

# sta210 project

Cole Walker, Madison Griffin

## loading packages & dataset

```
library(tidyverse)
library(tidymodels)
library(readxl)
library(MASS)
library(leaps)
library(caret)
library(glmnet)
library(Stat2Data)
#library(statnnet)
library(lme4)
library(UpSetR)
library(nlme)
library(sjstats)
set.seed(8)
soccer <- read_excel("AllTimeRankingByClub.xlsx")
```

## Introduction and Data

### Data Cleaning

```
soccer = soccer %>%
  rename(goals_for = `Goals For`,
         goals_against = `Goals Against`,
         goal_diff = `Goal Diff`)

soccer = soccer %>%
  dplyr::select(-Pts)
```

```

soccer = soccer %>%
  mutate(winpercentage = Win/Played,
         goalspermatch = goals_for/Played,
         goalsagainstpermatch = goals_against/Played,
         goalmarginpermatch = goal_diff/Played)

soccer = soccer %>%
  mutate(topfiveleague = ifelse(Country == 'ESP' | Country == 'ENG' | Country == 'GER' | C

soccer = soccer %>%
  mutate(points = (Win * 3) + (Draw * 1))

soccer = soccer %>%
  mutate(pointspersmatch = points/Played)

```

## EDA

Plot 1:

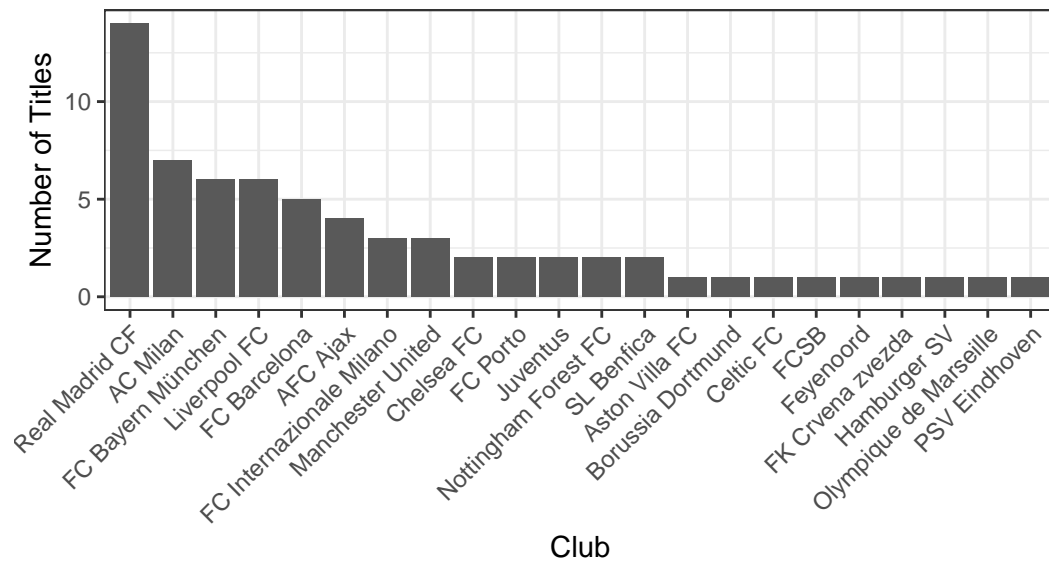
```

soccer %>%
  filter(Titles > 0) %>%
  ggplot(aes(x = reorder(Club, (-Titles)), y = Titles)) +
  geom_bar(stat = 'identity') +
  labs(x = 'Club', y = 'Number of Titles', title = 'Number of Titles for each Club',
       subtitle = 'Excluding Clubs That Have Never Won a Title') +
  theme_bw() +
  scale_x_discrete(guide = guide_axis(angle = 45))

```

## Number of Titles for each Club

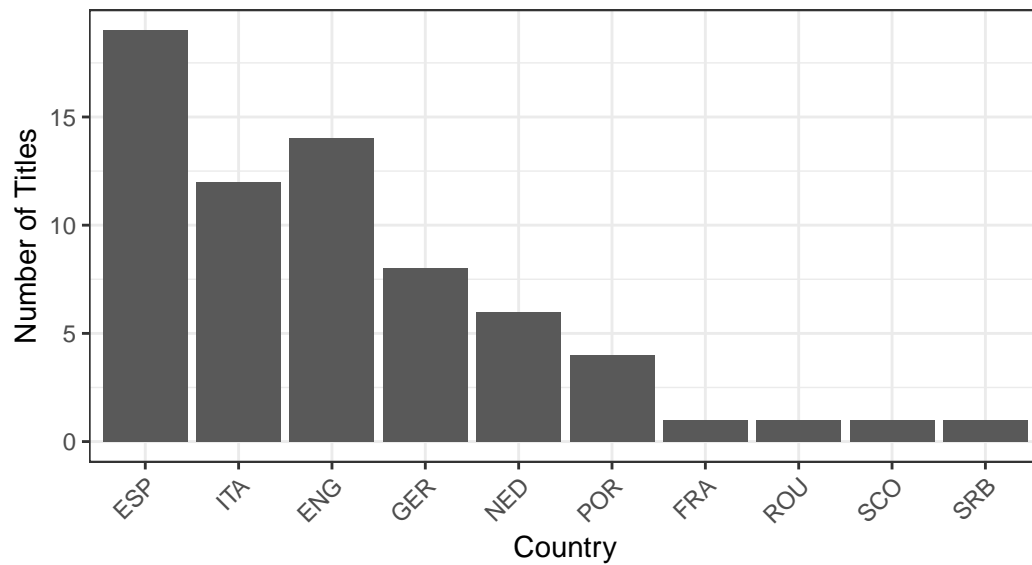
Excluding Clubs That Have Never Won a Title



Plot 2:

```
soccer %>%
  filter(Titles > 0) %>%
  ggplot(aes(x = reorder(Country, (-Titles)), y = Titles)) +
  geom_bar(stat = 'identity') +
  labs(x = 'Country', y = 'Number of Titles', title = 'Number of Titles per Country',
       subtitle = 'Excluding Clubs That Have Never Won a Title') +
  theme_bw() +
  scale_x_discrete(guide = guide_axis(angle = 45))
```

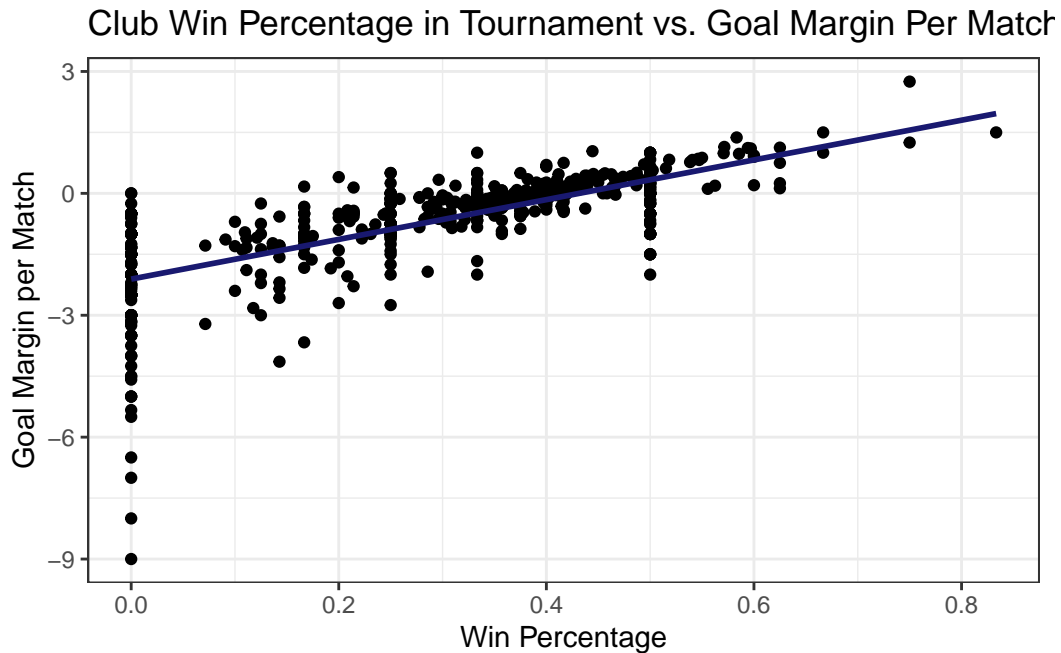
Number of Titles per Country  
Excluding Clubs That Have Never Won a Title



Plot 3:

```
ggplot(data = soccer, aes(x = winpercentage, y = goalmarginpermatch)) +  
  geom_point() +  
  geom_smooth(method = 'lm', se = F, color = 'midnightblue') +  
  labs(x = "Win Percentage", y = 'Goal Margin per Match',  
        title = 'Club Win Percentage in Tournament vs. Goal Margin Per Match') +  
  theme_bw()
```

`geom\_smooth()` using formula = 'y ~ x'



## Methods

we can only do linear or linear mixed effects...expand later

## Variable Selection - LASSO

```
y = soccer$pointspermatch
x = model.matrix(pointspermatch ~ winpercentage + goalspermatch + goalsagainstpermatch +
                  goalmarginpermatch + topfiveleague, data = soccer)
m_lasso_cv = cv.glmnet(x, y, alpha = 1)

best_lambda = m_lasso_cv$lambda.min
best_lambda
```

```
[1] 0.003322683
```

```
m_best = glmnet(x, y, alpha = 1, lambda = best_lambda)
m_best$beta
```

```
6 x 1 sparse Matrix of class "dgCMatix"
      s0
```

```
(Intercept)      .
winpercentage    2.37048724
goalspermatch    .
goalsagainstpermatch .
goalmarginpermatch 0.09665621
topfiveleaguetop five 0.01930645
```

```
bestlasso = lm(pointspermatch ~ winpercentage + goalmarginpermatch + topfiveleague,
               data = soccer)
```

### Variable Selection - Stepwise Selection

```
m_none = lm(pointspermatch ~ 1, data = soccer)
m_all = lm(pointspermatch ~ winpercentage + goalspermatch + goalsagainstpermatch +
           goalmarginpermatch + topfiveleague, data = soccer)
```

### Forward Selection

```
stepAIC(m_none,
        scope = list(lower = m_none, upper = m_all),
        data = soccer, direction = 'forward')
```

```
Start:  AIC=-578.94
pointspermatch ~ 1
```

	Df	Sum of Sq	RSS	AIC
+ winpercentage	1	162.816	14.292	-1910.99
+ goalmarginpermatch	1	111.422	65.686	-1102.63
+ goalspermatch	1	93.665	83.444	-975.81
+ goalsagainstpermatch	1	64.817	112.291	-818.44
+ topfiveleague	1	19.034	158.074	-637.20
<none>			177.108	-578.94

```
Step:  AIC=-1910.99
pointspermatch ~ winpercentage
```

	Df	Sum of Sq	RSS	AIC
+ goalmarginpermatch	1	4.6072	9.6847	-2115.2

```

+ goalsagainstpermatch 1 3.7403 10.5516 -2069.8
+ goalspermatch 1 0.4669 13.8250 -1926.6
+ topfiveleague 1 0.2923 13.9996 -1919.9
<none> 14.2919 -1911.0

```

Step: AIC=-2115.24

```
pointspermatch ~ winpercentage + goalmarginpermatch
```

	Df	Sum of Sq	RSS	AIC
+ topfiveleague	1	0.044462	9.6402	-2115.7
<none>			9.6847	-2115.2
+ goalspermatch	1	0.000047	9.6846	-2113.2
+ goalsagainstpermatch	1	0.000047	9.6846	-2113.2

Step: AIC=-2115.68

```
pointspermatch ~ winpercentage + goalmarginpermatch + topfiveleague
```

	Df	Sum of Sq	RSS	AIC
<none>			9.6402	-2115.7
+ goalspermatch	1	0.00015982	9.6400	-2113.7
+ goalsagainstpermatch	1	0.00015982	9.6400	-2113.7

Call:

```
lm(formula = pointspermatch ~ winpercentage + goalmarginpermatch +
    topfiveleague, data = soccer)
```

Coefficients:

	(Intercept)	winpercentage	goalmarginpermatch
	0.43402	2.37907	0.09770
topfiveleague	0.02556		

```
bestforward = lm(pointspermatch ~ winpercentage + goalmarginpermatch +
    topfiveleague, data = soccer)
```

Backward Selection

```
stepAIC(m_all,
    scope = list(lower = m_none, upper = m_all),
    data = soccer, direction = 'backward')
```

Start: AIC=-2113.69

```
pointspermatch ~ winpercentage + goalspermatch + goalsagainstpermatch +  
goalmarginpermatch + topfiveleague
```

Step: AIC=-2113.69

```
pointspermatch ~ winpercentage + goalspermatch + goalsagainstpermatch +  
topfiveleague
```

	Df	Sum of Sq	RSS	AIC
<none>			9.640	-2113.7
- topfiveleague	1	0.045	9.685	-2113.2
- goalspermatch	1	0.790	10.430	-2073.9
- goalsagainstpermatch	1	3.980	13.620	-1932.5
- winpercentage	1	43.043	52.684	-1215.5

Call:

```
lm(formula = pointspermatch ~ winpercentage + goalspermatch +  
goalsagainstpermatch + topfiveleague, data = soccer)
```

Coefficients:

(Intercept)	winpercentage	goalspermatch
0.43510	2.38121	0.09647
goalsagainstpermatch	topfiveleague	top five
-0.09789	0.02570	

```
bestbackward = lm(pointspermatch ~ winpercentage + goalspermatch + goalsagainstpermatch +  
topfiveleague, data = soccer)
```

Both Selection

```
stepAIC(m_none,  
scope = list(lower = m_none, upper = m_all),  
data = soccer, direction = 'both')
```

Start: AIC=-578.94

```
pointspermatch ~ 1
```

	Df	Sum of Sq	RSS	AIC
+ winpercentage	1	162.816	14.292	-1910.99



+ goalmarginpermatch	1	111.422	65.686	-1102.63
+ goalspermatch	1	93.665	83.444	-975.81
+ goalsagainstpermatch	1	64.817	112.291	-818.44
+ topfiveleague	1	19.034	158.074	-637.20
<none>			177.108	-578.94

Step: AIC=-1910.99

pointspermatch ~ winpercentage

	Df	Sum of Sq	RSS	AIC
+ goalmarginpermatch	1	4.607	9.685	-2115.24
+ goalsagainstpermatch	1	3.740	10.552	-2069.80
+ goalspermatch	1	0.467	13.825	-1926.59
+ topfiveleague	1	0.292	14.000	-1919.94
<none>			14.292	-1910.99
- winpercentage	1	162.816	177.108	-578.94

Step: AIC=-2115.24

pointspermatch ~ winpercentage + goalmarginpermatch

	Df	Sum of Sq	RSS	AIC
+ topfiveleague	1	0.044	9.640	-2115.7
<none>			9.685	-2115.2
+ goalspermatch	1	0.000	9.685	-2113.2
+ goalsagainstpermatch	1	0.000	9.685	-2113.2
- goalmarginpermatch	1	4.607	14.292	-1911.0
- winpercentage	1	56.002	65.686	-1102.6

Step: AIC=-2115.68

pointspermatch ~ winpercentage + goalmarginpermatch + topfiveleague

	Df	Sum of Sq	RSS	AIC
<none>			9.640	-2115.7
- topfiveleague	1	0.044	9.685	-2115.2
+ goalspermatch	1	0.000	9.640	-2113.7
+ goalsagainstpermatch	1	0.000	9.640	-2113.7
- goalmarginpermatch	1	4.359	14.000	-1919.9
- winpercentage	1	54.916	64.556	-1109.8

Call:

lm(formula = pointspermatch ~ winpercentage + goalmarginpermatch +

```
topfiveleague, data = soccer)
```

Coefficients:

```
      (Intercept)      winpercentage      goalmarginpermatch
      0.43402         2.37907         0.09770
topfiveleaguertop five
      0.02556
```

```
bestboth = lm(pointspermatch ~ winpercentage + goalmarginpermatch + topfiveleague, data =
```

### Variable Selection - All Subset

```
soccer_allsub = regsubsets(pointspermatch ~ winpercentage + goalspermatch +
                           goalsagainstpermatch + goalmarginpermatch + topfiveleague,
                           data = soccer,
                           nbest = 1, nvmax = 5)
```

Warning in leaps.setup(x, y, wt = wt, nbest = nbest, nvmax = nvmax, force.in = force.in, : 1 linear dependencies found

Reordering variables and trying again:

```
soccer_allsub
```

Subset selection object

Call: regsubsets.formula(pointspermatch ~ winpercentage + goalspermatch + goalsagainstpermatch + goalmarginpermatch + topfiveleague, data = soccer, nbest = 1, nvmax = 5)

5 Variables (and intercept)

	Forced in	Forced out
winpercentage	FALSE	FALSE
goalspermatch	FALSE	FALSE
goalsagainstpermatch	FALSE	FALSE
topfiveleaguertop five	FALSE	FALSE
goalmarginpermatch	FALSE	FALSE

1 subsets of each size up to 4

Selection Algorithm: exhaustive

```
summary(soccer_allsub)$rsq
```

```
[1] 0.9193042 0.9453179 0.9455690 0.9455699
```

```
summary(soccer_allsub)$which
```

	(Intercept)	winpercentage	goalspermatch	goalsagainstpermatch
1	TRUE	TRUE	FALSE	FALSE
2	TRUE	TRUE	FALSE	FALSE
3	TRUE	TRUE	FALSE	FALSE
4	TRUE	TRUE	TRUE	TRUE

	goalmarginpermatch	topfiveleague	top five
1	FALSE	FALSE	
2	TRUE	FALSE	
3	TRUE	TRUE	
4	FALSE	TRUE	

```
bestallsubset = lm(pointspermatch ~ winpercentage, data = soccer)
```

### Comparing RMSE after variable selection

RMSE All Subset: 0.1642128

**RMSE Best Backward: 0.1348656 - LOWEST**

RMSE Best Both, Forward, Lasso: 0.1348667

(they had the same predictors in it)

CONCLUSION:

- best backward has lowest rmse so better
- predictors: wins per match, top five league, goals per match, goals against per match

```
rmse(bestallsubset)
```

```
[1] 0.1642128
```

```
rmse(bestbackward)
```

```
[1] 0.1348656
```

```
rmse(bestboth)
```

```
[1] 0.1348667
```

```
rmse(bestforward)
```

```
[1] 0.1348667
```

```
rmse(bestlasso)
```

```
[1] 0.1348667
```

## Checking Assumptions

Model 1: Linear Regression

Outcome:

- points per match

Predictors:

- win percentage
- goal margin per match
- top five league

```
linear = lm(pointspermatch ~ winpercentage + goalmarginpermatch + topfiveleague,  
            data = soccer)  
summary(linear)
```

Call:

```
lm(formula = pointspermatch ~ winpercentage + goalmarginpermatch +  
    topfiveleague, data = soccer)
```

Residuals:

Min	1Q	Median	3Q	Max
-0.33632	-0.06813	0.00603	0.06892	0.56598

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	0.434020	0.016755	25.904	<2e-16 ***
winpercentage	2.379068	0.043462	54.739	<2e-16 ***
goalmarginpermatch	0.097704	0.006335	15.423	<2e-16 ***
topfiveleaguertop five	0.025563	0.016412	1.558	0.12

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.1354 on 526 degrees of freedom

Multiple R-squared: 0.9456, Adjusted R-squared: 0.9453

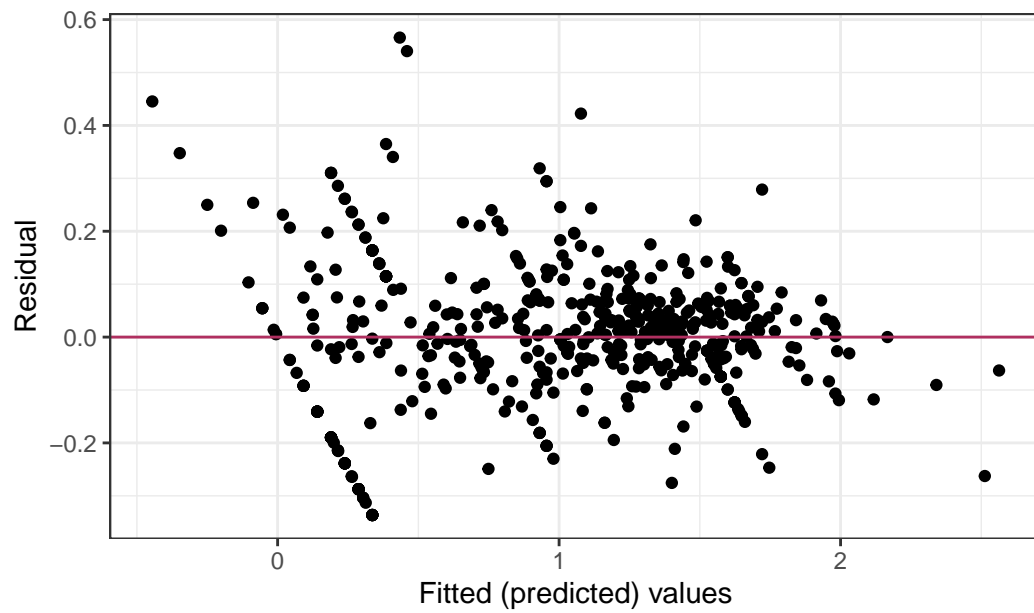
F-statistic: 3046 on 3 and 526 DF, p-value: < 2.2e-16

Conditions for Model 1: Violated linearity, constant variance, and normality

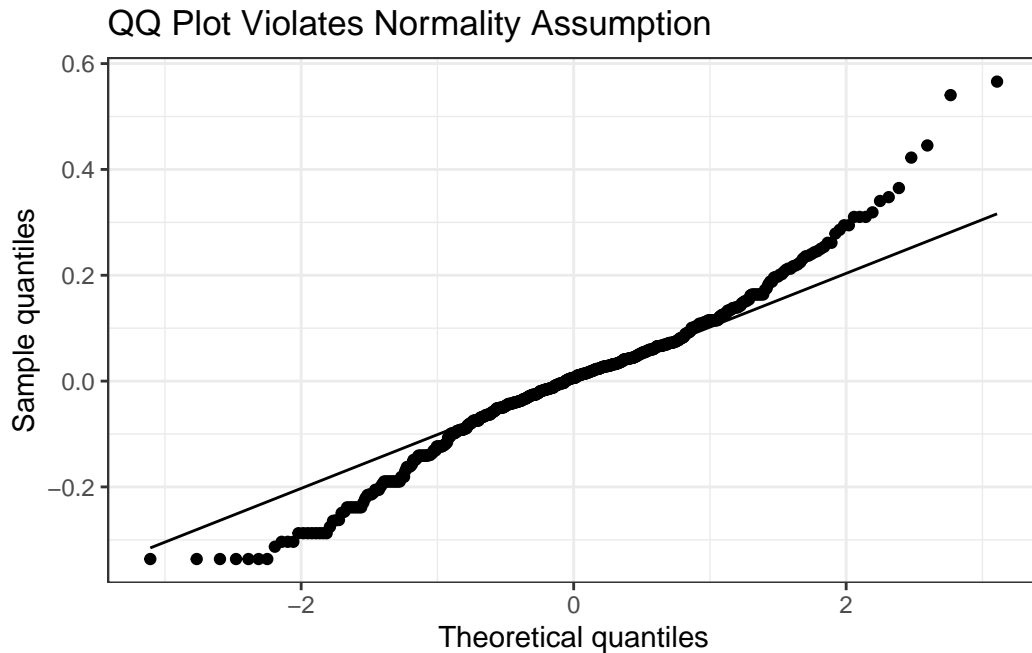
```
linearaug = augment(linear)

ggplot(linearaug, aes(x = .fitted, y = .resid)) +
  geom_point() +
  geom_hline(yintercept = 0, color = 'maroon') +
  labs(x = "Fitted (predicted) values", y = 'Residual') +
  ggtitle('Residual Plot Violates Linearity & Constant Variance Assumptions') +
  theme_bw()
```

Residual Plot Violates Linearity & Constant Variance Assumpt



```
ggplot(linearaug, aes(sample = .resid)) +  
  stat_qq() +  
  stat_qq_line() +  
  theme_bw() +  
  labs(x = 'Theoretical quantiles',  
       y = 'Sample quantiles',  
       title = 'QQ Plot Violates Normality Assumption')
```



Model 2: Linear Mixed Effects Model

Outcome:

- points per match

Predictors:

- win percentage
- goal margin per match
- random intercept for top five league

```
linearmixed = lmer(pointspermatch ~ 1 + winpercentage + goalmarginpermatch +
  (1|topfiveleague), data = soccer)
summary(linearmixed)
```

Linear mixed model fit by REML ['lmerMod']

Formula: `pointspermatch ~ 1 + winpercentage + goalmarginpermatch + (1 | topfiveleague)`

Data: soccer

REML criterion at convergence: -595.8

Scaled residuals:

Min	1Q	Median	3Q	Max
-2.4907	-0.5174	0.0556	0.5114	4.1696

Random effects:

Groups	Name	Variance	Std.Dev.
topfiveleague	(Intercept)	0.0001921	0.01386
Residual		0.0183274	0.13538

Number of obs: 530, groups: topfiveleague, 2

Fixed effects:

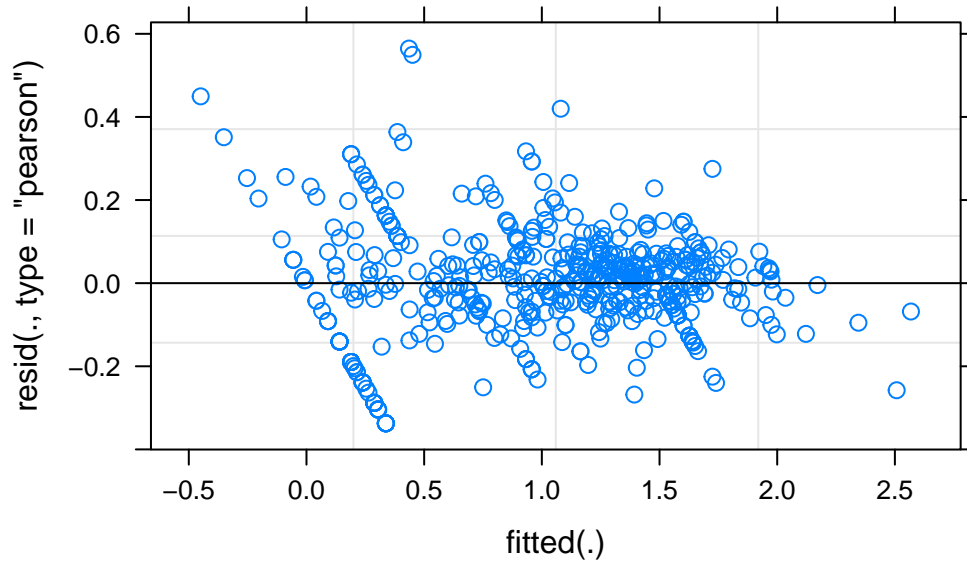
	Estimate	Std. Error	t value
(Intercept)	0.443040	0.019785	22.39
winpercentage	2.382252	0.043345	54.96
goalmarginpermatch	0.098334	0.006304	15.60

Correlation of Fixed Effects:

	(Intr)	wnprcn
winpercentg	-0.780	
glmrnprmtc	0.636	-0.690

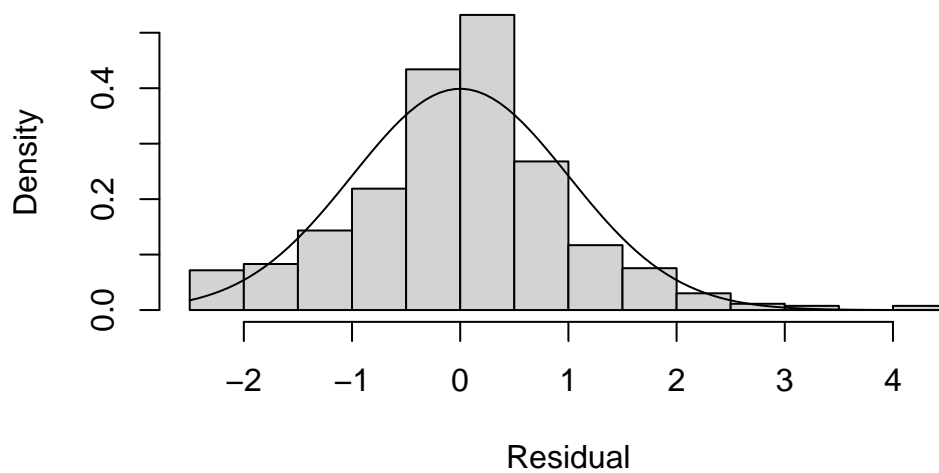
```
plot(linearmixed)
```





```
hist((resid(linearmixed) - mean(resid(linearmixed))) / sd(resid(linearmixed)), xlab = "Residuals", ylab = "Density", main = "Histogram of Residuals")
```

### Histogram of Residuals Violates Normality



Assumptions are worse for mixed effects...moving forward with linear regression

## Results

### FINAL MODEL:

$$y_{ij} = (\gamma_{00} + \mu_{0j}) + \gamma_1 \text{WinPercentage}_{ij} + \gamma_2 \text{TopFiveLeague}_{ij} + \gamma_3 \text{GoalsPerMatch}_{ij} + \gamma_4 \text{GoalsAgainstperMatch}_{ij} + \epsilon_{ij}$$

where

$y_{ij}$  = points per match

$\gamma_1$ : wins percentage

$\gamma_2$ : top five league, 1 = top five

$\gamma_3$ : goals per match

$\gamma_4$ : goals against per match

```
finalmodel = lmer(pointspermatch ~ 1 + winpercentage + goalspermatch + goalsagainstpermatch +
                  (1|topfiveleague), data = soccer)
summary(finalmodel)
```

Linear mixed model fit by REML ['lmerMod']

Formula:

```
pointspermatch ~ 1 + winpercentage + goalspermatch + goalsagainstpermatch +
  (1 | topfiveleague)
```

Data: soccer

REML criterion at convergence: -589.3

Scaled residuals:

Min	1Q	Median	3Q	Max
-2.4908	-0.5166	0.0546	0.5113	4.1647

Random effects:

Groups	Name	Variance	Std.Dev.
topfiveleague	(Intercept)	0.0001943	0.01394
	Residual	0.0183620	0.13551

Number of obs: 530, groups: topfiveleague, 2

Fixed effects:

Estimate	Std. Error	t value
----------	------------	---------

(Intercept)	0.443476	0.023240	19.082
winpercentage	2.383025	0.049148	48.487
goalspermatch	0.097878	0.014635	6.688
goalsagainstpermatch	-0.098400	0.006629	-14.843

Correlation of Fixed Effects:

	(Intr)	wnprcn	glsprm
winpercentg	-0.342		
goalsprmtch	-0.237	-0.687	
glsgnstprmt	-0.676	0.436	-0.134

## Conclusion