

ECS 171 : Midterm Review

Midterm Instructions

- This is a **closed book, in-person** midterm exam.
- Includes **20-30 questions**, including MCQs, True/False and around 5-7 numerical questions.
- The exam will test your knowledge on all topics covered so far, **except** 'Probabilistic Graphical Models'.
- Discussions are also part of the material which you need to study for the exam.
- There is **NO partial credits** on T/F and Multiple Choice Questions. Select the best answer.
- Scratch papers will be provided to you to work on numerical questions. You need to return scratch papers with your name written.
- The exam duration is **50 minutes**.
- Make sure to show your **student ID/picture ID** when submitting your work
- A **cheat sheet** will be provided by the proctor during the exam. You may not use any other sources during the exam.
- You can use a **calculator**.
- Communicating with anyone else during the exam is considered "cheating". You are not allowed to use earphone during the exam.
- Switch off your cell phone and let it stay in the off mode until the end of the exam.

Sample T/F Question

N-fold Cross validation is a method used to prevent overfitting.

- A. True
- B. False

Solution

True

In order to validate the training process of the model, n-fold (or k-fold) cross validation is used in order to generalize the training dataset.

Sample T/F Question

The following shows a simple linear regression model for a dataset with x_1, \dots, x_n attributes.

$$y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n$$

- A. True
- B. False

Solution

False

It is multiple linear regression because it has multiple features. If the features are n -degree polynomial, then it is polynomial regression.

Sample T/F Question

Regularization is a method that penalizes model coefficients to reduce overfitting.

- A. True
- B. False

Solution

True

The cost function of a regularized model, C_{reg} , is given as :

$$C_{\text{reg}} = C_{\text{original}} + [\text{Regularization term}]$$

Sample MCQ Question

Which of the following is an example of a flag variable?

- A. Gender: female/male
- B. Weather: clear/rainy/cloudy
- C. Temperature: [21, 80]
- D. (A) and (B)

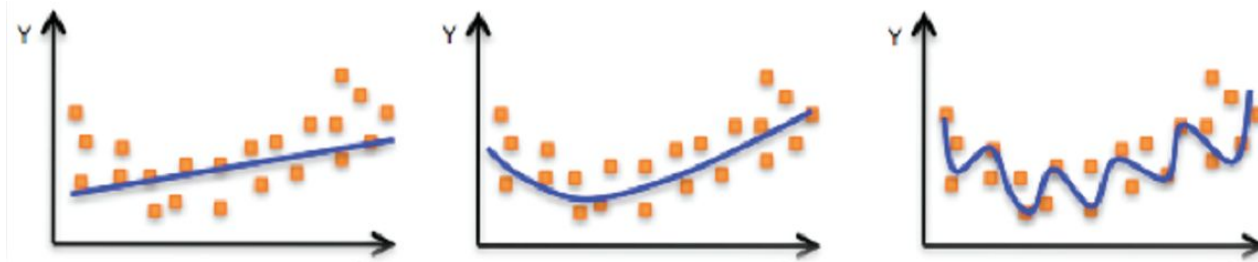
Solution

D. (A) and (B)

Flag variables, or categorical variables, are those variables which can be assigned with a string label

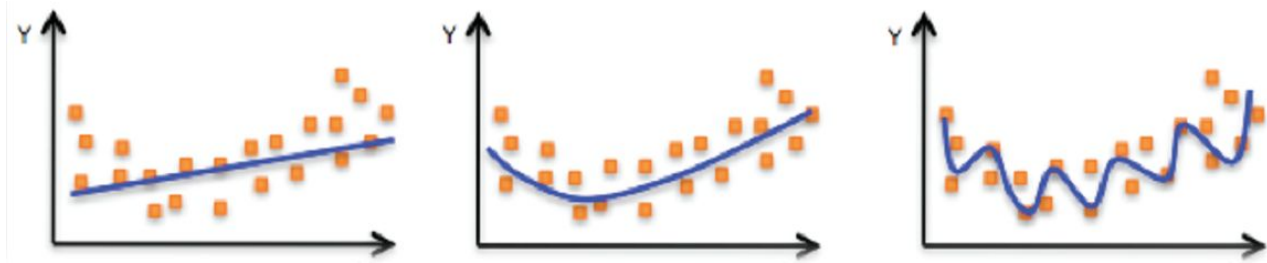
Sample MCQ Question

Indicate the model characteristics depicted in the following figure, from left to right.



- A. Overfitting, under-fitting, balanced
- B. Under-fitting, balanced, balanced
- C. Under-fitting, balanced, overfitting
- D. Overfitting, balanced, balanced

Solution



C. Under-fitting, balanced, overfitting

Sample MCQ Question

How many output neurons in ANN is needed to perform a binary classification?

- A. 1
- B. 2
- C. 3
- D. 4

Solution

A. 1

A single output node giving high or low output is required for binary classification

Sample Numerical Question

In the following dataset with input attributes $X = \{x_1, x_2\}$ and output variable y , calculate the total SSE for the following linear regression model:

$$f(X) = 0.5 + 0.8(x_1) - 0.6(x_2)$$

Note : SSE is calculated as $E(\mathbf{w}) = \frac{1}{2} \sum_{n=1}^N \{y(x_n, \mathbf{w}) - t_n\}^2$

Sample	x1	x2	y
1	3	4	0.7
2	2	5	-0.2
3	6	1	5

Solution

Sample	x1	x2	f(X)	y	e = (y - f(X)) ²
1	3	4	0.5	0.7	0.04
2	2	5	-0.9	-0.2	0.49
3	6	1	4.7	5	0.09

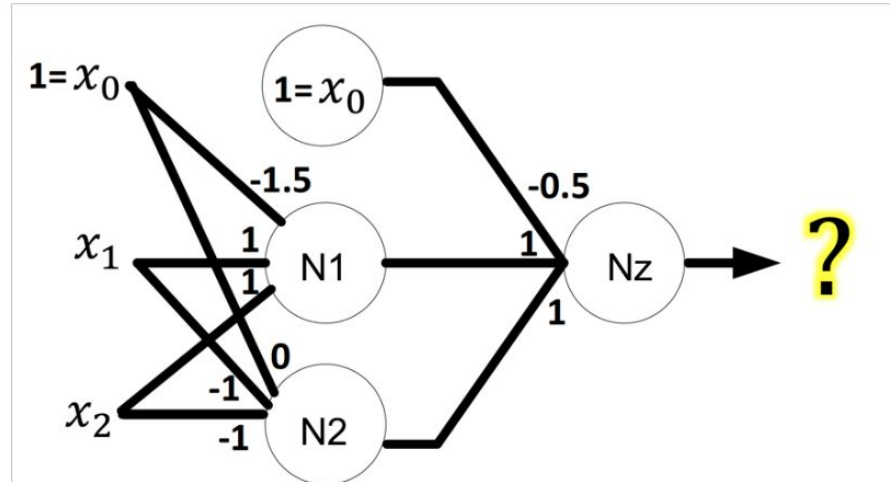
$$SSE = (e_1 + e_2 + e_3) / 2$$

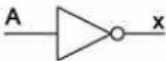






$$SSE = 0.31$$

Sample Numerical Question

Identify the logical gate for every neurons N1,N2,Nz respectively in the following figure if threshold is 0:

x_1	x_2	$y: g(x; w)$
0	0	?
0	1	?
1	0	?
1	1	?



Name	NOT	AND	NAND	OR	NOR	XOR	XNOR																																																																																																
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Solution

For any node :

$$z = w_0 + w_1x_1 + w_2x_2$$

$$y = 1 \quad \text{if } z \geq 0$$

$$= 0 \quad \text{if } z < 0$$

In N1 : Truth table similar to AND

x1	x2	$Z = -1.5 + 1(x1) + 1(x2)$	$Y = (z \geq 0)$
0	0	-1.5	0
0	1	-0.5	0
1	0	-0.5	0
1	1	0.5	1

Solution

In N2 : Truth table similar to NOR

x1	x2	$Z = 0 + (-1)(x1) + (-1)(x2)$	$Y = (z \geq 0)$
0	0	0	1
0	1	-1	0
1	0	-1	0
1	1	-2	0

Solution

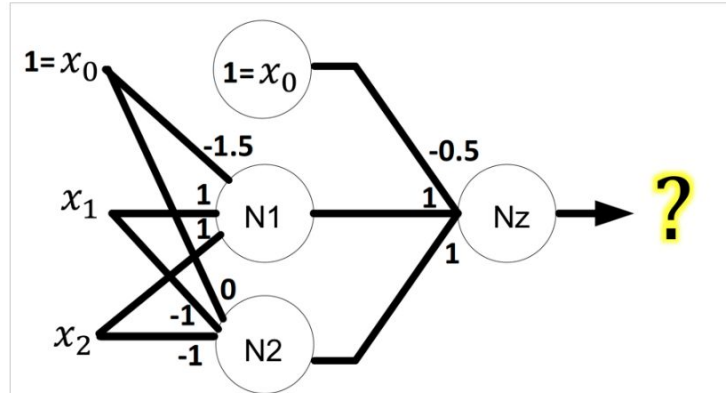
In N3 : Truth table similar to XNOR

x1	x2	x_n1	x_n2	$Z = -0.5 + 1(x_n1) + 1(x_n2)$	$Y = (z \geq 0)$
0	0	0	1	0.5	1
0	1	0	0	-0.5	0
1	0	0	0	-0.5	0
1	1	1	0	0.5	1

Note : Assume the same input for all nodes.

Solution

x_1	x_2	$y: g(x; w)$
0	0	?
0	1	?
1	0	?
1	1	?



N1 : AND

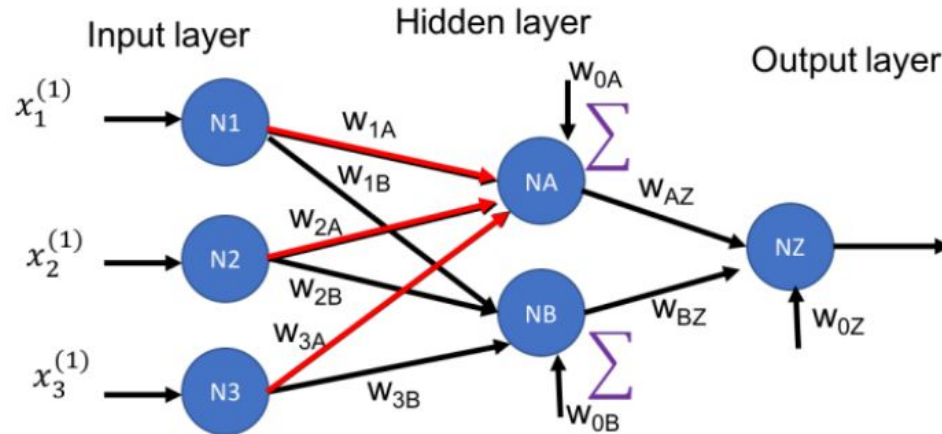
N2 : NOR

Nz : XNOR

Sample Numerical Question

Compute the output of the following neural network after 1 forward pass when sigmoid function is used as the activation function in all layers:

$$\begin{bmatrix} 1 & x_1^{(1)} & x_2^{(1)} & x_3^{(1)} \\ \vdots & & \ddots & \vdots \\ 1 & \dots & & x_3^{(n)} \end{bmatrix} = \begin{bmatrix} 1 & 0.4 & 0.2 & 0.7 \\ \vdots & \ddots & & \vdots \\ 1 & \dots & & x_3^{(n)} \end{bmatrix}$$



$w_{0A}=0.5$	$w_{0B}=0.7$	$w_{0Z}=0.5$
$w_{1A}=0.6$	$w_{1B}=0.9$	$w_{AZ}=0.9$
$w_{2A}=0.8$	$w_{2B}=0.8$	$w_{BZ}=0.9$
$w_{3A}=0.6$	$w_{3B}=0.4$	

$$net^{(i)}_j = \sum_k w_{kj} x_{kj}^{(i)}$$

$$net^{(1)}_A = w_{0j} + w_{1j}x_{1j}^{(1)} + w_{2j}x_{2j}^{(1)} + w_{3j}x_{3j}^{(1)} = 1.32$$

Solution

For any node :

$$z = w_0 + w_1x_1 + \dots + w_nx_n$$

$$y = 1 / (1 + e^{-z})$$

In NA :

$$z = 0.5 + 0.6(x_1) + 0.8(x_2) + 0.6(x_3)$$

$$= 1.32$$

$$x_A = y = 1 / (1 + e^{-z})$$

$$= 0.7892$$

Solution

In NB :

$$z = 0.7 + 0.9(x_1) + 0.8(x_2) + 0.4(x_3) \\ = 1.5$$

$$x_B = y = 1 / (1 + e^{-z}) \\ = 0.8176$$

In NZ :

$$z = 0.5 + 0.9(x_A) + 0.9(x_B) \\ = 1.94612$$

$$y = 1 / (1 + e^{-z})$$

$$\mathbf{y = 0.8750}$$