

## CS 3530: Assignment 2e

Fall 2023

### Problem 2.44 (20 points)

#### Problem

If  $A$  and  $B$  are languages, define  $A \diamond B = \{xy : x \in A \text{ and } y \in B \text{ and } |x| = |y|\}$ . Show that if  $A$  and  $B$  are regular languages, then  $A \diamond B$  is a CFL.

Note: a formal proof is not necessary; a detailed description of a suitable construction and an informal argument will suffice.

#### Solution

The strings generated by  $A \diamond B$  are concatenations of strings of equal length generated by languages  $A$  and  $B$  respectively. From the start state push a marker onto the stack to mark the bottom. Then for each character from  $A$  you will push a 1 onto the stack. Then while going thru  $B$  you will pop 1 from the stack for every character. This method does not accept unless  $A$  and  $B$  are of the same length, which will be known only if the stack marker is seen at the end of both strings.