Robust Cooperative Manipulation Without Force/Torque Measurements: Control Design and Experiments

Christos K. Verginis[®], Member, IEEE, Matteo Mastellaro, and Dimos V. Dimarogonas[®], Senior Member, IEEE

Abstract—This paper presents two novel control methodologies for the cooperative manipulation of an object by N robotic agents. First, we design an adaptive control protocol which employs quaternion feedback for the object orientation to avoid potential representation singularities. Second, we propose a control protocol that guarantees predefined transient and steady-state performance for the object trajectory. Both methodologies are decentralized, since the agents calculate their own signals without communicating with each other, as well as robust to external disturbances and model uncertainties. Moreover, we consider that the grasping points are rigid and avoid the need for force/torque measurements. Load distribution is also included via a grasp matrix pseudoinverse to account for potential differences in the agents' power capabilities. Finally, simulation and experimental results with two robotic arms verify the theoretical findings.

Index Terms—Adaptive control, cooperative manipulation, multiagent systems, prescribed performance control (PPC), robust control, unit quaternions.

I. INTRODUCTION

ULTIAGENT systems have gained significant attention in the past years due to the numerous advantages they yield with respect to single-agent setups. In the case of robotic manipulation, heavy payloads and challenging maneuvers necessitate the employment of multiple robotic agents. Although collaborative manipulation of a single object, both in terms of transportation (regulation) and trajectory tracking, has been considered in the research community the last decades, there still exist several challenges that need to be taken into account by on-going research, both in control design as well as experimental evaluation.

Early works develop control architectures where the robotic agents communicate and share information with each other,

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The authors are with the Centre for Autonomous Systems and ACCESS Linnaeus Centre, KTH Royal Institute of Technology, 10044 Stockholm, Sweden (e-mail: cverginis@kth.se; matteoma@kth.se; dimos@kth.se).

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and completely decentralized schemes, where each agent uses only local information or observers, avoiding potential communication delays (see, indicatively, [1]–[10]). Impedance and hybrid force/position control is the most common methodology used in [8]–[24], where a desired impedance behavior is imposed potentially with force regulation. Most of the aforementioned works employ force/torque sensors to acquire feedback of the object-robots contact forces/torques, which, however, may result in performance decline due to sensor noise or mounting difficulties. When the grasping object-agents contacts are rigid, the need for such sensors is redundant, since the overall system can be seen as a closed-chain robot. Regarding grasp rigidity, recent technological advances allow end-effectors to grasp *rigidly* certain objects, motivating the specific analysis.

In addition, many works in the related literature consider known dynamic parameters regarding the object and the robotic agents. However, the accurate knowledge of such parameters, such as masses or moments of inertia, can be a challenging issue, especially for complex robotic manipulators.

Force/torque sensor-free methodologies have been developed in [4], [6], [8], [16], [19], [22], [25], [26], and [21]; [16] develops a leader–follower communication-based scheme by partly accounting for dynamic parametric uncertainty, whereas [8] and [4] employ partial and full model information, respectively; [6] develops an adaptive control scheme that achieves boundedness of the errors based on known disturbance bounds, and [25] proposes an adaptive estimator for kinematic uncertainties, whose convergence affects the asymptotic stability of the overall scheme. In [21] and [22], adaptive fuzzy estimators for structural and parametric uncertainty are introduced, with the latter not taking into account the object dynamics; [26] develops an adaptive protocol that guarantees boundedness of the internal forces, and [19] employs an approximate force estimator for a human–robot cooperative task.

Another important feature is the representation of the agent and object orientation. The most commonly used tools for orientation representation are rotation matrices, Euler angles, unit quaternions, and the angle/axis convention. In this paper, we employ unit quaternions, which do not suffer from representation singularities and can be tuned to avoid undesired local equilibria, issues that characterize the other methods.

Unit quaternions in the control design of cooperative manipulation tasks have been employed in [11], where the

authors address the gravity-compensated pose regulation of the grasped object, as well as in [12], where a model-based force-feedback scheme is developed.

Full model information is employed in the works [1], [7], [9], [10], [13], [15], [17], [23]; [7] employs a velocity estimator, [23] uses a linearized model, and [15] and [14] considers kinematic and grasping uncertainties. Adaptive control schemes are developed in [20], where redundancy is used for obstacle avoidance and [27], where the object dynamics are not taken into account; [28] and [29] propose protocols based on graph-based communication by neglecting parts of the overall system dynamics, and [18] and [29] consider leader-follower approaches. An observer-based (for state and task estimation) adaptive control scheme is proposed in [24]. Model-based force-control control protocols with unilateral constraints are developed in [30] and [31]. Formation control approaches are considered in [32] and [31] and a navigation-function scheme is used in [33]; [34] includes hybrid control with intermittent contacts, and in our previous works [35], [36], we considered model predictive control approaches for cooperative object transportation. Finally, internal force and load distribution analysis in cooperative manipulation tasks is performed in a variety of works (e.g., [37]–[41]).

Note that most of the aforementioned adaptive control schemes (except e.g., [21]) employ the usual regressor matrix technique to compensate for unknown dynamic parameters [42], [43], which assumes a known structure of the dynamic terms. Such structures can still be difficult to obtain accurately, especially when complex manipulators are considered. Moreover, in terms of load distribution, many of the related works use load sharing coefficients (e.g., [4], [5], [21]), without proving that undesired internal forces do not arise, or the standard Moore–Penrose inverse of the grasp matrix (e.g., [6], [17]), which has been questioned in [37].

A. Contribution and Outline

In this paper, we propose two novel nonlinear control protocols for the trajectory tracking of an object that is rigidly grasped by N robotic agents, without using force/torque measurements at the grasping points. More specifically, our contribution lies in the following attributes.

- First, we develop a decentralized control scheme that combines the following:
 - a) adaptive control ideas to compensate for external disturbances and uncertainties of the agents' and the object's dynamic parameters and
 - b) quaternion modeling of the object's orientation that avoids undesired representation singularities.
- 2) Second, we propose a decentralized control scheme that does not depend on the dynamic structure or parameters of the overall system and guarantees *predefined* transient and steady-state performance for the object's center of mass, using the prescribed performance control (PPC) scheme [44].
- 3) We carry out extensive simulation studies and experimental results that verify the theoretical findings.

Moreover, both control schemes employ the load distribution proposed in [40] that provably avoids undesired internal forces.

The first control scheme is an extension of our preliminary work [45], where we designed a similar adaptive quaternion-based controller, guaranteeing, however, only *local* stability, and no experimental validation was provided. Furthermore, we have employed the PPC scheme in our previous work [46] to design timed transition systems for a cooperatively manipulated object. In this paper, however, we perform a more extended and detailed analysis by deriving specific bounds for the inputs of the robotic arms (i.e., joint velocities and torques), as well as real-time experiments. It is worth noting that PPC has also been used for single manipulation tasks in [47]–[49].

The rest of this paper is organized as follows. Section II provides the notation used throughout this paper and necessary background. The modeling of the system as well as the problem formulation are given in Section III. Section IV presents the details of the two proposed control schemes with the corresponding stability analysis, and Section V illustrates the simulation and experimental results. Finally, Section VI concludes this paper.

II. NOTATION AND PRELIMINARIES

A. Notation

The set of positive integers is denoted by $\ensuremath{\mathbb{N}}$ and the real *n*-coordinate space, with $n \in \mathbb{N}$, by \mathbb{R}^n ; $\mathbb{R}^n_{>0}$ and $\mathbb{R}^n_{>0}$ are the sets of real n-vectors with all elements nonnegative and positive, respectively. The $n \times n$ identity matrix is denoted by I_n , the *n*-dimensional zero vector by 0_n and the $n \times m$ matrix with zero entries by $0_{n \times m}$. Given a matrix $A \in$ $\mathbb{R}^{n \times m}$, we use $||A|| := (\lambda_{\max}(A^{\top}A))^{1/2}$, where $\lambda_{\max}(\cdot)$ is the maximum eigenvalue of a matrix. The vector connecting the origins of coordinate frames $\{A\}$ and $\{B\}$ expressed in frame $\{C\}$ coordinates in 3-D space is denoted as $p_{B/A}^C \in \mathbb{R}^3$. Given $a \in \mathbb{R}^3$, S(a) is the skew-symmetric matrix defined according to $S(a)b = a \times b$. The rotation matrix from $\{A\}$ to $\{B\}$ is denoted as $R_{B/A} \in SO(3)$, where SO(3) is the 3-D rotation group. The angular velocity of frame $\{B\}$ with respect to $\{A\}$ is denoted as $\omega_{B/A} \in \mathbb{R}^3$ and it holds that [43] $\dot{R}_{B/A} = S(\omega_{B/A})R_{B/A}$. We further denote as $\eta_{A/B} \in \mathbb{T}$ the Euler angles representing the orientation of $\{B\}$ with respect to $\{A\}$, with $\mathbb{T} := (-\pi, \pi) \times (-(\pi/2), (\pi/2)) \times (-\pi, \pi)$. We also define the set $\mathbb{M} := \mathbb{R}^3 \times \mathbb{T}$. In addition, S^n denotes the (n+1)-dimensional sphere. For notational brevity, when a coordinate frame corresponds to an inertial frame of reference $\{I\}$, we will omit its explicit notation (e.g., $p_B = p_{B/I}^I, \omega_B = \omega_{B/I}^I, R_B = R_{B/I}$, etc.). Finally, all vector and matrix differentiations are expressed with respect to an inertial frame $\{I\}$, unless otherwise stated.

B. Unit Quaternions

Given two frames $\{A\}$ and $\{B\}$, we define a unit quaternion $\zeta_{B/A} := [\varphi_{B/A}, \epsilon_{B/A}^{\top}]^{\top} \in S^3$ describing the orientation of $\{B\}$ with respect to $\{A\}$, with $\varphi_{B/A} \in \mathbb{R}$, $\varphi_{B/A}^2 + \epsilon_{B/A}^{\top} \epsilon_{B/A} = 1$. The relationship between $\zeta_{B/A}$ and the corresponding rotation

matrix $R_{B/A}$ as well as the axis/angle representation can be found in [43]. For a given quaternion $\zeta_{B/A} = [\varphi_{B/A}, \epsilon_{B/A}^{\top}]^{\top} \in S^3$, its conjugate, which $\{A\}$ with respect to $\{B\}$, is [43] $\zeta_{B/A}^+ := [\varphi_{B/A}, -\epsilon_{B/A}^{\top}]^{\top} \in S^3$. Moreover, given two quaternions $\zeta_i := \zeta_{B_i/A_i} = [\varphi_{B_i/A_i}, \epsilon_{B_i/A_i}^{\top}]^{\top}, \forall i \in \{1, 2\}$, the quaternion product is defined as [43]

$$\zeta_1 \otimes \zeta_2 := \begin{bmatrix} \varphi_1 \varphi_2 - \epsilon_1^\top \epsilon_2 \\ \varphi_1 \epsilon_2 + \varphi_2 \epsilon_1 + S(\epsilon_1) \epsilon_2 \end{bmatrix} \in S^3$$
 (1)

where $\varphi_i := \varphi_{B_i/A_i}$ and $\epsilon_i := \epsilon_{B_i/A_i}$, $\forall i \in \{1, 2\}$.

For a moving frame $\{B\}$ (with respect to $\{A\}$), the time derivative of the quaternion $\zeta_{B/A} = [\varphi_{B/A}, \epsilon_{B/A}^{\top}]^{\top} \in S^3$ is given by [43]

$$\dot{\zeta}_{B/A} = \frac{1}{2} E(\zeta_{B/A}) \omega_{B/A}^{A}$$
 (2a)

where $E: S^3 \to \mathbb{R}^{4\times 3}$ is defined as

$$E(\zeta) := \begin{bmatrix} -\epsilon^\top \\ \varphi I_3 - S(\epsilon) \end{bmatrix} \quad \forall \zeta = [\varphi, \epsilon^\top]^\top \in S^3.$$

Finally, it can be shown that $E(\zeta)^{\top}E(\zeta) = I_3, \forall \zeta \in S^3$, and hence, (2a) implies

$$\omega_{B/A}^A = 2E(\zeta_{B/A})^\top \dot{\zeta}_{B/A}. \tag{2b}$$

C. Prescribed Performance

PPC, recently proposed in [44], describes the behavior where a tracking error $e: \mathbb{R}_{\geq 0} \to \mathbb{R}$ evolves strictly within a predefined region that is bounded by certain functions of time, achieving prescribed transient and steady state performance. The mathematical expression of prescribed performance is given by the inequalities $-\rho_L(t) < e(t) < \rho_U(t), \forall t \in$ $\mathbb{R}_{\geq 0}$, where $\rho_L(t)$ and $\rho_U(t)$ are the smooth and bounded decaying functions of time satisfying $\lim_{t\to\infty} \rho_L(t) > 0$ and $\lim_{t\to\infty} \rho_U(t) > 0$, called performance functions. Specifically, for the exponential performance functions $\rho_i(t) :=$ $(\rho_{i,0}-\rho_{i,\infty})\exp(-l_it)+\rho_{i,\infty}$, with $\rho_{i,0},\rho_{i,\infty},\ l_i\in\mathbb{R}_{>0}$, $i \in \{U, L\}$, appropriately chosen constants, the terms $\rho_{L,0} :=$ $\rho_L(0), \rho_{U,0} := \rho_U(0)$ are selected such that $\rho_{U,0} > e(0) > \rho_{L,0}$ and the terms $\rho_{L,\infty} := \lim_{t \to \infty} \rho_L(t), \, \rho_{U,\infty} := \lim_{t \to \infty} \rho_U(t)$ represent the maximum allowable size of the tracking error e(t) at steady state, which may be set arbitrarily small to a value reflecting the resolution of the measurement device, thus achieving practical convergence of e(t) to zero. Moreover, the decreasing rate of $\rho_L(t)$, $\rho_U(t)$, which is affected by the constants l_L , l_U in this case, introduces a lower bound on the required speed of convergence of e(t). Therefore, the appropriate selection of the performance functions $\rho_L(t)$, $\rho_U(t)$ imposes performance characteristics on the tracking error e(t).

D. Dynamical Systems

Consider the initial value problem

$$\dot{\sigma} = H(\sigma, t), \quad \sigma(0) \in \Omega$$
 (3)

with $H: \Omega \times \mathbb{R}_{\geq 0} \to \mathbb{R}^n$ where $\Omega \subset \mathbb{R}^n$ is a nonempty open set.

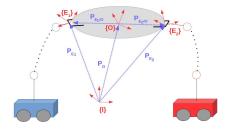


Fig. 1. Two robotic agents rigidly grasping an object.

Definition 1 [50]: A solution $\sigma(t)$ of the initial value problem (3) is maximal if it has no proper right extension that is also a solution of (3).

Theorem 1 [50]: Consider problem (3). Assume that $H(\sigma, t)$ is: 1) locally Lipschitz on σ for almost all $t \in \mathbb{R}_{\geq 0}$; 2) piecewise continuous on t for each fixed $\sigma \in \Omega$; and 3) locally integrable on t for each fixed $\sigma \in \Omega$. Then, there exists a maximal solution $\sigma(t)$ of (3) on $[0, t_{\text{max}})$ with $t_{\text{max}} > 0$ such that $\sigma(t) \in \Omega$, $\forall t \in [0, t_{\text{max}})$.

Proposition 1 [50]: Assume that the hypotheses of Theorem 1 hold. For a maximal solution $\sigma(t)$ on the time interval $[0, t_{\text{max}})$ with $t_{\text{max}} < \infty$ and for any compact set $\Omega' \subset \Omega$ there exists a time instant $t' \in [0, t_{\text{max}})$ such that $\sigma(t') \notin \Omega'$.

III. PROBLEM FORMULATION

Consider N fully actuated robotic agents (e.g., robotic arms mounted on omnidirectional mobile bases) rigidly grasping an object (see Fig. 1). We denote by $\{E_i\}$, $\{O\}$ the endeffector and object's center of mass frames, respectively; $\{I\}$ corresponds to an inertial frame of reference, as mentioned in Section II-A. The rigidity assumption implies that the agents can exert both forces and torques along all directions to the object. In the following, we present the modeling of the coupled kinematics and dynamics of the object and the agents, which follows closely the one in [6] and [4].

A. Robotic Agents

We denote by $q_i, \dot{q}_i \in \mathbb{R}^{n_i}$, with $n_i \in \mathbb{N}, \forall i \in \mathcal{N}$, the generalized joint-space variables and their time derivatives of agent i, with $q_i := [q_{i_1}, \dots, q_{i_{n_i}}]$. Here, q_i consists of the degrees of freedom of the robotic arm as well as the moving base. The overall joint configuration is then $q:=[q_1^\top,\ldots,q_N^\top]^\top,\dot{q}:=$ $[\dot{q}_1^\top, \dots, \dot{q}_N^\top]^\top \in \mathbb{R}^n$, with $n := \sum_{i \in \mathcal{N}} n_i$. In addition, the inertial position and Euler-angle orientation of the ith endeffector, denoted by p_{E_i} and η_{E_i} , respectively, can be derived b3y the forward kinematics and are smooth functions of q_i , i.e., $p_{E_i}: \mathbb{R}^{n_i} \to \mathbb{R}^3$, $\eta_{E_i}: \mathbb{R}^{n_i} \to \mathbb{T}$. The generalized velocity of each agent's end-effector $v_i := [\dot{p}_{E_i}^\top, \omega_{E_i}^\top]^\top \in \mathbb{R}^6$ can be computed through the differential kinematics v_i = $J_i(q_i)\dot{q}_i$ [43], where $J_i:\mathbb{R}^{n_i}\to\mathbb{R}^{6\times n_i}$ is a smooth function representing the geometric Jacobian matrix, $\forall i \in \mathcal{N}$ [43]. We define also the set $\mathbb{S}_i := \{q_i \in \mathbb{R}^{n_i} : \det(J_i(q_i)J_i(q_i)^\top) > 0\}$ which contains all the singularity-free configurations. The differential equation describing the dynamics of each agent

in task-space coordinates is [43]

$$M_i(q_i)\dot{v}_i + C_i(q_i, \dot{q}_i)v_i + g_i(q_i) + d_i(q_i, \dot{q}_i, t) = u_i - f_i$$
(4)

where $M_i: \mathbb{S}_i \to \mathbb{R}^{n_i \times n_i}$ is the positive definite inertia matrix, $C_i: \mathbb{S}_i \times \mathbb{R}^{n_i} \to \mathbb{R}^{n_i \times n_i}$ is the Coriolis matrix, $g_i: \mathbb{S}_i \to \mathbb{R}^{n_i}$ is the gravity term, $d_i: \mathbb{S}_i \times \mathbb{R}^{n_i} \times \mathbb{R}_{\geq 0} \to \mathbb{R}^{n_i}$ is a vector representing unmodeled friction, uncertainties and external disturbances, $f_i \in \mathbb{R}^6$ is the vector of generalized forces that agent i exerts on the grasping point with the object, and $u_i \in \mathbb{R}^6$ is the task space wrench, that acts as the control input; u_i is related to the input torques, denoted by τ_i , via $\tau_i = J_i^\top(q_i)u_i + (I_{n_i} - J_i^\top(q_i)[J_i^+(q_i)]^\top)\tau_{i0}$, where J_i^+ is a generalized inverse of J_i [43]. Moreover, τ_{i0} concerns redundant agents $(n_i > 6)$ and does not contribute to endeffector forces. The agent task-space dynamics (4) can be written in vector form as

$$M(q)\dot{v} + C(q,\dot{q})v + g(q) + d(q,\dot{q},t) = u - f$$
 (5)

where $v := [v_1^\top, \dots, v_N^\top] \in \mathbb{R}^{6N}, M := \text{diag}\{[M_i]_{i \in \mathcal{N}}\} \in \mathbb{R}^{6N \times 6N}, C := \text{diag}\{[C_i]_{i \in \mathcal{N}}\} \in \mathbb{R}^{6N \times 6N}, f := [f_1^\top, \dots, f_N^\top]^\top, u := [u_1^\top, \dots, u_N^\top]^\top, g := [g_1^\top, \dots, g_N^\top]^\top,$ and $d := [d_1^\top, \dots, d_N^\top]^\top \in \mathbb{R}^{6N}.$

B. Object

Regarding the object, we denote by $x_O := [p_O^\top, \eta_O^\top]^\top \in \mathbb{M}$, $v_O := [\dot{p}_O^\top, \omega_O^\top]^\top \in \mathbb{R}^{12}$ the pose and generalized velocity of its center of mass, with $\eta_O := [\phi_O, \theta_O, \psi_O]^\top$. We consider the following second-order dynamics, which can be derived based on the Newton–Euler formulation:

$$\dot{x}_O = J_O(\eta_O)v_O \tag{6a}$$

$$M_O(x_O)\dot{v}_O + C_O(x_O, \dot{x}_O)v_O + g_O(x_O) + d_O(x_O, \dot{x}_O, t) = f_O$$
(6b)

where $M_O: \mathbb{M} \to \mathbb{R}^{6 \times 6}$ is the positive definite inertia matrix, $C_O: \mathbb{M} \times \mathbb{R}^6 \to \mathbb{R}^{6 \times 6}$ is the Coriolis matrix, $g_O: \mathbb{M} \to \mathbb{R}^6$ is the gravity vector, $d_O: \mathbb{M} \times \mathbb{R}^6 \times \mathbb{R}_{\geq 0} \to \mathbb{R}^6$ a vector representing modeling uncertainties and external disturbances, and $f_O \in \mathbb{R}^6$ is the vector of generalized forces acting on the object's center of mass. Moreover, $J_O: \mathbb{T} \to \mathbb{R}^{6 \times 6}$ is the well-known object representation Jacobian and is not well-defined when $\theta_O = \pm (\pi/2)$, which is referred to as representation singularity. A way to avoid the aforementioned singularity is to transform the Euler angles to a unit quaternion for the orientation. Hence, η_O can be transformed to the unit quaternion $\zeta_O = [\varphi_O, \epsilon_O^{\top}]^{\top} \in S^3$ [43], for which, following Section II-B and (2), one obtains $\dot{\zeta}_O = (1/2)E(\zeta_O)\omega_O$ and $\omega_O = 2[E(\zeta_O)]^{\top} \dot{\zeta}_O$, Moreover, it can be proved that

$$||J_O(\eta_O)|| = \sqrt{\frac{|\sin(\theta_O)| + 1}{1 - \sin^2(\theta_O)}}$$
 (7a)

$$||J_O(\eta_O)^{-1}|| = \sqrt{1 + \sin(\theta_O)} \le \sqrt{2}$$
 (7b)

where $J_O(\cdot)^{-1}$ is the matrix inverse, which constitutes a singularity-free representation.

C. Coupled Dynamics

In view of Fig. 1, one concludes that the pose of the agents and the object's center of mass are related as

$$p_{E_i}(q_i) = p_O + p_{E_i/O}(q_i) = p_O + R_{E_i}(q_i)p_{E_i/O}^{E_i}$$
 (8a)

$$\eta_{E_i}(q_i) = \eta_O + \eta_{E_i/O}$$
(8b)

 $\forall i \in \mathcal{N}$, where $p_{E_i/O}^{E_i}$ and $\eta_{E_i/O}$ are the *constant* distance and orientation offset vectors between $\{O\}$ and $\{E_i\}$. Following (8), along with the fact that, due to the grasping rigidity, it holds that $\omega_{E_i} = \omega_O, \forall i \in \mathcal{N}$, one obtains

$$v_i = J_{O_i}(q_i)v_O (9)$$

where $J_{O_i}: \mathbb{R}^{n_i} \to \mathbb{R}^{6 \times 6}$ is the object-to-agent Jacobian matrix [45] for which it can be further proved that

$$||J_{O_i}(x)|| \le ||p_{O/E_i}^{E_i}|| + 1 \quad \forall x \in \mathbb{R}^{n_i}, \ i \in \mathcal{N}.$$
 (10)

The kinetostatics duality along with the grasp rigidity suggest that the force f_O acting on the object's center of mass and the generalized forces $f_i, i \in \mathcal{N}$, exerted by the agents at the grasping points, are related through $f_O = [G(q)]^\top f$, where $G : \mathbb{R}^n \to \mathbb{R}^{6N \times 6}$, with $G(q) := [[J_{O_1}(q_1)]^\top, \ldots, [J_{O_N}(q_N)]^\top]^\top$, is the full column-rank grasp matrix. By using the latter along with (5), (6), and (9) and its derivative, we obtain the overall system-coupled dynamics:

$$\widetilde{M}(x)\dot{v}_{o} + \widetilde{C}(x)v_{o} + \widetilde{g}(x) + \widetilde{d}(x,t) = [G(q)]^{\mathsf{T}}u \quad (11)$$

where $\widetilde{M} := M_O + G^\top M G$, $\widetilde{C} := C_O + G^\top C G + G^\top M \dot{G}$, $\widetilde{g} := g_O + [G(q)]^\top g(q)$, $\widetilde{d} := d_O + G^\top d$, x is the overall state $x := [q^\top, \dot{q}^\top, x_O^\top, \dot{x}_O^\top]^\top \in \mathbb{S} \times \mathbb{R}^{n+6} \times \mathbb{M}$, $\mathbb{S} := \mathbb{S}_1 \times \cdots \times \mathbb{S}_N$, and we have omitted the arguments for notational brevity. Moreover, the following Lemma, whose proof can be found in [45], is necessary for the following analysis.

Lemma 1: The matrix $\widetilde{M}(x)$ is symmetric and positive definite and the matrix $\widetilde{M}(x) - 2\widetilde{C}(x)$ is skew symmetric.

The positive definiteness of $\widetilde{M}(x)$ implies $\underline{m}I_6 \leq \widetilde{M}(x) \leq \overline{m}I_6$, $\forall x \in \mathbb{S} \times \mathbb{R}^{n+6} \times \mathbb{M}$, where \underline{m} and \overline{m} are the positive unknown constants.

We are now ready to state the problem treated in this paper. *Problem 1:* Given a desired bounded object smooth pose trajectory specified by $x_d(t) := [p_d(t)^\top, \eta_d(t)^\top]^\top$, $p_d(t) \in \mathbb{R}^3$, $\eta_d(t) := [\varphi_d(t), \theta_d(t), \psi_d(t)] \in \mathbb{T}$, with bounded first and second derivatives, and $\theta_d(t) \in [-\bar{\theta}, \bar{\theta}] \subset (-(\pi/2), (\pi/2)), \forall t \in \mathbb{R}_{\geq 0}$, as well as $v_0(0) = 0_6$, determine a decentralized control law u in (11) such that one of the following holds:

- 1) $\lim_{t\to\infty} [[p_o(t) p_d(t)]^\top, [\eta_o(t) \eta_d(t)]^\top]^\top = 0_3$
- 2) $\|[[p_O(t) p_d(t)]^\top, [\eta_O(t) \eta_d(t)]^\top]\| \le \lambda \exp(-lt) + \rho \quad \forall t \in \mathbb{R}_{>0}$, for positive λ, l, ρ .

Part 1 in the aforementioned problem statement corresponds to the asymptotic stability that will be guaranteed by the control scheme of Section IV-A, and part 2 is associated with the predefined transient and steady-state performance that will be guaranteed in Section IV-B. The requirement

 $\theta_d(t) \in [-\bar{\theta}, \bar{\theta}] \subset (-(\pi/2), (\pi/2)), \forall t \in \mathbb{R}_{\geq 0}$ is a necessary condition needed to ensure that tracking of θ_d will not result in singular configurations of $J_O(\eta_O)$, which is needed for the control protocol of Section IV-B. The constant $\bar{\theta} \in [0, (\pi/2))$ can be taken arbitrarily close to $(\pi/2)$.

To solve the aforementioned problem, we need the following assumptions regarding the agent feedback, the bounds of the uncertainties/disturbances, and the kinematic singularities.

Assumption 1 (Feedback): Each agent $i \in \mathcal{N}$ has continuous feedback of its own state q_i, \dot{q}_i .

Assumption 2 (Object Geometry): Each agent $i \in \mathcal{N}$ knows the constant offsets $p_{E_i/O}^{E_i}$ and $\eta_{E_i/O}$, $\forall i \in \mathcal{N}$.

Assumption 3 (Kinematic Singularities): The agents operate away from kinematic singularities, i.e., $q_i(t)$ evolves in a closed subset of \mathbb{S}_i , $\forall i \in \mathcal{N}$.

Assumption 1 is realistic for real manipulation systems, since on-board sensor can provide accurately the measurements q_i, \dot{q}_i . The object geometric characteristics in Assumption 2 can be obtained by on-board sensors, whose inaccuracies are not modeled in this paper. Finally, Assumption 3 states that the q_i that achieve $x_O(t) = x_d(t), \forall t \in \mathbb{R}_{\geq 0}$ are sufficiently far from singular configurations. Since each agent has feedback from its state q_i, \dot{q}_i , it can compute through the forward and differential kinematics the end-effector pose $p_{E_i}(q_i), \eta_{E_i}(q_i)$ and the velocity $v_i, \forall i \in \mathcal{N}$. Moreover, since it knows $p_{E_i/O}^{E_i}$ and $\eta_{E_i/O}$, it can compute $J_{O_i}(q_i)$ and x_O, v_O by inverting (8) and (9), respectively. Consequently, each agent can then compute the quaternion signals ζ_O and $\dot{\zeta}_O$.

Note that, due to Assumption 2 and the grasp rigidity, the object-agents configuration is similar to a single closed-chain robot. The considered multiagent setup, however, renders the problem more challenging, since the agents must calculate their own control signal in a decentralized manner, without communicating with each other. Moreover, each agent needs to compensate its own part of the (possibly uncertain/unknown) dynamics of the coupled dynamic equation (11), while respecting the rigidity kinematic constraints. Regarding Assumption 2, our future directions include its relaxation to uncertain/unknown object offsets for some agents, which would then not have exact feedback of the object's pose. In that case, the team would need to cooperate in a leader–follower fashion for the compensation/estimation of the state by these agents.

IV. MAIN RESULTS

In this section, we present two control schemes for the solution of Problem 1. The proposed controllers are decentralized, in the sense, that the agents calculate their control signal on their own, without communicating with each other, as well as robust, since they do not take into account the dynamic properties of the agents or the object (mass/inertia moments) or the uncertainties/external disturbances modeled by the function $\widetilde{d}(x,t)$ in (11). The first control scheme is presented in Section IV-A and is based on quaternion feedback and adaptation laws, while the second control scheme is given

in Section IV-B and is inspired by the PPC methodology introduced in [44].

A. Adaptive Control with Quaternion Feedback

The proposed controller of this section is based on the techniques of adaptive control, whose aim is the design of control systems that are robust to constant or slowly varying unknown parameters. For more details, we refer the reviewer to the related literature (e.g., [51] and the references therein).

First, we need the following assumption regarding the model uncertainties/external disturbances.

Assumption 4 (Uncertainties/Disturbance Parameterization): There exist constant unknown vectors $\bar{d}_O \in \mathbb{R}^{\mu_O}, \bar{d}_i \in \mathbb{R}^{\mu}$ and known functions δ_O : $\mathbb{M} \times \mathbb{R}^6 \times \mathbb{R}_{\geq 0} \to \mathbb{R}^{6 \times \mu_O}, \delta_i : \mathbb{R}^{2n_i} \times \mathbb{R}_{\geq 0} \to \mathbb{R}^{6 \times \mu}$, such that $d_O(x_O, \dot{x}_O, t) = \delta_O(x_O, \dot{x}_O, t) \bar{d}_O, d_i(q_i, \dot{q}_i, t) = \delta_i(q_i, \dot{q}_i, t) \bar{d}_i, \forall q_i, \dot{q}_i \in \mathbb{R}^{n_i}, x_O \in \mathbb{M}, \dot{x}_O \in \mathbb{R}^6, t \in \mathbb{R}_{\geq 0}, i \in \mathcal{N}, \text{ where } \delta_O(x_O, \dot{x}_O, t) \text{ and } \delta_i(q_i, \dot{q}_i, t) \text{ are the continuous in } (x_O, \dot{x}_O) \text{ and } (q_i, \dot{q}_i), \text{ respectively, and bounded in } t.$

The aforementioned assumption is motivated by the use of neural networks for approximating unknown functions in compact sets [51]. More specifically, any continuous function $f(x): \mathbb{R}^n \to \mathbb{R}^m$ can be approximated on a known compact set $X \subset \mathbb{R}^n$ by a neural network equipped with N radial basis functions $\Phi(x)$ and using unknown ideal constant connection weights that are stored in a matrix $\Theta \in \mathbb{R}^{N \times m}$ as $f(x) = \Theta^{\top} \Phi(x) + \varepsilon(x)$; $\Theta^{\top} \Phi(x)$ represents the parametric uncertainty and $\varepsilon(x)$ represents the unknown nonparametric uncertainty, which is bounded as $\|\varepsilon(x)\| < \bar{\varepsilon}$ in X. In our case, the functions δ_O , δ_i play the role of the known function $\Phi(x)$ and \bar{d}_O , \bar{d}_i , and μ , μ_O represent the unknown constants Θ and the number of layers of the neural network, respectively. Nevertheless, in view of neural network approximation, Assumption 4 implies that the nonparametric uncertainty is zero and that d_0 and d_i are known functions of time. These properties can be relaxed with nonzero bounded nonparametric uncertainties and unknown but bounded time-dependent disturbances, i.e., $d_i(q_i, \dot{q}_i, t) = \delta_{i,q}(q_i, \dot{q}_i)\bar{d}_i + d_{i,t}(t) + \varepsilon_{i,q}(q_i, \dot{q}_i)$ and $d_O(x_O, \dot{x}_O, t) = \delta_{O,x}(x_O, \dot{x}_O)d_O + d_{O,t}(t) + \varepsilon_{O,x}(x_O, \dot{x}_O),$ where $d_{i,t}$, $d_{O,t}$, $\varepsilon_{i,q}$, and $\varepsilon_{O,x}$ are bounded. In that case, instead of asymptotic convergence of the pose to the desired one, we can show convergence of the respective errors to a compact set around the origin. For more details on neural network approximation and adaptive control with illustrative examples, we refer the reader to [51, Ch. 12].

The desired Euler angle orientation vector $\eta_d: \mathbb{R}_{\geq 0} \to \mathbb{T}$ is transformed first to the unit quaternion $\zeta_d: \mathbb{R}_{\geq 0} \to S^3$ [43] and we define the position error $e_p:=p_o-p_d$. Since unit quaternions do not form a vector space, they cannot be subtracted to form an orientation error; instead, we should use the properties of the quaternion group algebra. Let $e_{\zeta} = [e_{\varphi}, e_{\epsilon}^{\top}]^{\top} \in S^3$ be the unit quaternion describing the orientation error. Then, it holds that [43]

$$e_{\zeta} = \zeta_d \otimes \zeta_o^+ = \begin{bmatrix} \varphi_d \\ \epsilon_d \end{bmatrix} \otimes \begin{bmatrix} \varphi_o \\ -\epsilon_o \end{bmatrix}$$

which, by using (1), becomes

$$e_{\zeta} = \begin{bmatrix} e_{\varphi} \\ e_{\epsilon} \end{bmatrix} := \begin{bmatrix} \varphi_{O}\varphi_{d} + \epsilon_{O}^{\top}\epsilon_{d} \\ \varphi_{O}\epsilon_{d} - \varphi_{d}\epsilon_{O} + S(\epsilon_{O})\epsilon_{d} \end{bmatrix}. \tag{12}$$

By employing (2) and certain properties of skew-symmetric matrices [52], the dynamics of e_p , e_{φ} can be shown to be

$$\dot{e}_p = \dot{p}_O - \dot{p}_d \tag{13a}$$

$$\dot{e}_{\varphi} = \frac{1}{2} e_{\epsilon}^{\top} e_{\omega} \tag{13b}$$

$$\dot{e}_{\epsilon} = -\frac{1}{2} [e_{\varphi} I_3 + S(e_{\epsilon})] e_{\omega} - S(e_{\epsilon}) \omega_d$$
 (13c)

where $e_{\omega} := \omega_O - \omega_d$ is the angular velocity error, with $\omega_d = 2E(\zeta_d)^{\top}\dot{\zeta}_d$, as indicated by (2b). Due to the ambiguity of unit quaternions, when $\zeta_O = \zeta_d$, then $e_{\zeta} = [1, 0_3^{\top}]^{\top} \in S^3$. If $\zeta_O = -\zeta_d$, then $e_{\zeta} = [-1, 0_3^{\top}]^{\top} \in S^3$, which, however, represents the same orientation. Therefore, the control objective is equivalent to $\lim_{t\to\infty} [e_p(t)^{\top}, |e_{\varphi}(t)|, e_{\varepsilon}(t)^{\top}]^{\top} = [0_3^{\top}, 1, 0_3^{\top}]^{\top}$.

The left-hand side of (4), after employing (9) and its derivative, becomes

$$\begin{aligned} M_{i}(q_{i})\dot{v}_{i} + C_{i}(q_{i}, \dot{q}_{i})v_{i} + g_{i}(q_{i}) + d_{i}(q_{i}, \dot{q}_{i}, t) \\ &= M_{i}(q_{i})(J_{O_{i}}(q_{i})\dot{v}_{O} + \dot{J}_{O_{i}}(q_{i})v_{O}) + C_{i}(q_{i}, \dot{q}_{i})J_{O_{i}}(q_{i})v_{O} \\ &+ g_{i}(q_{i}) + d_{i}(q_{i}, \dot{q}_{i}, t). \end{aligned}$$

which, according to Assumption 4 and the fact that the manipulator dynamics can be linearly parameterized with respect to dynamic parameters [42], becomes

$$\begin{aligned} M_{i}(q_{i})J_{O_{i}}(q_{i})\dot{v}_{O} + & (M_{i}(q_{i})\dot{J}_{O_{i}}(q_{i}) \\ & + C_{i}(q_{i},\dot{q}_{i})J_{O_{i}}(q_{i}))v_{O} + g_{i}(q_{i}) + d_{i}(q_{i},\dot{q}_{i},t) \\ & = Y_{i}(q_{i},\dot{q}_{i},v_{O},\dot{v}_{O})\vartheta_{i} + \delta_{i}(q_{i},\dot{q}_{i},t)\bar{d}_{i} \end{aligned}$$

 $\forall i \in \mathcal{N}$, where $\vartheta_i \in \mathbb{R}^\ell$, $\ell \in \mathbb{N}$, are the vectors of unknown but constant dynamic parameters of the agents, appearing in the terms M_i , C_i , g_i , and $Y_i : \mathbb{S} \times \mathbb{R}^{n_i+12} \to \mathbb{R}^{6 \times \ell}$ are the known regressor matrices, independent of ϑ_i , $i \in \mathcal{N}$. Without loss of generality, we assume here that ℓ is the same for all agents. Similarly, the dynamical terms of the left-hand side of (6b) can be written as

$$M_{O}(x_{O})\dot{v}_{O} + C_{O}(x_{O}, \dot{x}_{O})v_{O} + g_{O}(x_{O}) + d_{O}(x_{O}, \dot{x}_{O}, t)$$

$$= Y_{O}(x_{O}, \dot{x}_{O}, v_{O}, \dot{v}_{O})\vartheta_{O} + \delta_{O}(x_{O}, \dot{x}_{O}, t)\bar{d}_{O}$$

where $\vartheta_O \in \mathbb{R}^{\ell_O}$, $\ell_O \in \mathbb{N}$ are a vector of unknown but constant dynamic parameters of the object, appearing in the terms M_O , C_O , g_O , and $Y_O : \mathbb{M} \times \mathbb{R}^{18} \to \mathbb{R}^{6 \times \ell_O}$ is a known regressor matrix, independent of ϑ_O . It is worth noting that the choice for ℓ and ℓ_O is not unique. In view of the aforementioned expressions, the left-hand side of (11) can be written as

$$\widetilde{M}(x)\dot{v}_{o} + \widetilde{C}(x)v_{o} + \widetilde{g}(x) + \widetilde{d}(x,t)$$

$$= Y_{o}(x_{o}, \dot{x}_{o}, v_{o}, \dot{v}_{o})\vartheta_{o} + \delta_{o}(x_{o}, \dot{x}_{o}, t)\bar{d}_{o} + [G(q)]^{\top}$$

$$\times (\widetilde{Y}(q, \dot{q}, v_{o}, \dot{v}_{o})\vartheta + \widetilde{\delta}(q, \dot{q}, t)\bar{d})$$
(14)

where $\widetilde{Y}(q,\dot{q},v_o,\dot{v}_o) := \operatorname{diag}\{[Y_i(q_i,\dot{q}_i,v_o,\dot{v}_o)]_{i\in\mathcal{N}}\} \in \mathbb{R}^{6N\times Nl}, \ \vartheta := [\vartheta_1^\top,\dots,\vartheta_N^\top]^\top \in \mathbb{R}^{N\ell}, \ \overline{d} := [\overline{d}_1^\top,\dots,\overline{d}_N^\top]^\top \in \mathbb{R}^{N\mu}, \ \operatorname{and} \ \widetilde{\delta}(q,\dot{q},t) := \operatorname{diag}\{[\delta_i(q_i,\dot{q}_i,t)]_{i\in\mathcal{N}}\} \in \mathbb{R}^{6N\times N\mu}.$

Let us now introduce the states $\hat{\vartheta}_O \in \mathbb{R}^{\ell_O}$ and $\hat{\vartheta}_i \in \mathbb{R}^{\ell}$ which represent the estimates of ϑ_O and ϑ_i , respectively, by agent $i \in \mathcal{N}$, and the corresponding stack vector $\hat{\vartheta} := [\hat{\vartheta}_1^\top, \dots, \hat{\vartheta}_N^\top]^\top \in \mathbb{R}^{N\ell}$, for which the associated errors are

$$e_{\vartheta_O} := \vartheta_O - \hat{\vartheta}_O \in \mathbb{R}^{\ell_O} \tag{15a}$$

$$e_{\vartheta} := \left[e_{\vartheta_1}^{\top}, \dots, e_{\vartheta_N}^{\top} \right]^{\top} := \vartheta - \hat{\vartheta} \in \mathbb{R}^{N\ell}.$$
 (15b)

In the same vein, we introduce the states $\hat{d}_O \in \mathbb{R}^{\mu_O}$ and $\hat{d}_i \in \mathbb{R}^{\mu}$ that correspond to the estimates of \bar{d}_O and \bar{d}_i , respectively, by agent $i \in \mathcal{N}$, and the corresponding stack vector $\hat{d} := [\hat{d}_1, \dots, \hat{d}_N]^\top \in \mathbb{R}^{N\mu}$, for which we also formulate the associated errors as

$$e_{d_O} := \bar{d}_O - \hat{d}_O \in \mathbb{R}^{\mu_O} \tag{16a}$$

$$e_d := [e_{d_1}^\top, \dots, e_{d_N}^\top]^\top := \bar{d} - \hat{d} \in \mathbb{R}^{N_\mu}.$$
 (16b)

Next, we design the reference velocity

$$v_f := v_d - K_f e = \begin{bmatrix} \dot{p}_d - k_p e_p \\ \omega_d + k_\zeta e_\epsilon \end{bmatrix}$$
 (17)

where $v_d := [\dot{p}_d^\top, \omega_d^\top]^\top$, $e := [e_p^\top, -e_\epsilon^\top]^\top \in \mathbb{R}^6$, and $K_f := \operatorname{diag}\{k_pI_3, k_\zeta I_3\}$, with k_p, k_ζ positive control gains. We also introduce the respective velocity error e_v as

$$e_{v_f} := v_O - v_f, (18)$$

and design the adaptive control law u_i in (11), for each agent $i \in \mathcal{N}$, as

$$u_{i} = Y_{i}(q_{i}, \dot{q}_{i}, v_{f}, \dot{v}_{f})\hat{\vartheta}_{i} + \delta_{i}(q_{i}, \dot{q}_{i}, t)\hat{d}_{i} + J_{M_{i}}(q)$$

$$\times [-e + Y_{O}(x_{O}, \dot{x}_{O}, v_{f}, \dot{v}_{f})\hat{\vartheta}_{O}$$

$$+ \delta_{O}(x_{O}, \dot{x}_{O}, t)\hat{d}_{O} - K_{v}e_{v_{f}}]$$
(19)

where K_v is a diagonal positive definite gain matrix, and J_{M_i} : $\mathbb{R}^n \to \mathbb{R}^{6 \times 6}$ is the matrix [40]

$$J_{M_i}(q) := \begin{bmatrix} m_i^{\star} [m_O^{\star}]^{-1} I_3 & m_i^{\star} [J_O^{\star}(q)]^{-1} S(p_{O/E_i}(q_i)) \\ 0_{3\times 3} & J_i^{\star} [J_O^{\star}(q)]^{-1} \end{bmatrix} (20)$$

for some positive coefficients $m_i^* \in \mathbb{R}_{>0}$ and positive definite matrices $J_i^* \in \mathbb{R}^{3\times 3}$, $\forall i \in \mathcal{N}$, satisfying

$$\begin{split} m_{O}^{\star} &= \sum_{i \in \mathcal{N}} m_{i}^{\star}, \quad \sum_{i \in \mathcal{N}} p_{O/E_{i}}(q_{i}) m_{i}^{\star} = 0_{3} \\ J_{O}^{\star}(q) &= \sum_{i \in \mathcal{N}} J_{i}^{\star} - \sum_{i \in \mathcal{N}} m_{i}^{\star} [S(p_{O/E_{i}}(q_{i}))]^{2}. \end{split}$$

In addition, we design the following adaptation laws:

$$\dot{\hat{\theta}}_{i} = -\gamma_{i} [Y_{i}(q_{i}, \dot{q}_{i}, v_{f}, \dot{v}_{f})]^{\top} J_{O_{i}}(q_{i}) e_{v_{f}}$$
(21a)

$$\dot{\hat{\theta}}_{O} = -\gamma_{O} [Y_{O}(x_{O}, \dot{x}_{O}, v_{f}, \dot{v}_{f})]^{\mathsf{T}} e_{n_{f}} \tag{21b}$$

$$\hat{d}_i = -\beta_i [\delta_i(q_i, \dot{q}_i, t)]^{\top} J_{O_i}(q_i) e_{v_f}$$
 (21c)

$$\dot{\hat{d}}_O = -\beta_O [\delta_O(x_O, \dot{x}_O, t)]^\top e_{v_f}$$
 (21d)

with arbitrary bounded initial conditions, where β_i , β_O , γ_i , and $\gamma_O \in \mathbb{R}_{>0}$ are the positive gains, $\forall i \in \mathcal{N}$. The control and adaptation laws can be written in vector form

$$u = \widetilde{Y}(q, \dot{q}, v_{o}, \dot{v}_{o})\hat{\vartheta} + \widetilde{\delta}(q, \dot{q}, t)\hat{d} + G_{M}^{+}(q) \times [-e + Y_{o}(x_{o}, \dot{x}_{o}, v_{f}, \dot{v}_{f})\hat{\vartheta}_{o} + \delta_{o}(x_{o}, \dot{x}_{o}, t)\hat{d}_{o} - K_{v}e_{v_{f}}]$$
(22a)

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$$\dot{\hat{\vartheta}} = -\Gamma[\widetilde{Y}(q, \dot{q}, v_f, \dot{v}_f)]^{\top} G(q) e_{v_f}$$
 (22b)

$$\dot{\hat{d}} = -B[\tilde{\delta}(q, \dot{q}, t)]^{\top} G(q) e_{v_f}$$
 (22c)

$$\dot{\hat{\theta}}_o = -\gamma_o [Y_o(x_o, \dot{x}_o, v_f, \dot{v}_f)]^{\mathsf{T}} e_{v_f}$$
 (22d)

$$\dot{\hat{d}}_o = -\beta_o [\delta_o(x_o, \dot{x}_o, t)]^{\top} e_{v_f}$$
 (22e)

where $G_M^+(q) := [J_{M_1}^\top(q), \ldots, J_{M_N}^\top(q)]^\top \in \mathbb{R}^{6N \times 6}$, $B := \operatorname{diag}\{[\beta_i]_{i \in \mathcal{N}}\}$, and $\Gamma := \operatorname{diag}\{[\gamma_i]_{i \in \mathcal{N}}\}$. The matrix $G_M^+(q)$ was introduced in [40], where it was proven that it yields a load distribution that is free of internal forces. The parameters m_O^\star, m_i^\star are used to distribute the object's needed effort [the term that right multiplies $G_M^+(q)$ in (22a)] to the agents.

Remark 1 (Decentralized Manner (Adaptive Controller)): Notice from (19) and (21) that the overall control protocol is decentralized in the sense that the agents calculate their own control signals without communicating with each other. In particular, the control gains and the desired trajectory can be transmitted offline to the agents, which can compute the object's pose and velocity, and hence, the signals e, v_f , and e_{v_f} from the inverse kinematics. For the computation of $J_{M_i}(q)$, each agent needs feedback from all q_i to compute $S(p_{O/E_i}(q_i), \forall i \in \mathcal{N}$. However, by exploiting the rigidity of the grasps, it holds that $p_{O/E_i}(q_i) = R_O(q_i) p_{O/E_i}^O$. Therefore, since all agents can compute R_O , the computation of $J_{M_i}(q)$ reduces to knowledge of the offsets $p_{E_{i}/O}^{O}$, which can also be transmitted offline to the agents. Moreover, by also transmitting offline to the agents the initial conditions $\hat{\theta}_{o}$, \hat{d}_{o} , and via the adaptation laws (22d), (22e), each agent has access to the adaptation signals $\theta_O(t)$, $d_O(t)$, $\forall t \in \mathbb{R}_{>0}$. Finally, the structure of the functions δ_i , δ_o , Y_i , and Y_o , as well as the constants m_i^{\star} , J_i^{\star} can be also known by the agents a priori.

The following theorem summarizes the main results of this section.

Theorem 2: Consider N robotic agents rigidly grasping an object with coupled dynamics described by (11) and unknown dynamic parameters. Then, under Assumptions 1–4, by applying the control protocol (19) with the adaptation laws (21), the object pose converges asymptotically to the desired pose trajectory. Moreover, all closed-loop signals are bounded.

Proof: Consider the nonnegative function

$$V := \frac{1}{2} e_{p}^{\top} e_{p} + 2(1 - e_{\varphi}) + \frac{1}{2} e_{v_{f}}^{\top} \widetilde{M}(x) e_{v_{f}} + \frac{1}{2} e_{\vartheta}^{\top} \Gamma^{-1} e_{\vartheta} + \frac{1}{2\gamma_{o}} e_{\vartheta_{o}}^{\top} e_{\vartheta_{o}} + \frac{1}{2} e_{\vartheta}^{\top} B^{-1} e_{\vartheta} + \frac{1}{2\beta_{o}} e_{d_{o}}^{\top} e_{d_{o}}.$$
(23)

By taking the derivative of V and using (14), (17), (18), and Lemma 1, we obtain

$$\begin{split} \dot{V} &= -e^{\top} K_f e + e^{\top}_{v_f} [[G(q)]^{\top} (u - \widetilde{Y}(q, \dot{q}, v_f, \dot{v}_f) \vartheta \\ &- \widetilde{\delta}(q, \dot{q}, t) \bar{d}) + e - Y_o(x_o, \dot{x}_o, \dot{v}_f, \dot{v}_f) \vartheta_o \\ &- \delta_o(x_o, \dot{x}_o, t) \bar{d}_o - e^{\top}_{\vartheta} \Gamma^{-1} \dot{\hat{\vartheta}} \\ &- \frac{1}{\gamma_o} e^{\top}_{\vartheta o} \dot{\hat{\vartheta}}_o - e^{\top}_d B^{-1} \dot{\hat{d}} - \frac{1}{\beta_o} e^{\top}_{do} \dot{\hat{d}}_o \end{split}$$

and after substituting the adaptive control and adaptation laws (22) and using the fact that $[G(q)]^{\top}G_M^+ = I_6$

$$\dot{V} = -e^{\top} K_{f} e - e^{\top}_{v_{f}} K_{v} e_{v_{f}}
- e^{\top}_{v_{f}} [[G(q)]^{\top} (\widetilde{Y}(q, \dot{q}, v_{f}, \dot{v}_{f}) e_{\vartheta} + \widetilde{\delta}(q, \dot{q}, t) e_{d})
+ Y_{O}(x_{O}, \dot{x}_{O}, v_{f}, \dot{v}_{f}) e_{\vartheta_{O}} + \delta_{O}(x_{O}, \dot{x}_{O}, t) e_{d_{O}}]
+ e^{\top}_{\vartheta} [\widetilde{Y}(q, \dot{q}, v_{f}, \dot{v}_{f})]^{\top} G(q) e_{v_{f}} + e^{\top}_{d} [\widetilde{\delta}(q, \dot{q}, t)]^{\top} e_{v_{f}}
+ e^{\top}_{\vartheta_{O}} [Y_{O}(x_{O}, \dot{x}_{O}, v_{f}, \dot{v}_{f})]^{\top} e_{v_{f}} + e^{\top}_{d_{O}} [\delta_{O}(x_{O}, \dot{x}_{O}, t)]^{\top} e_{v_{f}}
= -k_{p} \|e_{p}\|^{2} - k_{\zeta} \|e_{\epsilon}\|^{2} - e^{\top}_{v_{f}} K_{v} e_{v_{f}}$$
(24)

which is nonpositive. Note, however, that \dot{V} is not negative definite, and we need to invoke invariancelike properties to conclude the asymptotic stability of e_p , e_ϵ , e_{v_f} . Since the closed-loop system is nonautonomous (this can be verified by inspecting (13), the derivative of (18) and (22)), LaSalle's invariance principle is not applicable, and we thus employ Barbalat's lemma [51, Lemma 8.1]. From (24), we conclude the boundedness of V and of χ , which implies the boundedness of the dynamic terms $\widetilde{M}(x)$, $\widetilde{C}(x)$, and $\widetilde{g}(x)$. Moreover, by invoking the boundedness of $p_d(t)$, $v_d(t)$, $\omega_d(t)$, $\dot{v}_d(t)$, and $\dot{\omega}_d(t)$, we conclude the boundedness of $v_f, v_o, v_i, \hat{\vartheta}_o, \hat{\vartheta}$, \vec{d} , and \vec{d}_o . By differentiating (13), we also conclude the boundedness of \dot{v}_f , and therefore, the boundedness of the control and adaptation laws (19) and (21). Thus, we can conclude the boundedness of the second derivative \ddot{V} and by invoking Corollary 8.1 of [51], the uniform continuity of \dot{V} . Therefore, according to Barbalat's lemma, we deduce that $\lim_{t\to\infty} V(t) = 0$ and, consequently, that $\lim_{t\to\infty} e_p(t) = 0_3$, $\lim_{t\to\infty} e_{v_f}(t) = 0_6$, and $\lim_{t\to\infty} \|e_{\epsilon}(t)\|^2 = 0$, which, given that e_{ζ} is a unit quaternion, leads to the configuration $(e_p, e_{v_f}, e_{\varphi}, e_{\epsilon}) = (0_3, 0_6, \pm 1, 0_3).$

Remark 2 (Unwinding): Note that the two configurations where $e_{\varphi}=1$ and $e_{\varphi}=-1$ represent the same orientation. The closed-loop dynamics of e_{φ} , as given in (13b), can be written, in view of (17), as $\dot{e}_{\varphi} = k_{\zeta}(1/2) \|e_{\epsilon}\|^2 + (1/2)[0_3^{\top}, e_{\epsilon}^{\top}]e_{v_f}$. Since the first term is always positive, we conclude that the equilibrium point $(e_p, e_{v_f}, e_{\varphi}, e_{\epsilon}) = (0_3, 0_6, -1, 0_3)$ is unstable. Therefore, there might be trajectories close to the configuration $e_{\varphi} = -1$ that will move away and approach $e_{\varphi} = 1$, i.e., a full rotation will be performed to reach the desired orientation [of course, if the system starts at the equilibrium $(e_p, e_{v_f}, e_{\varphi}, e_{\epsilon}) = (0_3, 0_6, -1, 0_3)$, it will stay there, which also corresponds to the desired orientation behavior]. This is the so-called unwinding phenomenon [53]. Note, however, that the desired equilibrium point $(e_p, e_{v_f}, e_{\varphi}, e_{\epsilon}) =$ $(0_3, 0_6, 1, 0_3)$ is eventually attractive, meaning that for each $\delta_{\varepsilon} > 0$, there exist finite a time instant $T \geq 0$ such that $1 - e_{\varphi}(t) < \delta_{\varepsilon}, \forall t > T \geq 0$. A similar behavior is observed if we stabilize the point $e_{\varphi} = -1$ instead of $e_{\varphi} = 1$, by setting $e := [e_n^{\top}, e_{\epsilon}^{\top}]^{\top}$ in (17) and considering the term $2(1 + e_{\theta})$ instead of $2(1 - e_{\varphi})$ in the function (23).

In order to avoid the unwinding phenomenon, instead of the error $e = [e_p^\top, -e_\epsilon^\top]^\top$, we can choose $e = [e_p^\top, -e_\varphi e_\epsilon^\top]^\top$ (see our preliminary result [45]). Then, by replacing the term $1 - e_\varphi$ with $1 - e_\varphi^2$ in (23) and using (22), we conclude by proceeding with a similar analysis that $(e_p, \|e_\epsilon\|e_\varphi, e_{v_f}) \to (0_3, 0, 0_6)$, which implies that the system is asymptotically driven to

either the configuration $(e_p, e_{v_f}, e_{\varphi}, e_{\epsilon}) = (0_3, 0_6, \pm 1, 0_3),$ which is the desired one, or a configuration $(e_p, e_{v_f}, e_{\varphi}, e_{\epsilon}) =$ $(0_3, 0_6, 0, \widetilde{e}_{\epsilon})$, where $\widetilde{e}_{\epsilon} \in S^2$ is a unit vector. The latter represents a set of invariant undesired equilibrium points. The closed-loop dynamics are $\dot{e}_{\varphi} = (1/2)e_{\varphi}||e_{\epsilon}||^2 +$ $(1/2)[0_3^{\top}, e_{\epsilon}^{\top}]e_{\nu}$, and $||e_{\epsilon}||^2 = -e_{\varphi}^2||e_{\epsilon}||^2 - e_{\varphi}[0_3^{\top}, e_{\epsilon}^{\top}]e_{\nu}$. We can conclude from the term $[0_3^{\dagger}, e_{\epsilon}^{\dagger}]e_{\nu}$ that there exist trajectories that can bring the system close to the undesired equilibrium, rendering thus the point $(e_p, e_{v_f}, e_{\varphi}, e_{\epsilon}) =$ $(0_3, 0_6, \pm 1, 0_3)$ only locally asymptotically stable. It has been proven that $e_{\varphi} = \pm 1$ cannot be globally stabilized with a purely continuous controller [53]. Discontinuous control laws have also been proposed (e.g., [54]), whose combination with adaptation techniques constitutes part of our future research directions. Another possible direction is tracking on SO(3)(see [55], [56]).

Remark 3 (Robustness (Adaptive Controller)): Notice also that the control protocol compensates the uncertain dynamic parameters and external disturbances through the adaptation laws (21), although the errors (15), (16) do not converge to zero, but remain bounded. Finally, the control gains k_p , k_ζ , K_v can be tuned appropriately so that the proposed control inputs do not reach motor saturations in real scenarios.

B. Prescribed Performance Control

In this section, we adopt the concepts and techniques of PPC, recently proposed in [44], in order to achieve predefined transient and steady-state response for the derived error, as well as ensure that $\theta_O(t) \in (-(\pi/2), (\pi/2)), \forall t \in \mathbb{R}_{\geq 0}$. As stated in Section II-C, prescribed performance characterizes the behavior where a signal evolves strictly within a predefined region that is bounded by absolutely decaying functions of time, called performance functions. This signal is represented by the object's pose error

$$e_s := [e_{s_x}, e_{s_y}, e_{s_z}, e_{s_\phi}, e_{s_\theta}, e_{s_\psi}]^\top := x_O - x_d.$$
 (25)

First, we relax Assumption 4.

Assumption 5 (Uncertainties/Disturbance Bound): The functions $d_O(x_O, \dot{x}_O, t)$ and $d_O(q_i, \dot{q}_i, t)$ are continuous in (x_O, \dot{x}_O) and (q_i, \dot{q}_i) , respectively, and bounded in t by unknown positive constants \bar{d}_O and \bar{d}_i , respectively, $\forall i \in \mathcal{N}$. The mathematical expressions of prescribed performance are given by the following inequalities:

$$-\rho_{s_k}(t) < e_{s_k}(t) < \rho_{s_k}(t) \quad \forall k \in \mathcal{K}$$
 (26)

where $\mathcal{K} := \{x, y, z, \phi, \theta, \psi\}$ and $\rho_k : \mathbb{R}_{\geq 0} \to \mathbb{R}_{> 0}$, with

$$\rho_{Sk}(t) := (\rho_{Sk,0} - \rho_{Sk,\infty}) \exp(-l_{Sk}t) + \rho_{Sk,\infty} \quad \forall k \in \mathcal{K} \quad (27)$$

are designer-specified, smooth, bounded, and decreasing positive functions of time with l_{s_k} , $\rho_{s_k,\infty}$, $k \in \mathcal{K}$, positive parameters incorporating the desired transient and steady-state performance, respectively. The terms $\rho_{s_k,\infty}$ can be set arbitrarily small, achieving thus practical convergence of the errors to zero. Next, we propose a state feedback control protocol that does not incorporate any information on the agents' or the object's dynamics or the external disturbances

and guarantees (26) for all $t \in \mathbb{R}_{\geq 0}$. Given the errors (25) as follows.

Step I-a: Select the functions ρ_{s_k} as in (27) with

- 1) $\rho_{s_{\theta},0} = \rho_{s_{\theta}}(0) = \theta^*, \rho_{s_{k},0} = \rho_{s_{k}}(0) > |e_{s_{k}}(0)|, \forall k \in \mathcal{K} \setminus \{\theta\}$
- 2) $l_{s_k} \in \mathbb{R}_{>0}, \forall k \in \mathcal{K}$
- 3) $\rho_{s_k,\infty} \in (0, \rho_{s_k,0}), \forall k \in \mathcal{K}$

where θ^* is a positive constant satisfying $\theta^* + \bar{\theta} < (\pi/2)$ and $\bar{\theta}$ is the desired trajectory bound (see statement of Problem 1). *Step I-b:* Introduce the normalized errors

$$\xi_s := [\xi_{s_r}, \dots, \xi_{s_m}]^\top := \rho_s^{-1} e_s$$
 (28)

where $\rho_s := \text{diag}\{[\rho_{s_k}]_{k \in \mathcal{K}}\} \in \mathbb{R}^{6 \times 6}$, as well as the transformed state functions ε_s , and signals $r_s : (-1, 1)^6 \to \mathbb{R}^{6 \times 6}$, with

$$\varepsilon_{s} := \left[\varepsilon_{s_{x}}, \dots, \varepsilon_{s_{\psi}}\right]^{\top}
:= \left[\ln\left(\frac{1+\zeta_{s_{x}}}{1-\zeta_{s_{x}}}\right), \dots, \ln\left(\frac{1+\zeta_{s_{\psi}}}{1-\zeta_{s_{\psi}}}\right)\right]^{\top}
r_{s}(\zeta_{s}) := \operatorname{diag}\left\{\left[r_{s_{k}}(\zeta_{s_{k}})\right]_{k \in \mathcal{K}}\right\} := \operatorname{diag}\left\{\left[\frac{\partial \varepsilon_{v_{k}}}{\partial \zeta_{s_{k}}}\right]_{k \in \mathcal{K}}\right\}
= \operatorname{diag}\left\{\left[\frac{2}{1-\zeta_{s_{k}}^{2}}\right]_{k \in \mathcal{K}}\right\}$$
(30)

and design the reference velocity vector

$$v_r := -g_s J_o (\eta_d + \rho_{s_n} \xi_{s_n})^{-1} \rho_s^{-1} r_s(\xi_s) \varepsilon_s \tag{31}$$

where $\rho_{s_{\eta}} := \operatorname{diag}\{\rho_{s_{\phi}}, \rho_{s_{\theta}}, \rho_{s_{\psi}}\}, \, \xi_{s_{\eta}} := [\xi_{s_{\phi}}, \xi_{s_{\eta}}, \xi_{s_{\phi}}]^{\top}$, and we have further used the relation $\xi_s = \rho_s^{-1}(x_O - x_d)$ from (25) and (28).

Step II-a: Define the velocity error vector

$$e_v := [e_{v_x}, \dots, e_{v_{\psi}}]^{\top} := v_O - v_r$$
 (32)

and select the corresponding positive performance functions $\rho_{v_k}: \mathbb{R}_{\geq 0} \to \mathbb{R}_{>0}$ with $\rho_{v_k}(t) := (\rho_{v_k,0} - \rho_{v_k,\infty}) \exp(-l_{v_k}t) + \rho_{v_k,\infty}$, such that $\rho_{v_k,0} = \|e_v(0)\| + \alpha, l_{v_k} > 0$ and $\rho_{v_k,\infty} \in (0, \rho_{v_k,0}), \forall k \in \mathcal{K}$, where α is an arbitrary positive constant.

Step II-b: Define the normalized velocity error

$$\xi_v := [\xi_{v_x}, \dots, \xi_{v_w}]^\top := \rho_v^{-1} e_v$$
 (33)

where $\rho_v := \text{diag}\{[\rho_{v_k}]_{k \in \mathcal{K}}\}$, as well as the transformed states ε_v and signals $r_v : (-1, 1)^6 \to \mathbb{R}^{6 \times 6}$, with

$$\varepsilon_{v} := \left[\varepsilon_{v_{x}}, \dots, \varepsilon_{v_{\psi}}\right]^{\top}
:= \left[\ln\left(\frac{1+\zeta_{v_{x}}}{1-\zeta_{v_{x}}}\right), \dots, \ln\left(\frac{1+\zeta_{v_{\psi}}}{1-\zeta_{v_{\psi}}}\right)\right]^{\top}
r_{v}(\zeta_{v}) := \operatorname{diag}\left\{\left[r_{v_{k}}(\zeta_{v_{k}})\right]_{k \in \mathcal{K}}\right\} := \operatorname{diag}\left\{\left[\frac{\partial \varepsilon_{v_{k}}}{\partial \zeta_{v_{k}}}\right]_{k \in \mathcal{K}}\right\}
= \operatorname{diag}\left\{\left[\frac{2}{1-\zeta_{v_{k}}^{2}}\right]_{k \in \mathcal{K}}\right\}$$
(34)

and design the decentralized feedback control protocol for each agent $i \in \mathcal{N}$ as

$$u_i := -g_p J_M(q) \rho_p^{-1} r_p(\xi_p) \varepsilon_p \tag{35}$$

where g_v is a positive constant gain and J_{M_i} as defined in (20). The control laws (35) can be written in vector form $u := [u_1^\top, \dots, u_N^\top]^\top$, with

$$u = -g_v G_M^+(q) \rho_v^{-1} r_v(\xi_v) \varepsilon_v. \tag{36}$$

Remark 4 (Decentralized Manner and Robustness (PPC)): Similar to (22), notice from (35) that each agent $i \in \mathcal{N}$ can calculate its own control signal, without communicating with the rest of the team, rendering thus the overall control scheme decentralized. The terms l_k , $\rho_{k,0}$, $\rho_{k,\infty}$, α , l_{v_k} , and $\rho_{v_k,\infty}, k \in \mathcal{K}$ needed for the calculation of the performance functions can be transmitted offline to the agents. Moreover, the PPC protocol is also robust to uncertainties of model uncertainties and external disturbances. In particular, note that the control laws do not even require the structure of the terms M, C, \tilde{g} , and d, but only the positive definiteness of M, as will be observed in the subsequent proof of Theorem 3. It is worth noting that in the case that one or more agents failed to participate in the task, then the remaining agents would need to appropriately update their control protocols (e.g., update J_{M_i}) to compensate for the failure.

Remark 5 (Internal Forces): Internal force regulation can be also guaranteed by including in the control laws (22a) and (36), a term of the form $(I_{6N} - G_M^+(q)G(q)]^\top)\hat{f}_{\text{int,d}}$, where $\hat{f}_{\text{int,d}} \in \mathbb{R}^{6N}$ represents desired internal forces (e.g., to avoid grasp sliding) that can be transmitted offline to the agents.

The main results of this section are summarized in the following theorem.

Theorem 3: Consider N agents rigidly grasping an object with unknown coupled dynamics (11). Then, under Assumptions 1–3 and 5, the decentralized control protocol (28)–(35) guarantees that $-\rho_{s_k}(t) < e_{s_k}(t) < \rho_{s_k}(t)$, $\forall k \in \mathcal{K}, t \in \mathbb{R}_{\geq 0}$ from all initial conditions satisfying $|\theta(0) - \theta_d(0)| < \theta^*$ [from Step I-a (i)], with all closed-loop signals being bounded.

Proof: The proof consists of two main parts. First, we prove that there exists a maximal solution $(\xi_s(t), \xi_v(t)) \in (-1, 1)^{12}$ for $t \in [0, \tau_{\text{max}})$, where $\tau_{\text{max}} > 0$. Second, we prove that $(\xi_s(t), \xi_v(t))$ is contained in a compact subset of $(-1, 1)^{12}$ and, consequently, that $\tau_{\text{max}} = \infty$.

Part A: Consider the combined state $\sigma := [q, \xi_s, \xi_v] \in \mathbb{S} \times \mathbb{R}^{12}$. Differentiation of σ yields, in view of (9), (28), and (33)

$$\dot{\sigma} = \begin{bmatrix} \tilde{J}(q)G(q)v_{o} \\ \rho_{s}^{-1}(\dot{x}_{o} - \dot{x}_{d} - \dot{\rho}_{s}\xi_{s}) \\ \rho_{v}^{-1}(\dot{v}_{o} - \dot{v}_{r} - \dot{\rho}_{v}\xi_{v}), \end{bmatrix}$$
(37)

where $\widetilde{J}(q) := \operatorname{diag}\{[J_i(q_i)^\top(J_i(q_i)J_i(q_i)^\top)^{-1}]_{i\in\mathcal{N}}\} \in \mathbb{R}^{6N\times n}$ is well-defined due to Assumption 3. Then, by employing (6), (25), (28), and (31)–(36) as well as $[G(q)]^\top G_M^+ = I_6$, we can express the right-hand side of (37) as a function of σ and t, i.e., $\dot{\sigma} = f_{\text{cl}}(\sigma,t) := [f_{\text{cl},q}(\sigma,t)^\top, f_{\text{cl},s}(\sigma,t)^\top, f_{\text{cl},v}(\sigma,t)^\top]^\top$. The analytic expressions for $f_{\text{cl},q}(\sigma,t)$, $f_{\text{cl},s}(\sigma,t)$, and $f_{\text{cl},v}(\sigma,t)$ can be found in the Appendix. Consider now the open and nonempty set $\Omega := \mathbb{S} \times (-1,1)^{12}$. The choice of the parameters $\rho_{s_k,0}$ and $\rho_{v_k,0}, k \in \mathcal{K}$ in $Step\ I-a$ and $Step\ II-a$, respectively, along with the fact that the initial conditions satisfy $|\theta_O(0) - \theta_d(0)| < \theta^*$ imply that $|e_{s_k}(0)| < \rho_{s_k}(0), |e_{v_k}(0)| < \rho_{v_k}(0), \forall k \in \mathcal{K}$ and, hence, $[\xi_S(0)^\top, \xi_V(0)^\top]^\top \in (-1,1)^{12}$. Moreover, it can be

verified that $f_{\rm cl}: \Omega \times \mathbb{R}_{\geq 0} \to \mathbb{R}^{n+12}$ is locally Lipschitz in σ over the set Ω and continuous and locally integrable in t for each fixed $\sigma \in \Omega$. Therefore, the hypotheses of Theorem 1 stated in Section II-D hold and the existence of a maximal solution $\sigma: [0, \tau_{\rm max}) \to \Omega$, for $\tau_{\rm max} > 0$, is ensured. We thus conclude

$$\xi_{Sk}(t), \xi_{Dk}(t) \in (-1, 1)$$
 (38)

 $\forall k \in \mathcal{K}, t \in [0, \tau_{\max}), \text{ which also implies that } \|\xi_s(t)\| \leq \sqrt{6}$ and $\|\xi_v(t)\| \leq \sqrt{6}, \forall t \in [0, \tau_{\max}).$ In the following, we show the boundedness of all closed-loop signals and $\tau_{\max} = \infty$.

Part B: Note first from (38) that $|\theta_O(t) - \theta_d(t)| < \rho_{\theta}(t) \le \rho_{\theta}(0) = \theta^*$, which, since $\theta_d(t) \in [-\bar{\theta}, \bar{\theta}], \forall t \in \mathbb{R}_{\ge 0}$, implies that $|\theta_O(t)| \le \tilde{\theta} := \bar{\theta} + \theta^* < (\pi/2), \forall t \in [0, \tau_{\text{max}})$. Therefore, by employing (7), one obtains that, $\forall t \in [0, \tau_{\text{max}})$,

$$||J_O(\eta_O(t))|| \le \bar{J}_O := \sqrt{\frac{|\sin(\widetilde{\theta})| + 1}{1 - \sin^2(\widetilde{\theta})}} < \infty.$$
 (39)

Consider now the positive definite function $V_s = (1/2)\|\varepsilon_s\|^2$. Differentiating V_s along the solutions of the closed-loop system yields $\dot{V}_s = \varepsilon_s^{\top} r_s(\xi_s) \rho_s^{-1} \dot{\xi}_s$, which, in view of (31), (37), and (33) and the fact that $\dot{x}_O = J_O(\eta_O) v_O = J_O(\eta_O) (v_r + e_v)$ becomes

$$\dot{V}_{s} = -g_{s} \| \rho_{s}^{-1} r_{s}(\xi_{s}) \varepsilon_{s} \|^{2} - \varepsilon_{s}^{\top} r_{s}(\xi_{s}) \rho_{s}^{-1}
\times (\dot{x}_{d} + \dot{\rho}_{s} \xi_{s} - J_{O}(\eta_{O}) e_{v})
\leq g_{s} \| \rho_{s}^{-1} r_{s}(\xi_{s}) \varepsilon_{s} \|^{2} + \| \rho_{s}^{-1} r_{s}(\xi_{s}) \varepsilon_{s} \|
\times (\| \dot{x}_{d} \| + \| J_{O}(\eta_{O}) \rho_{v} \xi_{v} \| + \| \dot{\rho}_{s} \xi_{s} \|).$$
(40)

In view of (38), (39), and the structure of ρ_{s_k} , ρ_{v_k} , $k \in \mathcal{K}$, as well as the fact that $v_O(0) = 0$ and the boundedness of \dot{x}_d , the last inequality becomes

$$\dot{V}_{s} \le -g_{s} \| \rho_{s}^{-1} r_{s}(\xi_{s}) \varepsilon_{s} \|^{2} + \| \rho_{s}^{-1} r_{s}(\xi_{s}) \varepsilon_{s} \| \bar{B}_{s}$$
 (41)

 $\forall t \in [0, \tau_{\text{max}})$, where \bar{B}_s is a positive constant independent of τ_{max} . Therefore, \dot{V}_s is negative when $\|\rho_s^{-1}r_s(\xi_s)\varepsilon_s\| > (\bar{B}_s/g_s)$, which, by employing (30), the decreasing property of ρ_{s_k} , $k \in \mathcal{K}$ as well as (38), is satisfied when $\|\varepsilon_s\| > (\max_{k \in \mathcal{K}} \{\rho_{s_k,0}\}\bar{B}_s/2 g_s)$. Hence, we conclude that

$$\|\varepsilon_s(t)\| \le \bar{\varepsilon}_s := \max\left\{\|\varepsilon_s(0)\|, \frac{\max_{k \in \mathcal{K}} \{\rho_{s_k,0}\}\bar{B}_s}{2g_s}\right\}$$
 (42)

 $\forall t \in [0, \tau_{\text{max}})$. Furthermore, since $|\varepsilon_{s_k}| \leq \|\varepsilon_s\|$, $\forall k \in \mathcal{K}$, taking the inverse logarithm function from (29), we obtain

$$-1 < \frac{\exp(-\bar{\varepsilon}_s) - 1}{\exp(-\bar{\varepsilon}_s) + 1} =: -\bar{\xi}_s \le \xi_{s_k}(t) \le \bar{\xi}_s := \frac{\exp(\bar{\varepsilon}_s) - 1}{\exp(\bar{\varepsilon}_s) + 1} < 1$$
(43)

 $\forall t \in [0, \tau_{\text{max}})$. Hence, recalling (30) and (31), we obtain the boundedness of $v_r(t)$, $\forall t \in [0, \tau_{\text{max}})$, and in view of $v_o = v_r + e_v$, (32), (38), (9), and (10), the boundedness of $v_o(t)$ and $v_i(t)$, $\forall t \in [0, \tau_{\text{max}})$. From (6a), (25), and (43), we also conclude the boundedness of $x_o(t)$, $\dot{x}_o(t)$, $\forall t \in [0, \tau_{\text{max}})$. The coupled kinematics (8) and Assumption 3 imply also the boundedness of $p_{E_i}(t)$, $q_i(t)$, and $\dot{q}_i(t)$, $\forall i \in \mathcal{N}$, $[0, \tau_{\text{max}})$. In a similar vein, by differentiating the reference velocity (31) and using (29),

(30), and (42), we also conclude the boundedness of $\dot{v}_r(t)$, $\forall t \in [0, \tau_{\text{max}})$.

Applying the aforementioned line of proof, we consider the positive definite function $V_v = (1/2)\|\varepsilon_v\|^2$. By differentiating V_v , we obtain $\dot{V}_v = \varepsilon_v^\top r_v(\xi_v) \rho_v^{-1} \dot{\xi}_v$, which, in view of (37), (32), and (11), becomes

$$\dot{V}_{v} = -g_{v}\varepsilon_{v}^{\top}r_{v}(\xi_{v})\rho_{v}^{-1}\widetilde{M}(x)\rho_{v}^{-1}r_{v}(\xi_{v})\varepsilon_{v}
+ \varepsilon_{v}^{\top}r_{v}(\xi_{v})\rho_{v}^{-1}(-\dot{\rho}_{v}\xi_{v} - \widetilde{M}(x)[\widetilde{C}(x)[\rho_{v}\xi_{v} + v_{r}]
+ \widetilde{g}(x) + \widetilde{d}(x,t)] - \dot{v}_{r}).$$
(44)

Invoking Assumption 5 and the boundedness of $q_i(t)$, $\dot{q}_i(t)$, $x_O(t)$, $\dot{x}_O(t)$, $\dot{x}_O(t)$, $\forall t \in [0, \tau_{\max})$, we conclude the boundedness of $d_O(x_O(t), \dot{x}_O(t), t)$ and $d_i(q_i(t), \dot{q}_i(t), t)$, $\forall t \in [0, \tau_{\max})$. Hence, from (10) and (11), we also obtain the boundedness of $\widetilde{d}(x(t))$. In addition, the continuity of $\widetilde{M}(x)$, $\widetilde{C}(x)$, and $\widetilde{g}(x)$ implies their boundedness $\forall t \in [0, \tau_{\max})$.

Thus, by combining the aforementioned discussion with the boundedness of \dot{v}_r , the positive definitiveness of $\widetilde{M}(x)$, and (38), we obtain from (44)

$$\dot{V}_v \le -g_v \underline{m} \| \rho_v^{-1} r_v(\xi_v) \varepsilon_v \|^2 + \| \rho_v^{-1} r_v(\xi_v) \varepsilon_v \| \bar{B}_v$$
 (45)

 $\forall t \in [0, \tau_{\text{max}})$, where \bar{B}_v is a positive and finite constant, independent of τ_{max} .

By proceeding similarly as with \dot{V}_s , we conclude that

$$\|\varepsilon_v(t)\| \le \bar{\varepsilon}_v := \max\left\{\|\varepsilon_v(0)\|, \frac{\max_{k \in \mathcal{K}} \{\rho_{v_k,0}\}\bar{B}_v}{2g_v \underline{m}}\right\}$$
 (46)

 $\forall t \in [0, \tau_{\text{max}})$, from which we obtain

$$-1 < \frac{\exp(-\bar{\varepsilon}_{v}) - 1}{\exp(-\bar{\varepsilon}_{v}) + 1} =: -\bar{\xi}_{v} \le \xi_{v_{k}}(t) \le \bar{\xi}_{v} := \frac{\exp(\bar{\varepsilon}_{v}) - 1}{\exp(\bar{\varepsilon}_{v}) + 1} < 1$$
(47)

 $\forall t \in [0, \tau_{\max})$. What remains to be shown is that $\tau_{\max} = \infty$. We can conclude from the aforementioned analysis, Assumption 3, (43), and (47) that the solution $\sigma(t)$ remains in a compact subset Ω' of Ω , $\forall t \in [0, \tau_{\max})$, namely, $\sigma(t) \in \Omega'$, $\forall t \in [0, \tau_{\max})$. Hence, assuming $\tau_{\max} < \infty$ and since $\Omega' \subset \Omega$, Proposition 1 in Section II-D dictates the existence of a time instant $t' \in [0, \tau_{\max})$ such that $\sigma(t') \notin \Omega'$, which is a contradiction. Therefore, $\tau_{\max} = \infty$. Thus, all closed-loop signals remain bounded, and moreover, $\sigma(t) \in \Omega' \subset \Omega$, $\forall t \in \mathbb{R}_{\geq 0}$. Finally, by multiplying (43) by $\rho_k(t), k \in \mathcal{K}$, we obtain

$$-\rho_{s_k}(t) < -\bar{\xi}_s \rho_{s_k}(t) \le e_{s_k}(t) \le \bar{\xi}_s \rho_{s_k}(t) < \rho_{s_k}(t), \quad (48)$$

 $\forall t \in \mathbb{R}_{>0}$, which leads to the conclusion of the proof.

Remark 6 (Prescribed Performance): From the aforementioned proof, it can be deduced that the PPC scheme achieves its goal without resorting to the need of rendering the ultimate bounds $\bar{\varepsilon}_s$, $\bar{\varepsilon}_v$ of the modulated pose and velocity errors $\varepsilon_s(t)$, $\varepsilon_v(t)$ arbitrarily small by adopting extreme values of the control gains g_s and g_v (see (42) and (46)). More specifically, notice that (43) and (47) hold no matter how large the finite bounds $\bar{\varepsilon}_s$, $\bar{\varepsilon}_v$ are. In the same spirit, large uncertainties involved in the coupled model (11) can be compensated, as they affect only the size of ε_v through \bar{B}_v , but leave unaltered the achieved stability properties. Hence, the actual performance given in (48), which is solely determined by the

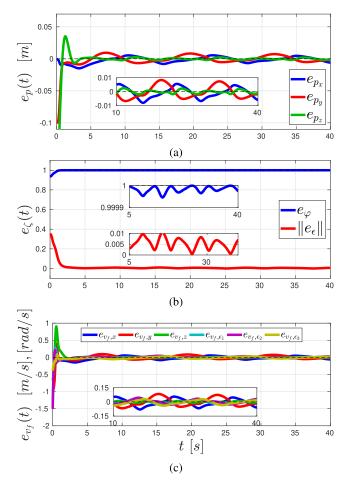


Fig. 2. Simulation results for the control scheme of Section IV-A. (a) Position errors $e_p(t)$. (b) Quaternion errors $e_{\varphi}(t)$, $\|e_{\varepsilon}(t)\|$. (c) Velocity errors $e_{v_f}(t)$, $\forall t \in [0, 40]$. A zoomed version of the steady-state response has been included in all plots.

designed-specified performance functions $\rho_{s_k}(t)$, $\rho_{v_k}(t)$, $k \in \mathcal{K}$, becomes isolated against model uncertainties, thus extending greatly the robustness of the proposed control scheme.

Remark 7 (Control Input Bounds): The aforementioned analysis of the PPC methodology reveals the derivation of bounds for the velocity v_i and control input u_i of each agent. In contrast to our previous work [46], we derive in the Appendix explicit bounds \bar{v}_i and \bar{u}_i for v_i and u_i (see (55), (56)), respectively, which depend on the control gains, the bounds of the dynamic terms, the desired trajectory, and the performance functions. Therefore, given desired bounds for the agents' velocity $\bar{v}_{i,b}$ and input $\bar{u}_{i,b}$ (derived from bounds on the joint velocities and torques \dot{q}_i , τ_i , respectively) and that the upper bounds of the dynamic terms are known, we can tune appropriately the control gain g_s , g_v as well as the parameters $\rho_{s_k,0}, \rho_{v_k,0}, \rho_{s_k,\infty}, \rho_{v_k,\infty}, l_{s_k}, l_{v_k}$ in order to achieve $\bar{v}_i \leq \bar{v}_{i,b}, \bar{u}_i \leq \bar{u}_{i,b}, \forall i \in \mathcal{N}$. It is also worth noting that the selection of the control gains g_s , g_v affects the evolution of the errors e_s , e_v inside the corresponding performance envelopes.

V. SIMULATION AND EXPERIMENTAL RESULTS

In this section, we provide simulation and experimental results for the two developed control schemes.

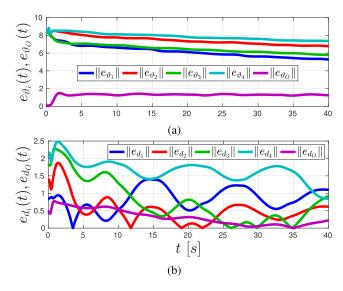


Fig. 3. Adaptation error norms (a) $\|e_{\vartheta_i}(t)\|$, $i \in \mathcal{N}$, $\|e_{\vartheta_O}(t)\|$, (b) $\|e_{d_i}(t)\|$, $i \in \mathcal{N}$, $\|e_{d_O}(t)\|$, of the control scheme of Section IV-A $\forall t \in [0, 40]$.

More specifically, Section V-A presents computer simulation results and Section V-B presents experimental results for both control algorithms.

A. Simulation Results

The tested scenario consists of four UR5 robotic manipulators rigidly grasping a rectangular The object's initial pose [-0.225,is $x_o(0)$ $-0.612,0161,-\pi,(\pi/3),0]^{\perp}$ ([m], [rad]) with respect to a chosen inertial frame and the desired trajectory is set as $p_d(t) = [-0.225 + 0.1\sin(0.5t), -0.612 +$ $0.2\cos(0.5t), 0.25 + 0.05\sin(0.5t)$ ^T [m], $\eta_d(t) = [-\pi +$ $0.25\cos(0.5t), (\pi/3) + A_{\theta}\sin(0.25t), 0.25\cos(0.5t)]^{\top}$ rad, where A_{θ} takes different values for the two control schemes. In particular, we set $A_{\theta} = (\pi/6)$ for the adaptive quaternionfeedback control scheme, meaning that the desired pitch angle reaches the configuration of $(\pi/2)$. This would be singular for the PPC scheme, for which we set $A_{\theta} = (\pi/9)$. In view of Assumption 4, we set $d_i = (\|q_i\|\sin(\omega_{d_i}t + \phi_{d_i}) + \dot{q}_i)d_i$ and $d_O = (\|\dot{x}_O\|\sin(\omega_{d_O}t + \phi_{d_O}) + v_O)d_O$, where the constants $\omega_{d_i}, \phi_{d_i}, \omega_{d_O}, \omega_{d_O}$ are randomly chosen in the interval (0, 1), $\forall i \in \mathcal{N}$. Regarding the force distribution matrix (20), we set $m_i^* = 1$, $\forall i \in \mathcal{N}$, and $J_1^* = 0.6I_3$, $J_2^{\star} = 0.4I_3, J_3^{\star} = 0.75I_3, J_4^{\star} = 0.25I_3$ to demonstrate a potential difference in the agents' power capabilities. In addition, we set an artificial saturation limit for the joint motors as $\bar{\tau} = 150$ Nm. For the adaptive quaternionfeedback control scheme of Section IV-A, we set the control gains appearing in (19) and (21) as $k_p = \text{diag}\{[5, 5, 2]\},$ $k_{\zeta} = 3I_3, K_v = 400I_6, \gamma_i = \gamma_o = \beta_i = \beta_o = 1,$ $\forall i \in \mathcal{N}$. The simulation results are depicted in Figs. 2–4 for $t \in [0, 40]$ s. More specifically, Fig. 2 shows the evolution of the pose and velocity errors $e_p(t)$, $e_{\zeta}(t)$, $e_{v_f}(t)$, Fig. 3 depicts the norms of the adaptation errors $e_{\vartheta_i}(t)$, $e_{\vartheta_O}(t)$, $e_{d_i}(t), e_{d_O}(t)$, and Fig. 4 shows the resulting joint torques $\tau_i(t), \ \forall i \in \{1, \ldots, 4\}.$ Note that $e_p(t), e_{\zeta}(t),$ and $e_{v_f}(t)$

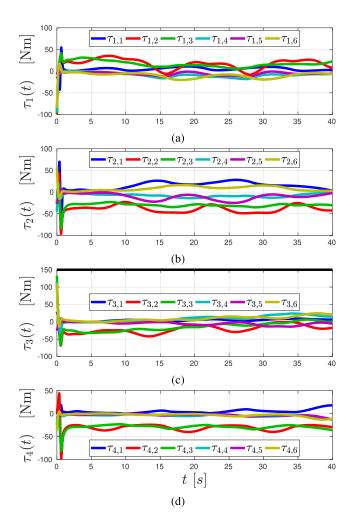


Fig. 4. Agents' joint torques $\tau_i(t)$, $i \in \mathcal{N}$ [in (a)–(d), respectively] of the control scheme of Section IV-A $\forall t \in [0, 40]$, and the motor saturation (with black), which has not been plotted in (a), (b), and (d) for better visualization.

converge to the desired values and the adaptation errors are bounded, as predicted by the theoretical analysis. For the PPC scheme of Section IV-B, we set the performance functions as $\rho_{s_k}(t) = (|e_{s_k}(0)| + 0.09) \exp(-0.5t) + 0.01$, $\rho_{v_k}(t) = (|e_{v_k}(0)| + 0.95) \exp(-0.5t) + 0.05$, $\forall k \in \mathcal{K}$, and the control gains of (31), (35) as $g_s = 0.005$, $g_v = 10$, respectively, by following the Appendix and considering known dynamic bounds. The simulation results are depicted in Figs. 5–7, for $t \in [0, 40]$ s. In particular, Fig. 5 depicts the evolution of the pose errors $e_s(t)$ (in blue), along with the respective performance functions $\rho_s(t)$ (in red), Fig. 6 depicts the evolution of the velocity errors $e_v(t)$, along with the respective performance functions $\rho_v(t)$, and Fig. 7 shows the resulting joint torques $\tau_i(t)$, $\forall i \in \{1, ..., 4\}$.

One can conclude from the aforementioned figures that the simulation results verify the theoretical findings, since the errors $e_s(t)$, $e_v(t)$ stay confined in the performance function funnels. Moreover, the joint torques in both control schemes respect the saturation values we set. For comparison purposes, we also simulate the same system by using the PPC methodology of [46], without taking into account any input constraints, since the input constraint analysis of the Appendix is not

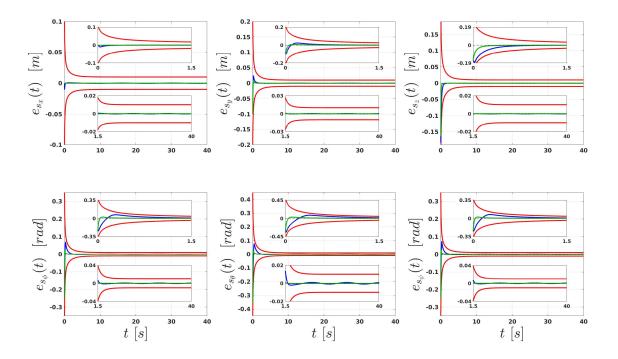


Fig. 5. Simulation results for the controller of Section IV-B, and of [46]. Position errors $e_{s_\chi}(t)$, $e_{s_\chi}(t)$, $e_{s_\chi}(t)$ (with blue and green, respectively) along with the respective performance functions (with red) (top). Orientation errors $e_{s_\phi}(t)$, $e_{s_\theta}(t)$, $e_{s_\psi}(t)$ (with blue and green, respectively) along with the respective performance functions (with red), $\forall t \in [0, 40]$ (bottom). Zoomed versions of the transient and steady-state response have been included for all plots.

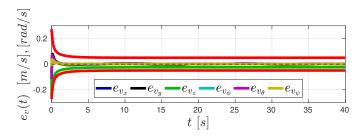


Fig. 6. Velocity errors $e_v(t)$ along with the respective performance functions (with red) for the controller of Section IV-B, $\forall t \in [0, 40]$.

performed in [46]. In order to achieve good performance in terms of overshoot, rise, and settling time, we set the control gains as $g_s = 1$, $g_v = 200$. The resulting pose errors are depicted in Fig. 5 for $t \in [0, 40]$ s (with green) along with the performance functions (with red), and the resulting torques are depicted in Fig. 8 for $t \in [0, 0.001]$ s. This small time interval is sufficient to observe the high-value initial peaks of the torque inputs that do not satisfy the desired constraint of $\bar{\tau}$ 150 Nm, which can be attributed to the lack of gain calibration. Nevertheless, note also the better performance of the pose errors, in terms of overshoot, rise, and settling time, as pictured in Fig. 5. Finally, note that any PPC methodology would fail to solve Problem 1 with $\theta(0) = (\pi/2)$ or $\theta_d(t) = (\pi/2)$ for some $t \in \mathbb{R}_{\geq 0}$, in contrast to the adaptive quaternion-feedback control scheme of Section IV-A. The torque illustration for the remaining time as well as the velocity error convergence is omitted due to space constraints. The simulations were carried out in the MATLAB R2017a environment on a i7-5600 laptop computer at 2.6 Hz, with 8 GB of RAM.

B. Experimental Results

The tested scenario for the experimental setup consists of two WidowX Robot Arms rigidly grasping a wooden cuboid object of initial pose $x_0(0)$ $[0.3, 0, 0.15, 0, 0, 0]^{T}$ ([m], [rad]), which has to track a planar time trajectory $p_d(t) = [0.3 + 0.05 \sin(\frac{2\pi t}{35}), 0.15 - 0.05 \cos(\frac{2\pi t}{35})]^{\top}$ [m], $\eta_d(t) = \frac{\pi}{20} \sin(\frac{5\pi t}{35})$ [rad]. For that purpose, we employ the three rotational—with respect to the y-axis—joints of the arms. The lower joint consists of an MX-64 Dynamixel Actuator, whereas each of the two upper joints consists of an MX-28 Dynamixel Actuator from the MX Series. Both actuators provide feedback of the joint angle and rate $q_i, \dot{q}_i, \forall i \in \{1, 2\}$. The microcontroller used for the actuators of each arm is the ArbotiX-M Robocontroller, which is serially connected to an i-7 desktop computer with 4 cores and 16-GB RAM. All the computations for the real-time experiments are performed at a frequency of 120 Hz. Finally, we consider that the MX-64 motor can exert a maximum torque of 3 Nm, and the MX-28 motors can exert a maximum torque of 1.25 Nm, values that are slightly more conservative than the actual limits. The load distribution coefficients are set as $m_1^{\star}=m_2^{\star}=1$, and $J_1^{\star}=0.75I_3$, $J_2^{\star}=0.25I_3$. For the adaptive quaternion-feedback control scheme, we set $\delta_O(x_O, \dot{x}_O, t) = 0_{6 \times \mu_O}, \ \delta_i(q_i, \dot{q}_i, t) = 0_{6 \times \mu}, \ \forall i \in \mathcal{N},$ which essentially means that we do not model any external disturbances. We also set the control gains appearing in (19) and (21) as $k_p = 50$, $k_{\zeta} = 80$, $K_v = \text{diag}\{3.5, 0.5, 0.5\}$. The experimental results are depicted in Fig. 9–11 for $t \in [0, 70]$ s. More specifically, Fig. 9 pictures the pose and velocity errors $e_p(t), e_{\zeta}(t), e_{v_f}(t)$, Fig. 10 depicts the norms of the adaptation

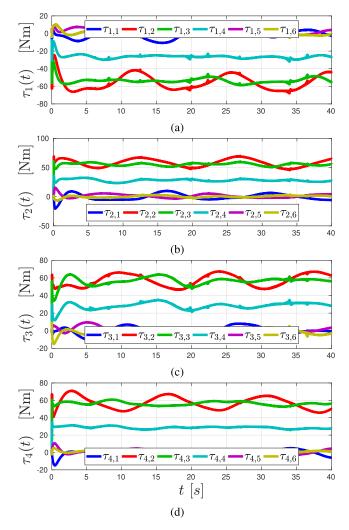


Fig. 7. Agents' joint torques $\tau_i(t)$, $i \in \mathcal{N}$ [in (a)–(d), respectively] of the control scheme of Section IV-B $\forall t \in [0, 40]$.

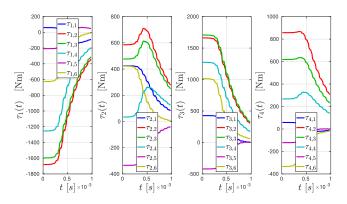


Fig. 8. Agents' joint torques $\tau_i(t)$, $i \in \mathcal{N}$ [in (a)–(d), respectively] of the control scheme of [46] $\forall t \in [0, 0.001]$.

errors $e_{\vartheta_i}(t)$, $e_{\vartheta_O}(t)$, and Fig. 11 shows the joint torques $\tau_1(t)$, $\tau_2(t)$ of the agents. Although external disturbances and modeling uncertainties are not taken into account in the system model, they are indeed present during the experiment run time and one can observe that the errors converge to the desired values and the adaptation errors remain bounded, verifying the theoretical findings. For the PPC scheme, we set the

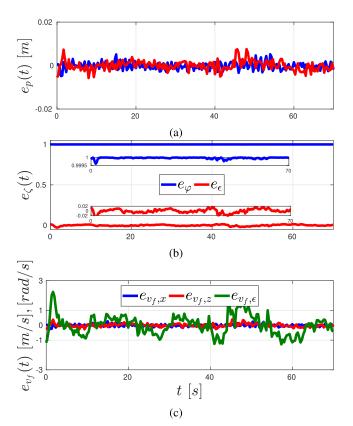


Fig. 9. Experimental results for the control scheme of Section IV-A. (a) Position errors $e_p(t)$. (b) Quaternion errors $e_{\varphi}(t)$, $e_{\varepsilon}(t)$. (c) Velocity errors $e_{\varphi}(t)$, $\forall t \in [0, 70]$.

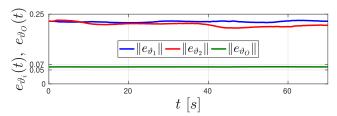


Fig. 10. Norms of the adaptation signals $e_{\vartheta_i}(t)$, $\forall i \in \{1, 2\}$ (left) and $e_{\vartheta_O}(t)$ (right) $\forall t \in [0, 70]$ of the experiment of the controller in Section IV-A.

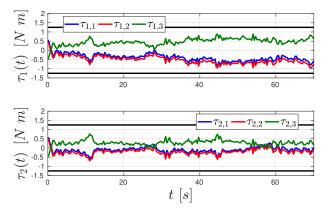


Fig. 11. Agents' joint torques of the experiment of the controller in Section IV-A, for $t \in [0, 70]$, with their respective limits (with black).

performance functions as $\rho_{s_x}(t) = \rho_{s_z}(t) = 0.03 \exp(-0.2t) + 0.02$ [m], $\rho_{s_\theta}(t) = 0.2 \exp(-0.2t) + 0.2$ [rad], $\rho_{v_x}(t) = 5 \exp(-0.2t) + 5$ [m/s], $\rho_{v_z}(t) = 5 \exp(-0.2t) + 10$ [m/s],

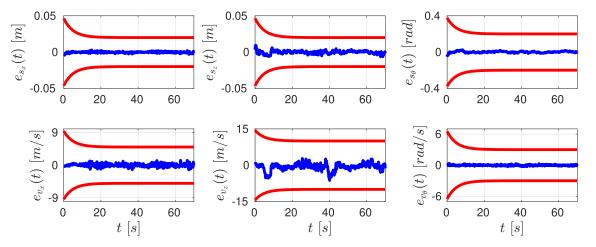


Fig. 12. Experimental results for the controller of Section IV-B. Pose errors $e_{s_X}(t)$, $e_{s_Z}(t)$, $e_{s_Z}(t)$, $e_{s_Z}(t)$ (with blue) along with the respective performance functions (with red), $\forall t \in [0, 70]$ (bottom).

and $\rho_{v_{\theta}}(t) = 4 \exp(-0.2t) + 3$ [m/s], and the control gains of (31) and (35) as $g_s = 0.05$ and $g_v = 10$, respectively, by following the Appendix. The experimental results are depicted in Fig. 12 and 13 for $t \in [0, 70]$ s. In particular, Fig. 12 shows the pose and velocity errors $e_s(t)$, $e_v(t)$ along with the respective performance functions, and Fig. 13 depicts the joint torques $\tau_1(t)$, $\tau_2(t)$ of the agents. We can conclude that the experimental results verify the theoretical analysis, since the errors evolve strictly within the prespecified performance bounds. Note also that in both control schemes the joint torques respect the saturation limits. A video illustrating the results can be found on https://youtu.be/jJWeI5ZvQPY.

C. Discussion

In view of the aforementioned results, we mention some worth-noting differences between the two control schemes. First, note that the PPC methodology allows for exponential convergence of the errors to the set defined by the values $\rho_{s_k,\infty}$, $\rho_{v_k,\infty}$, achieving *predefined* transient and steady-state performance, without the need to resort to tuning of the control gains. The adaptive quaternion-feedback methodology, however, can only guarantee that the errors converge to zero as $t \to \infty$. This is verified by the simulation results, where the error trajectories $e_p(t)$, $e_{\zeta}(t)$ and $e_v(t)$ show an oscillatory behavior. Improvement of such performance (in terms of overshoot, rise, and settling time) would require appropriate gain tuning. Second, note that, as shown in the simulations section, the quaternion-feedback methodology allows for trajectories where the pitch angle of the object (θ_0) can be ± 90 °, in contrast to the PPC methodology, where that configuration is ill-posed, since the matrix $J_O(\eta_O)$ is not defined. Finally, the adaptive quaternion-feedback methodology can be considered less robust to modeling uncertainties in real-time scenarios, since it accounts only for parametric uncertainties (the unknown terms θ_i , θ_o , d_i , and d_o), assuming a known structure of the dynamic terms. The PPC methodology, however, does not require any information about the structure or the parameters of the dynamic model (note that the only requirements are the positive definiteness of the coupled inertia matrix,

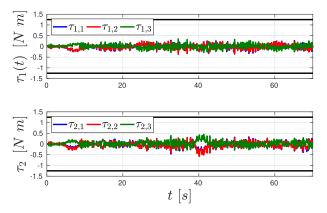


Fig. 13. Agents' joint torques of the experiment of the controller in Section IV-B, $\forall t \in [0, 70]$, with their respective limits (with black).

the locally Lipschitz and continuity properties of the dynamic terms and the boundedness—with respect to time—of the disturbances d_i , d_O). In that sense, one would expect the PPC methodology to perform better in real-time experiments, where unmodeled dynamics are involved. The fact, however, that PPC is a control scheme that does not contain any information of the model structure makes it more difficult to tune (in terms of gain tuning) in order to achieve robot velocities and torques that respect specific bounds, especially when the bounds of the dynamic terms are unknown. This has been noticed during both simulations and experiments.

VI. CONCLUSION

We presented two novel decentralized control protocols for the cooperative manipulation of a single object by N robotics agents. First, we developed a quaternion-based approach that avoids representation singularities with adaptation laws to compensate for dynamic uncertainties. Second, we developed a robust control law that guarantees prescribed performance for the transient and steady state of the object. Both methodologies were validated via realistic simulations and experimental results. Future efforts will be devoted toward

applying the proposed techniques to cases with nonrigid grasping points and uncertain object geometric characteristics.

APPENDIX

In the following, we derive explicit expressions for the terms $f_{cl,q}$, $f_{cl,s}$, and $f_{cl,v}$ of (37), as well as bounds for the dynamics terms of the model and the velocity and control inputs v_i , u_i , respectively, $i \in \mathcal{N}$.

Note first from (25), (28), (32), and (33) that the states x_O , v_O can be expressed as

$$x_O = x_d(t) + \rho_s(t)\xi_s \tag{49a}$$

$$v_O = \rho_v(t)\xi_v + v_r(\xi_s, t) \tag{49b}$$

where with a slight abuse of notation, we right v_r as a function of ξ_s and t. Then, from (37) and (31), we obtain

$$f_{\text{cl},q}(\sigma,t) = \widetilde{J}(q)G(q)(\rho_v(t)\xi_v + v_r(\xi_s,t)). \tag{50}$$

Regarding $f_{cl.s}$, we obtain from (37) by using (6a) and (49)

$$f_{\text{cl},s}(\sigma,t) = \rho(t)^{-1} [J_O(\eta_d(t) + \rho_{s_\eta}(t)\xi_{s_\eta})\rho_v(t)\xi_v - \dot{\rho}_s(t)\xi_s - g_s\rho(t)^{-1}r_s(\xi_s)\varepsilon_s(\xi_s) - \dot{x}_d(t)]$$
(51)

where we also express ε_s , from (29), as a function of ζ_s .

Next, we differentiate v_r from (31) and use (28), (30), and (49) to obtain

$$\dot{v}_{r} = -g_{s}J_{O}(\eta_{d}(t) + \rho_{s_{\eta}}(t)\xi_{s})^{-1}$$

$$\times [\rho_{s}(t)^{-1}\dot{r}_{s}(\xi_{s})\varepsilon_{s}$$

$$+ \rho_{s}(t)^{-1}r_{s}(\xi_{s})^{2}f_{\text{cl},s}(\sigma,t) - \rho_{s}(t)^{-2}\dot{\rho}_{s}(t)r_{s}(\xi_{s})\varepsilon_{s}]$$

$$-g_{s}\frac{\partial}{\partial t}[J_{O}(\eta_{O})^{-1}]\rho_{s}(t)^{-1}r_{s}(\xi_{s})\varepsilon_{s}(\xi_{s})$$
(52)

where

$$\dot{r}_s(\xi_s) = \operatorname{diag}\left\{ \left[\frac{2\xi_{s_k}}{(1 - \xi_{s_k})^2} \right]_{k \in \mathcal{K}} \right\} \sum_{k \in \mathcal{K}} \bar{E}_k f_{\operatorname{cl},s}(\sigma, t) \bar{e}_k \quad (53)$$

with $\bar{E}_k \in \mathbb{R}^{6 \times 6}$ being the matrix with 1 in the element (k, k) and zeros everywhere else, and $\bar{e}_k \in \mathbb{R}^6$ being the vector with 1 in the element k and zeros everywhere else. Note from (52) and (49), and the fact that $\dot{x}_O = J_O(\eta_d(t) + \rho_{s_\eta}(t)\xi_{s_\eta})v_O$ that \dot{v}_r can be expressed as a function of σ and t. Hence, in view of (11), (36), and $[G(q)]^T G_M^+ = I_6$, one obtains from (37)

$$\dot{\xi}_{v} = \rho_{v}(t)^{-1}(-\dot{\rho}_{v}(t)\xi_{v} - \widetilde{M}(x(\sigma, t))$$

$$\times [\widetilde{C}(x(\sigma, t))[\rho_{v}(t)\xi_{v} + v_{r}(\xi_{s}, t)]$$

$$+ \widetilde{g}(x(\sigma, t)) + \widetilde{d}(x(\sigma, t), t)$$

$$- g_{v}\rho_{v}(t)^{-1}r_{v}(\xi_{v})\varepsilon_{v}(\xi_{v})] - \dot{v}_{r}(\sigma, t))$$

$$=: f_{cl, v}(\sigma, t) \tag{54}$$

and where, by using (49) and (50), we have written x (that was first defined in (11)) as a function of σ and t, that is,

$$x(\sigma,t) = \begin{bmatrix} q \\ \dot{q} \\ x_0 \\ \dot{x}_0 \end{bmatrix}$$

$$= \begin{bmatrix} q \\ f_{\text{cl},q}(\sigma,t) \\ x_d(t) + \rho_s(t)\xi_s \\ J_O(\eta_d(t) + \rho_\eta(t)\xi_{s_\eta})[\rho_v(t)\xi_v + v_r(\xi_s,t)] \end{bmatrix}$$

We proceed by deriving expressions for the bounds of the agent velocities and control inputs v_i , u_i , and $i \in \mathcal{N}$. By inspecting (40) and (41), we can conclude that $\bar{B}_s := \sqrt{6}\bar{J}_O(\|v_r(0)\| + \alpha) + \bar{\dot{x}}_d + \sqrt{6}\max_{k \in \mathcal{K}}\{l_k(\rho_{s_k,0} - \rho_{s_k,\infty})\}$ where $\bar{\dot{x}}_d$ is the bound of $\dot{x}_d(t)$. Moreover, in view of (30) and (43), one obtains $\|r_s(\xi_s(t))\| \leq \bar{r}_s := (2/(1 - \bar{\xi}_s^2)) = ((\exp(\bar{\varepsilon}_s) + 1)^2/2 \exp(\bar{\varepsilon}_s))$. Therefore, we obtain from (31)

$$||v_r(t)|| \le \bar{v}_r := g_s \sqrt{2} \frac{\bar{\varepsilon}_s(\exp(\bar{\varepsilon}_s) + 1)^2}{2 \min_{k \in \mathcal{K}} \{\rho_{s_k, \infty}\} \exp(\bar{\varepsilon}_s)}.$$

From $v_O = v_r + \rho_v(t)\xi_v$, we also conclude

$$||v_O(t)|| \le \bar{v}_O := g_s \sqrt{2} \frac{\bar{\varepsilon}_s (\exp(\bar{\varepsilon}_s) + 1)^2}{2 \min_{k \in \mathcal{K}} \{\rho_{k,\infty}\} \exp(\bar{\varepsilon}_s)} + \sqrt{6} \max_{k \in \mathcal{K}} \{\rho_{v_k,0}\}$$

which, through (9) and (10), leads to

$$||v_i(t)|| \le \bar{v}_i := (||p_{O/E_i}^{E_i}|| + 1)\bar{v}_O \quad \forall i \in \mathcal{N}.$$
 (55)

By considering the derivative of the reference velocity (52), as well as (29), (51), (53), and (55), we can obtain a bound $\|\dot{v}_r(t)\| \leq \dot{v}_r$, which is not written explicitly for presentation clarity. From (43), (6a), and (25), we also obtain $||x_o(t)|| \le$ $\bar{x}_O := \bar{x}_d + \sqrt{6\xi_s} \max_{k \in \mathcal{K}} \{\rho_{s_k,0}\}, \text{ and } \|\dot{x}_O(t)\| \le J_O \bar{v}_O.$ Next, by using (8) and the fact that the rotation matrix $R_{E_i}(q_i)$ is an orthogonal matrix, we obtain $||x_{E_i}(t)|| :=$ $\|[p_{E_i}^\top(q_i(t), \eta_{E_i}^\top(q_i(t))]^\top\| \le \|x_O(t)\| + \|[(p_{E_i/O}^{E_i})^\top, \eta_{E_i/O}^\top]^\top\|,$ and hence, in view of the inverse kinematics of the agents [43], we conclude the boundedness of q(t) as $||q(t)|| \leq \bar{q}$, where \bar{q} is a positive constant. From Assumption 3 and the forward differential agent kinematics, we can also conclude that there exists a positive constant \bar{J} such that $\|\dot{q}(t)\| \le$ $\bar{J}||v|| \leq \bar{J} \sum_{i \in \mathcal{N}} \bar{v}_i$, where \bar{v}_i was defined in (55). Therefore, we conclude that $||x(t)|| \leq \bar{x} := \bar{q} + \bar{J} \sum_{i \in \mathcal{N}} \bar{v}_i + \bar{x}_o +$ $\bar{J}_{O}\bar{v}_{O}$. Assumption 5 and the boundedness of x imply that $\|d_i(q_i,\dot{q}_i,t)\| \leq \underline{d}_i', \|d_O(x_O,\dot{x}_O,t)\| \leq \underline{d}_O'$ for positive and finite constants \underline{d}_O' and \underline{d}_i' , respectively, $\forall i \in \mathcal{N}$. Hence, from (10) and (11), we obtain $\|\widetilde{d}(x(t))\| \leq \underline{d} := \underline{d}_O' + \sum_{i=1}^{E_i} \|d_O(x_i)\|^2$ $\sum_{i \in \mathcal{N}} \{\|p_{O/E_i}^{E_i}\| + 1\}\underline{d_i'}$. Similarly, the continuity of $\widetilde{C}(x)$, $\widetilde{g}(x)$ along with the boundedness of x implies the existence of positive and finite constants \bar{c}, \bar{g} such that $||C(x(t))|| \leq \bar{c}$, $\|\widetilde{g}(x(t))\| \leq \overline{g}$. Therefore, we can obtain from (44) and (45), after some algebraic manipulations, that

$$\bar{B}_{v} := \sqrt{6} \max_{k \in \mathcal{K}} \{l_{v_{k}}(\rho_{v_{k},0} - \rho_{v_{k},\infty})\} + \bar{\dot{v}}_{r}
+ \bar{m}(\bar{g} + \underline{d} + \bar{c}(\bar{v}_{r} + \sqrt{6}(\|v_{r}(0)\| + \alpha))).$$

Moreover, by combining (34) and (47), one obtains $||r_v(\xi_v(t))|| \leq \bar{r}_v := (2/(1-\bar{\xi}_{v_k}^2)) = (((\exp(\bar{\epsilon}_v)+1)^2)/2\exp(\bar{\epsilon}_v))$. Finally, it can also be shown, from the fact that $p_{O/E_i} = R_O(q_i)p_{O/E_i}^o$, $\forall i \in \mathcal{N}$, that the norm $||J_{M_i}(q)||$, as defined in (20), is independent of q.

Hence, we can also conclude the boundedness of the control inputs (35)

$$||u_{i}(t)|| \leq \bar{u}_{i} := g_{v}||J_{M_{i}}(q)|| \max_{k \in \mathcal{K}} \left\{ \frac{1}{\rho_{v_{k},\infty}} \right\} \bar{r}_{v} \bar{\varepsilon}_{v}$$

$$\forall t \in [0, \tau_{\max}). \quad (56)$$

By considering (17), (22a), (23), and (24), we can also derive the respective upper bounds for the controller of Section IV-A.

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Christos K. Verginis (M'17) was born in Athens, Greece, in 1989. He received the Diploma degree in electrical and computer engineering and the M.sc. degree in automatic control systems and robotics from the National Technical University of Athens, Greece, in 2013 and 2015, respectively. He is currently pursuing the Ph.D. degree with the KTH Royal Institute of Technology, Stockholm, Sweden.

His current research interests include multiagent systems, formal verification, and hybrid control of cooperative manipulation tasks.



Matteo Mastellaro received the B.Sc. degree in information engineering from the Universita Degli Studi di Padova, Padua, Italy, in 2014, and the M.Sc. degree in automation engineering from the University of Padova. His master thesis was carried out at the KTH Royal Institute of Technology, Stockholm, Sweden, and involved cooperative manipulation schemes without force/torque feedback.



Dimos V. Dimarogonas (SM'17) was born in Athens, Greece, in 1978. He received the Diploma degree in electrical and computer engineering and the Ph.D. degree in mechanical engineering from the National Technical University of Athens, Athens, Greece, in 2001 and 2006, respectively.

From 2007 to 2009, he was a Post-Doctoral Researcher with the Automatic Control Laboratory, School of Electrical Engineering, ACCESS Linnaeus Center, KTH Royal Institute of Technology, Stockholm, Sweden. From 2009 to 2010, he was a Post-

Doctoral Associate with the Laboratory for Information and Decision Systems, Massachusetts Institute of Technology, Boston, MA, USA. He received a Docent in automatic control from KTH Royal Institute of Technology in 2012. He is currently a Professor with the Automatic Control Laboratory, ACCESS Linnaeus Center, KTH Royal Institute of Technology. His current research interests include multiagent systems, hybrid systems and control, robot navigation, and networked control.

Dr. Dimarogonas is a member of the Technical Chamber of Greece. He serves as an Editorial Board for *Automatica* and *IET Control Theory and Applications*.