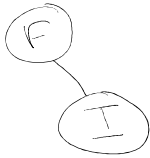


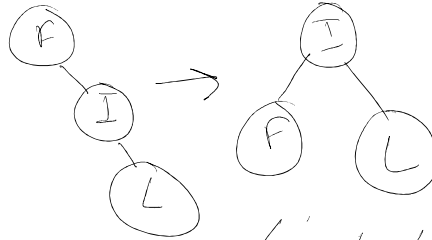
Insert 'F'



Insert 'I'

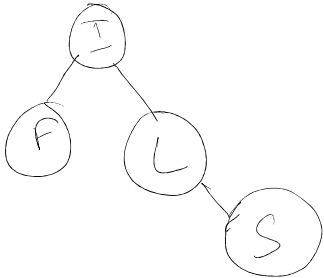


Insert 'Z'

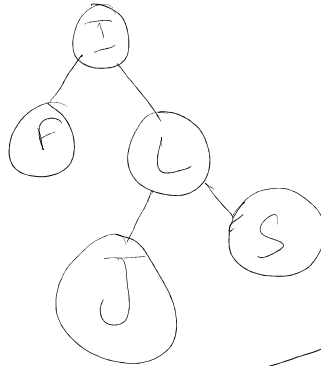


Single Left Rotation

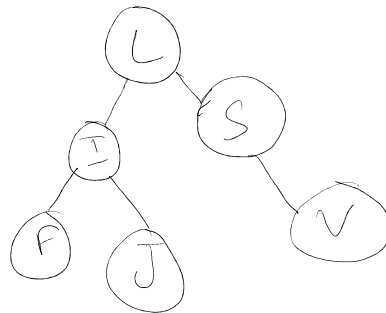
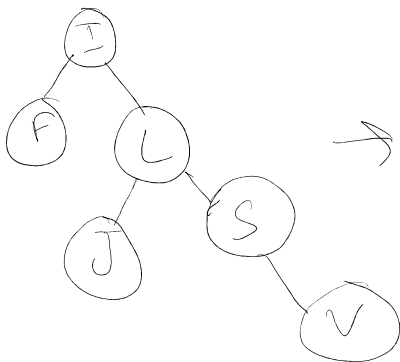
Insert 'S'



Insert 'J'

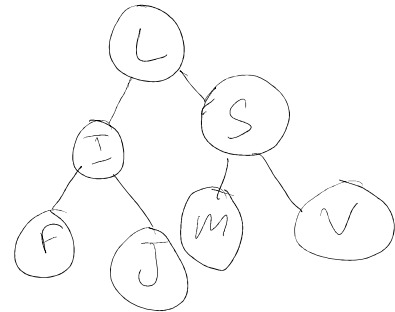


Insert 'V'

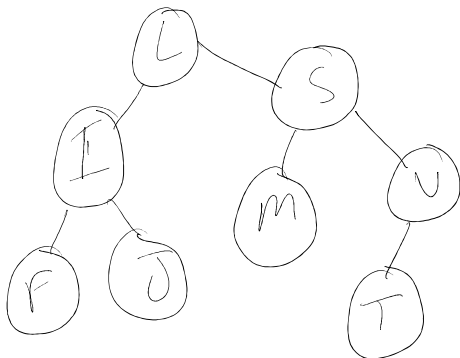


single left rotation at 'I'

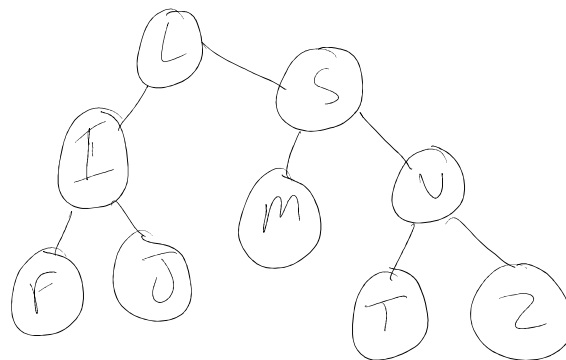
Insert 'M'



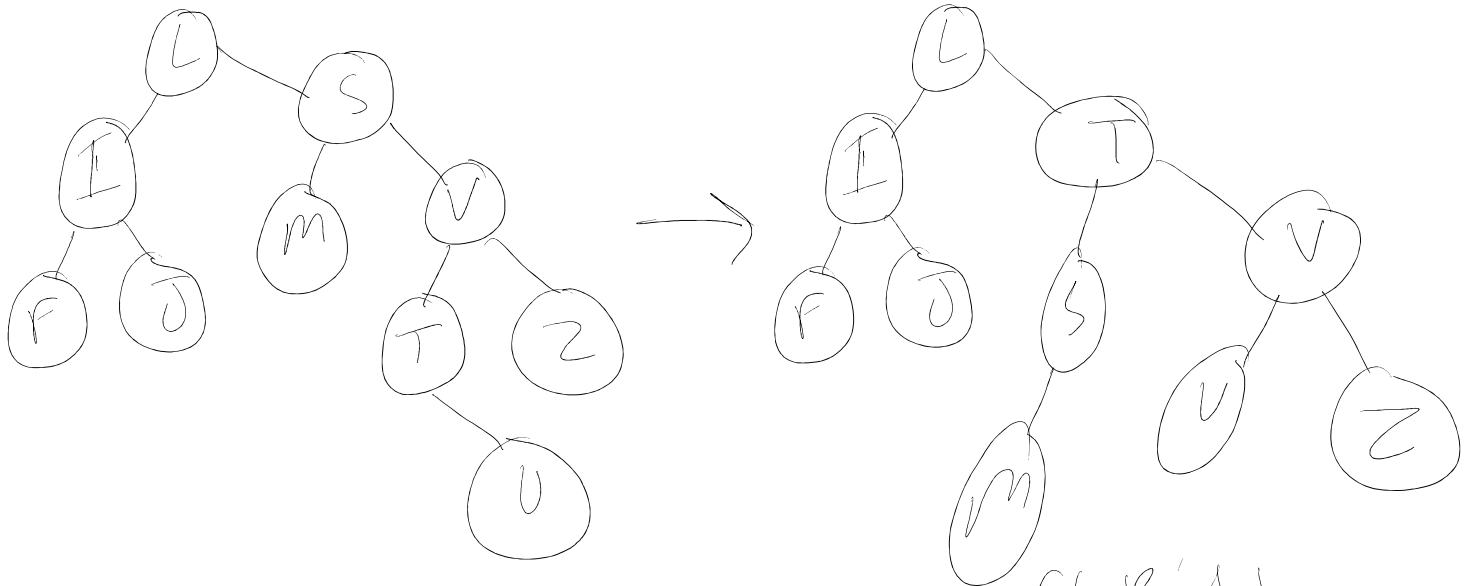
Insert 'T'



Insert 'Z'

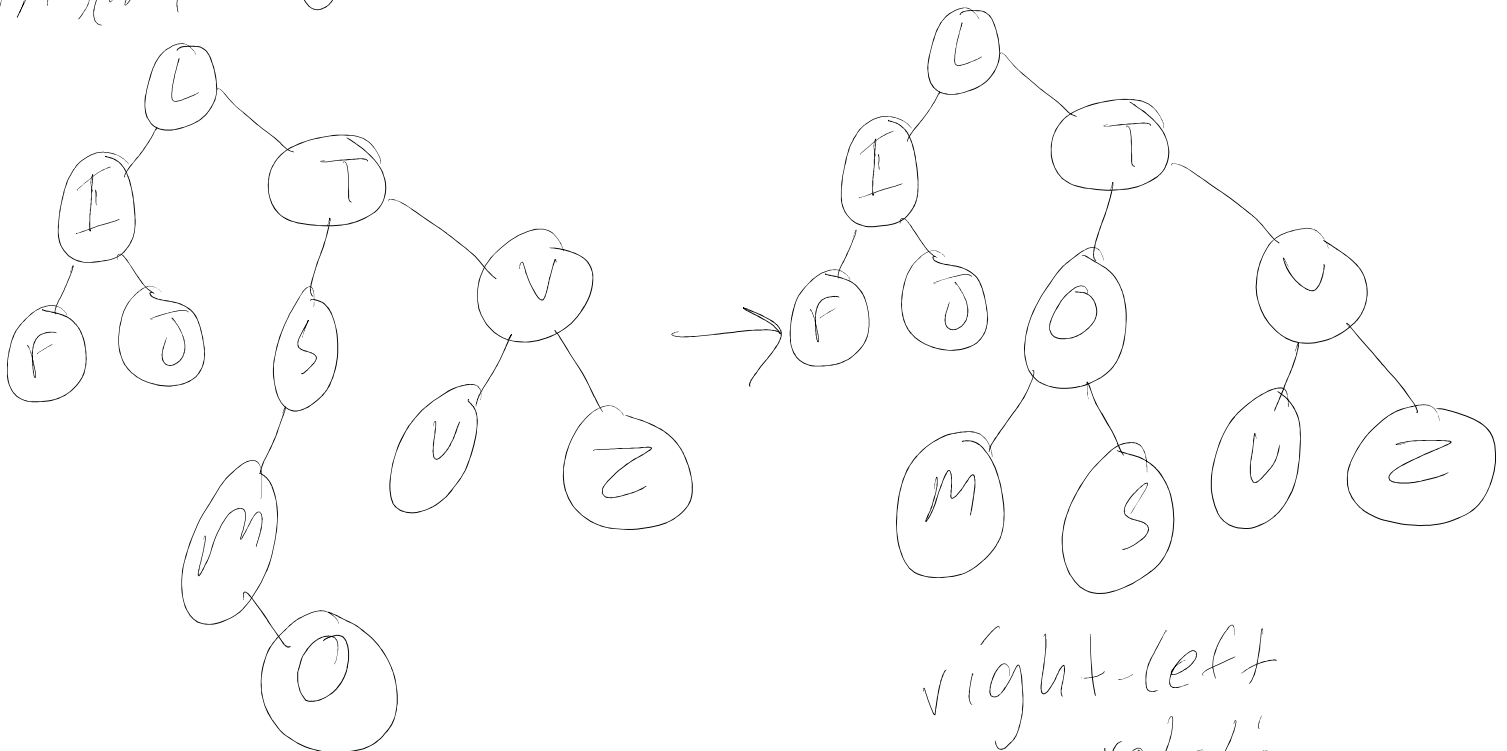


Insert 'U'



Left-Right
rotation

Insert 'O'



right-left
rotation

Q1b)

```
double computeMedian(Treenode *rootptr) {
    int n; // nodecount
    bool isodd;
    int nMedian, nMedian2;
    int nthval, nthval2;
```

```
func inorder (rootptr, incrementCount(n)) // incrementCount increases node count on
// each visit
```

```
isodd = checkOdd(nodecount)
```

```
if (isodd) {
```

```
    nMedian = (n-1)/2
```

```
else { nMedian = (n/2)
```

```
    nMedian2 = (n/2)-1 }
```

```
if (isodd) {
```

```
func inorder (rootptr, getNodeValat(nMedian, nthval)) // getNodeValat has local node count
```

```
return nthval
```

```
}
```

// that increments on each visit

// if nodecount == n, return the value at that

// point to nthval

```
else {
```

```
func inorder (rootptr, getNodeValat(nMedian, nthval))
```

```
func inorder (rootptr, getNodeValat(nMedian2, nthval2))
```

```
return (nthval + nthval2) / 2
}
```

The time complexity is $O(\log n)$. The logic

of algorithm is to do an inorder traversal and get

total number of nodes. If total number of nodes

is odd, the median element is at $\frac{n}{2}$ location (when going through AVL tree in inorder traverse)

Likewise, if its even, the median is value of

$$\frac{(n/2) + ((n/2)-1)}{2}$$

(The Treenode structure and methods referenced here are from slides such as inorder function)

```
int CheckAVL (Treenode* rootptr, bool& isbalanced=true) { // in main function we would return
    return 0 if rootptr is null // isbalanced
```

```
int lh = CheckAVL (root->left, isbalanced)
int rh = CheckAVL (root->right, isbalanced) // or less than -1
if |lh-rh| is greater than 1, isbalanced=false
return (max(lh, rh)+1) }
```

The time complexity is $O(n^2)$. The algorithm is based on recursive calls. It takes root pointer till it reaches the bottom nodes. If the node is a leaf, it returns 0. For all else, it returns the max of height of their subtrees plus 2 for the node itself. If at any point the left and right height of nodes are greater than 1 or less than -1, it makes boolean isbalanced false thus indicating it is not an AVL tree.

Q3

A better strategy to find optimum number of computers would be to start from a big number of computers and keep halving number of computers till waiting time is greater than required. Then take that as minimum and keep increasing till we get satisfying waiting time for a number of computers