrity and attention. This is not easily to be accounted for, if we consider only the influence which a greater abundance of coin has in the kingdom itself, by heightening the price of commodities, and obliging every one to pay a greater number of these little yellow or white pieces for every thing he purchases.

Hume's considerations suggest that any effective economic model requires an understanding of both how people interact with others, changing their individual economic agreements in a way that pushes markets toward equilibrium of supply and demand, but also an understanding of the role of money as an essential tool is those market transactions.

Considering the economic process in the absence of currency, the process of supply and demand as we understand it, infers a macro-economic equilibrium where aggregate demand and aggregate supply are in equllity, i.e. that if we aggregate excess supply and demand across markets, they should average out to close to zero.

[more details here]

However, contrary to Figure **??** which implies full-employment Figure 1 shows a vastly differing results.
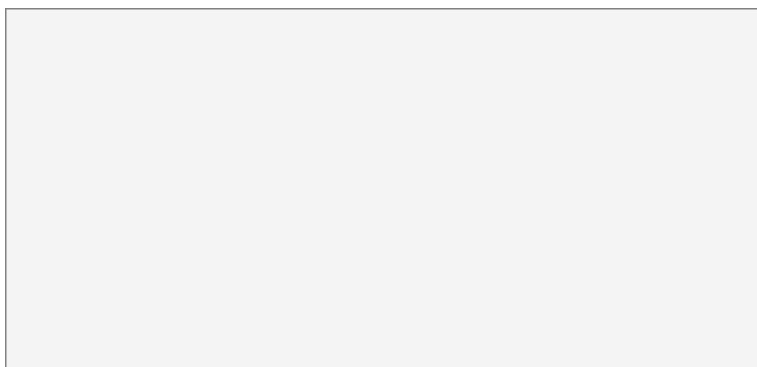
Figure 1: Inflation Rate vs. Unemployment Data

[asymmetry diagram].

Positive rates of unemployment are so consistent across all countries and throughout the decades of recorded economic history, to such an extent that unemployment appears as solid as physical law.

Economic theorists have been seeking a solution to this problem for many years without success. Considering that any currency mechanism is absent from this model of supply and demand, despite Hume's observations suggest currencies have significant effects, it seems reasonable to find a way to include currency in our model. This leads to the question of what

methods should be used to analyze the properties of currency. The fundamental insight that we present is that because currency is a digital system, the way to approach its analysis is roughly analogous to the way we approach the analysis and design of other digital systems (the internet being an interesting example), i.e. that we should approach the analysis of currency as an engineering problem, and in particular the engineering and control of dynamic systems.

Economic theory approaches economic problems similarly to the way medicine treats the human body, by applying relatively small changes, such as medicine, in response to various pathologies. Destructuring and rebuilding biological systems is impossible. Importantly however, the control system for economies, the currency, can indeed be destructured and rebuilt from first principles. Thus we take a different approach, viewing currency more like a robotics problem, something that can be built from the bottom up.

1.1 Transactions

The mechanism of accounts holding a monetary value that can be transfered to other accounts mirrors the physical world or transfer of ownership of a limited supply of paper money or similar means. This mechanism can be used by people in many ways. We categorize the main uses into different kinds of transactions. This is important because a digital currency can apply a layer of abstraction and control on the different kinds of transactions in such a way as to achieve desirable global conditions. So while money as a transfer of a single value is flexible, it also limits the currency's ability to control transactions to achieve desirable goals. Digital currencies allow for the possibility of stricter control at the transaction level in order to achieve global conditions that a simple token exchange currency cannot achieve.

Historical experience is a good guide to the main uses which people use money for, and these can be categorized into various types of transactions. The simplest and most fundamental transaction are exchange transactions as shown in figure 2.
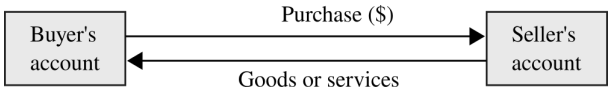
Figure 2: Exchange Transaction

We can consider exchange transactions as occuring at a point in time, where goods or services are exchanged for currency. Another common type of transaction we will call a time transaction,
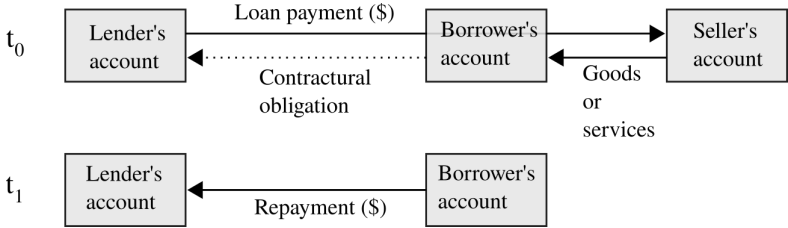
Figure 3: Time Transaction

where at time t_0 money is borrowed and used to make an exchange transaction of currency in exchange for goods and service. At a later time t_1, the principal and interest is repaid to the lender. The third transaction category we call contract transactions. Contract transactions are characterized by a transfer of money in return for a change in owner of contractural obligations.

Figure 4: Contract Transactions

Contractural transactions and variations on them can become complex. Transactions are not limited to these categories. We will examine some other transaction categories later in the paper.

1.2 Feedback Regulators
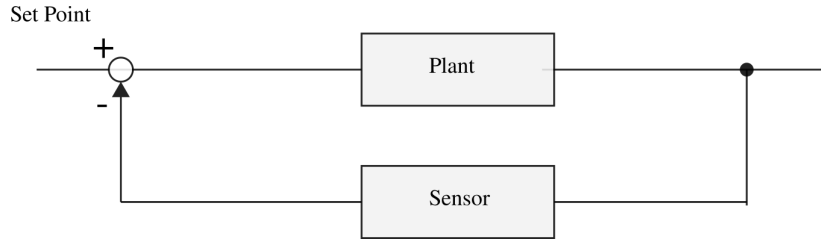
Figure 5: Economic Feedback Schema

A general control system schema with a single control variable can be represented as
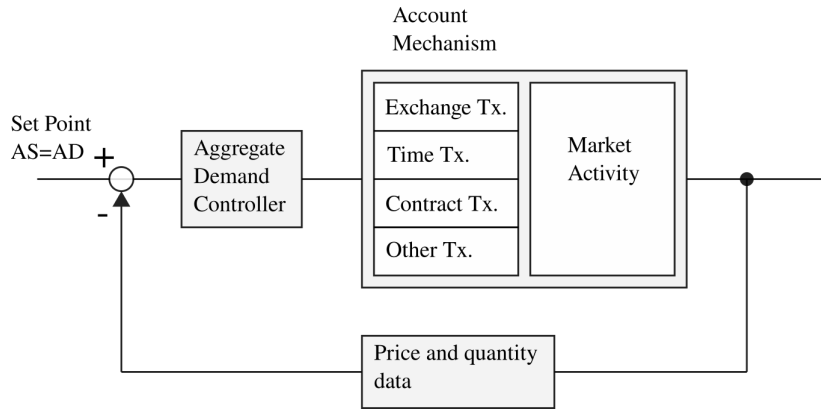
Figure 6: Economic Feedback Schema

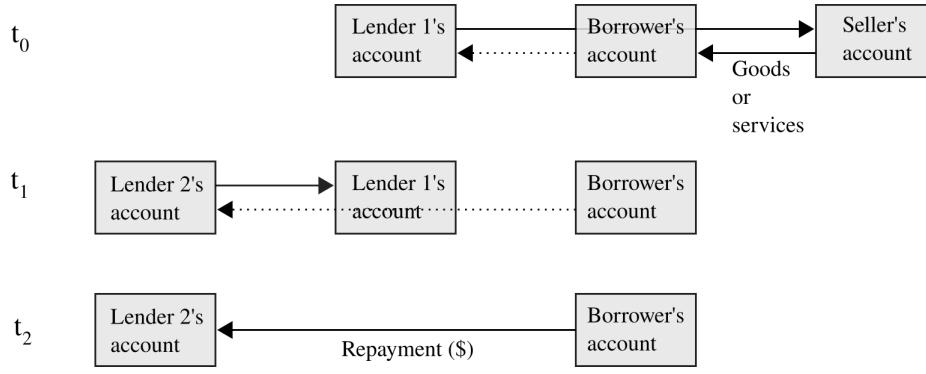A set of possible transactions provides an interface to the currency's accounts. In designing a digital currency, we have considerably more control over the way in which accounts are used, compared to a paper currency where everyone is free to exchange units of currency. The currency also consists of a also a feedback mechanism, controlled algorithmically or through a monetary authority, to regulate aggregate demand. The process by which people drive markets to an equilibrium of aggregate supply and aggregate demand occurs in the Market Activity box. This process which we think of as the central driver of market activity, is internal to currency feedback mechanism. As we will show, the design of the currency constrains can prevent this process from reaching equilibrium and we required further regulatory mechanisms built into the currency.

1.3 Results

Engineering methods are applied to the the currency mechanism not the behaviour of people. The only assumptions made about people's decision-making processes and the basic tenets of supply and demand interaction, that people drive markets

to equilibrium (and this assumption itself is confirmed when we test the theory against data (8)). In the remainder of the paper by start with the the currency control system as shown in Figure 6, and step-by-step take each transaction category, introduce it into the model and apply engineering analytical methods. As a result of this process we find the following requirements,

1. Aggregate demand must be continuously increasing at a rate sufficient to compensate for errors. Without this requirement the currency constrains the transaction possibility space of markets, preventing people from driving markets to macro-economic equilibrium.

2. All units written into contracts must be independent of the price level. Without this condition a positive feedback instability can result in runaway behaviour under increases in the inflation rate.

3. Contract transactions must be prevented. Without this condition contract transactions can result in runaway behaviour in prices, difficulties in controlling an overly complex system. Preventing contract transactions allows for a currency design with precise control over aggregate demand.

1.4 Implementation

There appear to be effective design solutions to meet these requirements.

In the absence of contract transactions a unique global value, a *Demand Index D_x* can be used by a central monetary authority or by algorithm to precisely control aggregate demand. Accounts store a base value and payments are in purchase value, demoninated in a unit (such as \$) that is a product of the base value and the demand index. In general the base value is hidden from users and accounts appear as purchasing value.

The *Price Index P_x* is regularly published, and all legal contracts must be written in a unit of account of constant purchasing power. This setup has been used in Chile for several decades for almost all contracts and has proven practical even when being used with a paper currency. With thus unit of account in place, the aggregate demand of a currency can be directly controlled and variable rates of inflation without risk of runaway behaviour.

A digital currency can be designed to distinguish between exchange transactions and time transactions.

Exchange transactions would require both the buyer and lender to record the quantity of goods and services purchase. This record could also be used by sellers and buyers to record agreements, but the use of cryptographic methods to prevent such purchase data being available to others except those directly involved in the transaction is required. This mechanism would also ensure that accurate price and quantity data could be recorded for the calculation of a Price Index.

Time transactions would require the same conditions as an exchange transaction, but also that the repayment schedule is determined at the time of the initial loan payment, and that the recipient of the loan repayment is the same account from which the load payment was made.

This would generally prevent the use of contract transactions which require that the recipient of repayment changes. It is still possible for people to make informal contracts, and to obfuscate the initial loan payment and repayments as exchange transactions, by recording a false good or service. This however, would forgo both parties any right to legal process in the case of a dispute, because the transactions are clearly marked as an exchange, with no further contractural obligations.

2 Introduction to Dynamic Systems and Control

The purpose of this section is to present the field of dynamic systems and control to a reader who is not familiar with the topic. Our goal is to demonstrate the huge technological significance of control system design, and to make clear that the methods used in this paper are all very much standard practice. Other than the original insight of the application of control system design to the economic problem, the analysis is nothing new, albeit presented in a somewhat unusual way so as to provide a crash-course in the intuitions and basic analytical method while avoiding formal mathematical methods.

2.1 Control System Design

2.2 System Specification

2.3   Brief History of Mechanic Feedback Mechanisms

Prior to the Wright brother's first flight in December 1903, Orville and Wilbur Wright believed that the most fundamental problems they needed to solve were control problems. In September 1901 Wilbur Wright's first public presentation on the feasibility of heavier-than-air flight stated that "When this one feature [control] has been worked out the age of flying machines will have arrived, for all other difficulties are of minor importance."[50]

2.4   Feedback

feedforward
  negative feedback
  positive feedback

2.5   PID Controllers

PID controllers are very simple. PID controllers are remarkably robust and in universal use for a great variety of feedback control. So while they are not the only solution, they are a good starting model for thinking about feedback systems.

  History
  TODO: Huygens
  TODO: Watt
  TODO: Maxwell
  (around 1912)
  Elmer Sperry, who introduced the gyroscope invented by TODO to the USA, developed various automatic steering systems.

> Elmer Sperry realized that the performance of the gyropilot seemed uncanny, for he had been told that no one could possibly invent a device incorporating the intuition of an expert quartermaster. He had in fact analyszed the "intuition" problem when he first began work on the pilot in 1912 and had decided that the helmsman's intuition was, in essence, tha ability to "ease off" and "meet" the helm.[21] Easing off involved lessening the rudder angle after the rudder had been put over and the ship had responded by swinging toward the desired heading; meeting was putting the rudder over to the other side (overthrow) to counter the tendency of the ship's angular momentum to carry it past the desired heading. If the helmsman did not perform these functions with skill, the ship continued to yaw. Sperry set out to devise a way of performing these functions mechanically and automatically.[22]

'Easing off' is 'Meeting' take the role of the 'D' component of a PID controller, where the controller responds to the *rate* at which the plant is moving towards the set point.

  TODO: Integral?

2.6   How Feedback Systems Go Wrong

Wrong Model
  Complexity
  Delay
  Not Smooth
  Errors
  Wrong Parameters
  While we introduced PID controllers in some detail, we don't consider their application to our problem in detail. Th The general notion of feedback is critical to our model. To deepen our understanding of feedback controllers. The reason why contemporary economies are unstable and sub-optimal, running at high levels of unemployment is because we have the wrong model. Before the practical application of PID controllers to currency control systems, we must find a better model.

2.7 Errors and Noise

2.8 Internet

Introduction

2.9 Discrete Model

3 Exchange Transactions

3.1 An Exchange Transaction Only Model

We will start with a model simplified from Figure 6. that includes only exchange transactions.
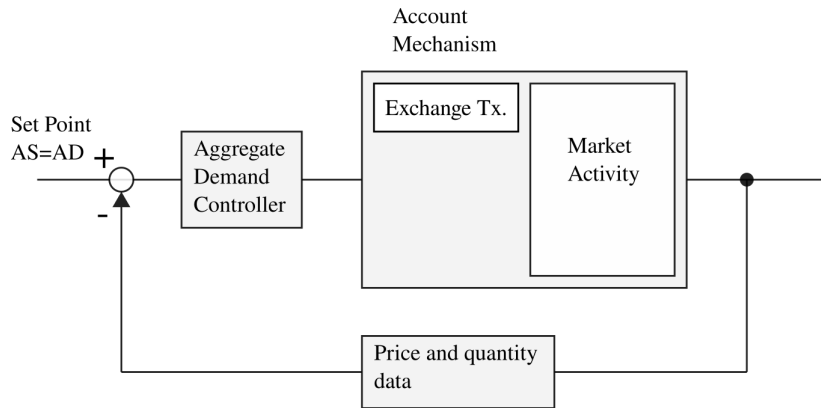

Figure 7: Exchange Only Feedback Schema

This diagram represents the global behavior of the system, which is the result of the aggregate effects of local behaviour. An obvious example, is that market behaviour at the global level is the result of a distributed system of many people interacting with each other in the context of markets. This is represented as the "Market Activity" box. Another example is that the "Exchange Tx." box represents aggregate effects of all exchange transactions. We need a way to aggregate from individual transactions to sum variables that summarize their global, macro-level properties.

3.2 Price and Quantity

Starting with exchange transactions
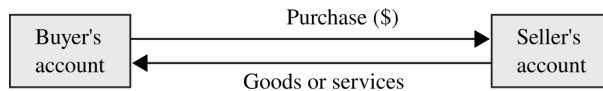
Figure 8: Exchange Transaction

we want to construct some aggregate variables. These aggregate variables could be sums, averages or some other kind of measures of centrality. We'll categorize exchange transactions into different "goods categories". We'll use this term rather than say "goods and services" for brevity and because it more closely reflects our requirements. We'll assume at this point that these goods categories are sufficiently well-defined and precise as not to introduce too much noise into our aggregate measures. For a given currency at a given period of time the transactions, we sum the quantities for each goods category.

$$(q_1, \ldots, q_N)$$

and then let pi be the average price of these transactions for a given good category. Let N be the total number of different goods categories. We'll denote the units for these values as

$$([q_1], \ldots, [q_N])$$

We'll denote the average price for each q_i.

$$(p_1, \ldots, p_N)$$

The units for the average prices are

$$\left(\left[\frac{\$}{p_1} \right], \ldots, \left[\frac{\$}{p_N} \right] \right)$$

We cannot sum either these prices or quantities because they can have different units. But each payment $p_i q_i$ can be summed because its unit, using dimensional analysis, is

$$\left[\frac{\$}{q_i} \right] [q_i] = [\$]$$

So for a given time period, total payments for transactions for a currency is

$$F = p_i q_i + \ldots + p_N q_N$$

We want to construct a aggregate measure of prices. As will become clear later in the paper we want a measure P that can be used to isolate purchasing power from the inflation rate. For example, if a person has a certain amount of currency in their account at time $t = 0$, and that they can buy a certain amount with this currency, we want to know how much money they must have in their account at time $t = 1$ so that they can buy the same amount. As written, the notion of "price level", "purchasing power" and "amount" are vague and require mathematical treatment.

Suppose at a given time the transactions with quantites

$$\overline{Q} = (q_1, \ldots, q_N) \text{ with corresponding prices } (p_1, \ldots, p_N)$$

occurs. We'll introduce Alice. We'll feed Alice a 1 dollar and Alice will spend this 1 dollar by randomly selecting goods categories in such a way that in the limit they purchase quantities all in proportion to total transactions. In other words,

$$\varepsilon_{q_1, \ldots, q_n} = c_1 \overline{Q}$$

where c_1 is a number between 0 and 1 and $\varepsilon_{q_1, \ldots, q_n}$ is the expected value of the "abstract person"'s purchases. The c_1 represents the purchasing power of the Alice. It represents the proportion of all transactions over which Alice has the power to purchase, per dollar. While purchasing power is the amount of goods that will buy a given unit of currency, the price level is its reciprocal, the amount of currency that will buy a unit of quantity.

We need to make things more precise, and to check that our measure of price can be used as an index to isolate Alice's purchasing power from changes in the inflation rate. The motivate for this will become clear later in the paper.

First we'll do a static analysis, and try to construct meaningful measures of aggregate price and quantity for a time period that has

$$\overline{Q} = (q_1, \ldots, q_N) \text{ with corresponding prices } (p_1, \ldots, p_N)$$

Here, the vector $\overline{Q}$ represents a collection of values, but we want to construct a single value that is a aggregate of these values. The problem is that each of these values may have different units. We can construct units that such as "one apple and two oranges". The problem is that if we do this it is impossible to express "two apples and two oranges" in these units. But if we consider only a single period of time that has $\overline{Q}$ transactions, then we can express this value in any unit of the form

$$([\gamma q_1], \ldots [\gamma q_N]) \tag{1}$$

for any number γ. So in fact there is not just one, but a set of feasible units in which to express $\overline{Q}$. We refer to any one of these set of units as a "basket of goods". Given that we select one of these sets of units, we can then express $\overline{Q}$ as some

number Q, where the units given by equation (1) with a specific γ. The units of Q is this basket of goods. Now we can set the price level as the payment for this basket of goods. This value P is in units \$ per basket. And so

$$F = PQ$$

The units used depends on the $\overline{Q}$ at a point in time. Of the proportion of q_i changes we would have to use a different unit, and so we couldn't do any dynamic analysis (comparisions across time). We can solve this problem by further constraining our units. As noted, for any $\overline{Q}$ at any time we can construct a new unit. We further constrain this by setting the rule that given one basket of goods whose value of γ is arbitrarily chosen, we constrain all other baskets of goods, by setting their γ to a value such that all baskets of goods have the same average of quantities weighted by their share of trade.

$$\gamma' = \gamma \frac{\varepsilon\left([q_1], \ldots, [q_N]\right)}{\varepsilon\left([q_1'], \ldots, [q_N']\right)} \tag{2}$$

Now, because γ depends only the average of the units in the baskets of goods, the distribution of q_i around this average becomes irrelevant. This means that *however* $\overline{Q}$ changes, whatever its distribution, the relation $F = PQ$ is exact.

This section has involved various manipulations of units, most critically the ratio of dollar payments to a quantity of some good or service of a collection of different quantities of goods and services. Throughout the paper we will see that questions of units are important. Section 4. will show that the price unit must change over time. In Section 6. we show that the price unit written into contracts must be constant over time. To isolate these different units and construct a control system that has sufficient degrees of freedom required for control, the use of indices is useful.

3.3   Aggregate Supply and Demand

We can now take a digital currency and measure aggregate properties F, P and Q from the set of transactions. We can also measure their relative change between two time periods.

$$\frac{\Delta F}{F} = \frac{\Delta P}{P} + \frac{\Delta Q}{Q}$$

We'll denote the rate of change of the price level as the inflation rate I. We'll denote the rate of rate of Q as the growth rate G, so

$$\frac{\Delta F}{F} = I + G \tag{3}$$

]

At the micro-level equilibriation process for a market for a good or service is driven by excess demand and excess supply. The details of this process are the result of an aggregate of human decisions and is to a large-extent un-knowable, un-measurable and un-predictable. Nevertheless it is undeniable that such an equilibriation process exists, and we can abstract this process it a reaction of prices and quantities to excess supply and excess demand at the level of a market for a good or service. Excess supply and excess demand can be measures in \$, and all the micro-level values for excess supply and demand can be summed to get a value for aggregate demand AD and aggregate supply AS.

While we can accurately measure transactions and calculate aggregate properties from these, the value of AD and AS are less concrete. We can't measure AD directly but we can see its effects in that if there is no AD or AS, then there is nothing to drive prices and quantities which will therefore remain constant. On the other hand, the unemployment rate is a good measure of excess AS. From AD and AS we can derive a set of agreements, which is the minimum of these two values (denominated in \$), and it is assumed that agreements maps directly to transactions.
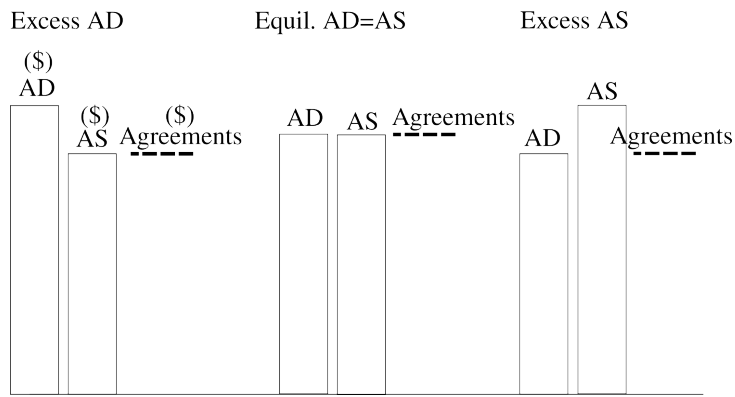
Figure 9: Agreements as a function of aggregate supply and demand

Agreements occur when both sellers and buyers want to transact and so agreements are the minimum of aggregate supply and aggregate demand as shown in Figure 9.

3.4 Market Feedback

We build here the simplest model that we can think with sufficient explanatory power. The use of supply and demand models of the decision making processes of economic participants in most useful in that it encapsulates the notion of markets being driven to equilibrium. We can capture the same notion by thinking of markets as feedback regulatiors. The value of this model of human behaviour is not that it is quanititively useful (no-one knows how to predict the decision making process of economic participants with any accuracy) but that it encapsulates the notion of an equilibriating process. This process is drive by excess supply and excess demand.
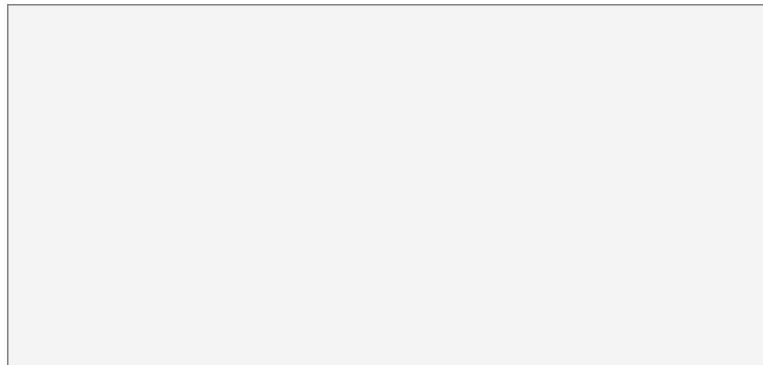

Figure 10: Model of a market for a good or service

The aggregate equilibriation process is driven by the summation of the excess supplys and excess demands of the individual goods markets it constitutes. We can also model the aggregate equilibriation process as a feedback regulator.
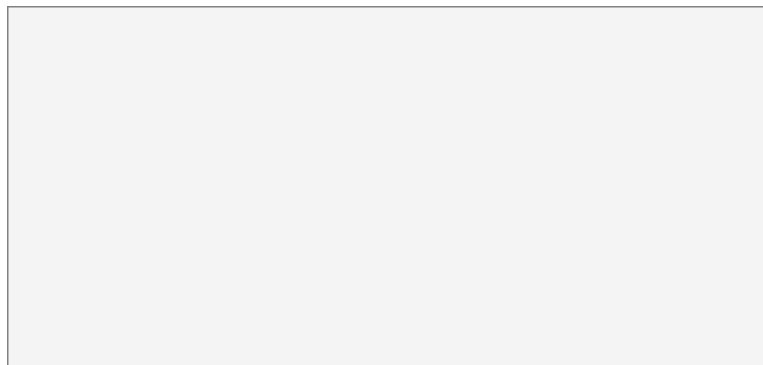

Figure 11: Model of excess aggregate demand/supply response

In the rest of the paper, only assumption we make about market behaviour is that this simple model we have presented here is sufficiently accurate for our purposes to explain the behaviour of markets. Accepting this assumption we focus our

attention of the way the design of a currency impacts on this model.

3.5 Aggregate Demand Feedback Model

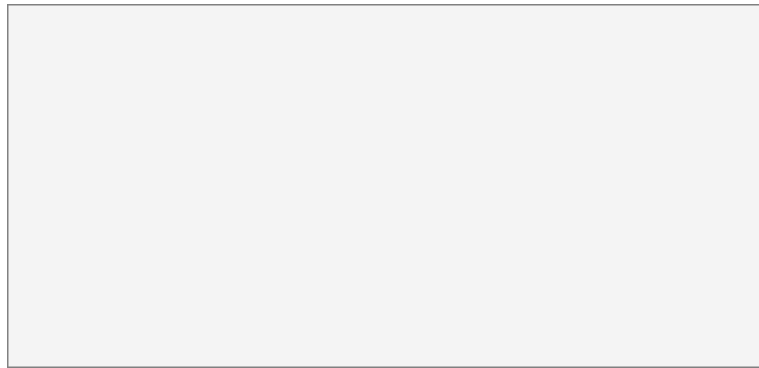
Figure 12: Feedback schema for the control of money supply

3.6 Market Symmetry

The model of excess supply and excess demand driving markets to equilibrium is the foundation of economic theory. The model we have presented is symmetrical in that there is no difference between markets being driven to equilibrium as a result of excess demand or markets being drive to equilibrium as a result
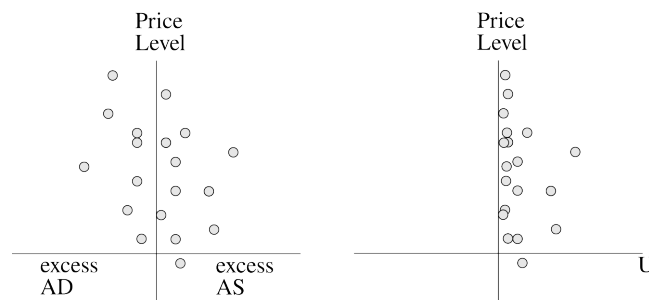
Figure 13: Symmetric Market Model

In fact if we take unemployment and inflation rate data for all countries we get results like as shown in Figure 14.
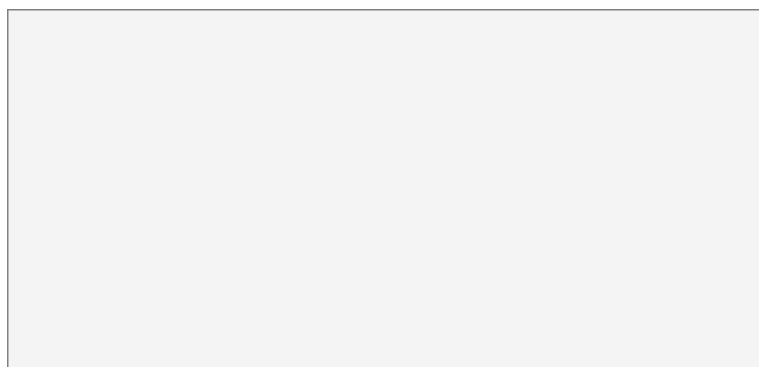
Figure 14: Unemployment and Inflation Rate

This simple model of supply and demand does not explain macro-economic data very well. The method invariably used by economists is to try to explain this anomalous behaviour as a property of decision making by economic participants as they interact in the context of markets. We will take our cue from David Hume's consideration that currency is important, and so apply methods suitable to understanding the mechanics of currencies.

3.7 Control of Price Level

In Section 3.3 we briefly introduced the idea that we could model macro-level market equilibriation as a feedback regulator, that feeds back excess aggregate supply and excess aggregate demand back into the price and quantity adjustment process that people engage in when interacting with others in the context of markets.

Another important regulation process is the control of the inflation rate through control of aggregate demand.

Before examining exchange transactions, we will briefly consider the feedback control mechanism. Indexation is an important method for controlling distributed systems like a currency. An index is a single value that is utilized by multiple components. An example of indexation in digital currencies is Bitcoin's method for regulating the rate of production of blocks by Bitcoin miners. In this case the indexation is algorithmic rather than controlled by a central authority. TODO

Another example of indexation is

The simplest way to control the price level in a digital currency is to use indexation.

TODO

The feedback control loop does not work, however, in legacy currencies because the core currency doesn't account for all money. Most money in legacy currencies is banking money, termed M1, M2 and M3. Under these conditions, money authorities must use alternative methods to try and induce financial institutions to increase the amount of banking money mainly through changing the interest rate at which the money authority lends core currency to those financial institutions. At times this method has been effective at controlling the price level, at other times less so. The process lacks precision and has a long time-lag, making its use as the main mechanism for controlling economic conditions problematic. Its effectiveness is also determined by financial institution's ability and willingness to respond to decreases or increases in the monetary authority's core lending rate in a way the maps to increases or decreases in aggregate demand.

4 Exchange Transactions and Errors
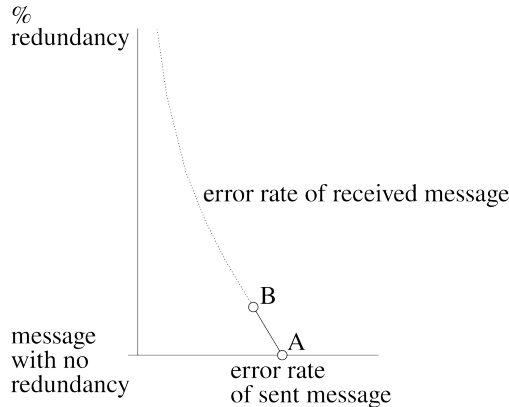
4.1 Information Theory

Figure 15: Intuition about Error Rates

Intuitively we might think about how adding redundancy to a message might change the error rate as in Figure 15. The original message with a certain error rate and no redundancy is represented by point A. If we add some redundancy to the error message we might be able to reduce the error rate of the received message to B. It seems that the problem is that for each piece of redundancy we add to the message, we introduce more errors, and so as we increase redundancy we would get decreasing returns on improved error rate. Claude Shannon proved mathematically that this intuition is incorrect, and that there exists a method of adding redundancy to our message such that if we add a H rate of redundancy we can remove all errors from the message. The correct bound on the possible error rate is show in Figure 4.2.
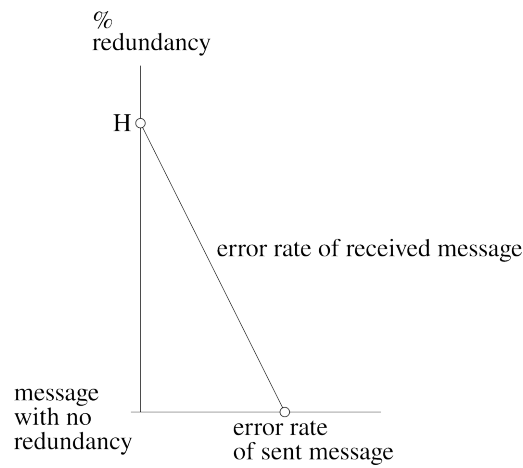
Figure 16: Shannon's Theorem of Noisy Channels

The value H indicates the extra length required of a message so as to compensate for all messages. It is determined by the probabilistic properties of the sent messages. We look into this in more details in **??**.

4.2 Aggregate Supply and Demand

In Section 3.3 we presented a simple dynamic model of aggregate supply and demand. For any engineering system we must handle the effects of errors or noise on the system. In this section we will look at the effects of an error rate that reduces the per period aggregate agreements of an economy to the actual transactions that eventuate in that period.
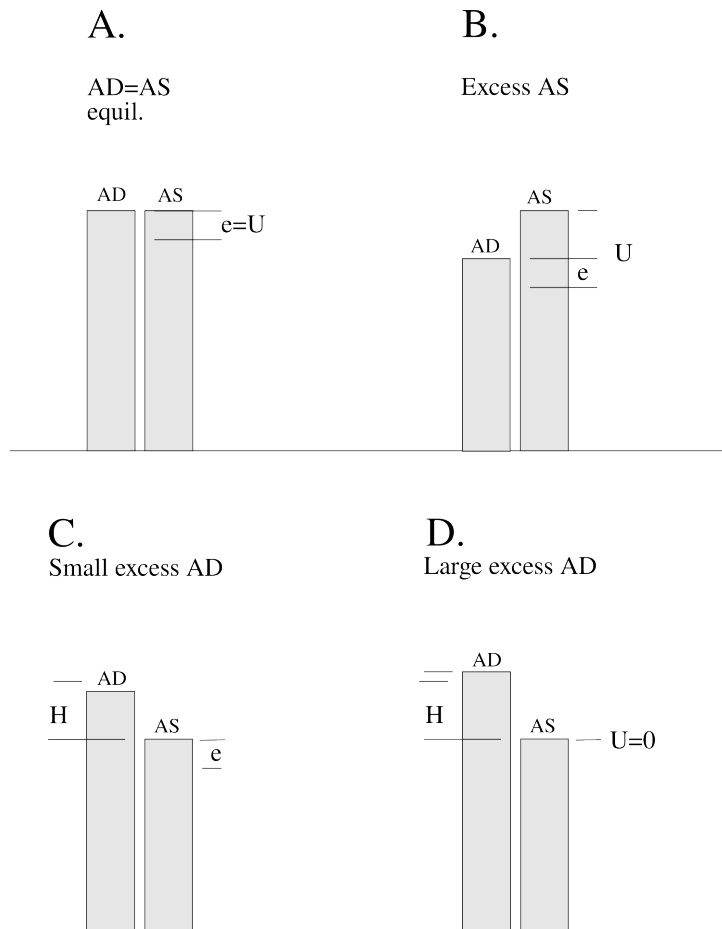

Figure 17: Unemployment as a Function of Aggregate Supply and Demand

Case A. $AD = AS$ equilibrium
In this case the level of agreements, measured in $ is equal to aggregate supply and aggregate supply. There is no
Case B. Excess AS
Case C. Small excess AD

14

Case D. Large excess AD

We enumerated four cases above, but we can think about this more abstractly, as each $ being a carrier for a message. We don't need to quantify the amount of information each unit of currency carries. We do need to know what the relative reduction in that quantity is as it is 'transmitted' across the economy. So currency can be thought of as a carrier of economic information that is distributed across the economy, and that its capability of reducing the error rate in this transmission process is dependent on providing redundancy through increases in aggregate amount of currency.

Whatever way we think about the problem, we can use Figure . to determine the increase in F required. The physical bound on market interactions is therefore shown in the Figure below. Case A, C and D are represented on the graph.
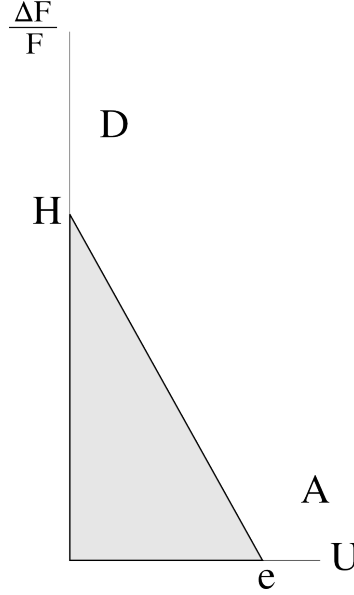

Figure 18: Grey Triangle is the Error Bound

The error bound is a physical contraint on the possibility space of economic interactions. The slope of the line is determined by the mathematical properties of the error rate, and in particular H.

From our simple model of aggregate equilibriation in Section 3.4 and from equation **??**

$$\frac{\Delta F}{F} = I + G \tag{4}$$
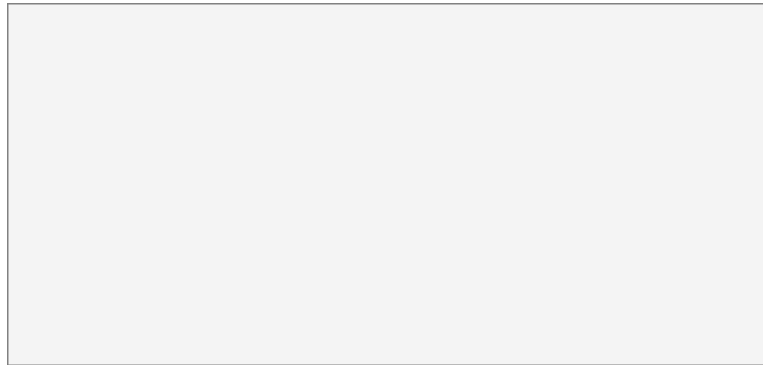
Figure 19: Bound on the Unemployment rate as a function of the Inflation Rate

we can show this bound in terms of the inflation rate I and the unemployment rate U for various different growth rates G, where $G_0 > G_1 > G_2$. Understanding this relation has been central to macroeconomic theory. For instance Fisher Fisher [13] in 1926, Phillips Phillips [25] in 1958 and Lucas [22] all present these relations in graphical form.

We have now been able to shed light on David Hume's problem. His question was why changing units of price should have any affect real quantities. We have now come, at least part-way to solving this problem. However, as we introduce more kinds of transactions into our system, we will find more challenges to the design of a currency that will result in sustained and stable market equilibriation.

5 Control

Figure **??** is plotted with the inflation rate on the vertical axis and the unemployment rate on the horizontal axis in accordance to convention. However, the independent variable is the inflation rate, which we control through money supply as indicated in 6. We can control the inflation rate, but in general the growth rate is external to our control. The unemployment bound is a function of I and G. Contrary to convention, the independent variable appears on the vertical axis while the dependent variable appears on the horizontal axis.
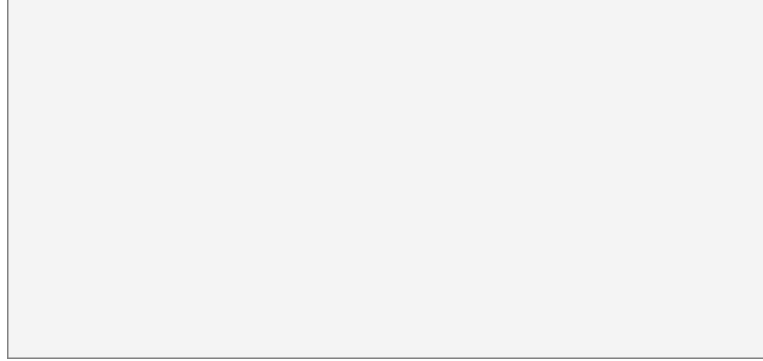
Figure 20: Control for Aggregate Market Equilibriation

Decreasing the unemployment rate to zero requires increasing the inflation rate. At various times in the past, monetary authorities have attempted to reduce the unemployment rate by increasing money supply. At times this has been successful but at times it has resulted in increasing unemployment rates rather than decreasing unemployment rates. In the next section we will examine why this control solution has in many conditions been unsuccessful.

6 Time Transactions
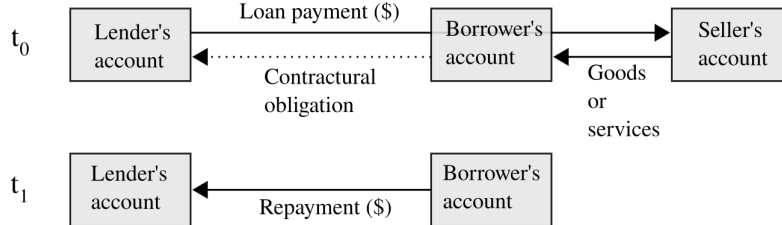
Figure 21: Time Transactions

6.1 Including Time Transactions in Our Model

Figure 22: Exchange and Time Transaction Feedback Schema

In Section 4 we showed that there is a bound on the set of economic transactions that are possible, and that the error bound is determined by H (which we can consider as beyond out control), the inflation rate I and the growth rate G. We can

control the inflation rate, but in general the growth rate is external to our control. We also showed that to achieve the goals of our currency requires a positive inflation rate. The unit in which we write prices is continuously changing. The unit used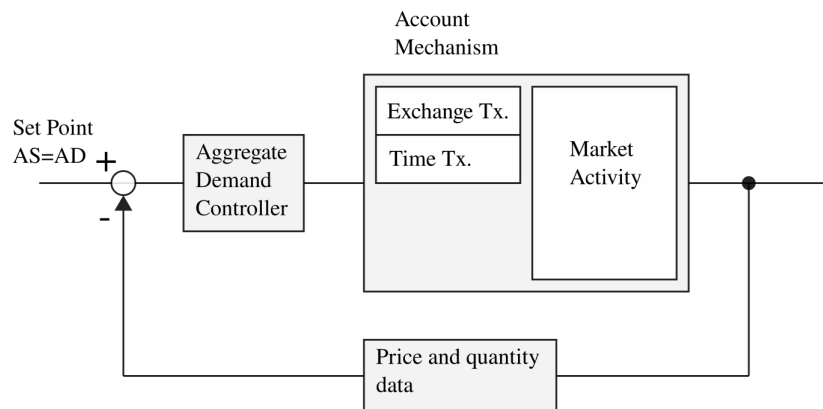 to denominate payments in contracts is generally this price unit. We show that this method of choosing interest rates is undercontrollable as discussed in Section 2.2 such that under conditions of a positive rate of change in the inflation rate, i.e. when

$$\frac{\Delta I}{I} > 0$$

then either the real costs of borrowing must increase or the output Q must decrease. Based on Figure 19 this results in unemployment/inflation tracking that appears as indicated in Figure ??.
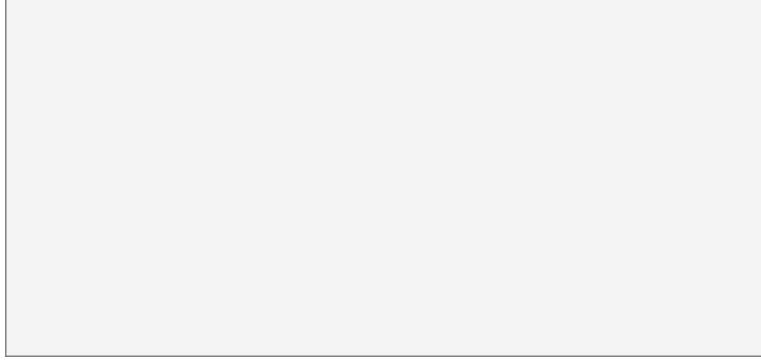

Figure 23: Interest Control Failure

Control failure occurs until the rate of change in the inflation rate drops to zero or becomes negative. The combination of the error bound and underspecification tracking leads to a fundamental control problem. To set conditions where aggregate equilibrium is possible, the inflation rate must be increased to region D as shown in Figure 19. As the inflation rate increases, uncontrollability tracking reduces the growth rate, increases the unemployment rate. The solution to this problem is to correct the units in which contracts are written. If a unit of account of constant value is used, real interest rates can be trivially specified because the unit directly measures real payments and so fully specifies our control problem. Given that a currency limits transactions to exchange transactions and time transactions, and that a unit of account of constant value is used, and given that there are no other unforseen destabilizing effects, the currency can be controlled to maintain aggregate equilibrium. If a unit of account of constant value is not used, it is not possible for a currency to maintain aggregate equilibrium.

6.2   Interest Control Failure

We showed in Section 4. that the unit in which prices are denominated must be continuously changing.
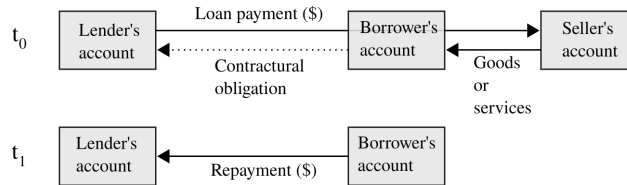
Figure 24: Time Transactions

This unit is used in time transactions to denominate the initial lending of currency, to denominate the repayment, and it is also common practice to use it to specify the repayment in a contract. Because this unit in continuously changing, the value written into contracts must be written in such a way as to specify a real interest rate, i.e. an interest rate written in terms of purchasing power. Fisher [14] notes that in order to specify a real interest rate r then the value i needs to be written into contracts, where

$$i = (1+r)(1+I)$$

Whatever real interest rate r lenders and borrows agree upon, its is possible to write the value i into contracts to achieve this outcome. For a given principle k the repayment of the principal is $k(1+I)$ and the repayment of interest on that principal is $k(1+I)(1+r)$, and so total the repayment of both principle and interest is

$$k(1+r)(1+I) = k(1+I) + k(1+I)(1+r)$$

From the left-hand side of this equation we can see that the payment denominated in the unit of currency increases at the same rate as the inflation rate. Figure 20. illustrates that to maintain a market equilibriation set point we need a feedback regulator that responds to deviations in the inflation rate from the set point. Not only does the inflation rate I changes, the rate of change of the inflation rate $\Delta I/I$ changes. This changes the requirement to control the real iterest rate from a single-variable control problem, to a two variable specification problem. For every inflation rate I there are many rates of change of the inflation rate $\Delta I/I$ that affect the real interest rate of a contract. This means that to correctly specify a real interest rate, two number are required, not one. This is a case where our control system is uncontrollable. The real interest rate is a function of i, I and $\Delta I/I$.

$$r = (1+i)\left(1 + I\left(1 + \frac{\Delta I}{I}\right)\right) = (1+i)\left(1 + I + \Delta I\right) \tag{5}$$

Given that we only have one control, when two are required, we'll look at the effects of controlling the single control we do have.
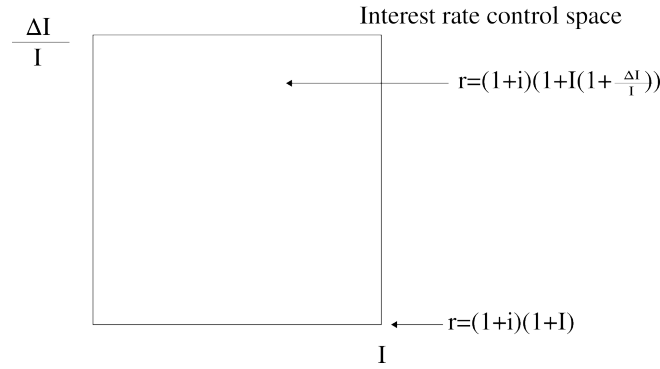
Figure 25: Interest Rate Control Space

We are limited to control options along the horizontal axis. Suppose we are given an r_0 that controls for a given I and where $\Delta I/I = 0$. And then supoose that the rate of change increases so that $\Delta I/I > 0$. The two possible options are to leave i as it is, or to increase i.

Case 1: No change to i

In this case the real interest rate facing lenders will decrease, causing some lender to reject a set of agreements that they would have previously accepted, resulting in decreases in Q and a decrease in the growth rate G.

Case 2: An increase in i

Under these conditions the real costs facing borrowers will increase, causing some lenders to reject a set of agreement that they would have previously accepted, resulting in decreases in Q and a decrease in the growth rate G.
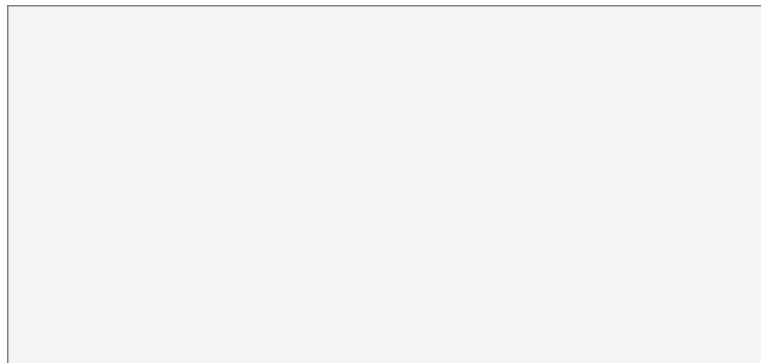
Figure 26: Interest Control Failure

Because of the shape of the error bound, we can see that if the inflation rate is increased sufficiently, the reduction in the unemployment rate due to increases in the inflation rate can compensate for *all* decreases in the growth rate due to interest control failure. It is possible to double-down on control-failure for a short period of time but maintenance of this state will result in hyper-inflation and high unemployment rates.

The combination of the error bound and interest control failure result in a set point of aggregate equilibrium being unstable, and any attempts to increase the inflation rate toward the set point will leave the system in a state worse, in the sense of a higher unemployment rate, than when it started.

7 Solution

The solution to this problem is to use a unit that directly maps to real interest rates and is independent of the inflation rate, and so also independent of the rate of change of inflation. This unit is termed a unit of account of constant value. To map between this unit of account and prices, the unit of account is multiplied by the price level, and conversely to convert from a price to the unit of account we divide by the price level. The result is a unit that is independent of the exchange rate. Because the value written is independent of the inflation rate, equation (5) becomes

$$r = i$$

As a way of reducing uncertainty in house prices this unit, called the *unidad de formento*, has been used in Chile for several decades [32]. Without interest control failure, the inflation rate can be regulated to a set point in region D of Figure 18.

8 Data

9 Contract Transactions

10 External Transactions

11 Other Transactions

12 Implementation

Abstraction Layer over Accounts

To implement a currency design that does not constrain

we need to reconsider the interaction between the micro-level, the economic participants and owners of accounts, and the macro-level requirements.

The design strategy we take is to define the macro-level requirements and then to search for ways to control the currency so that the currency is likely to map out to those macro-level requirements.

We specify the macro-level requirements as

1. Sustained stability.

2. Macro-level equilibriation.

Simple accounts that hold a number with some control of the aggregate value in all accounts is the digital equivalent of paper money. This design is insufficiently controlled to achieve our two macro-level requirements.

To achieve these outcomes we apply a abstraction layer over these accounts. This abstraction layer does the following:

Exchange Transactions

1. Present to the user a value that is the product of the user's base account value and an single, global value that we call the demand index (D_x). This product is the value that users generally see and is the value in which price agreements are made. This value gradually changes as the demand index changes, appearing to users much as a bank account that has gradual increases as an interest rate is applied to it. As such, it presents no usability difficulties to the user.

3. All exchange transactions must be associated with a quantity and a goods or service category. An exchange transaction is only valid if both the seller and buyer confirm the same goods or service category. This serves three purposes.

a. It asserts that the transaction is an exchange transaction, and as such, has no associated contract with it beyond the current delivery of the goods or service. By doing this it confirms that there are no future legal commitments to any future repayment. This is required to limit the use of exchange transactions for the purpose of some other transaction category.

b. The data can be used, with necessary software mechanism to ensure the privacy of the data, to accurately calculate the price index.

c. It serves as a record for the seller and buyer to resolve any disputes, i.e. it acts as a receipt or record of agreement.

Beyond the seller and buyer entering the same goods and service category, it is easy for seller and buyer to collude and provide incorrect information.

4. There are intermediate accounts. These are required because all exchange transactions must be associated

TODO

Time Transactions

2. Values that set future payments, in particular for repayments on time transactions, are denominated in a root value and the product of the price index (P_x). In this way, the purchasing power of that value remains absolutely constant, and as such there it present any possibility of inflation feedback. All repayments on time transactions must be defined at the time the money is borrowed and designated as a time transaction.

Contract Transactions

Contract transactions are prevented by the requirement that borrowers must make repayments to the same party that initially lent the money. There are possible ways that users could subvert these requirements which we discuss in a later section.

External Transactions

The provision of an exchange transaction mechanism will be deferred. The possibility of providing exchange transaction functionality with external currencies depends on the design of external currencies, in particular the accuracy of their price index, and their control over contract transactions. If we consider external transactions between two currencies of the kind we are presenting in this paper, then an external exchange rate fixed to the relative price index of the two currencies, and restricting transactions to exchange transactions by requiring the recording of goods or service cateogry and quantity may be a suitable design. This kind of system would require a pair of special aggregate accounts specifically for external transactions to pair up inflow and outflow. In this system, the pairing of inflow and outflow would halt if either account became empty. Another possibility would be to implement a floating exchange rate. The potential difficulty with this design is that it is relatively easy for users to use exchange accounts in lieu or time or contract transactions, and so it may be possible for users to engage in high-frequency capital interactions across the external boundary despite the disincentive of having no legal resort on repayment failure.

Usability

The controls we plan to implement will have minimal impact on any user who intends to use the currency for exchange or time transactions. There is an additional requirement for both seller and buyer to agree on a transaction and to record goods category. Indexed units of account have been used in Chile for a number of decades without significant usability problems, and the use of indexed units of account in a digital currency could potentially further simplify their use.

One important exception, however, are restrictions on the types of repayment schedules for time transactions. If repayment schedules are overly flexible, the repayments could possibly be used, given people's ingenuity in using financial mechanisms to enrich themselves, as a substitute for contract transactions. The extent to which this would happen in practice is unknown, and so starting with relatively strict controls and relaxing restrictions with experience is probably a reasonable approach.

Using One Transaction Category in Lieu of Another

The are various methods that users may potentially use to one category of transaction of another. The most serious risk is that users find ways to make contract transactions. The main barrier to preventing this is to ensure that repayments can only be made to the initial lender's account. The second barrier is to ensure that there is no legal protection to protect creditors from debtor's failure to make "repayments". These barriers should be sufficient on the condition that there are no significant economic incentives for engaging in such activity. In general such users will choose to use other currencies, rather than a currency with these barriers.

13 Conclusion

We summarize the theoretical components according to the level of confidence in the results.

The error effect and Fisher lines

This property is determined by physical properties and the inferences made from these rules are sufficiently precise and measurable to be subject to falisification.

Aggregate equilibrium

The property is an aggregate of people's behaviour that has been observed over long-periods or time with great consistency and is a plausible outcome of people's general incentives. Our model remains robust even if we relax this assumption to a large degree. Almost all fields of economic research are predicated implicitly or otherwise on the idea that this condition must be modified heavily to explain real-world conditions, and therefore require significant re-appraisal given that these effects are better explained as a property of currency design.

Inflation feedback and financial bubbles and crashes

These processes are best explained as positive feedbacks that, while their degree and timing cannot be reasonable determined quanititatively with precision, if unchecked will have clear consequences and these consequences have consistently observed. These positive feedback processes are fundamentally uncontrollable with possible rapid changes that we cannot easily regulate. A successful control system will strongly limit the impact of positive feedback processes.

Market driven changes in aggregate quantities and prices

We cannot expect to be able to predict theses changes, but the rate of change is not sufficiently fast that it cannot be controlled or adjusted for through feedback regulation.

We hope that this paper can lead to new directions in research. In all new engineering endeavours, theory and practice diverge. We can take advantage of the relative easy of building digital currencies to specific design specifications to make currency engineering into an experimental science. Given the theoretical foundations presented in this paper there is a reasonable high chance that we can design and build currencies that will not prevent markets from reaching equilibrium, that that a stable equilibrium can be maintained indefinitely in response to changing conditions.

13.1 Endnotes

According to Rathgeber's notes, the error effect was discovered in 1974. Rathgeber's papers glossed over some matters that caused considerable confusion and doubt about the value of his work. I have tried to make explicit those sources of ambiguity. Rathgeber discusses the need to separate out the "functions of money". This was a source of confusion and lack of precision, which I tried to deal with using the notion of transactions as a way to delineate the different functions of money. Rathgeber did not make a clear distinction between a currency as a technical property as compared to the market behaviour of people, but the notion was implicit in his work. This was also a source a confusion, because people, quite reasonably, object to the application of engineering method directly to social interaction. Making explicit the difference between markets and currency hopefully clear that engineering method is applied to currencies, not social interaction. Rathgeber was working in the context of a single, national, centralized currency. I have extended the application of his ideas to digital currencies. At the time he wrote his private papers, he had access only to Australian inflation and unemployment data. I have extended this to data available up to the time of publication.

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