

Kaitlin Hoffmann

Office Hours:

SH 243 MR 11:00 - 12:30 PM via appointment <https://calendly.com/hoffmank4/15min>

Email: hoffmank4@newpaltz.edu

For TA Office Hours and Email – Please see syllabus

NEW! Supplemental Instruction: Sign up at my.newpaltz.edu

RECURSION

COMPUTER SCIENCE I

OBJECTIVES

- Recursive Methods



WHAT IS RECURSION?

- ▶ A recursive method is a method that calls **itself**.
- ▶ It is an alternative to using loops (for, while, etc), however, it's not always the best way to solve problems.
- ▶ Most of the time, loops will do the job just fine, however, some data structures, such as binary trees (you'll learn this in CS2), are better suited for recursive methods.
- ▶ Let's see an example...

LOOP VS RECURSION

- ▶ Say we have a problem that asks us to **print out the numbers from 1 to n**. We can do this using a loop (iterative process) or using recursion:

```
public static void printLoop(int n) {  
    for(int i = 1; i<=n; i++) {  
        System.out.print(i + " ");  
    }  
}
```

Iterative (loop)

```
public static void printRecursively(int n) {  
    if(n == 0) {  
        return;  
    }  
    printRecursively(n-1);  
    System.out.print(n + " ");  
}
```

Recursive

- ▶ The **base case** is going to tell us when to stop making recursive calls.
- ▶ The **general case** will include a recursive call and possibly some other computations.
- ▶ Usually in recursion we need to find a **pattern** to develop our method. The pattern is going to involve some information about the previous step or computation.

```
public static void printRecursively(int n) {  
    if(n == 0) {  
        return;  
    }  
    printRecursively(n-1);  
    System.out.print(n + " ");  
}
```

Output:
1 2 3 4 5 6 7 8

Base Case (points to `if(n == 0) { return; }`)

General Case (points to `printRecursively(n-1);`)

- ▶ The **base case** is going to tell us when to **stop** making recursive calls.
- ▶ If we want to print 1 through n, we want to **stop** making recursive methods when n reaches 0. This is our base case:
$$\text{if}(n == 0) \{ \dots$$
- ▶ With void types, we can just use the keyword **return;** by itself to stop the calls.

```
public static void printRecursively(int n) {  
    if(n == 0) {  
        return;  
    }  
    printRecursively(n-1);  
    System.out.print(n + " ");  
}
```

Output:
1 2 3 4 5 6 7 8

Base Case (points to `if(n == 0) { return; }`)

General Case (points to `printRecursively(n-1);`)

- ▶ The **general case** will include a ***recursive*** call and possibly some other computations.
- ▶ If we want to make n decrease by 1 every time and print n :
printRecursively($n-1$);
System.out.print($n + " "$);

```
public static void printRecursively(int n) {  
    if(n == 0) {  
        return;  
    }  
    printRecursively(n-1);  
    System.out.print(n + " ");  
}
```

Output:

1 2 3 4 5 6 7 8

Base Case

General Case

HOW DOES RECURSION WORK?

- ▶ When a method calls itself, it adds the code of the **general case** onto a data structure called a **stack**. It will keep "stacking" until the base case is hit. Once hit, it will remove each from the stack to perform the code.
- ▶ Let's see an example...

HOW DOES RECURSION WORK?

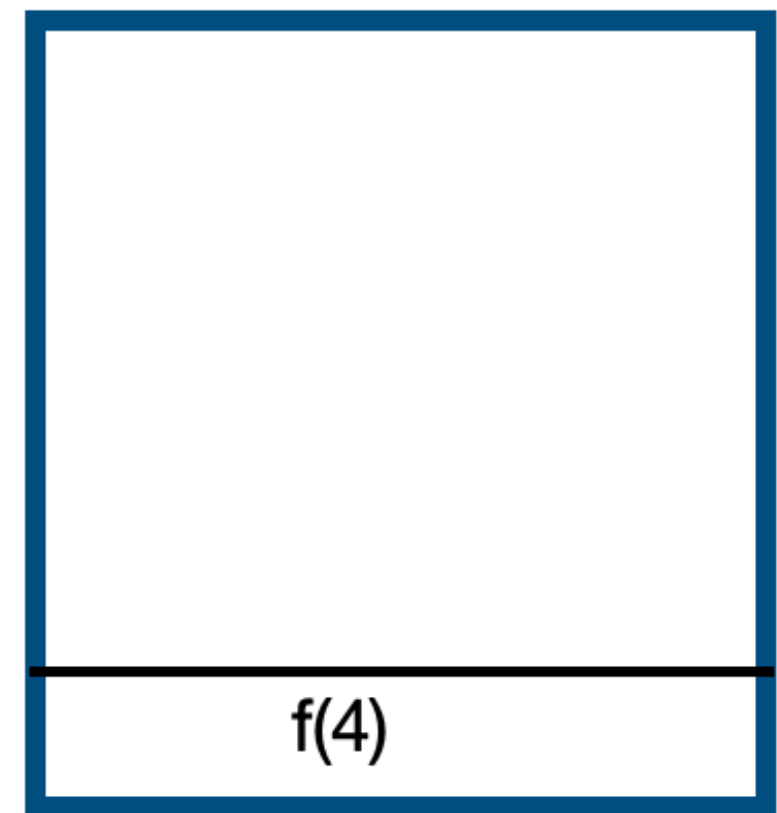
9

```
public static void f(int n) {  
    if (n <= 0) {  
        return;  
    }  
    f(n-1);  
    System.out.print(n + " ");  
}
```

Trace for **f(4)**

f(4) → f(3)

Didn't reach base case, so 4 - 1...



Stack

HOW DOES RECURSION WORK?

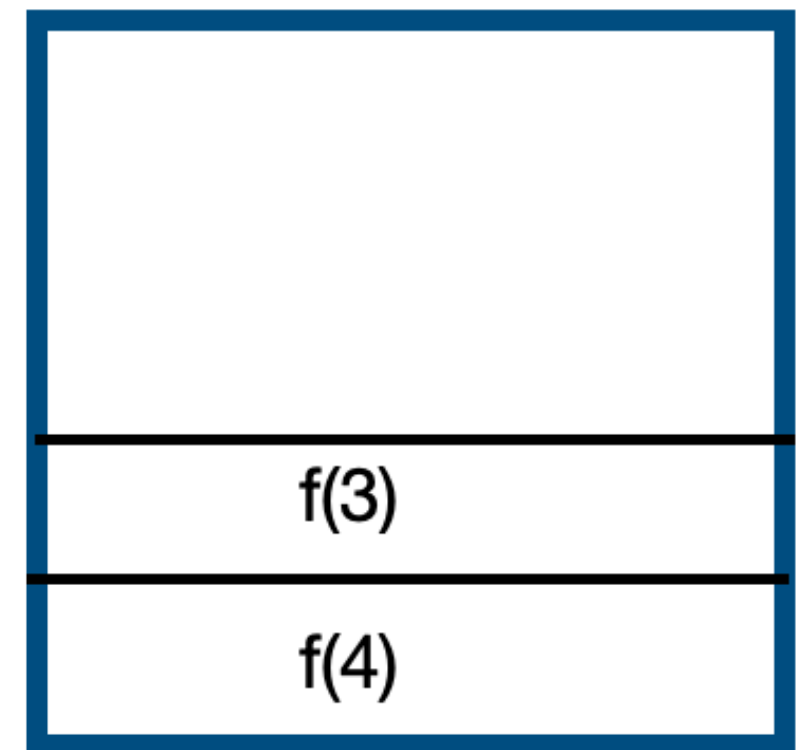
10

```
public static void f(int n) {  
    if (n <= 0) {  
        return;  
    }  
    f(n-1);  
    System.out.print(n + " ");  
}
```

Trace for **f(4)**

f(4) → f(3) → f(2)

Didn't reach base case, so 3 - 1...



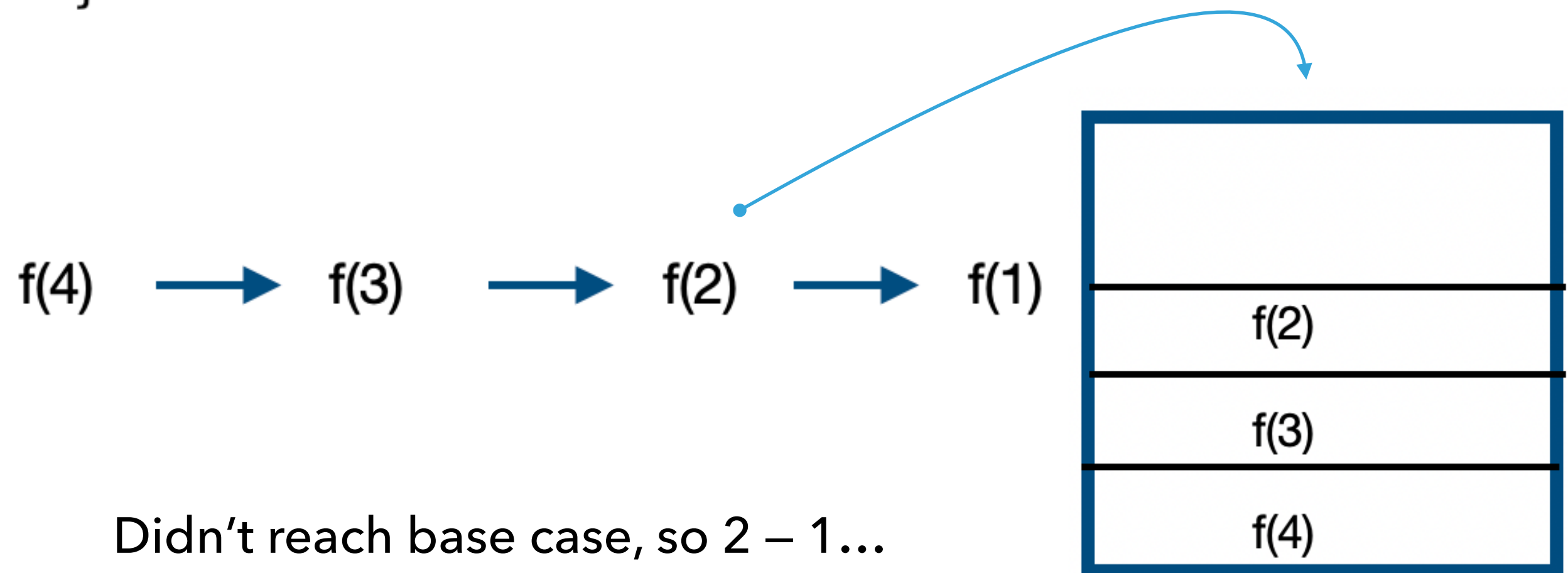
Stack

HOW DOES RECURSION WORK?

11

```
public static void f(int n) {  
    if (n <= 0) {  
        return;  
    }  
    f(n-1);  
    System.out.print(n + " ");  
}
```

Trace for **f(4)**



Didn't reach base case, so 2 - 1...

Stack

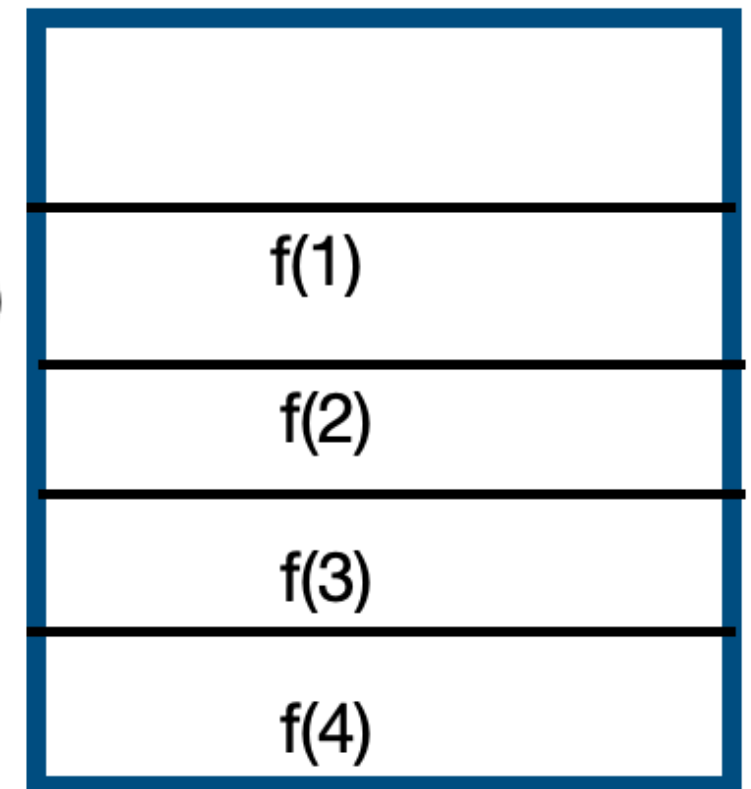
HOW DOES RECURSION WORK?

12

```
public static void f(int n) {  
    if (n <= 0) {  
        return;  
    }  
    f(n-1);  
    System.out.print(n + " ");  
}
```

Trace for **f(4)**

f(4) → f(3) → f(2) → f(1) → f(0)



Didn't reach base case, so 1 - 1...

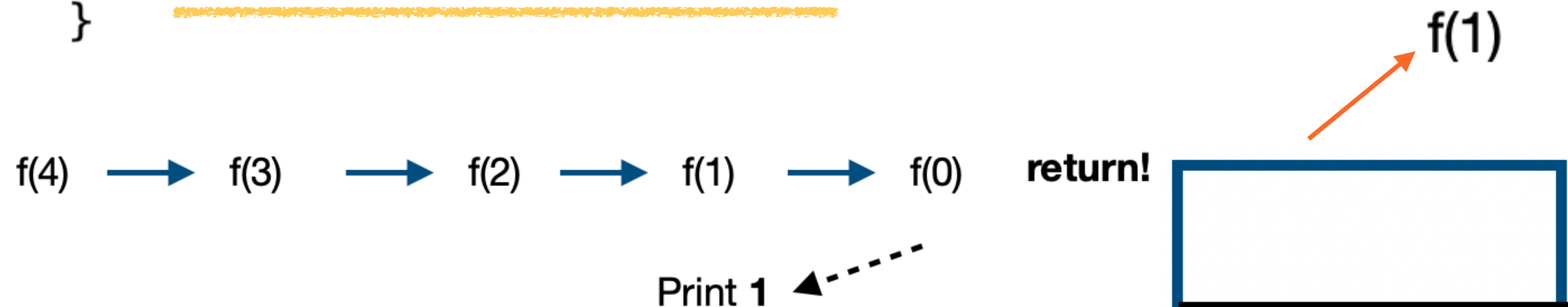
Stack

HOW DOES RECURSION WORK?

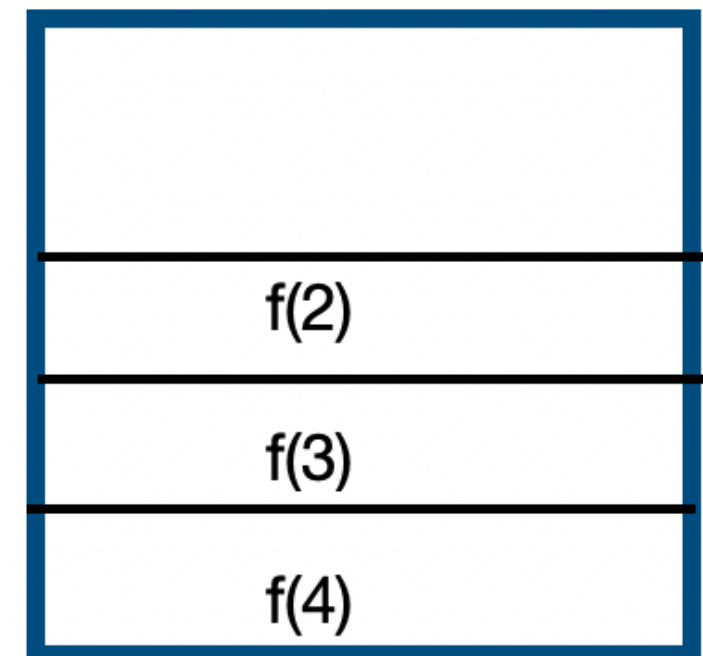
13

```
public static void f(int n) {  
    if (n <= 0) {  
        return;  
    }  
    f(n-1);  
    System.out.print(n + " ");  
}
```

Trace for **f(4)**



Reach base so we **return** and the stack empties one by one



Stack

HOW DOES RECURSION WORK?

14

```
public static void f(int n) {  
    if (n <= 0) {  
        return;  
    }  
    f(n-1);  
    System.out.print(n + " ");  
}
```

Trace for **f(4)**

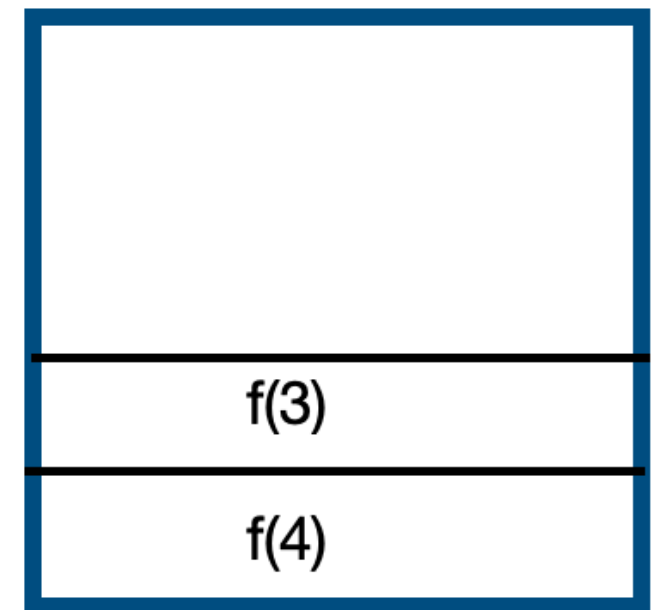
f(2)



f(4) → f(3) → f(2) → f(1) → f(0) **return!**

Print 2 ← - - - Print 1 ← - - -

Reach base so we **return** and the stack empties one by one



Stack

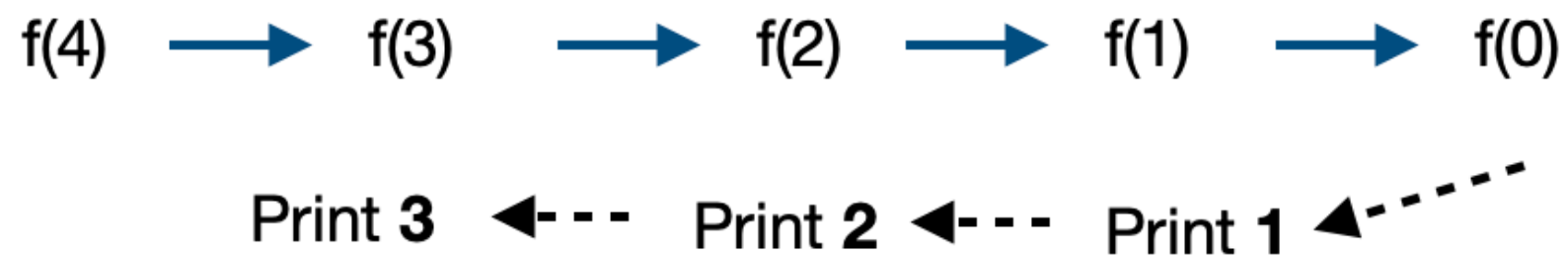
HOW DOES RECURSION WORK?

15

```
public static void f(int n) {  
    if (n <= 0) {  
        return;  
    }  
    f(n-1);  
    System.out.print(n + " ");  
}
```

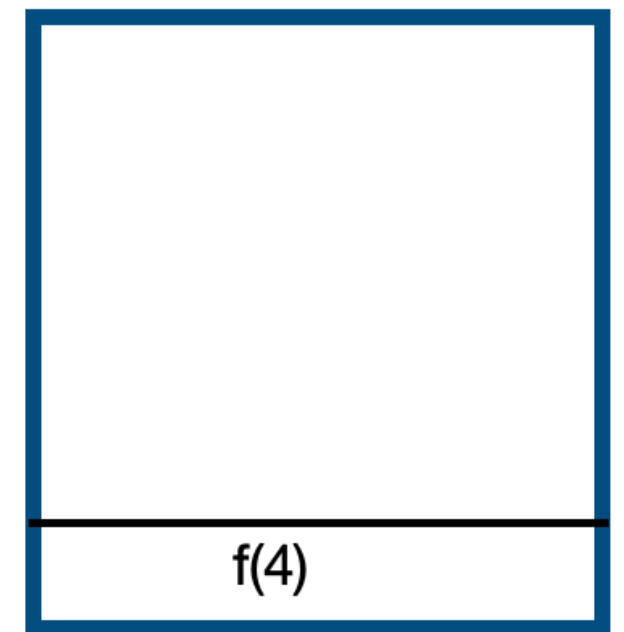
Trace for **f(4)**

f(3)



return!

Reach base so we **return** and the stack empties one by one



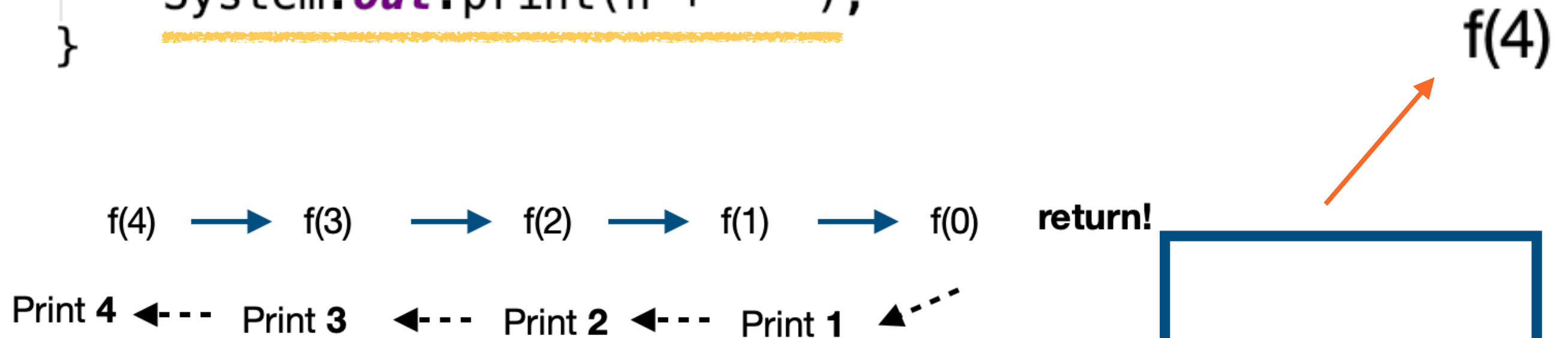
Stack

HOW DOES RECURSION WORK?

16

```
public static void f(int n) {  
    if (n <= 0) {  
        return;  
    }  
    f(n-1);  
    System.out.print(n + " ");  
}
```

Trace for **f(4)**



Stack is empty, so output is: **1 2 3 4**

Stack

EXAMPLE 1

- ▶ Printing 1 to n recursively. Let's put this together now...

EXAMPLE 2

- ▶ Printing ***n to 1*** recursively.
- ▶ What is our **base** case (when to stop)? **$n \leq 0$**

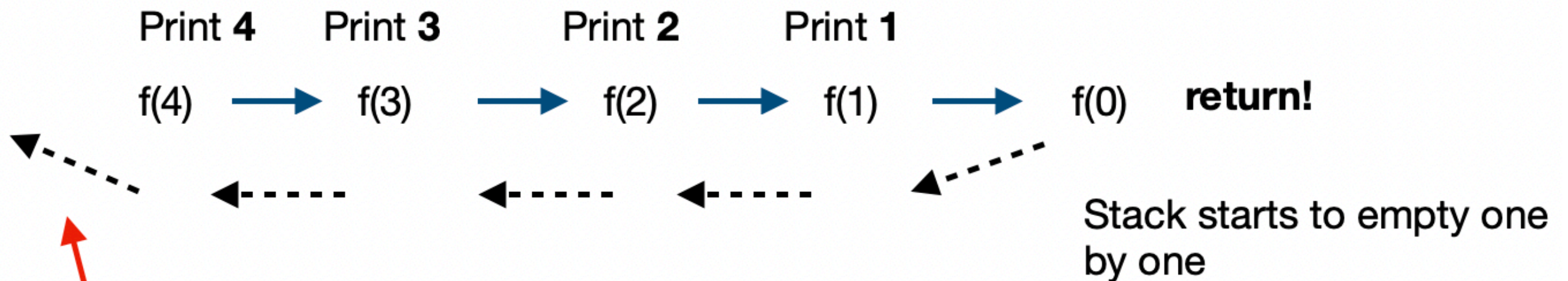
HOW DOES RECURSION WORK?

19

```
public static void f(int n) {  
    if (n <= 0) {  
        return;  
    }  
    System.out.print(n + " ");  
    f(n-1);  
}
```

Let's print **n to 1** (backwards from last exercise). Notice we just **switch** the print and method call.

Trace for **f(4)**



This represents going back to initial call in main.

EXERCISE 1

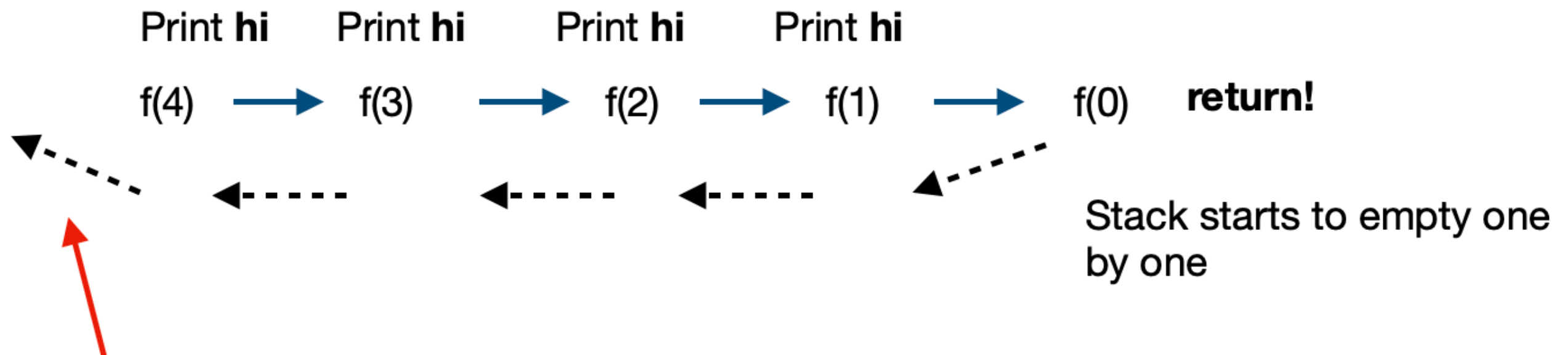
- ▶ Create a recursive method that prints a String **n** amount of times. The String and n should be parameters.
- ▶ Make sure you determine the **base case** first (when to stop).
- ▶ Don't overthink recursion! All you need to do is to subtract 1 from n every call.

EXERCISE 1 — SOLUTION

21

```
public static void printString(String s, int n) {  
    if (n <= 0) {  
        return;  
    }  
    System.out.println(s);  
    printString(s, n-1);  
}
```

Trace for **printString("hi", 4)**



This represents going back to initial call in main.

Stack starts to empty one by one

EXAMPLE 3

- ▶ Let's find the sum of **1 to n** recursively.
- ▶ We can't use a variable to hold the sum since it will re-initialize it to 0 every time the method is called.
- ▶ That's okay! We can continuously **add to the stack**, allowing the sum to be stored.
- ▶ First, what should be our **base case** and what should we return in the base case?

$n \leq 0$

return 0;

HOW DOES RECURSION WORK?

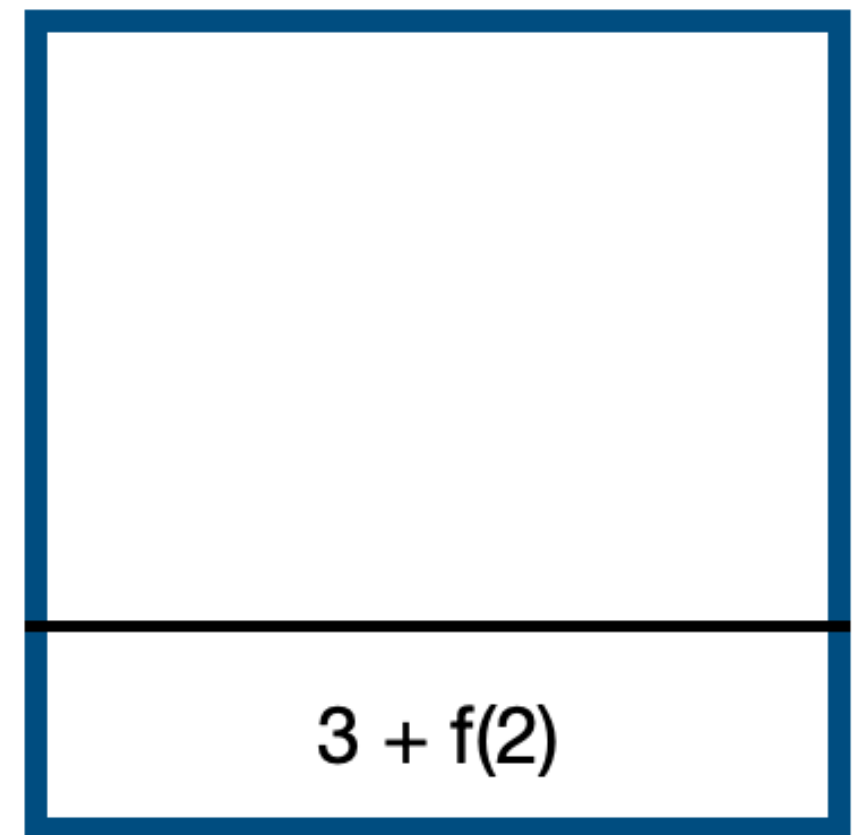
23

```
public static int findSum(int n) {  
    if(n <= 0) {  
        return 0;  
    }  
    return n + findSum(n - 1);  
}
```

Trace for **f(3)**

f(3) → f(2)

Didn't reach base case, so 3 - 1...



Stack

HOW DOES RECURSION WORK?

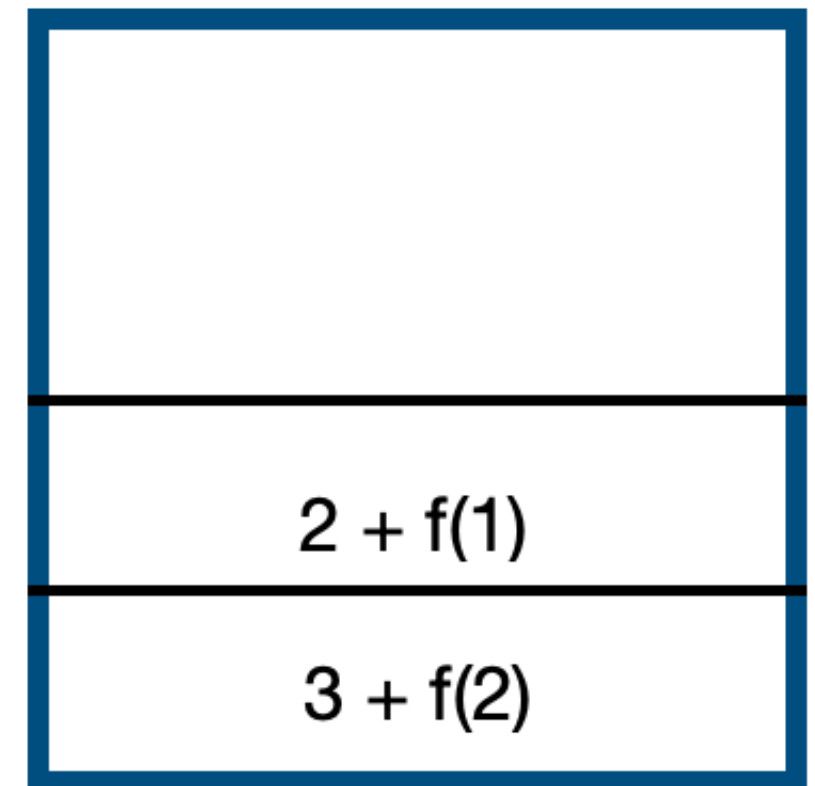
24

```
public static int findSum(int n) {  
    if(n <= 0) {  
        return 0;  
    }  
    return n + findSum(n - 1);  
}
```

Trace for **f(3)**

f(3) → f(2) → f(1)

Didn't reach base case, so 2 - 1...



Stack

HOW DOES RECURSION WORK?

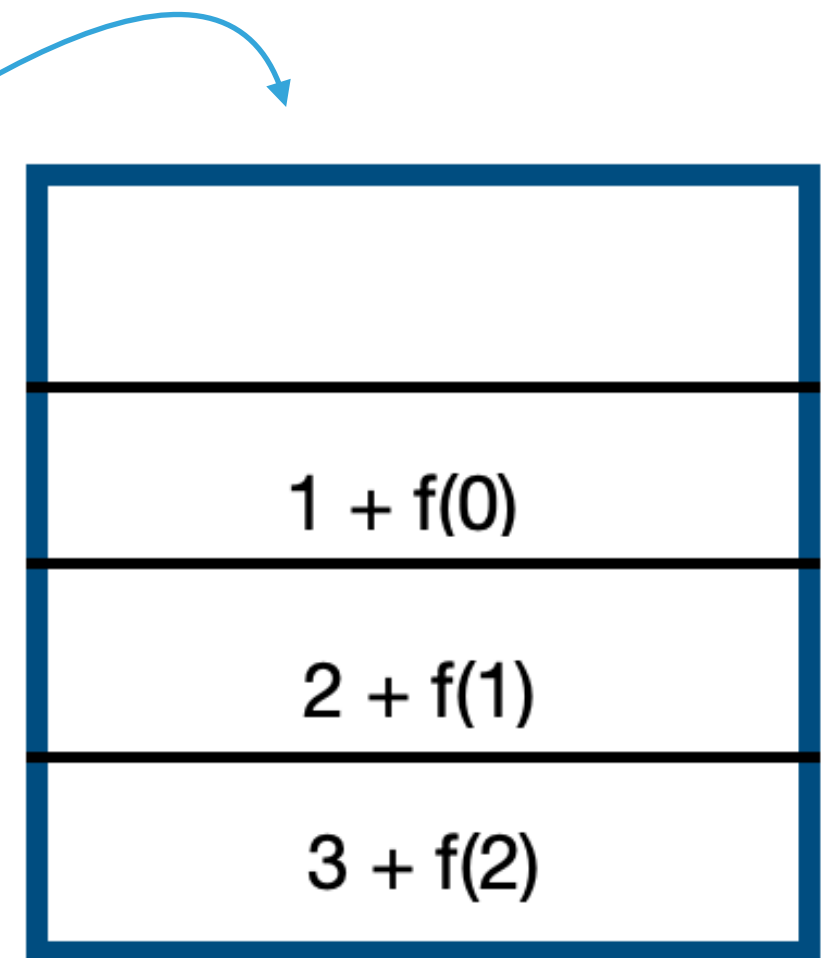
25

```
public static int findSum(int n) {  
    if(n <= 0) {  
        return 0;  
    }  
    return n + findSum(n - 1);  
}
```

Trace for **f(3)**

f(3) → f(2) → f(1) → f(0) **return 0!**

Didn't reach base case, so 1 - 1...



Stack

HOW DOES RECURSION WORK?

26

```
public static int findSum(int n) {  
    if(n <= 0) {  
        return 0;  
    }  
    return n + findSum(n - 1);  
}
```

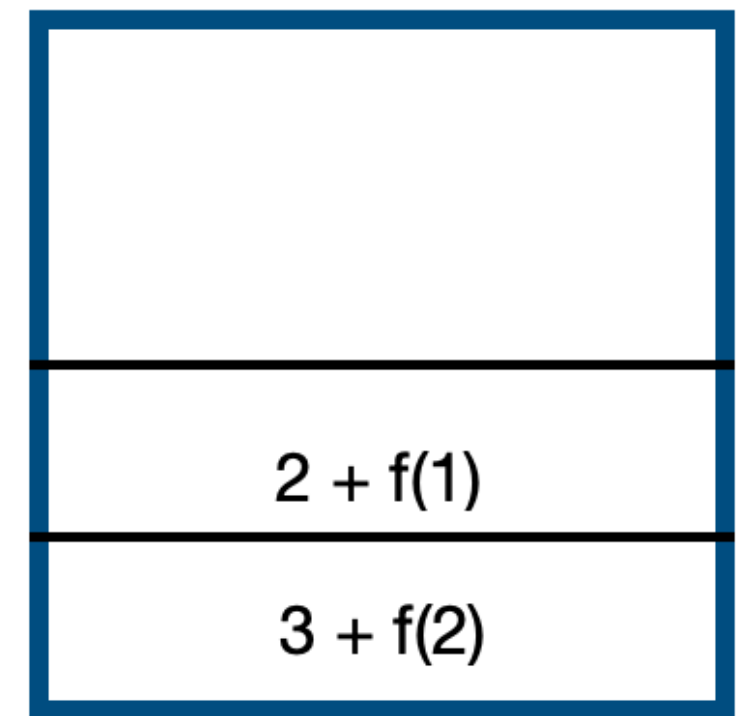
Trace for **f(3)**

f(3) → f(2) → f(1) → f(0) **return 0!**

1 + 0

1 + f(0)

Reach base so we **return** the previous number and add until the stack is empty



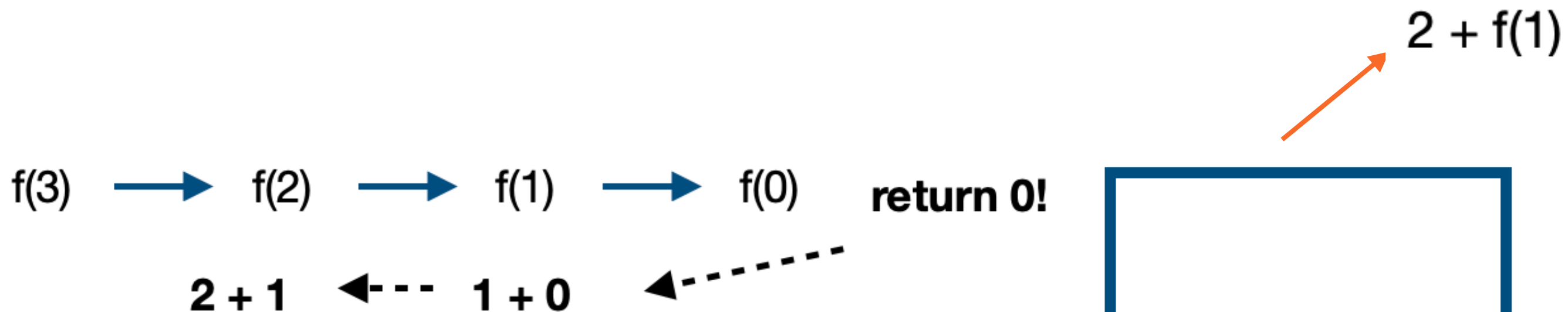
Stack

HOW DOES RECURSION WORK?

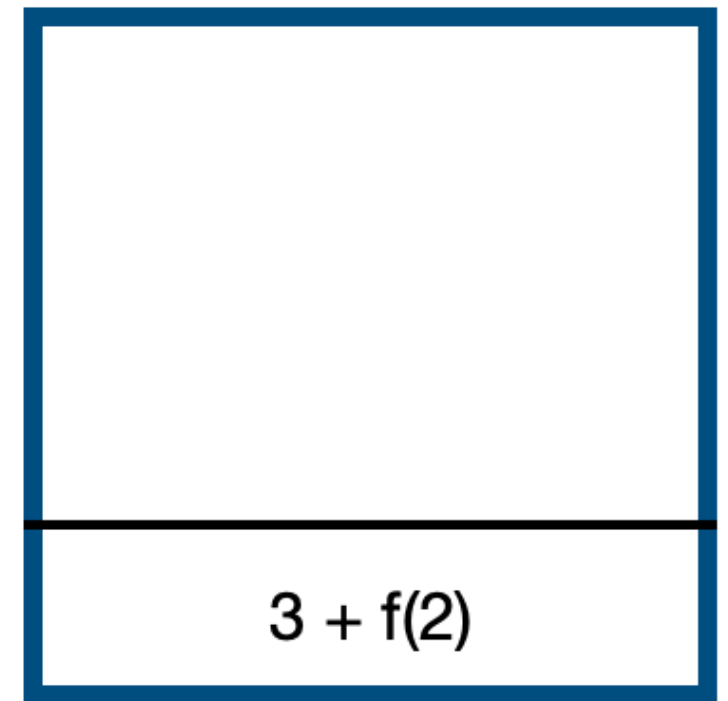
27

```
public static int findSum(int n) {  
    if(n <= 0) {  
        return 0;  
    }  
    return n + findSum(n - 1);  
}
```

Trace for **f(3)**



Reach base so we **return** the previous number and add until the stack is empty



Stack

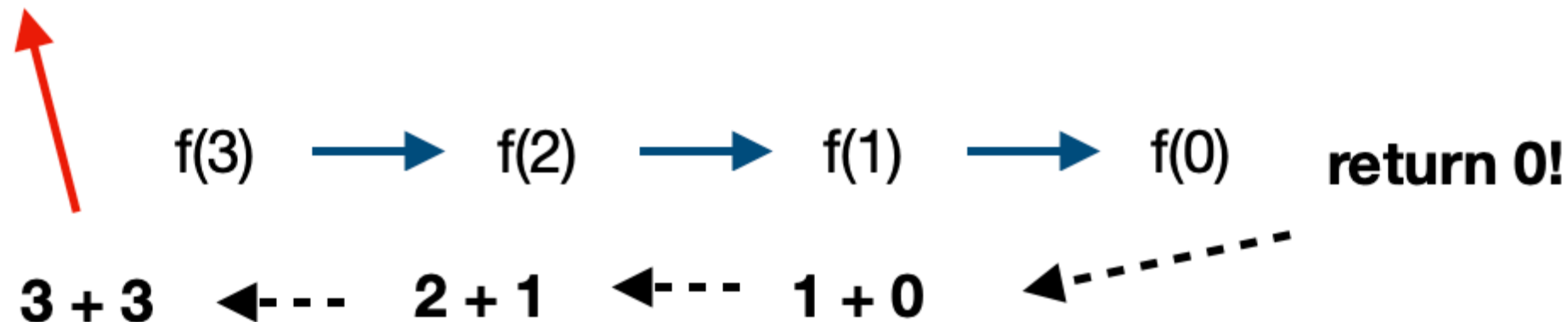
HOW DOES RECURSION WORK?

28

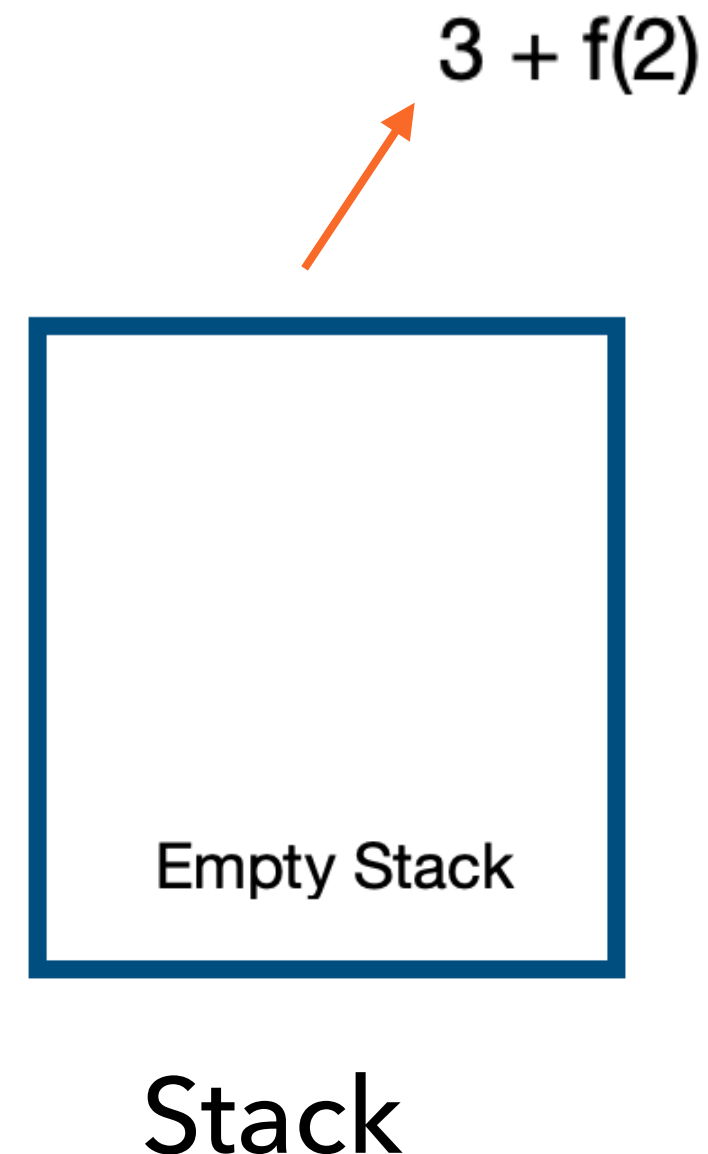
```
public static int findSum(int n) {  
    if(n <= 0) {  
        return 0;  
    }  
    return n + findSum(n - 1);  
}
```

Trace for **f(3)**

6 returned to main



Stack is empty, so output is: **6**



EXAMPLE 3

- ▶ Let's find the sum of **1 to n** recursively. Let's do this now.

EXAMPLE 4

- ▶ Let's write a method to recursively sum x to the ***nth*** power (x^n) starting with $n = 0$. Example: $x^0 + x^1 + x^2 + \dots x^n$
- ▶ What is our base case (when should we stop)? **$n \leq 0$**

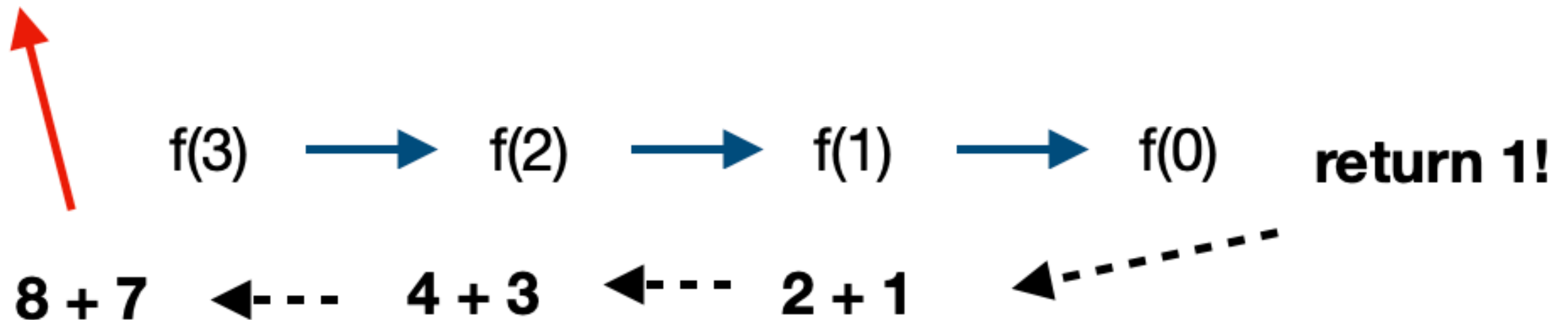
EXAMPLE 4 – SOLUTION

31

```
public static int raisePower(int x, int n) {  
    if(n <= 0) {  
        return 1;  
    }  
    return (int)Math.pow(x, n) + raisePower(x, n-1);  
}
```

Trace for **f(2, 3)**

15 returned to main

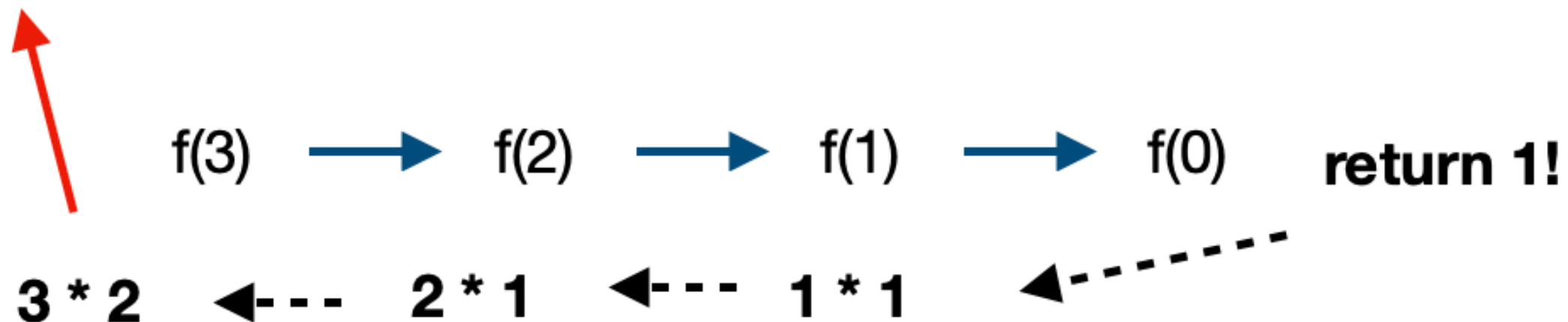


EXERCISE 2

- ▶ Create a recursive method that computes **factorial of n**.
Example: **$5! = 1 * 2 * 3 * 4 * 5 = 120$**
- ▶ **NOTE: $0!$ is **1**** so what should be your base case?

```
public static int fact(int n) {  
    if (n == 0) {  
        return 1;  
    }  
    return n * fact(n-1);  
}
```

6 returned to main

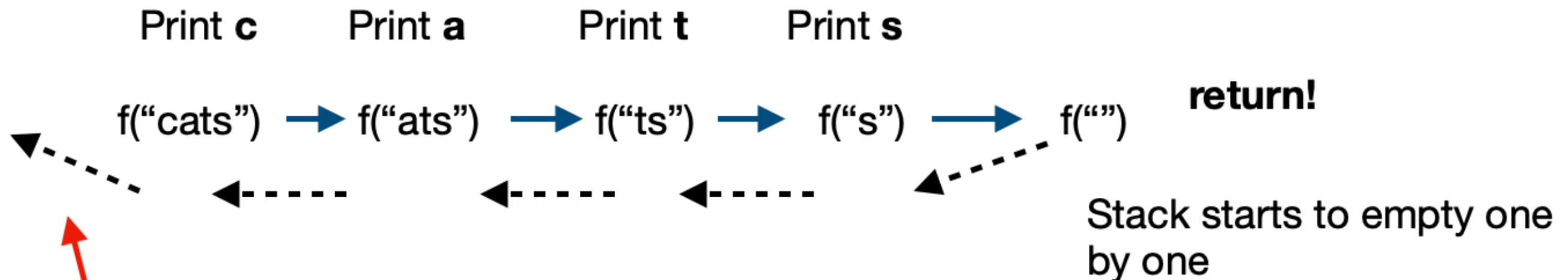


EXAMPLE 5

- ▶ Let's write a method to recursively display a string 1 character per line.
- ▶ We'll have to use the **substring** method to remove characters from our String every call. When our String has no more characters, we'll stop.
- ▶ What do you think our base case will be? **s.length() == 0**

```
public static void displayChars(String s) {  
    if(s.length() == 0) {  
        return;  
    }  
    System.out.println(s.charAt(0));  
    displayChars(s.substring(1));  
}
```

Trace for **f("cats")**



This represents going back to initial call in main.

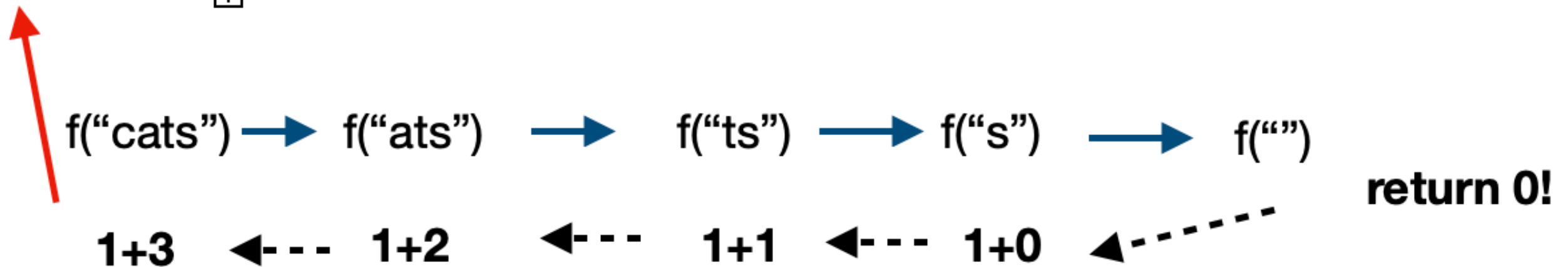
EXAMPLE 6

- ▶ Let's write a method to recursively compute the length of a string.
- ▶ What do you think our base case will be? **s.length() == 0**


```
public static int length(String s) {
    if(s.length() == 0) {
        return 0;
    }
    return 1 + length(s.substring(1));
}
```

Trace for **f("cats")**

4 returned to main



EXERCISE 3

- ▶ Write a method to recursively reverse a string.

```
public static void displayBackwards(String s) {  
    if(s.length() == 0) {  
        return;  
    }  
    System.out.println(s.charAt(s.length()-1));  
    displayBackwards(s.substring(0, s.length()-1));  
}
```

Trace for **f("cats")**

