

# **AA 279 D – SPACECRAFT FORMATION- FLYING AND RENDEZVOUS: LECTURE 1**

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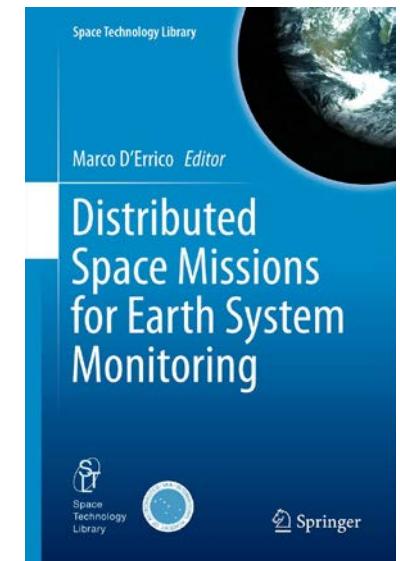
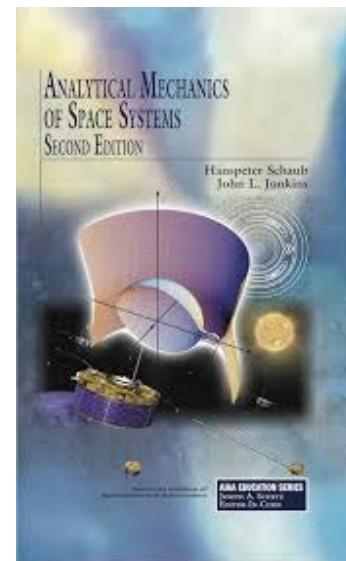
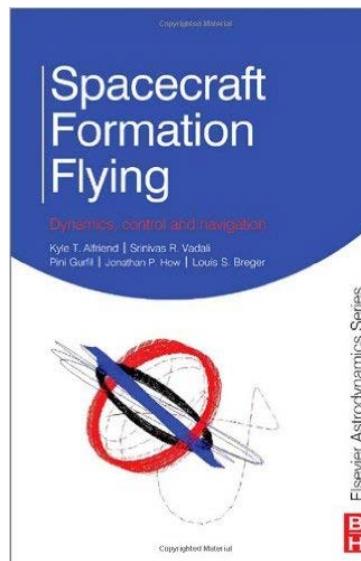
Prof. Simone D'Amico

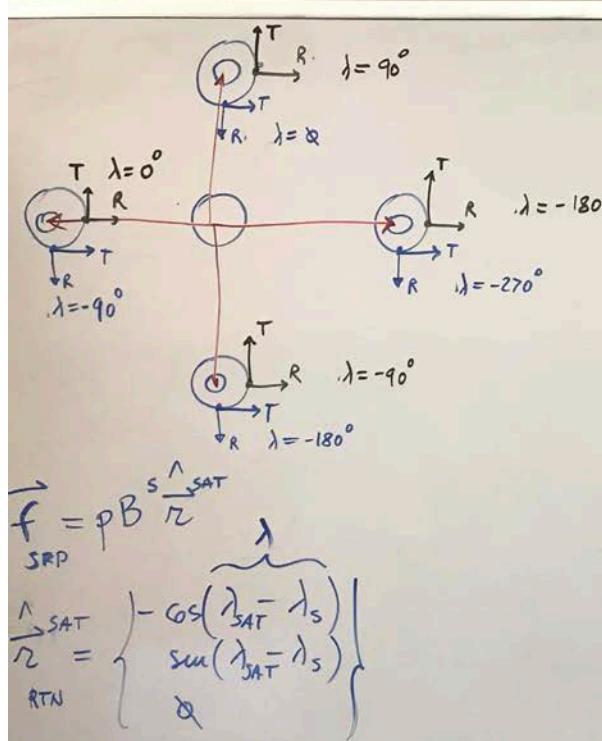
Stanford's Space Rendezvous Laboratory (SLAB)



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- Course Introduction
- Distributed Space Systems
- Highlights from Missions and Needs
- Textbooks





G.V.E.

$$\frac{d\alpha_c}{dt} = \frac{2\alpha_c^2 v_c}{\mu} f_{SRP_T} = \frac{2\alpha_c^2 v_c}{\mu} \rho B_c \sin \lambda_c$$

$$\frac{d\alpha_d}{dt} = \frac{2\alpha_d^2 v_d}{\mu} f_{SRP_T} = \frac{2\alpha_d^2 v_d}{\mu} \rho B_d \sin \lambda_d$$

$$\Delta \dot{a} = \frac{d\alpha_d}{dt} - \frac{d\alpha_c}{dt}$$

$$\boxed{\Delta \dot{a}} = \frac{2\rho}{\mu} (B_d - B_c) \left( \underbrace{\alpha_d^2 v_d \sin \lambda_d - \alpha_c^2 v_c \sin \lambda_c}_{\sin(\lambda_c + \Delta \lambda)} \right) \approx$$

$$\sin(\lambda_c + \Delta \lambda) = \sin \lambda_c \cos \Delta \lambda + \cos \lambda_c \sin \Delta \lambda \approx$$

$$\approx \sin \lambda_c + \Delta \lambda \cos \lambda_c \quad \Delta \lambda \ll 1$$

$$\approx \frac{2\rho}{\mu} (B_d - B_c) \left[ (\alpha_d^2 v_d - \alpha_c^2 v_c) \sin \lambda_c + \alpha_d^2 v_d \Delta \lambda \cos \lambda_c \right] = \text{PHASOR}$$

$$= \frac{2\rho}{\mu} (B_d - B_c) \sqrt{(\alpha_d^2 v_d - \alpha_c^2 v_c)^2 + (\alpha_d^2 v_d \Delta \lambda)^2} \sin(\lambda_c + \phi)$$

$$\phi = \arctan \left( \frac{\alpha_d^2 v_d \Delta \lambda}{\alpha_d^2 v_d - \alpha_c^2 v_c} \right)$$

AMPLITUDE

PHASE

NEAR CIRCULAR ORBIT

$$\alpha_c^2 v_c = \alpha_c^3 n_c = \alpha_c^3 \sqrt{\frac{\mu}{a_c^3}} = \sqrt{\mu a_c^3}$$

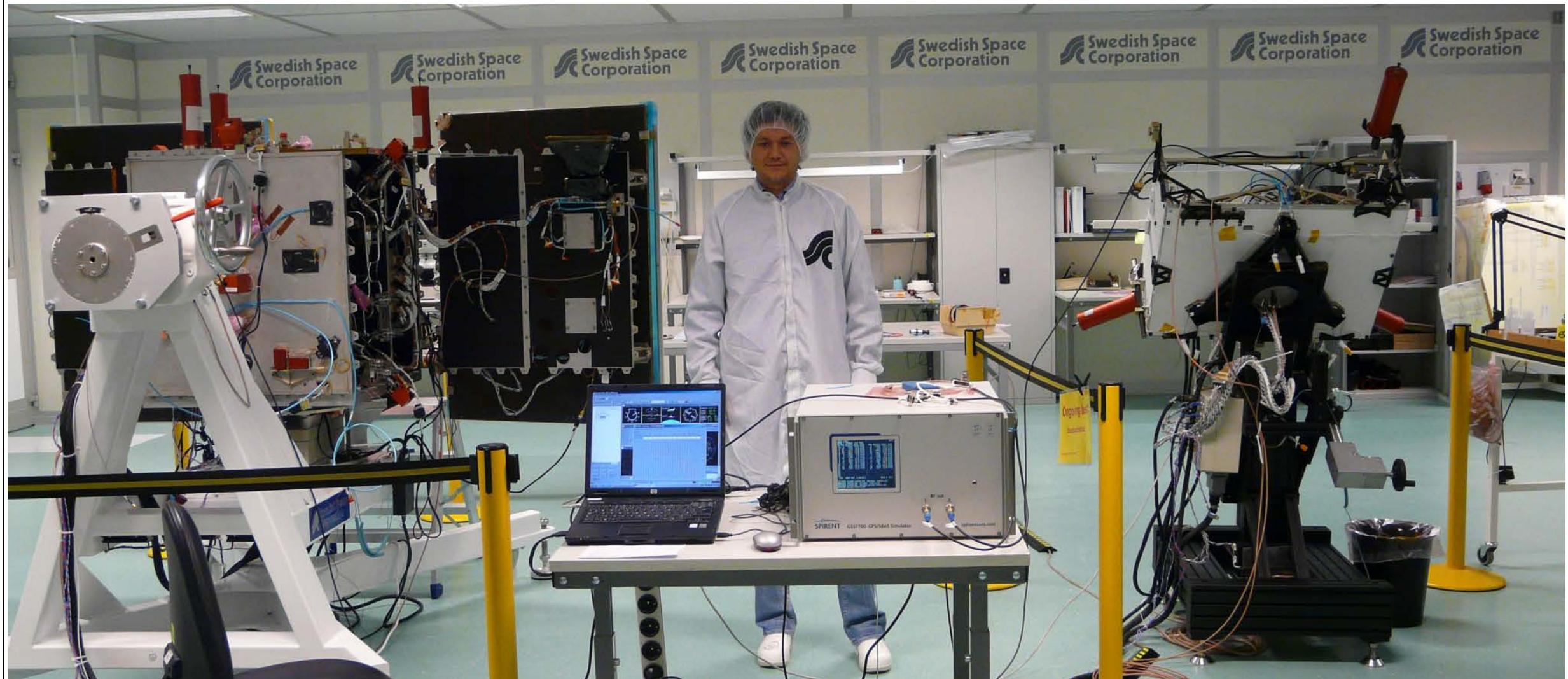
$$\alpha_d^2 v_d = \sqrt{\mu} (a_c + \Delta a)^{3/2} = \sqrt{\mu a_c^3} \left( 1 + \frac{3}{2} \frac{\Delta a}{a_c} \right) \quad \frac{\Delta a}{a_c} \ll 1$$

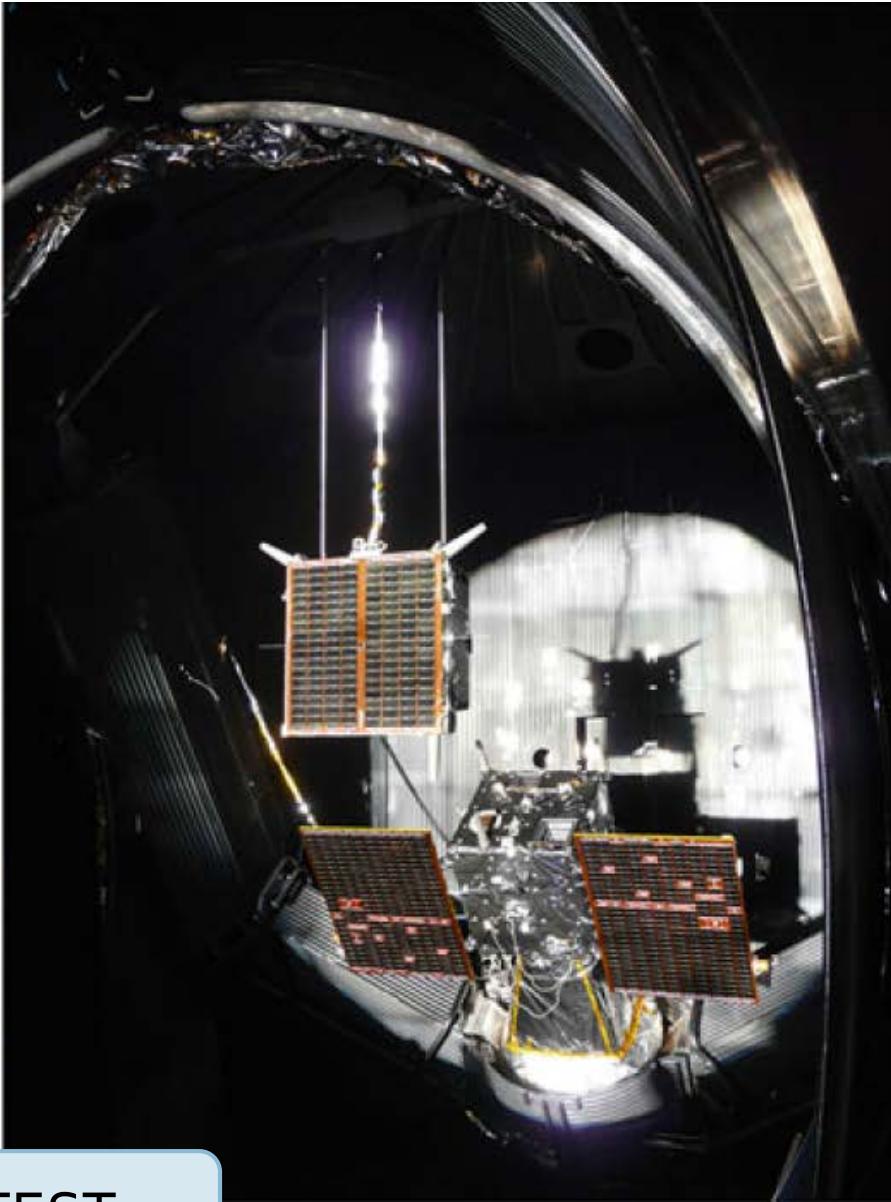
$$\boxed{\Delta a \stackrel{K}{\sim} \frac{3\rho a_c}{m \sqrt{\mu}} (B_d - B_c) \sqrt{\Delta a + \frac{\alpha_c^2 \Delta \lambda}{2}}} \sin(\lambda_c + \phi)$$

$$\phi = \arctan \left( \frac{2}{3} \frac{\alpha_c \Delta \lambda}{\Delta a} \right)$$

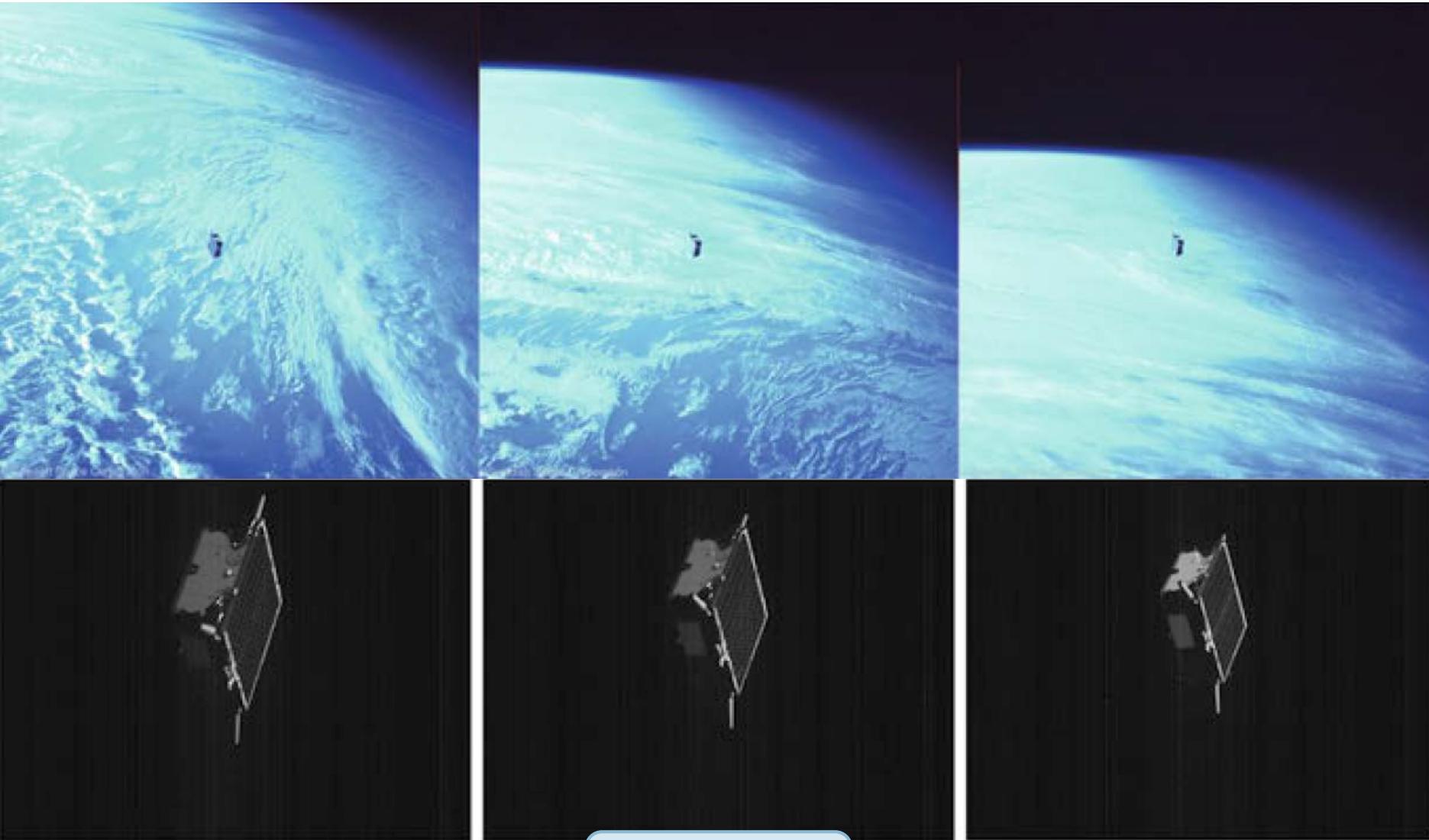
$$\Delta a(\lambda) = \frac{c^2}{4} - K \frac{c}{2} \cos(\lambda) + \frac{K^2}{4} \cos^2(\lambda) + \phi$$

ANALYSE





TEST

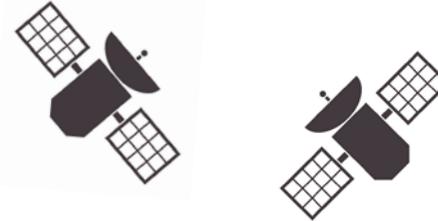


FLY

# Mission Statement

“The goal of SLAB is to enable future (**miniature**) distributed space systems (DSS). DSS are made of two or more spacecraft that **interact** to meet **objectives** otherwise very difficult to achieve”

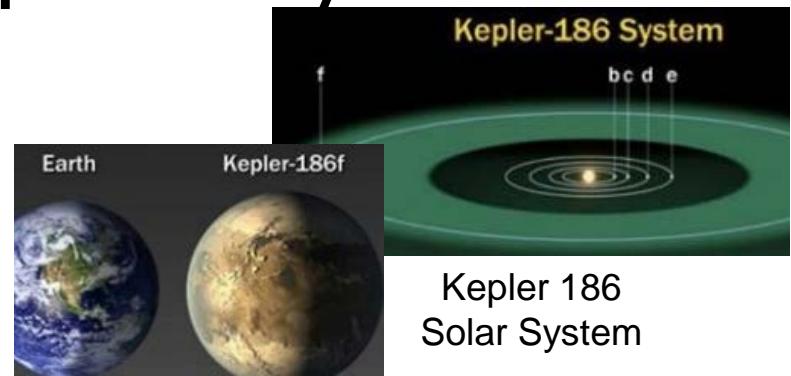
Simone D'Amico, 12/01/2013



# Objectives of Distributed Space Systems

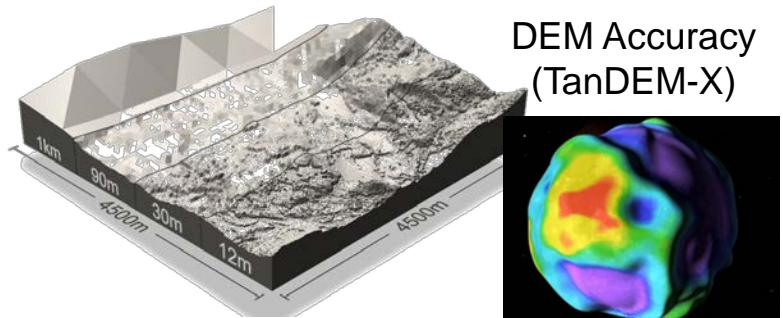
- Space Science

- Astronomical search for origins (exoplanets)
- Solar system exploration (asteroids)
- Structure and evolution of the universe (gravitation)



- Planetary Science

- Synthetic aperture radar interferometry
- Gravity and shape mapping
- Atmosphere and magnetosphere characterization

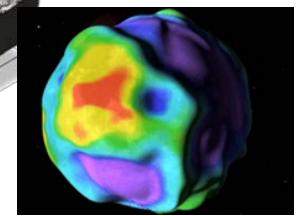


- Technology

- Human exploration technology
- On-orbit servicing and assembly
- Development of space infrastructure



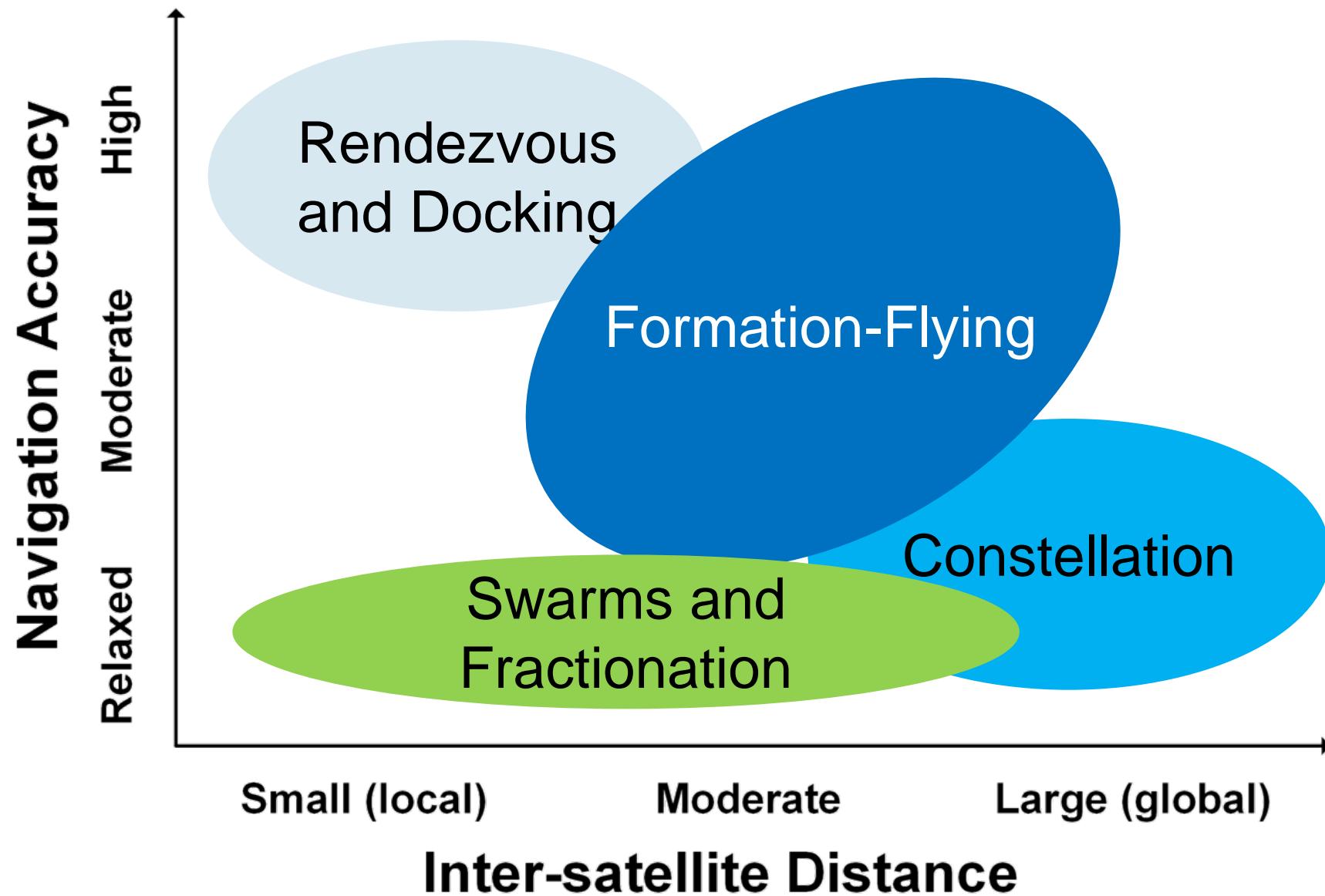
DEM Accuracy  
(TanDEM-X)



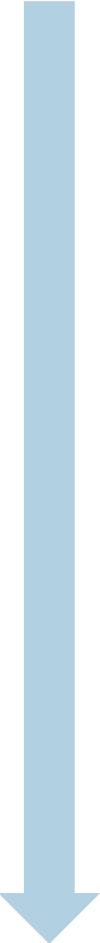
Moon gravity  
(GRAIL)

Autonomous  
approach to the ISS  
(HTV)

# Interaction of Distributed Space Systems



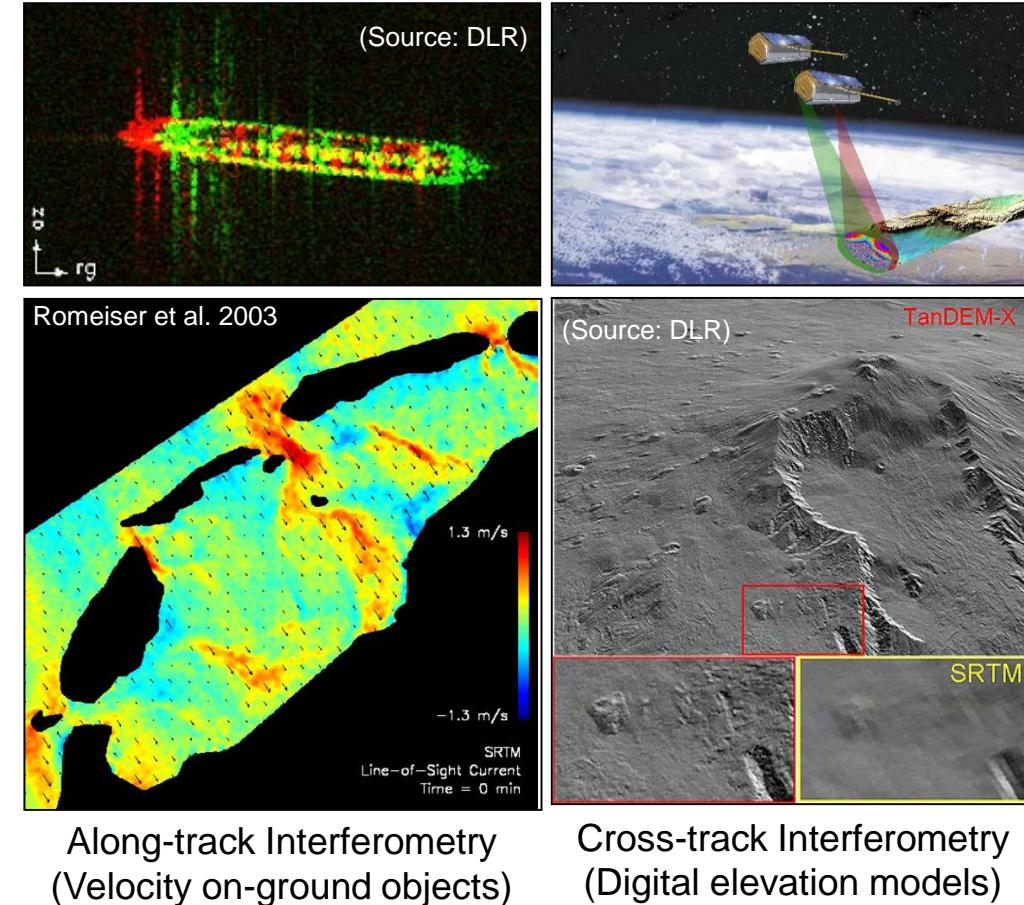
# Distributed Space Systems are NOT New

- 
- Historic milestones
    - Short duration
    - Ground-control
    - Blank checks
  - Contemporary
    - Long duration
    - Autonomy
    - Cost constraints
  - Future
    - Miniaturization
    - Distribution
    - Standardization

Type	Involved	Year
First FF experiment	Gemini 6A & 7	1965
First automated docking	Kosmos 186 & 188	1967
RvD at other celestial bodies	Columbia & Eagle	1969
RvD with vehicles from 2 nations	Apollo & Soyuz	1975
RvD of 3 “objects”	D.Gardner, Weststar VI, Discovery	1984
Collision due to FF	Progress & MIR	1997
Autonomous FF	ETS-7	1998
Autonomous microsatellite RvD	XSS-11 & Minotaur 4th stage	2005
Collision due to RvD	DART & MUBLCOM	2005
First on-orbit servicing demo	Orbital Express	2007
Fully autonomous docking	ATV & ISS	2008

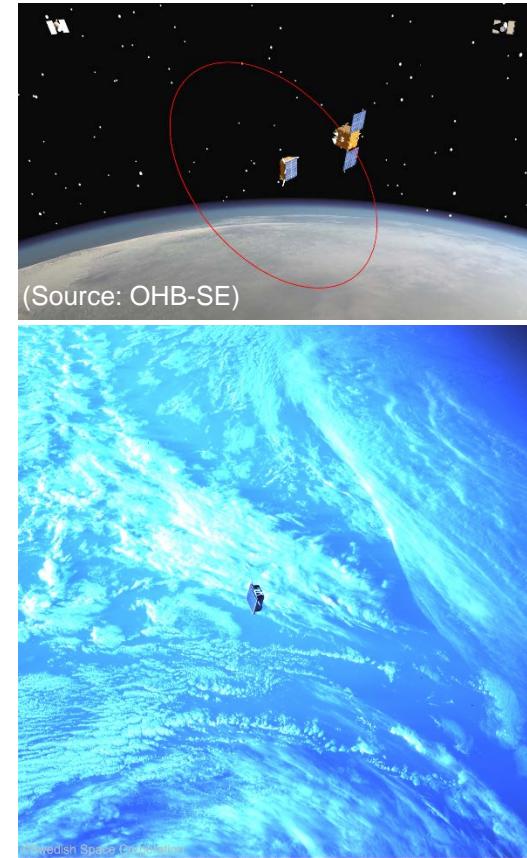
# TanDEM-X

- Scope
  - Global Level-3 DEM  
(2m height, 12m pixel)
  - Local Level-4 DEMs
  - Innovative SAR techniques
- Mission Profile
  - Dual SAR satellites  
(TSX&TDX)
  - Formation flying  
(close&wide)
  - Launch 2007/2010
  - > 3 years overlap



# PRISMA

- Two microsatellites (Mango, Tango)
  - Launch 2010 (Dnepr from Yasny)
  - Presently in extended mission phase
- GNC software experiments
  - Autonomous formation flying (5 km – 20 m)
  - Homing and rendezvous (< 50 km)
  - Proximity operations (100 m – 0 m)
- GNC hardware experiments
  - Green propellant & Micro-propulsion
  - GPS (DLR), FFRF (CNES), VBS (DTU)



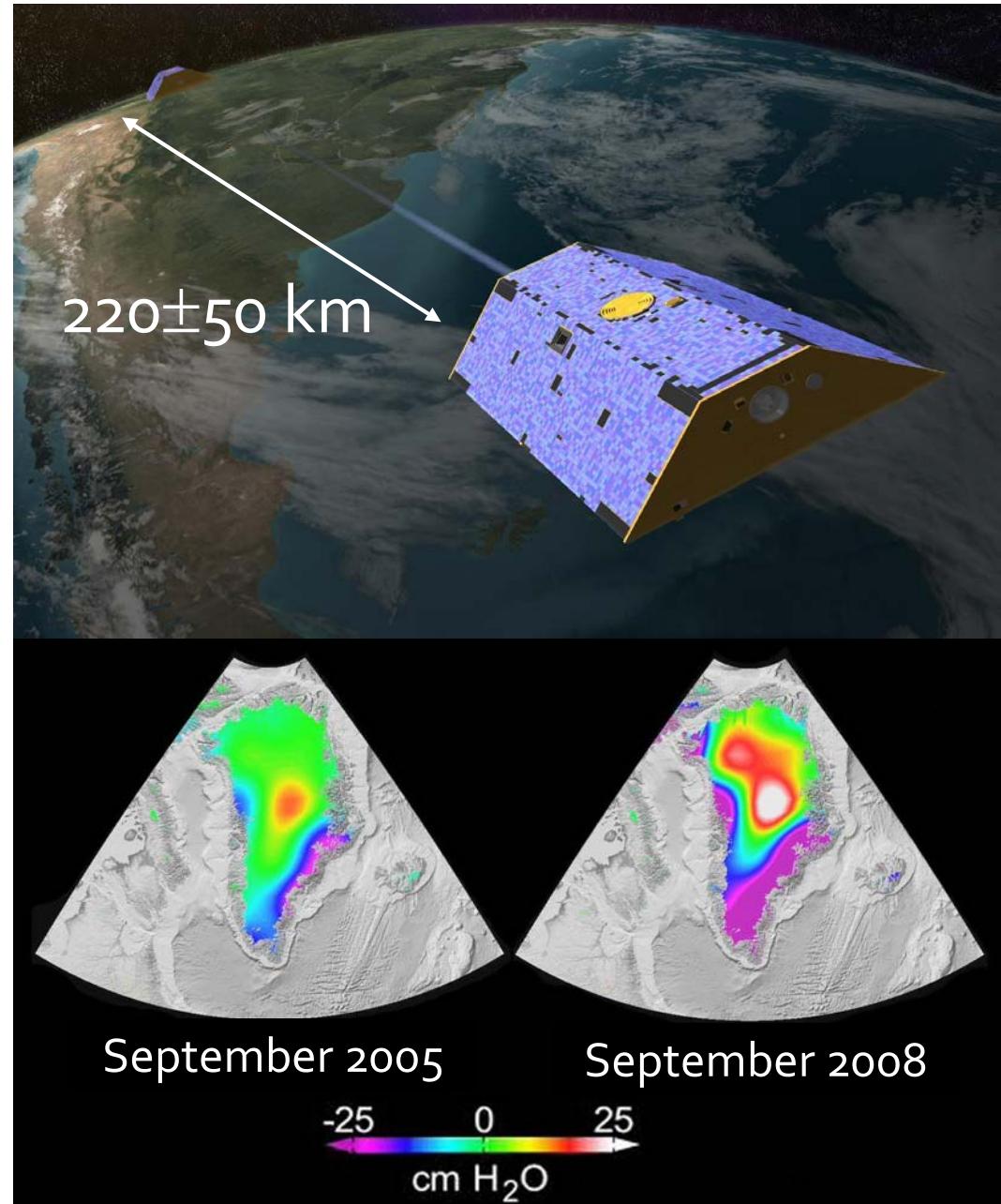
Fly around  
March 27, 2011

# PRISMA (Close-In Inspection Experiment – 2 m)



# GRACE

- GRACE twin satellites, Tom and Jerry, launched in 2002, to be replaced by the GRACE-FO
- Relative motion represents the total differential forces acting on the formation (measured by k-band radar)
- Non-conservative forces measured by precision accelerometers
- Besides understanding the planet-dynamics system, GRACE gravity field models are used every day for precise orbit determination and prediction around the world
- Flight dynamics requirements:  $220\pm50$  km separation, longitude swap maneuver required

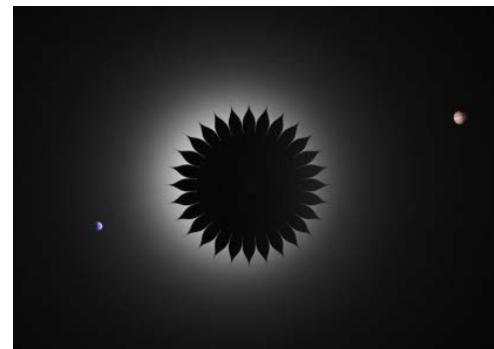
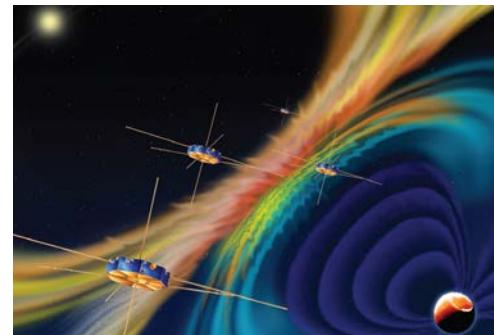


# PROBA-3 (Mission Objectives and Scenario)

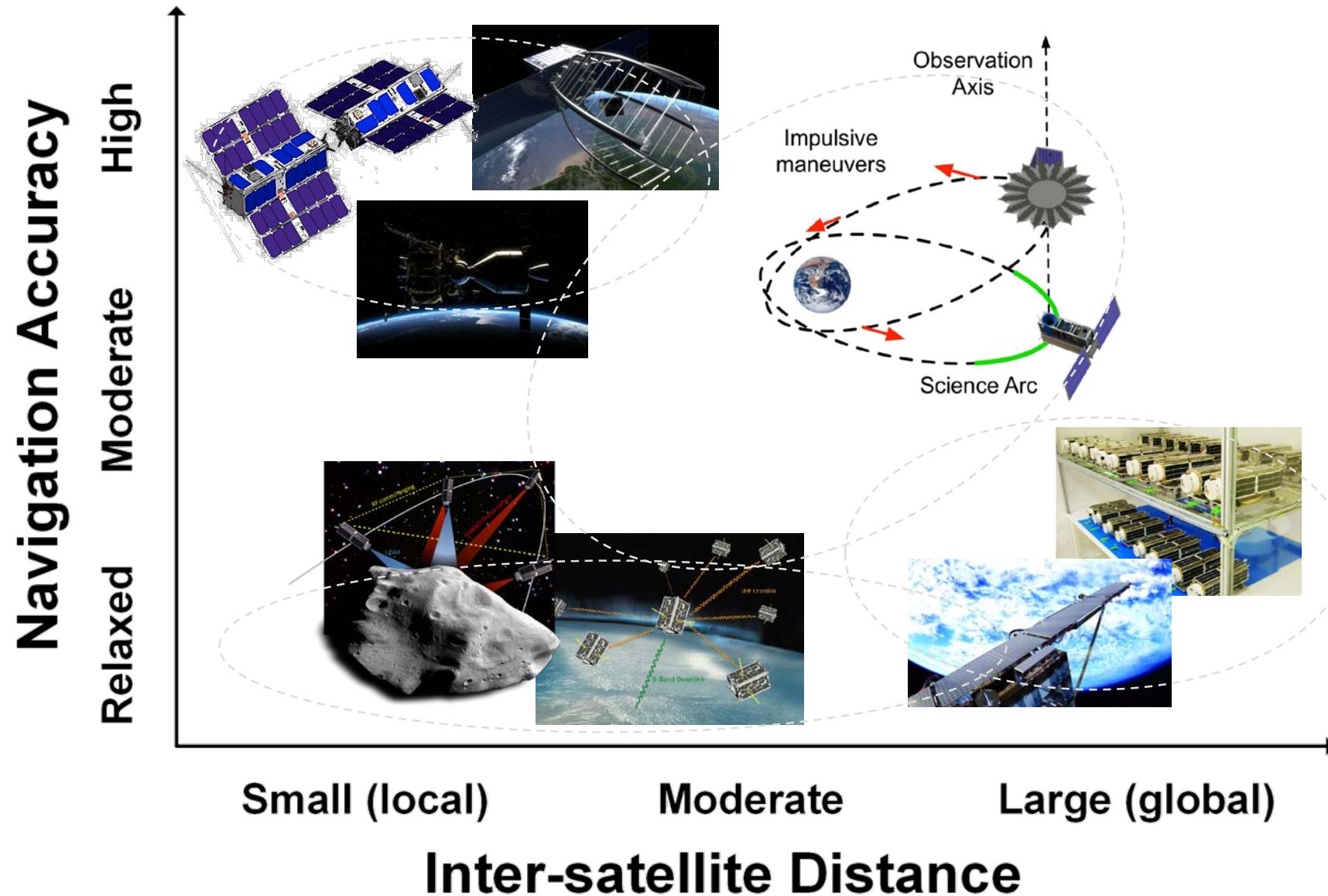


# Other Flagship Missions (NASA/ESA)

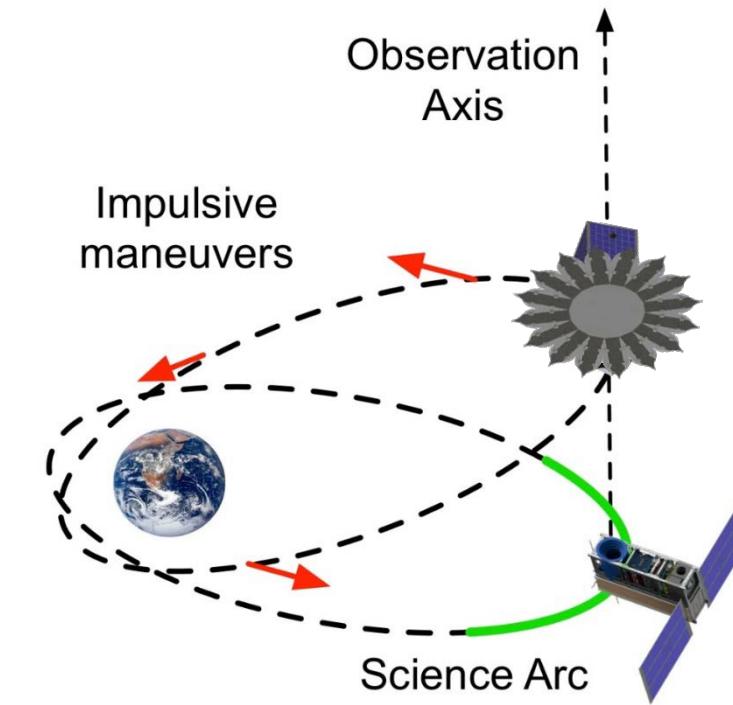
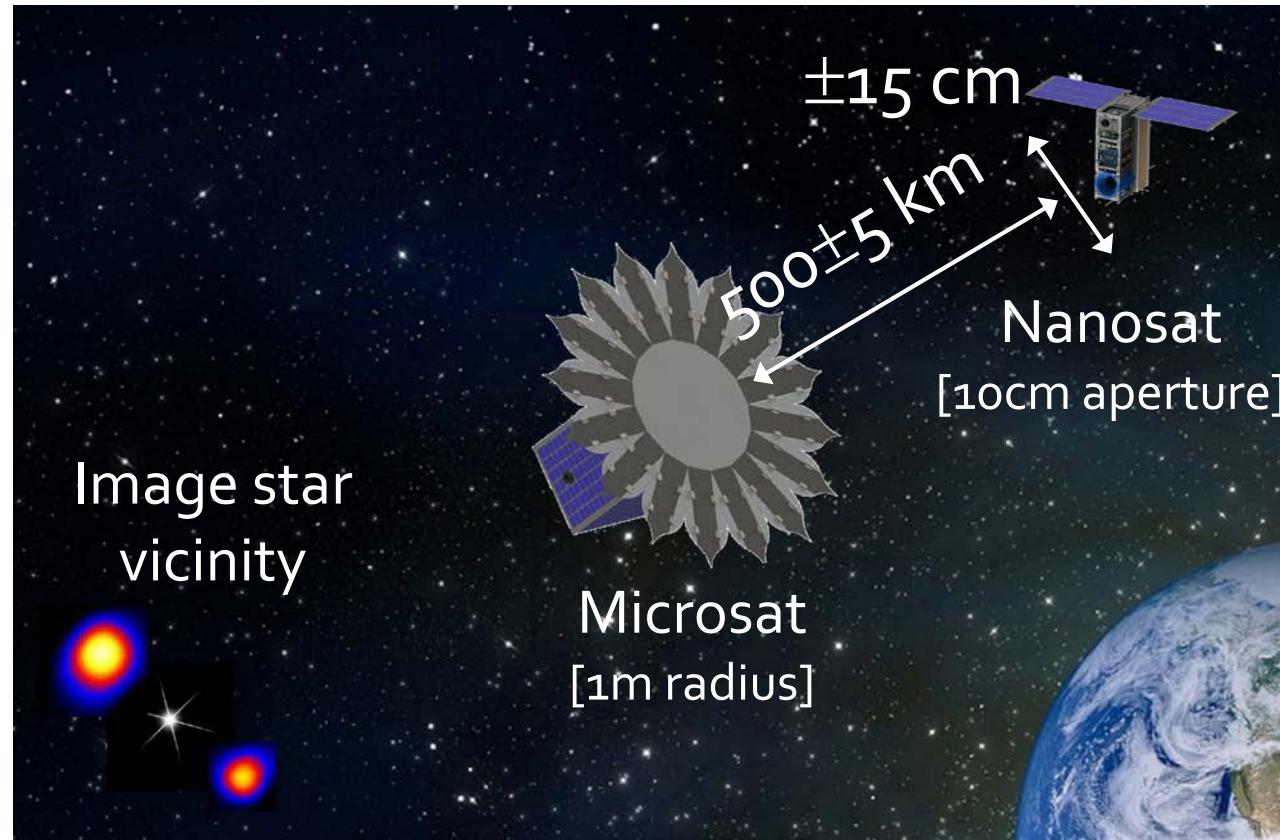
- Laser Interferometer Space Antenna (LISA)
  - Detect and measure gravitational waves
  - Equilateral triangle with arm length of 5M km
  - Precisely tracked free-floating proof masses
- Magnetospheric Multiscale Mission (MMS)
  - Understand magnetic reconnection
  - Variably spaced tetrahedron (1 km to several Earth radii)
  - Electron and ion plasma spectrometers
- New Worlds Observer (NWO)
  - Discover and directly image Earth-like planets
  - Telescope+Starshade at 50K km distance
  - Diffraction limited telescope in visible band



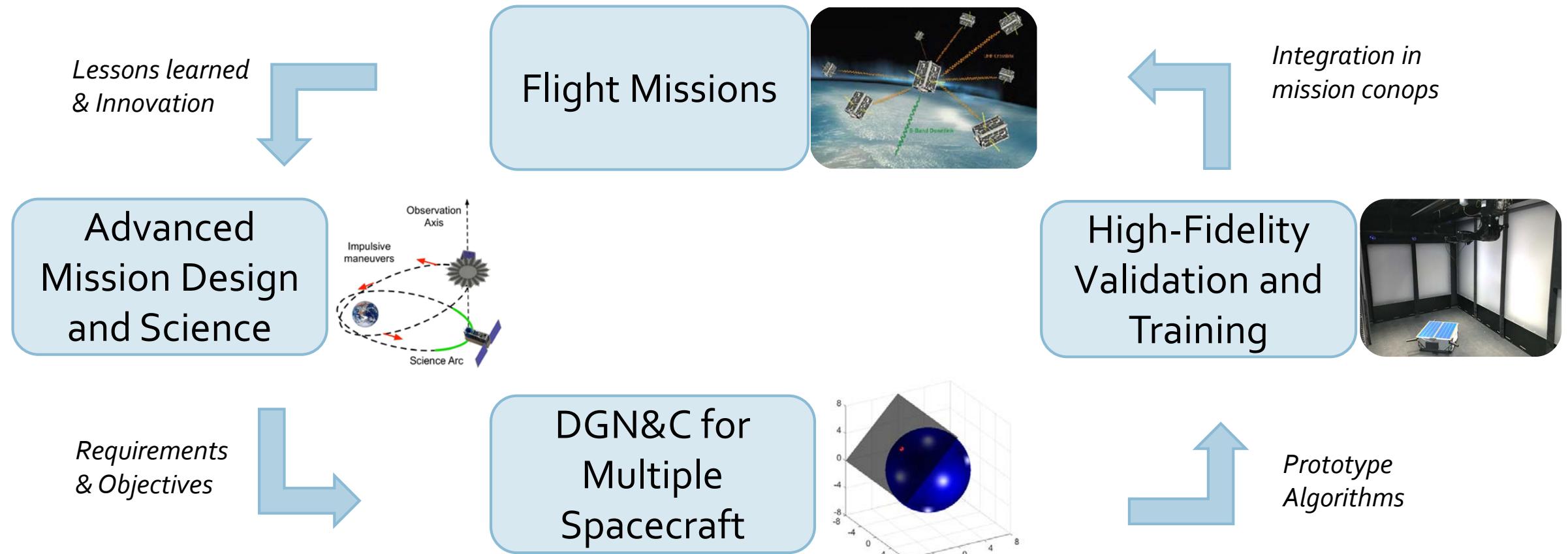
# Miniature Distributed Space Systems



# Can a miniaturized Distributed Occulter/Telescope (mDOT) image exoplanets from Earth's orbit?

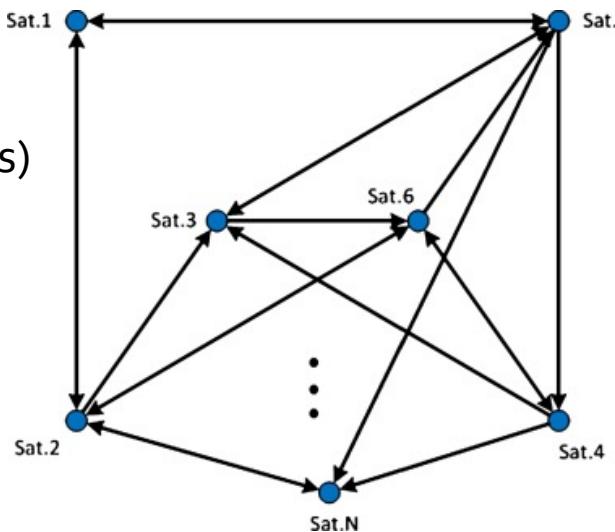


# Research Pillars



# Coordination Approaches

- Orbit tracking
  - Similar to single satellite missions
  - Each satellite in the formation is controlled to a particular desired orbit
  - No cooperation required, but does not exploit coupled nature (more maneuvers)
- Leader/Follower
  - Leader controlled to reference orbit
  - Follower(s) controlled w.r.t. leader
  - Satellites follow natural dynamics of absolute orbit of leader
  - Fuel usage is not balanced because leader controls its absolute motion only
- Virtual structure
  - Fitting desired states of formation so to minimize overall state error
  - State error pertain all the satellites in the formation
  - Fuel usage can be balanced methodically
- Swarming
  - Simple heuristic laws to arrange many satellites based on local info
  - Easily scale to arbitrary number of vehicles without large computation and communication burdens
  - Typically not fuel optimal and rarely guarantee collision avoidance



# Fuel-Use Drivers

- Primary concern in the design of any spacecraft controller
- Minimizing fuel use is critical in any space mission, since fuel is expensive to launch and non-replenishable
- Keeping formation from drifting apart and achieving science requirements at the same time is generally more expensive than single spacecraft control
- Typical fuel-use drivers in a spacecraft formation are
  - Mission requirements
  - Initial conditions
  - Navigation uncertainty
  - Actuation errors
  - Dynamical process noise
  - Algorithms



# Control Approaches

- Although many formation control strategies are proposed in the literature
  - Proportional-derivative (PD)
  - Linear quadratic regulation (LQR)
  - Linear matrix inequalities (LMI)
  - Lyapunov
  - Rapidly exploring random trees (RRT)
  - Model predictive control (MPC)
- Thrusting schemes which exploit the inversion of the state transition matrix remains the most commonly used in practice because of their
  - Impulsive nature
  - Determinism
  - Simplicity
  - Higher technology readiness level

$$\sum_{i=0}^{\infty} \frac{x}{2^i}$$

Numerical

$$10000 \sum_{i=0}^{\infty} \frac{x}{2^i}$$

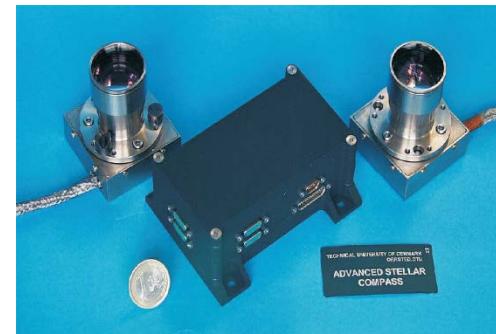
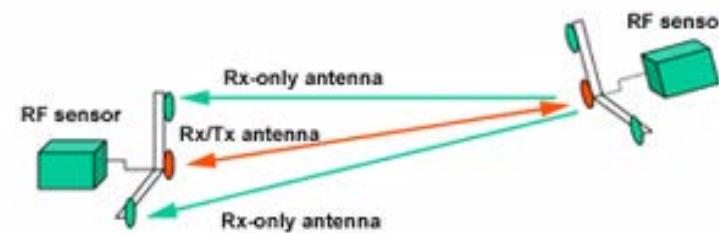
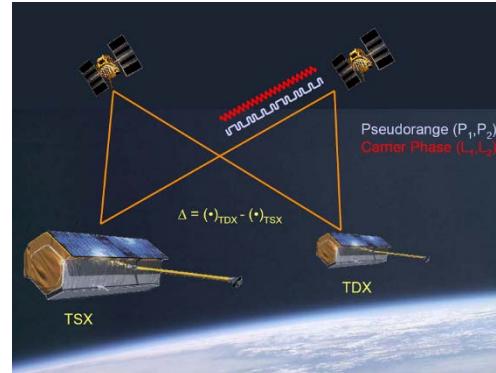
Closed-form

2x

Solution

# Navigation Approaches

- GPS/GNSS
  - Cooperative, rely on GNSS constellation
  - Phase difference = Projected baseline + bias
  - Ambiguity resolution
- Radio Frequency
  - Cooperative, self-contained
  - Pseudolites provide GPS like signals
  - Applicable for deep space navigation
- Vision-Based
  - (Non-)Cooperative, optical/infrared
  - High dynamics range: far- to short-range
  - Support angles-only to full pose estimation



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