1 Analysing an Algorithm

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\label{eq:coeffs} \begin{split} &\text{def } r(\text{coeffs}):\\ &\text{coeffs} = \text{np.array}(\text{coeffs}[:-1])\\ &\text{n} = \text{len}(\text{coeffs})\\ &\text{A} = \text{np.eye}(\text{n}, \text{ k} = -1)\\ &\text{A}[:,-1] = -\text{coeffs}\\ &\text{lam, } v = \text{np.linalg.eig}(\text{A})\\ &\text{return lam} \end{split}
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- 1. Which algorithm is implemented in the function above? What role does the parameter coeffs play?
- 2. Which value lam will the function return at coeffs = [-1,0,1]? (No proof needed)
- 3. What would the function return at coeffs = [-1,0,-1]? Can you give a suggestion for improvement, in order to make the function more robust to bad input data?

Solution:

- 1. "coeffs" are the coefficients of a polynomial and the function r finds the roots of the polynomial.
- 2. The corresponding polynomial is $x^2 1$. Hence lam= 1, -1.
- 3. In case of [-1,0,1] we get the same answer. The case of non-normed polynomials should be handled.