1 Uniqueness of Inverse Matrix

Show that an invertible matrix $A \in \mathbb{F}^{n \times n}$ has exactly one inverse matrix.

solution
Suppose $BA = I_n$

$[=[[=[$ and $AC = I_n$, then

$$B = BI_n = B(AC) = (BA)C = I_nC = C.$$