

# Take Me Out to (Analyze) the Ballgame

## Visualization and Analysis Techniques for Big Spatial Data

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## Contents

<b>1 Shiny Heat Map Confidence Intervals</b>	<b>1</b>
1.1 Generalized Linear Model for Hitter Success Probabilities . . . . .	1
1.1.1 Biomechanically Interpretable Covariates . . . . .	2
1.1.2 Generalized Linear Model with Biomechanically Interpretable Covariates . . . . .	3
1.1.3 Hosmer-Lemeshow Goodness of Fit Test . . . . .	4
1.2 Heat Map Confidence Intervals . . . . .	4
1.2.1 Current Best Practices . . . . .	5
1.2.2 Shiny Innovation . . . . .	6
1.3 Appendix: ShinyHMCI, An R Package . . . . .	9

## 1 Shiny Heat Map Confidence Intervals

### 1.1 Generalized Linear Model for Hitter Success Probabilities

As one of our research goal, we aim to create a statistical model for the heat map of success probabilities. Nonparametric methods, while straightforward, sacrifice interpretability; they achieve a modeled heat map, but without contextually interpretable components. Nonparametric models cannot relate spatially varying hitter success probabilities to hitter attributes. We propose a parametric approach using biomechanically interpretable covariates. Existing research analyzes the biomechanics of the baseball swing [Welch et al., 1995], but no research integrates those results with spatial swing outcomes in a statistical model.

Let success indicator variable,  $Y_{ijklm}$ , be a Bernoulli random variable with spatially varying mean [Sheldon et al., 2002]. Subscript  $i = 1, \dots, n_{jklm}$  indexes hitter  $j$ 's swings in at bat  $k$  against pitcher  $l$  in year  $m$ . Subscript  $k = 1, \dots, n_{jlm}$  indexes hitter  $j$ 's at bats against pitcher  $l$  in year  $m$ . Subscript  $l = 1, \dots, n_{jm}$  indexes pitchers hitter  $j$  faced, where  $n_{jm}$  is the total number of pitchers hitter  $j$  faced; and  $m = 2007, \dots, 2016$  indexes year. Let  $\mathbf{s}_{ijkl} = (px_{ikl}, pz_{ijkl}) \in \mathbf{D} \subseteq \mathbf{R}^2$  be the horizontal and vertical locations, respectively, of pitch  $ijkl$  as it passes through the two dimensioned vertical face of the hitting zone. The origin,  $\mathbf{s}_\cdot = (0, 0)$ , is the midpoint of the front edge of home plate, at ground level. From the pitcher's point of view, pitches to the left (right) of the center of home plate correspond to negative (positive) values of  $px..$ . Pitches that bounce before reaching home plate correspond to negative values of  $pz..$ .

In this study we make the simplifying assumption that location success probabilities depend on only location and hitter. This means we dispense with subscripts  $k, l$ , and  $m$ . We also assume that, given pitch location to hitter  $j$ ,  $\mathbf{s}_{ij} = (px_{ij}, pz_{ij})$ , swings are independent Bernoulli trials. This gives  $Y_{ij}|\mathbf{s}_{ij} \sim \text{Bernoulli}(p_{ij})$ , where  $E[Y_{ij}|\mathbf{s}_{ij}] = p_{ij}$

Accordingly, let  $i = 1, \dots, n_j$  index hitter  $j$ 's swings, out of  $n_j$  total swings on record. Let  $\mathbf{X}_{ij}(\mathbf{s}_{ij})$  be covariates specific to hitter  $j$  and location  $\mathbf{s}_{ij}$  on swing  $i$ . A Bernoulli random variable suggests a generalized linear model with logit link function for relating success probability to covariate information:

$$\text{logit}(p_{ij}|\mathbf{X}_{ij}(\mathbf{s}_{ij})) = \mathbf{X}_{ij}(\mathbf{s}_{ij})\boldsymbol{\beta}_j, \quad (1)$$

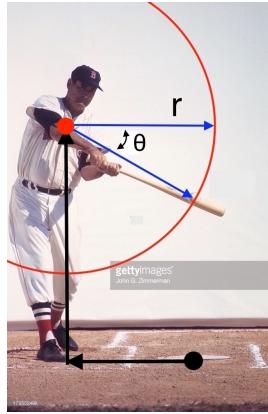
where  $\boldsymbol{\beta}_j$  is the vector of covariate coefficient parameters specific to hitter  $j$  [Myers et al., 2012]. Next, we discuss and develop covariates.

### 1.1.1 Biomechanically Interpretable Covariates

Why does Peralta, and why do hitters in general, hit pitches in some locations better than others? We submit biomechanics as potentially part of the answer. Biomechanics underpin why hitters prefer some pitch locations more than others. Given the choice, athletes select a specific place for the ball before swinging. Consider golf, a sport where the ball is stationary, and the acting athlete chooses where to stand in relation to the ball. In fact, golfers position themselves very precisely in relation to the ball to achieve impact at the optimal point in their swing [Cochran and Stobbs, 2005]. If the impact point deviates from the ideal location, performance suffers. Consider tennis, a step closer to baseball, in that the ball approaches, but the player has time to position himself relative to the incoming ball. Once again, tennis players strive to hit the ball at a specific point in their forehand, a precise distance from the ground and from their body

[Elliott, 2006]. As with golf, if the point of impact deviates from this location, performance suffers. Note that in both sports the ideal player to ball positioning depends on, at the very least, anatomy, biomechanics, and equipment. We submit the same dynamics affect baseball hitting. However, in baseball the hitter cannot predetermine ball location, nor does he have time to reposition himself in response to the location and trajectory of the incoming pitch. For these reasons, meaningful measurements of hitter to ball distance and angle are reasonable covariates. Polar coordinate pitch locations would inherently provide this type of meaningful covariate for use and interpretation in our models.

To illustrate, in Figure 3 we shift the origin to a hitter’s approximate center of gravity in his stance, where the extended bat line intersects his axis of rotation at the moment of contact [Welch et al., 1995].



**Figure 1:** The ground level black dot represents the origin  $(0,0)$  in the rectangular coordinate system. The translated origin (red dot) coincides with the hitter’s approximate center of gravity, and thus the polar origin. The bold arrows show the origin shift. The length of the arrows moving out from his center of gravity to specific grid locations represent  $r$ , and the angle between the same two arrows represent  $\theta$ .

Referring to Figure 3, let  $r$  measure the distance from the hitter’s center of gravity to the ball at impact, and let  $\theta$  be the angle below horizontal of the line segment connecting the center of gravity and the ball at impact. As in golf and tennis, ball location—too far/close to the hitter, or above/below the ideal point of impact— affects hitting performance. Letting  $\mathbf{X}_{ij}(\mathbf{s}_{ij})$  in (1) be comprised of  $r_{ij}$  and  $\theta_{ij}$  terms provides an exploratory starting point.

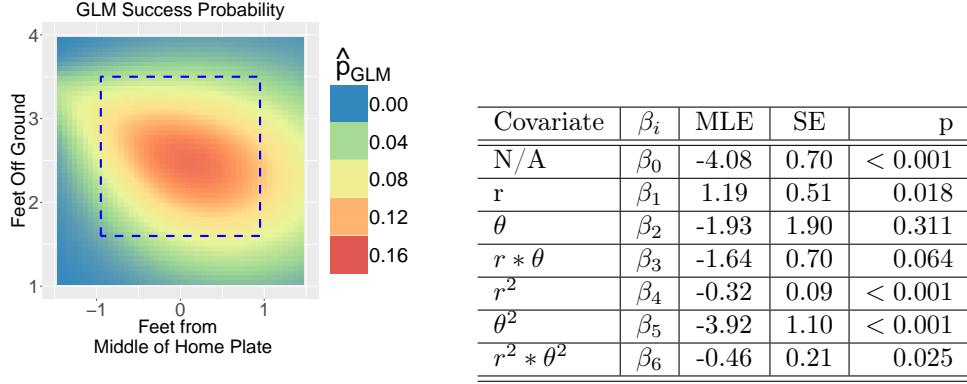
### 1.1.2 Generalized Linear Model with Biomechanically Interpretable Covariates

Let covariate vector  $\mathbf{X}_{ij}(\mathbf{s}_{ij})$  in (1) be defined as  $\mathbf{X}_{ij}(\mathbf{s}_{ij}) = \{r_{ij}, \theta_{ij}, r_{ij}\theta_{ij}, r_{ij}^2, \theta_{ij}^2, r_{ij}^2\theta_{ij}^2\}$ . Substituting into (1) yields:

$$\text{logit}(p_{ij}|\mathbf{s}_{ij}, r_{ij}, \theta_{ij}) = \beta_{j0} + \beta_{j1}r_{ij} + \beta_{j2}\theta_{ij} + \beta_{j3}r_{ij}\theta_{ij} + \beta_{j4}r_{ij}^2 + \beta_{j5}\theta_{ij}^2 + \beta_{j6}r_{ij}^2\theta_{ij}^2 \quad (2)$$

Note that given a hitter  $j$ , and pitch location  $\mathbf{s}_{ij}$ , the elements of  $\mathbf{X}_{ij}$  are simply a trigonometric function of  $\mathbf{s}_{ij}$  and the translated origin. Thus, for convenience, we replace  $\text{logit}(p_{ij}|\mathbf{s}_{ij}, r_{ij}, \theta_{ij})$  with  $\text{logit}(p_{ij}|\mathbf{s}_{ij})$  for the remainder of this study.

We choose Johnny Peralta from Chapter 1 to illustrate, and let  $j = P$  for convenience. We fit model (2) using Peralta's  $n_P = 9177$  observed swings, find maximum likelihood estimates of  $\beta_P$  using an iteratively reweighted least squares algorithm [Myers et al., 2012].



**Figure 2 & Table 1:** A table beside a figure

### 1.1.3 Hosmer-Lemeshow Goodness of Fit Test

Generalized Linear Models [Myers et al., 2012]

- (pg 147) Hosmer-Lemeshow test = Logistic regression Goodness of Fit test.
- Like Pearson Chi-Sq, but for continuous covariates.
- Order all responses according to fitted  $\hat{p}$ , then group into deciles.
- Then basically  $\chi^2 = \sum \sum \frac{(O-E)^2}{E}$
- p-value = 0.1513

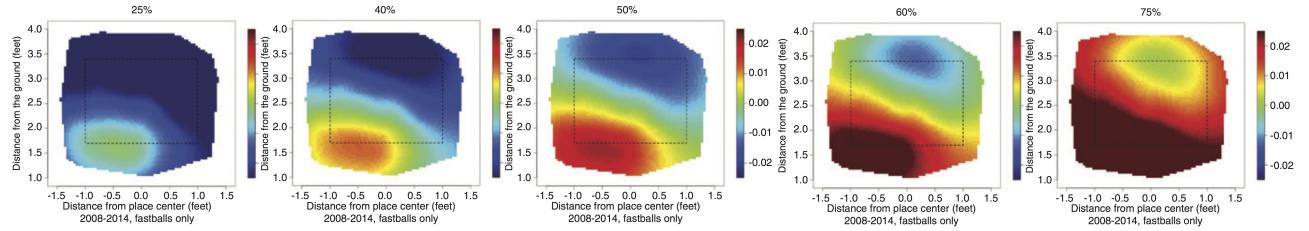
## 1.2 Heat Map Confidence Intervals

A heat map presents, essentially, a two dimensional surface “painted” with point estimates. That is, each (x,y) point on the surface maps a point estimate of a parameter to a color. This effectively communicates the behavior of the parameter, or at least the point estimates, across the spatial domain. However, the

usefulness of a point estimate depends on confidence interval accompaniment; and therein lies the challenge: how to present heat map confidence intervals (CIs)? This problem exists across disparate academic areas of research—any area where heat maps are used! “...question asked in other areas.” For example, Dr. Sarah Emerson reports that collaborative genomics research with Dr. Yanming Di lacked a satisfactory heat map confidence interval option [Emerson, 2017], (cite paper). Next we present the current heat map CI best practices, and examine why they can and should be improved.

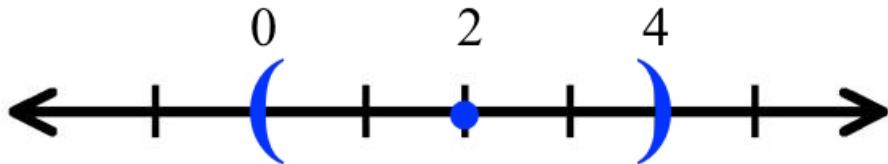
### 1.2.1 Current Best Practices

The current heat map best practice simply presents the CI lower bound heat map and upper bound heat map, and sometimes maps for additional percentiles. For example, Cross and Sylvan [2015] provides the following collection of heat maps to communicate prediction confidence.



**Figure 3:** In line with best practices, Cross and Sylvan [2015] present four percentiles to convey confidence interval information for the point estimate heat map in the middle. We submit this method resists easy comprehension and intuition.

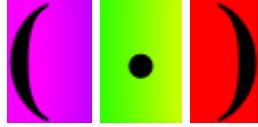
This heat map collection unfortunately challenges the viewer to understand the information content, conceptually and intuitively. To elaborate, consider a one-dimensional, hypothetical point estimate 2 and CI (0,4) which makes plain its information content and structure. Our familiarity with the number line contributes to easy comprehension.



**Figure 4:** Our brain readily understands and interprets the content of a confidence interval on the number line. However, the same is not true for the color spectrum.

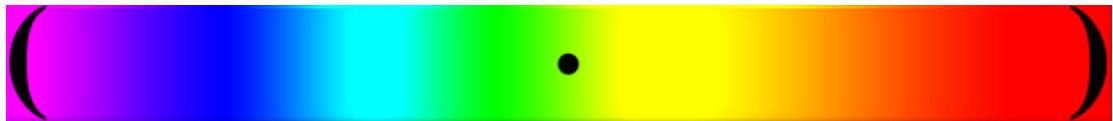
While one quickly, intuitively, and easily understand the content of the number line, this is not necessarily true for the color spectrum. Heat map CIs are less clear because *colors* represent the point estimate and

confidence bounds! A point estimate of “green” with a CI of (purple, red) confounds.



**Figure 5:** This representation of a confidence interval on the color spectrum demonstrates the interpretive challenge. What stream of colors exist between each bound and the point estimate?

However, comprehension comes more easily with the entire spectrum within the confidence interval visible, as in Figure 6.



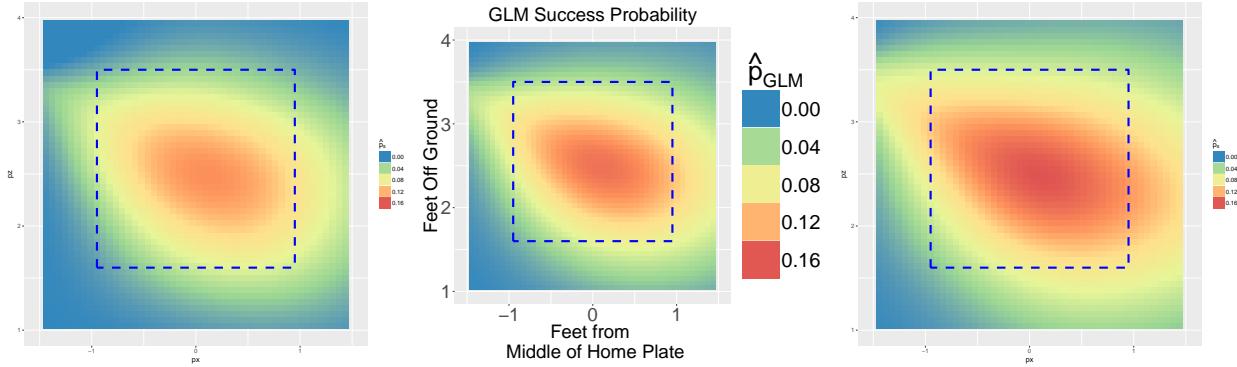
**Figure 6:** This representation of a confidence interval on the color spectrum hints at the interpretive solution. Interpretation simplifies with the portions of the color spectrum between each bound and the point estimate visible. The question then—how do we achieve this for a heat map *surface*?

This simplifies interpretation immensely. However, the problem remains; how do we achieve this for a heat map surface? A continuous model maps a limitless number of point estimates to a color on a surface, making a visible color spectrum confidence interval for each point estimate infeasible. We propose a dynamic solution using RStudio’s Shiny [Chang et al., 2017], [RStudio Team, 2016].

### 1.2.2 Shiny Innovation

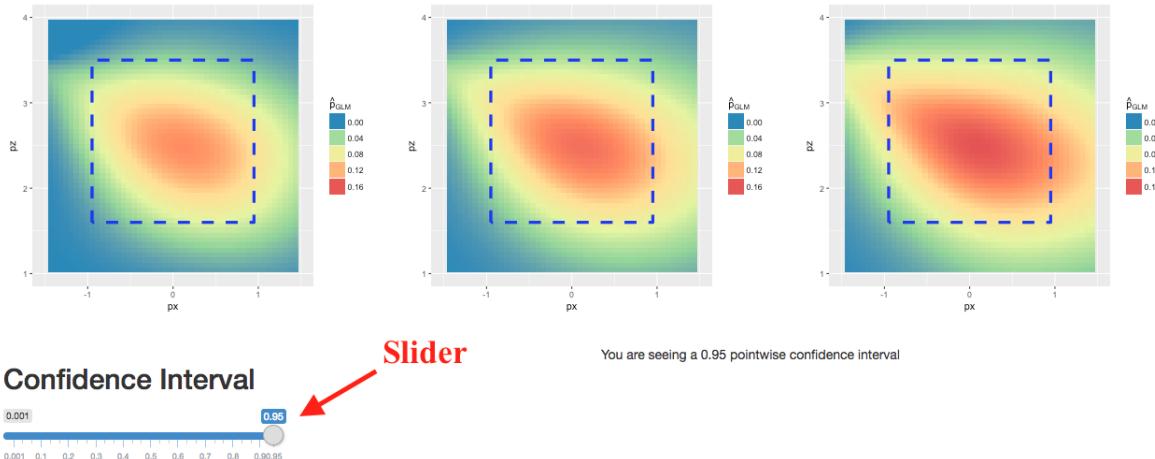
The inimitable RStudio created the Shiny framework to facilitate interactive web application development. Deployed directly out of the RStudio integrated development environment (IDE) [Wikipedia, 2017], Shiny applications provide statisticians, all scientists in fact, with a powerful new tool for presenting analytical results. We take advantage of Shiny’s capability to innovate a solution to the heat map CI problem articulated in the previous section.

Recall the GLM fit heat map for Jhony Peralta. Figure 7 shows the lower and upper 95% pointwise CI heat maps.

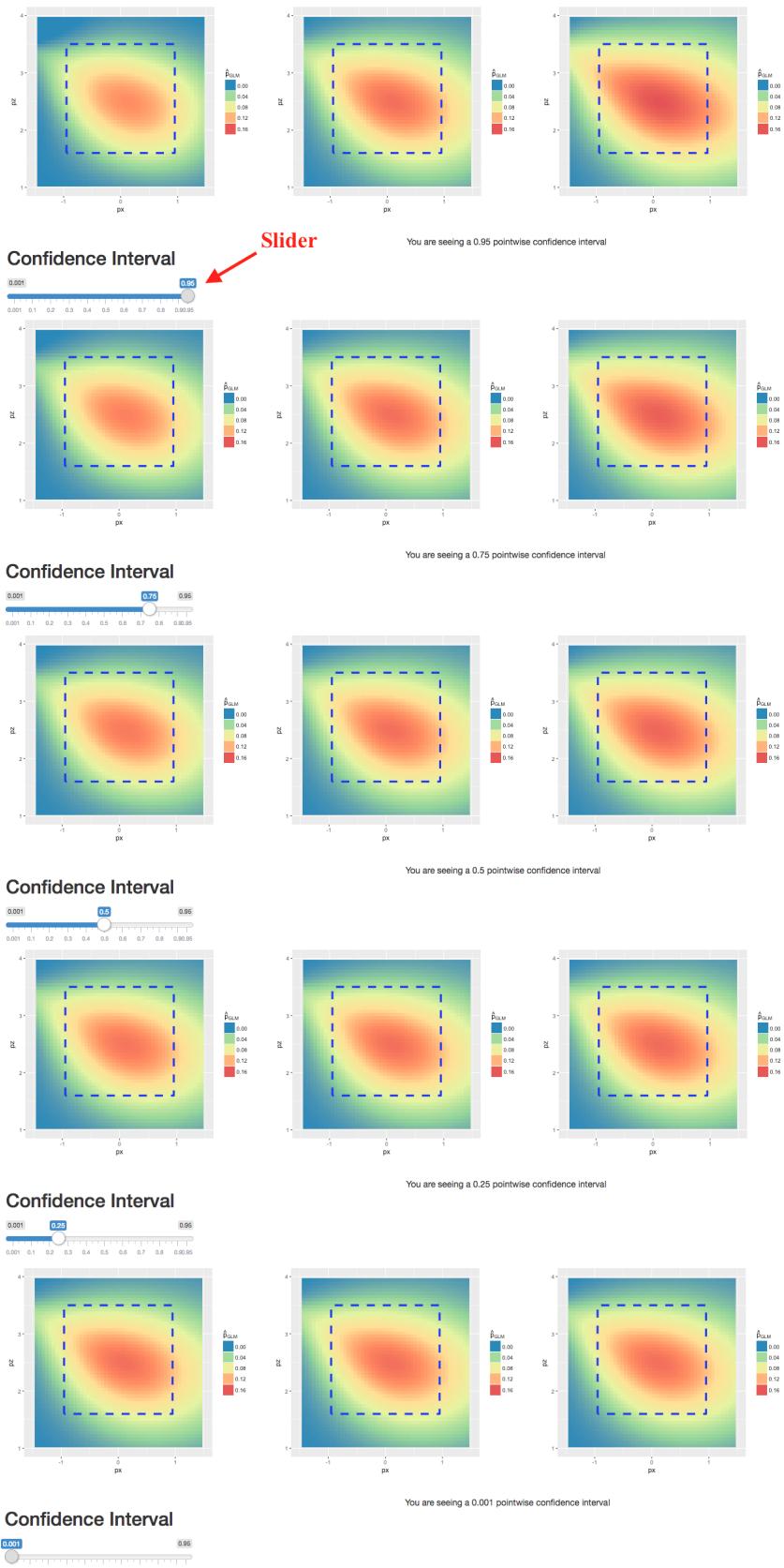


**Figure 7:** Current best practices for a heat map confidence interval (CI). The generalized linear model fit for Jhony Peralta in the center, the pointwise CI lower bound on the left, and the pointwise CI upper bound on the right. Our interactive, dynamic heat map CIs will make improve interpretability.

The heat map on the left gives the lower bound of the 95% CI, the heat map in the middle gives the model fit point estimates, and the heat map on the right gives the upper bound of the 95% CI. The labels are removed from the left and right heat maps for simplicity. The challenge lies in somehow filling in the space between the bounds and point estimate.



**Figure 8:** We created interactive confidence intervals (CIs) with Shiny. The slider in the lower left allows the user to move *through* the CI. As the user adjusts the slider, the heat maps bounds adjust.



**Figure 9:** A dynamic, Shiny, interactive heat map confidence interval. As the user adjusts the Shiny widget slider, the heat maps bounds adjust. This interactive app lets you move **through** a heat map confidence interval.

### 1.3 Appendix: ShinyHMCI, An R Package

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