

Due on Dec 20th, 2022 at 11:59pm

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1. [Deep Learning Models]

(a) Consider a 3D convolution layer. Suppose the input size is $32 \times 32 \times 3$ (width, height) and we use ten 5×5 (width, height) kernels to convolve with it. Set stride = 1 and pad = 2. What is the output size? Let the bias for each kernel be a scalar, how many parameters do we have in this layer?

Solution:

The input data shape is

$$[C_{in}, D_{in}, H_{in}, W_{in}] = [1, 3, 32, 32]$$

and the kernel size is

$$[C_{out}, D_{kernel}, H_{kernel}, w_{kernel}] = [10, 3, 5, 5]$$

Then by the formula, we have output data with a shape

$$[C_{out}, D_{out}, H_{out}, W_{out}]$$

and

$$D_{out} = \frac{D_{in} + 2 \times pad - (D_{kernel} - 1) - 1}{stride} + 1 = 1$$

$$H_{out} = \frac{H_{in} + 2 \times pad - (H_{kernel} - 1) - 1}{stride} + 1 = 32$$

$$W_{out} = \frac{W_{in} + 2 \times pad - (W_{kernel} - 1) - 1}{stride} + 1 = 32$$

Thus, the output size is $[C_{out}, D_{out}, H_{out}, W_{out}] = [10, 1, 32, 32]$ Moreover, the total number of parameters is

$$\#\{parameters\} = \#\{parameters\ in\ kernel\} + \#\{biases\} = 5 \times 5 \times 3 \times 10 + 10 = 760$$

(b) The convolution layer is followed by a max pooling layer with 2×2 (width, height) filter and stride = 2. What is the output size of the pooling layer? How many parameters do we have in the pooling layer?

Solution:

The input data shape is

$$[C_{in}, D_{in}, H_{in}, W_{in}] = [10, 1, 32, 32]$$

and the kernel shape is

$$[C_{out}, D_{kernel}, H_{kernel}, W_{kernel}] = [10, 1, 2, 2]$$

Then by the formula, we have output data with a shape

$$[C_{out}, D_{out}, H_{out}, W_{out}]$$

and

$$\begin{split} D_{out} &= \frac{D_{in} + 2 \times pad - (D_{kernel} - 1) - 1}{stride} + 1 = 1 \\ H_{out} &= \frac{H_{in} + 2 \times pad - (H_{kernel} - 1) - 1}{stride} + 1 = 16 \\ W_{out} &= \frac{W_{in} + 2 \times pad - (W_{kernel} - 1) - 1}{stride} + 1 = 16 \end{split}$$

Thus, the output size is $[C_{out}, D_{out}, H_{out}, W_{out}] = [10, 1, 16, 16].$

Moreover, given that the max pooling layer only performs maximizing, there are no parameters in the pooling layer. Thus, the total number of parameters of the pooling layer is 0.

- 2. [Deep Learning Models]
 - (a) (i.) When r = 1, W is exactly the eigenvector of XX^T corresponding to its largest eigenvalue.

When r = 1, we know that $\mathbf{W}^T \mathbf{X} \mathbf{X}^T \mathbf{W}$ is a scalar, which means

$$Tr(\mathbf{W}^T \mathbf{X} \mathbf{X}^T \mathbf{W}) = \mathbf{W}^T \mathbf{X} \mathbf{X}^T \mathbf{W}$$

Hence, the optimization problem can be rewritten as follows:

Then, the Lagrangian is:

$$\mathcal{L}(\boldsymbol{W}, \lambda) = \boldsymbol{W}^T \boldsymbol{X} \boldsymbol{X}^T \boldsymbol{W} - \lambda \boldsymbol{W}^T \boldsymbol{W}$$

Taking the derivative of \mathcal{L} w.r.t W and setting it to 0, we get

$$2XX^{T}W^{*} - 2\lambda^{*}W^{*} = 0$$

$$\Rightarrow$$

$$XX^{T}W^{*} = \lambda^{*}W^{*}$$

Thus, λ^* is eigenvalue of XX^T and W^* is the corresponding eigenvector. Moreover, since

$$\mathbf{W}^{\star T} \mathbf{X} \mathbf{X}^T \mathbf{W}^{\star} = \lambda^{\star}$$

Therefore, we need to get the largest eigenvalue λ^* to maximize $W^T X X^T W$, which means W^* is the eigenvector corresponding to the largest eigenvalue.

(ii.) \boldsymbol{W} is also the solution to

$$\begin{array}{ll} \text{minimize} & ||\boldsymbol{X} - \boldsymbol{W} \boldsymbol{W}^T \boldsymbol{X}||_F^2 \quad s.t. \quad \boldsymbol{W}^T \boldsymbol{W} = \boldsymbol{I}_r \\ \end{array}$$

Proof:

Given that
$$|\mathbf{P}|_F = \sqrt{Tr(\mathbf{P}^T\mathbf{P})}$$
, we get

$$\begin{aligned} ||\boldsymbol{X} - \boldsymbol{W} \boldsymbol{W}^T \boldsymbol{X}||_F^2 &= Tr[(\boldsymbol{X} - \boldsymbol{W} \boldsymbol{W}^T \boldsymbol{X})^T (\boldsymbol{X} - \boldsymbol{W} \boldsymbol{W}^T \boldsymbol{X})] \\ &= Tr[\boldsymbol{X}^T \boldsymbol{X} - \boldsymbol{X}^T \boldsymbol{W} \boldsymbol{W}^T \boldsymbol{X} - \boldsymbol{X}^T \boldsymbol{W} \boldsymbol{W}^T \boldsymbol{X} + \boldsymbol{X}^T \boldsymbol{W} \boldsymbol{W}^T \boldsymbol{W} \boldsymbol{W}^T \boldsymbol{X}] \\ &= Tr[\boldsymbol{X}^T \boldsymbol{X} - \boldsymbol{X}^T \boldsymbol{W} \boldsymbol{W}^T \boldsymbol{X}] \\ &= Tr(\boldsymbol{X}^T \boldsymbol{X}) - Tr(\boldsymbol{X}^T \boldsymbol{W} \boldsymbol{W}^T \boldsymbol{X}) \\ &= Tr(\boldsymbol{X}^T \boldsymbol{X}) - Tr(\boldsymbol{W}^T \boldsymbol{X} \boldsymbol{X}^T \boldsymbol{W}) \end{aligned}$$

Since the first term of the equation has nothing to do with W, the optimization problem can be rewritten as follows:

$$\begin{array}{ll}
\text{minimize} & -Tr(\boldsymbol{W}^T \boldsymbol{X} \boldsymbol{X}^T \boldsymbol{W}) & s.t. \ \boldsymbol{W}^T \boldsymbol{W} = \boldsymbol{I}_r
\end{array}$$

which is equivalent to the PCA problem.

(b) (i.) \boldsymbol{A}_2^{\star} can be solved from:

$$egin{aligned} & ext{minimize} & ||oldsymbol{X} - oldsymbol{A}_2 oldsymbol{A}_2^\dagger oldsymbol{X}||_F^2 \end{aligned}$$

- (ii.) The solution W from (a) can be taken as the same as A_2^* .
- 3. [Ensemble Learning] Suppose there are L independent two-class classifiers used for simple voting and the output of classifier j ($j = 1 \cdots L$) is denoted as d_j . From the point of view that the mean squared error of an estimator can be decomposed into the bias part and the variance part, explain why increasing L can lead to an increase in classification accuracy.

Proof:

By the definition of MSE, we get

$$\begin{split} MSE(\hat{y}) &= \mathbb{E}[(\hat{y} - y)^2] = \mathbb{E}[(\hat{y} - \mathbb{E}[\hat{y}] + \mathbb{E}[\hat{y}] - y)^2] \\ &= \mathbb{E}[(\hat{y} - \mathbb{E}[\hat{y}])^2 + 2(\hat{y} - \mathbb{E}[\hat{y}])(\mathbb{E}[\hat{y}] - y) + (\mathbb{E}[\hat{y}] - y)^2] \\ &= \mathbb{E}[(\hat{y} - \mathbb{E}[\hat{y}])^2] + 2\mathbb{E}[(\hat{y} - \mathbb{E}[\hat{y}])]\mathbb{E}[(\mathbb{E}[\hat{y}] - y)] + \mathbb{E}[(\mathbb{E}[\hat{y}] - y)^2] \\ &= \mathbb{E}[(\hat{y} - \mathbb{E}[\hat{y}])^2] + 2(\mathbb{E}[\hat{y}] - \mathbb{E}[\hat{y}])\mathbb{E}[(\mathbb{E}[\hat{y}] - y)] + (\mathbb{E}[\hat{y}] - y)^2 \\ &= \mathbb{E}[(\hat{y} - \mathbb{E}[\hat{y}])^2] + (\mathbb{E}[\hat{y}] - y)^2 \\ &= \mathrm{Var}(\hat{y}) + \mathrm{Bias}^2(\hat{y}, y) \end{split}$$

Then, for the second term of the equation above, we get

$$\begin{aligned} \operatorname{Bias}^2(\hat{y}, y) &\propto \operatorname{Bias}(\hat{y}, y) \\ &= \mathbb{E}[\hat{y}] - y \\ &\propto \mathbb{E}[\hat{y}] \\ &= \mathbb{E}\left[\frac{1}{L}\sum_j d_j\right] \\ &\geq \frac{1}{L} \times L \min_j \{\mathbb{E}[d_j]\} \\ &= \min_j \{\mathbb{E}[d_j]\} \end{aligned}$$

which means that the Bias term won't change as L gets larger.

As for the first term, we get

$$\operatorname{Var}(\hat{y}) = \operatorname{Var}\left(\frac{1}{L}\sum_{j}d_{j}\right)$$

$$= \frac{1}{L^{2}}\operatorname{Var}\left(\sum_{j}d_{j}\right)$$

$$\leq \frac{1}{L^{2}} \times L \max_{j}\left(\operatorname{Var}(d_{j})\right)$$

$$= \frac{1}{L}\max_{j}\left\{\operatorname{Var}(d_{j})\right\}$$

which means that the Variance term will get smaller when L gets larger.

In conclusion, $MSE(\hat{y})$ will get smaller as L gets larger, so the classification will be more accurate.

4. [Model Assessment and Selection] Suppose we carry out a K-fold cross-validation on a dataset and obtain the classification error rates $\{p_i\}_{i=1}^K$, describe the steps of a one-sided t test on testing the null hypothesis H_0 that the classifier has error percentage p_0 or less at a significance level α .

HW5-Coding

December 18, 2022

1 Homework 5: Convolutional neural network (30 points)

In this part, you need to implement and train a convolutional neural network on the CIFAR-10 dataset with PyTorch. ### What is PyTorch?

PyTorch is a system for executing dynamic computational graphs over Tensor objects that behave similarly as numpy ndarray. It comes with a powerful automatic differentiation engine that removes the need for manual back-propagation.

1.0.1 Why?

- Our code will now run on GPUs! Much faster training. When using a framework like Py-Torch or TensorFlow you can harness the power of the GPU for your own custom neural network architectures without having to write CUDA code directly (which is beyond the scope of this class).
- We want you to be ready to use one of these frameworks for your project so you can experiment more efficiently than if you were writing every feature you want to use by hand.
- We want you to stand on the shoulders of giants! TensorFlow and PyTorch are both excellent frameworks that will make your lives a lot easier, and now that you understand their guts, you are free to use them:)
- We want you to be exposed to the sort of deep learning code you might run into in academia or industry. ## How can I learn PyTorch?

Justin Johnson has made an excellent tutorial for PyTorch.

You can also find the detailed API doc here. If you have other questions that are not addressed by the API docs, the PyTorch forum is a much better place to ask than StackOverflow.

Install PyTorch and Skorch.

```
[1]: # !pip install -q torch skorch torchvision torchtext
[2]: import numpy as np
import sklearn
import skorch
import torch
import torch.nn as nn
import torchvision
from matplotlib import pyplot as plt
```

1.1 0. Tensor Operations (5 points)

Tensor operations are important in deep learning models. In this part, you are required to get famaliar to some common tensor operations in PyTorch.

1.1.1 1) Tensor squeezing, unsqueezing and viewing

Tensor squeezing, unsqueezing and viewing are important methods to change the dimension of a Tensor, and the corresponding functions are torch.squeeze, torch.unsqueeze and torch.Tensor.view. Please read the documents of the functions, and finish the following practice.

```
[3]: \# x \text{ is a tensor with size being (3, 2)}
     x = torch.Tensor([[1, 2],
                        [3, 4],
                        [5, 6]])
     print(x.shape)
     # Add two new dimensions to x by using the function torch.unsqueeze, so that the
      \rightarrowsize of x becomes (3, 1, 2, 1).
     x = torch.unsqueeze(x, 1)
     x = torch.unsqueeze(x, 3)
     print(x.shape)
     # Remove the two dimensions justed added by using the function torch.squeeze,
      \rightarrow and change the size of x back to (3, 2).
     x = torch.squeeze(x)
     print(x.shape)
     # x is now a two-dimensional tensor, or in other words a matrix. Now use the
      →function torch. Tensor. view and change x to a one-dimensional vector with size
      \rightarrowbeing (6).
     x = x.view(6)
     print(x.shape)
    torch.Size([3, 2])
    torch.Size([3, 1, 2, 1])
    torch.Size([3, 2])
    torch.Size([6])
```

1.1.2 2) Tensor concatenation and stack

Tensor concatenation and stack are operations to combine small tensors into big tensors. The corresponding functions are torch.cat and torch.stack. Please read the documents of the functions, and finish the following practice.

```
[4]: # x is a tensor with size being (3, 2)
x = torch.Tensor([[1, 2], [3, 4], [5, 6]])

# y is a tensor with size being (3, 2)
y = torch.Tensor([[-1, -2], [-3, -4], [-5, -6]])
```

1.1.3 3) Tensor expansion

Tensor expansion is to expand a tensor into a larger tensor along singleton dimensions. The corresponding functions are torch. Tensor. expand and torch. Tensor. expand_as. Please read the documents of the functions, and finish the following practice.

```
[5]: # x is a tensor with size being (3)
x = torch.Tensor([1, 2, 3])

# Our goal is to generate a tensor z with size (2, 3), so that z[0,:,:] = x,
\[
\times z[1,:,:] = x.

# [TO DO]
# Change the size of x into (1, 3) by using torch.unsqueeze.
x = x.unsqueeze(0)
print(x.shape)

# [TO DO]
# Then expand the new tensor to the target tensor by using torch.Tensor.expand.
z = torch.Tensor.expand(x, 2, 3)
print(z.shape)

torch.Size([1, 3])
```

1.1.4 4) Tensor reduction in a given dimension

torch.Size([2, 3])

In deep learning, we often need to compute the mean/sum/max/min value in a given dimension of a tensor. Please read the document of torch.mean, torch.sum, torch.max, torch.min, torch.topk, and finish the following practice.

```
[6]: # x is a random tensor with size being (10, 50)
     x = torch.randn(10, 50)
     # Compute the mean value for each row of x.
     # You need to generate a tensor x_mean of size (10), and x_mean[k, :] is the
      \rightarrowmean value of the k-th row of x.
     x_{mean} = torch.mean(x, 1)
     print(x_mean[3,])
     # Compute the sum value for each row of x.
     # You need to generate a tensor x_sum of size (10).
     x_sum = torch.sum(x, 1)
     print(x_sum.shape)
     # Compute the max value for each row of x.
     # You need to generate a tensor x_max of size (10).
     x_{max}, _ = torch.max(x, 1)
     print(x_max.shape)
     # Compute the min value for each row of x.
     # You need to generate a tensor x_min of size (10).
     x_{min}, _ = torch.min(x, 1)
     print(x_min.shape)
     # Compute the top-5 values for each row of x.
     # You need to generate a tensor x_mean of size (10, 5), and x_top[k, :] is the
      \rightarrow top-5 values of each row in x.
     x_{mean} = torch.topk(x, 5, 1)
     print(x_mean_xtop.shape)
    tensor(0.0931)
    torch.Size([10])
    torch.Size([10])
    torch.Size([10])
    torch.Size([10, 5])
```

1.2 Convolutional Neural Networks

Implement a convolutional neural network for image classification on CIFAR-10 dataset.

CIFAR-10 is an image dataset of 10 categories. Each image has a size of 32x32 pixels. The following code will download the dataset, and split it into train and test. For this question, we use the default validation split generated by Skorch.

```
[7]: train = torchvision.datasets.CIFAR10("./data", train=True, download=True) test = torchvision.datasets.CIFAR10("./data", train=False, download=True)
```

Files already downloaded and verified Files already downloaded and verified

The following code visualizes some samples in the dataset. You may use it to debug your model if necessary.

```
[8]: def plot(data, labels=None, num_sample=5):
    n = min(len(data), num_sample)
    for i in range(n):
        plt.subplot(1, n, i + 1)
        plt.imshow(data[i], cmap="gray")
        plt.xticks([])
        plt.yticks([])
        if labels is not None:
            plt.title(labels[i])
train.labels = [train.classes[target] for target in train.targets]
plot(train.data, train.labels)
```



1.2.1 1) Basic CNN implementation

Consider a basic CNN model

- It has 3 convolutional layers, followed by a linear layer.
- Each convolutional layer has a kernel size of 3, a padding of 1.
- ReLU activation is applied on every hidden layer.

Please implement this model in the following section. The hyperparameters is then be tuned and you need to fill the results in the table.

a) Implement convolutional layers (10 Points) Implement the initialization function and the forward function of the CNN.

```
[9]: class CNN(nn.Module):
    def __init__(self, channels):
        super(CNN, self).__init__()
    # implement parameter definitions here
        # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)*****
        self.conv_1 = torch.nn.Conv2d(in_channels=3, out_channels=channels,__
        ⇒kernel_size=3, padding=1)
```

```
self.conv_2 = torch.nn.Conv2d(in_channels=channels,__
→out_channels=channels, kernel_size=3, padding=1)
      self.conv_3 = torch.nn.Conv2d(in_channels=channels,__
→out_channels=channels, kernel_size=3, padding=1)
      self.relu = torch.nn.ReLU()
      self.linear = torch.nn.Linear(in_features=32 * 32 * channels,
→out_features=10)
       # ****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
  def forward(self, images):
       # implement the forward function here
       # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
      out = self.relu(self.conv_1(images))
      out = self.relu(self.conv_2(out))
      out = self.relu(self.conv_3(out))
      out = torch.nn.Flatten(1, -1)(out)
      out = self.linear(out)
       # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
      return out
```

b) Tune hyperparameters Train the CNN model on CIFAR-10 dataset. We can tune the number of channels, optimizer, learning rate and the number of epochs for best validation accuracy.

```
[10]: # implement hyperparameters here
      learning_rate = 1e-4
      optimize = torch.optim.Adam
      channel = 64
      train_data_normalized = torch.Tensor(train.data / 255)
      train_data_normalized = train_data_normalized.permute(0, 3, 1, 2)
      print(f'The channel was {channel}, the learning rate was {learning_rate} and the
       →optimizer was {str(optimize)}')
      cnn = CNN(channels=channel)
      model = skorch.NeuralNetClassifier(cnn, criterion=torch.nn.CrossEntropyLoss,
                                         device="cuda",
                                         optimizer=optimize,
                                         # optimizer__momentum=0.90,
                                         lr=learning_rate,
                                         max_epochs=15,
                                         batch_size=64,
                                         callbacks=[skorch.callbacks.
       →EarlyStopping(lower_is_better=True)])
```

```
# implement input normalization & type cast here
model.fit(train_data_normalized, np.asarray(train.targets))
```

The channel was 64, the learning rate was 0.0001 and the optimizer was <class 'torch.optim.adam.Adam'>

epoch	train_loss		valid_loss	dur
1		0.5020	1.4174	
10.9766				
2	1.3244	0.5650	1.2413	
9.9119				
3	1.1825	0.5860	1.1763	
9.9063				
4	1.0709	0.6101	1.1131	
9.9199				
5	0.9765	0.6264	1.0658	
9.9347				
6	0.8994	0.6411	1.0356	
10.7903				
7	0.8355	0.6520	1.0182	
9.8990				
8	0.7797	0.6573	1.0091	
9.8756				
9	0.7293	0.6609	1.0072	
9.9047				
10	0.6823	0.6622	1.0101	10.0021
11	0.6373	0.6630	1.0206	9.8481
12	0.5937	0.6618	1.0378	9.8932
13	0.5516	0.6587	1.0656	9.8847

Stopping since valid_loss has not improved in the last 5 epochs.

Write down **validation accuracy** of your model under different hyperparameter settings. Note the validation set is automatically split by Skorch during model.fit().

#channel for each layer	optimizer	Adam
(64, 64, 64)		0.6630

1.2.2 2) Full CNN implementation (10 points)

Based on the CNN in the previous question, implement a full CNN model with max pooling layer.

- Add a max pooling layer after each convolutional layer.
- Each max pooling layer has a kernel size of 2 and a stride of 2.

a) Implement max pooling layers Copy the CNN implementation in previous question. Implement max pooling layers.

```
[11]: class CNN_MaxPool(nn.Module):
          def __init__(self, channels):
              super(CNN_MaxPool, self).__init__()
              # implement parameter definitions here
              # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
              assert len(channels) == 1 or len(
                  channels) == 3, f"invalid channels number, expect 1 or 3 but get_
       →{len(channels)} instead."
              if len(channels) == 1:
                  CHANNELS = channels * 3
              else:
                  CHANNELS = channels
              self.conv_1 = torch.nn.Conv2d(in_channels=3, out_channels=CHANNELS[0],
       →kernel_size=3, padding=1)
              self.conv_2 = torch.nn.Conv2d(in_channels=CHANNELS[0],__
       →out_channels=CHANNELS[1], kernel_size=3, padding=1)
              self.conv_3 = torch.nn.Conv2d(in_channels=CHANNELS[1],__
       →out_channels=CHANNELS[2], kernel_size=3, padding=1)
              self.relu = torch.nn.ReLU()
              self.max_pool = torch.nn.MaxPool2d(kernel_size=2, stride=2)
              self.linear = torch.nn.Linear(in_features=4 * 4 * CHANNELS[2],__
       →out_features=10)
              # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
          def forward(self, images):
              # implement the forward function here
              # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
              out = self.relu(self.max_pool(self.conv_1(images)))
              out = self.relu(self.max_pool(self.conv_2(out)))
              out = self.relu(self.max_pool(self.conv_3(out)))
              out = torch.nn.Flatten(1, -1)(out)
              out = self.linear(out)
              # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
              return out
```

b) Tune hyperparameters Based on best optimizer found in the previous problem, we can tune the number of channels and learning rate for best validation accuracy.

```
[12]: channel = 64
      train_data_normalized = torch.Tensor(train.data / 255)
      train_data_normalized = train_data_normalized.permute(0, 3, 1, 2)
      cnn_max_pool_same_channels = CNN_MaxPool(channels=[channel])
      # cnn_max_pool_diff_channels = CNN_MaxPool(channels=[c, 2 * c, 4 * c])
      model = skorch.NeuralNetClassifier(cnn_max_pool_same_channels, criterion=torch.
       →nn.CrossEntropyLoss,
                                                       device="cuda",
                                                       optimizer=torch.optim.Adam,
                                                       lr=0.0001,
                                                       max_epochs=25,
                                                       batch_size=64,
                                                       callbacks=[skorch.callbacks.
       →EarlyStopping(lower_is_better=True)], )
      # implement input normalization & type cast here
      model.fit(train_data_normalized, np.asarray(train.targets))
```

epoch	train_loss	valid_acc	valid_loss	dur
1	1.9269	0.4119	1.6712	
3.4668				
2	1.6067	0.4523	1.5397	
3.5056				
3	1.4981	0.4770	1.4602	
3.6588	1 4011	0 5040	1 2000	
4 3.5595	1.4211	0.5048	1.3998	
5.5595 5	1.3675	0.5217	1.3588	
4.0562	1.0070	0.0217	1.0000	
6	1.3265	0.5365	1.3244	
3.6377				
7	1.2920	0.5464	1.2912	
3.7853				
8	1.2612	0.5584	1.2617	
3.8943				
9	1.2331	0.5683	1.2352	
3.5465				
10	1.2072	0.5769	1.2106	
3.6510 11	1.1830	0.5853	1.1882	
3.5429	1.1030	0.5655	1.1002	
12	1.1600	0.5929	1.1679	
3.4975	2,200	0.0020	2,20,0	
13	1.1383	0.5988	1.1495	
3.4832				
14	1.1177	0.6024	1.1318	
3.4758				
15	1.0980	0.6076	1.1161	

```
3.4716
                     1.0791
                                  0.6131
                                                 1.1012
          16
     3.4695
          17
                     1.0612
                                  0.6193
                                                 1.0876
     3.4775
                     1.0441
                                  0.6215
                                                 1.0742
          18
     4.2113
                     1.0279
                                  0.6265
                                                 1.0615
     4.5485
                     1.0126
                                  0.6287
                                                 1.0497
     3.6776
                     0.9979
          21
                                  0.6339
                                                 1.0389
     4.7526
                                  0.6370
                                                 1.0286
          22
                     0.9839
     4.3440
                     0.9706
                                  0.6396
                                                 1.0188
          23
     4.2747
                                  0.6434
          24
                     0.9578
                                                 1.0091
     4.2250
          25
                     0.9456
                                  0.6470
                                                 1.0014
     4.2377
[12]: <class 'skorch.classifier.NeuralNetClassifier'>[initialized](
        module_=CNN_MaxPool(
          (conv_1): Conv2d(3, 64, kernel_size=(3, 3), stride=(1, 1), padding=(1, 1))
          (conv_2): Conv2d(64, 64, kernel_size=(3, 3), stride=(1, 1), padding=(1, 1))
          (conv_3): Conv2d(64, 64, kernel_size=(3, 3), stride=(1, 1), padding=(1, 1))
          (relu): ReLU()
          (max_pool): MaxPool2d(kernel_size=2, stride=2, padding=0, dilation=1,
      ceil_mode=False)
          (linear): Linear(in_features=1024, out_features=10, bias=True)
        ),
```

Write down the **validation accuracy** of the model under different hyperparameter settings.

#channel for each layer	validation accuracy
(64, 64, 64)	0.6470

For the best model you have, test it on the test set.

)

```
[13]: # implement the same input normalization & type cast here
test_data_normalized = torch.Tensor(test.data / 255)
test_data_normalized = test_data_normalized.permute(0, 3, 1, 2)
test.predictions = model.predict(test_data_normalized)
sklearn.metrics.accuracy_score(test.targets, test.predictions)
```

[13]: 0.654

How much **test accuracy** do you get? What can you conclude for the design of CNN structure and tuning of hyperparameters? (5 points)

Your Answer: 0.654