1 numbers=left def fun(A, b, theta=.1, m=50): $n = A.shape[1] \times = np.zeros(n)$ for k in range(m): x = x - theta * (A @ x - b) return x

Algorithm 1: Unknown Python code

- 1. Please describe what each line of the code does (please do not write into the pseudocode).
- 2. Which algorithm is implemented, and what is its purpose? Which role does theta play here?

Solution:

1. Description:

```
(1P) 1 Function declaration with input: A, b, \theta := 0, 35, m = 50

(1P) 2 Set n :=  number of rows of A

(1P) 3 Set x := (0, ..., 0)^T \in \mathbb{R}^n

(1P) 4 /

(1P) 5 Start for-loop from k = 0, ..., m - 1

(1P) 6 Update x by x - \theta(Ax - b)

(1P) 7 Output x after m iterations
```

2. The Richardson Iteration is implemented. (1P) It is used to solve a linear system Ax = b iteratively. (1P) θ is preconditioner to assure that $\rho(\underbrace{\theta(I-A)}) < 1$. (2P) iteration matrix