SOURCEBOOK R ANNOTATED OUTPUT

Abstract: This chapter is intended to facilitate the connection between standard introductory statistics concepts and their implementation in R. It shows the output from various types of analyses, describes how to interpret the output, and shows the link between hand calculation formulas and R output. Results derive from the examples in the other sections of this project.

Keywords: R output, annotation, statistical interpretation

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This document is part of an online statistics sourcebook.

A browser-friendly viewing platform for the sourcebook is available: https://cwendorf.github.io/Sourcebook

> All data, syntax, and output files are available: https://github.com/cwendorf/Sourcebook

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Frequencies

- > ### Frequency Distribution
- > FrequencyTable <- table(Outcome)
- > FrequencyTable

Outcome 0 3 4 5 7 9 2 1 2 1 1 1 The first column lists all the actual scores in the entire data set. "Freq" indicates the number of times that score exists. For example, the score 4 was listed 2 times.

> prop.table(FrequencyTable)

Outcome

The "prop.table" provides the proportion of cases for each possible score. For example, of the 8 scores in the entire data set, the score of 4 was listed 2 times and 2/8 is .250.

- > ### Descriptive Statistics
- > length (Outcome)

[1] 8

> summary (Outcome)

"Summary" provides the scores associated with particular percentile ranks. For example, the 50th percentile is the score in the following position:

$$Position = PR(N + 1) = .50(8 + 1) = 4.5$$

Thus, the score at the 50^{th} percentile ("Median") is the 4.5^{th} score in the frequency distribution – a score of 4.

Descriptives

- > ### Frequency Distribution
- > FrequencyTable <- table(Outcome)</pre>
- > FrequencyTable

Outcome

- 0 3 4 5 7 9
- 2 1 2 1 1 1
- > prop.table(FrequencyTable)

Outcome

- > ### Descriptive Statistics
- > length (Outcome)

> mean (Outcome)

> var(Outcome)

> sd(Outcome)

These statistics were obtained using the command described on the previous page of this guide. Note that they are calculated separately for each variable.

The Mean and Standard Deviation are calculated as unbiased estimates of the respective population parameter. Here, the mean ("M") is determined as the average of the scores weighted by their frequencies:

$$M = \frac{\sum (fY)}{N} = \frac{(2 \times 0) + (1 \times 3) + (2 \times 4) + (1 \times 5) + (1 \times 7) + (1 \times 8)}{8} = 4$$

The Variance and Standard Deviation are both functions of the Sum of Squares (not shown in the output) of the scores in the frequency distribution:

$$SS = \sum f(Y - M)$$

$$SS = 2(0 - 4)^2 + 1(3 - 4)^2 + 2(4 - 4)^2 + 1(5 - 4)^2 + 1(7 - 4)^2 + 1(8 - 4)^2 = 68$$

Then, the Variance (also known as Mean Squares) is calculated as:

$$MS = \frac{SS}{(N-1)} = \frac{68}{7} = 9.714$$

Finally, the Standard Deviation ("SD") is determined by:

$$SD = \sqrt{MS} = \sqrt{9.71} = 3.117$$

Correlations

```
> ### Descriptive Statistics
> lapply(CorrelationData, function(x) c(length(x), mean(x), sd(x)))
50utcome1
[1] 4.00000 2.00000 2.44949
$Outcome2
111 4.00000 6.00000 2.44949
> cov(Outcome1,Outcome2)
[1] 3
> cor(Outcome1,Outcome2)
[1] 0.5
> ### Inferential Statistics
> cor.test(Outcome1,Outcome2)
      Pearson's product-moment correlation
data: Outcome1 and Outcome2
t = 0.8165, df = 2, p-value = 0.5
alternative hypothesis: true correlation is not equal to
95 percent confidence interval:
-0.8876337 0.9868586
sample estimates:
0.5
```

These statistics calculated separately for each variable using procedures described previously.

These boxes represent the conjunction of both variables and therefore present the statistics relevant to the relationship between the two variables.

The Sum of Cross Products ("SCP") is not easily determined from the summary statistics of the output, but rather from the data (and the calculations are therefore not shown here).

The Covariance ("COV") is a function of the Sum of Cross Products and the sample size:

$$COV = \frac{SCP}{(N-1)} = \frac{9.000}{(4-1)} = 3.000$$

The Correlation coefficient ("r") is a function of the covariance and the standard deviations of both variables:

$$r = \frac{COV}{(SD_X)(SD_Y)} = \frac{3.000}{(2.449)(2.449)} = .500$$

The "t", "df", and "p" columns provide a statistical significance test of whether the correlation differs from zero:

$$t = \frac{r}{\sqrt{(1 - r^2)/(N - 2)}} = \frac{.500}{\sqrt{(1 - .500^2)/(4 - 2)}} = .816$$

The t statistic follows a non-normal (studentized or t) distribution that depends on degrees of freedom. Here, df = N - 2 = 4 - 2 = 2. A t with 2 df that equals .816 has a two-tailed probability (p) of .500, which is not a statistically significant finding.

Regression

```
> ### Descriptive Statistics
> lapply(CorrelationData, function(x) c(length(x), mean(x), sd(x)))
$Outcome1
11 4.00000 2.00000 2.44949
$outcome2
[1] 4.00000 6.00000 2.44949
> cov(Outcome1,Outcome2)
[1] 3
> ### Inferential Statistics
> model <- lm(Outcome2 ~ Outcome1)</pre>
> summary(model)
Call:
lm(formula = Outcome2 ~ Outcome1)
Residuals:
-1.0 2.0 -2.5 1.5
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept)
               5.0000
                          1.7854
                                    2.801
                                              0.107
Outcome1
               0.5000
                          0.6124
                                    0.816
                                              <del>0.5</del>00
```

Residual standard error: 2.598 on 2 degrees of freedom

F-statistic: 0.6667 on 1 and 2 DF, p-value: 0.5

Multiple R-squared: 0.25, Adjusted R-squared: -0.125

These statistics calculated separately for each variable using procedures described previously.

The Covariance ("COV") is not easily determined from the summary statistics of the output, but rather from the data (and the calculations are therefore not shown here).

The Unstandardized Regression Coefficients ("Estimate") are also a function of the Covariance and the descriptive statistics:

$$B_1 = \frac{COV}{(SD_X)^2} = \frac{3.000}{(2.449)^2} = 0.500$$

$$B_0 = M_Y - (B_1)(M_X) = 6.000 - (0.500)(2.000) = 5.000$$

The Standardized Regression Coefficient for the predictor can be similarly determined:

$$\beta_1 = B_1 \left(\frac{SD_X}{SD_Y} \right) = 0.500 \left(\frac{2.449}{2.449} \right) = 0.500$$

"R" is a function of the covariance and the standard deviations of both variables:

$$R = \frac{COV}{(SD_X)(SD_Y)} = \frac{3.000}{(2.45)(2.45)} = 0.500$$

$$R^2 = 0.500^2 = 0.250$$

Confidence Interval for a Mean

```
> ### Descriptive Statistics
> length(Outcome)
[1] 8
> mean(Outcome)
[1] 4
> sd(Outcome)
[1] 3.116775
> ### Inferential Statistics
> t.test(Outcome) $conf.int
[1] 1.394311 6.605689
attr(,"conf.level")
[1] 0.95
```

These values are produced by the "Descriptives" commands. See the earlier annotated output for details of how these are computed from frequency distributions.

The Standard Error of the Mean ("SE") provides an estimate of how spread out the distribution of all possible random sample means would be. Here it's calculated as:

$$SE_M = \frac{SD}{\sqrt{N}} = \frac{3.117}{\sqrt{8}} = 1.102$$

This provides a confidence interval around (centered on) the Mean ("M"). Calculation requires the appropriate critical value. Specifically, the *t* statistic (with 7 *df*) that has a probability of .05 equals 2.365. As a result:

$$CI_M = M \pm (t_{CRITICAL})(SE_M) = 4.000 \pm (2.365)(1.102)$$

Thus, the researcher estimates that the true population mean is somewhere between 1.394 and 6.606 (knowing that the estimate could be incorrect).

One Sample t Test

See the earlier annotated output for details of how these are computed from frequency distributions.

The Standard Error of the Mean ("SE") provides an estimate of how spread out the distribution of all possible random sample means would be. Here it's calculated as:

$$SE_M = \frac{SD}{\sqrt{N}} = \frac{3.117}{\sqrt{8}} = 1.102$$

The "t", "df", and "p" values provide the results of the statistical significance test. First, *t* provides the standardized statistic for the mean difference:

$$t = \frac{M - \mu}{SE_M} = \frac{-3.000}{1.102} = -2.722$$

The t statistic follows a non-normal (studentized or t) distribution that depends on degrees of freedom. Here, df = N - 1 = 8 - 1 = 7. A t with 7 df that equals -2.722 has a two-tailed probability (p) of .030, a statistically significant finding.

The Mean Difference is the difference between the sample mean (M = 4) and the user-specified test value (u = 7). For the example, the sample had a mean one point higher than the test value. This raw effect size is important for the significance test, the confidence interval, and the effect size.

Cohen's "d" provides a standardized effect size for the difference between the two means.

$$d = \frac{M - \mu}{SD} = \frac{-3.000}{3.117} = 0.963$$

Given Cohen's heuristics for interpreting effect sizes, this would be considered a large effect.

Paired Samples t Test

- > ### Descriptive Statistics
- > lapply(PairedData, function(x) c(length(x), mean(x), sd(x)))

These statistics are calculated separately for each variable.

\$Outcome1 [1] 4.00000 2.00000 2.44949 \$Outcome2 [1] 4.00000 6.00000 2.44949

- > ### Inferential Statistics
- > t.test(Outcome2,Outcome1,paired=TRUE)

Paired t-test

mean difference

data: Outcome2 and Outcome1

t = 3.266, df = 3, p-value = 0.04692

alternative hypothesis: true mean difference is not aqual to 0

95 percent confidence interval:

0.1023152 7.8976848

sample estimates:

Cohen's "d" provides a standardized effect size for the difference between the two means.

$$d = \frac{M_D}{SD_D} = \frac{4.000}{2.449}$$
$$d = 1.633$$

Given Cohen's heuristics for interpreting effect sizes, this would be considered an extremely large effect.

The Mean Difference is simply the difference between the two means listed above. However, the "SE" is not determinable from the summary statistics presented here but rather the raw data.

The Std. Deviation of the differences can be determined from this information:

$$SD_D = (SE_D)(\sqrt{N})$$

 $SD_D = (1.225)(\sqrt{4}) = 2.449$

The "t", "df", and "p" values provide the results of the statistical significance test. First, *t* provides the standardized statistic for the mean difference:

$$t = \frac{M_D}{SE_D} = \frac{4.000}{1.225} = 3.226$$

The t statistic follows a non-normal (studentized or t) distribution that depends on degrees of freedom. Here, df = N - 1 = 4 - 1 = 3. A t with 3 df that equals 3.226 has a two-tailed probability (p) of .047, a statistically significant finding.

This confidence interval is centered on the Mean Difference ("Diff") of the two variables. Calculation requires the appropriate critical value. Specifically, the *t* statistic (with 3 *df*) that has a probability of .05 equals 3.182. As a result:

$$CI_D = M_D \pm (t_{CRITICAL})(SE_D)$$

 $CI_D = 4.00 \pm (3.182)(1.225)$

Thus, the researcher estimates that the true population mean difference is somewhere between 0.1.02 to 7.898 (knowing that the estimate could be incorrect).

Independent Samples t Test

> ### Descriptive Statistics

These values of the group statistics are calculated separately for each level or condition. They are not identical to the values obtained from analyzing the variable as a whole.

> tapply(Outcome, Factor, function(x) c(length(x), mean(x), sd(x)))

```
11 4.00000 2.00000 2.44949
[1] 4.00000 6.00000 2.44949
```

- > ### Inferential Statistics
- > t.test(Outcome~Factor,var.equal=T)

Two Sample t-test

```
data: Outcome by Factor
t = -2.3094, df = 6, p-value = 0.06032
alternative hypothesis: true difference in means between group 1 and group 2 is not equal to 0
95 percent confidence interval:
-8.2381756 0.2381756
sample estimates:
mean in group 1 mean in group 2
```

This section provides a confidence interval around (centered on) the Mean Difference. Calculation requires the appropriate critical value. Specifically, the t statistic (with 6 df) that has a probability of .05 equals 2.447. As a result:

$$CI_{DIFF} = M_{DIFF} \pm (t_{CRITICAL})(SE_{DIFF})$$

$$CI_{DIFF} = 4 \pm (2.447)(1.732)$$

Thus, the researcher estimates that the true population mean difference is somewhere between -.238 and 8.238 (knowing that the estimate could be incorrect).

The standard errors for each condition can be calculated separately but note that both groups have the same standard deviation and sample size.:

$$SE_M = \frac{SD}{\sqrt{N}} = \frac{2.449}{\sqrt{4}} = 1.225$$

The "SE" is a function of the two groups' individual standard errors. When sample sizes are equal:

$$SE_{DIFF} = \sqrt{SE_1^2 + SE_2^2} = \sqrt{1.225^2 + 1.225^2} = 1.732$$

This value is important for both the significance test and the confidence interval. [Importantly, the computation of the standard error of the difference is more complex for unequal sample sizes.]

The "t", "df", and "p" values provide the results of the statistical significance test. First, t provides the standardized statistic for the mean difference:

$$t = \frac{M_{DIFF}}{SE_{DIFF}} = \frac{4.000}{1.732} = 2.309$$

The t statistic follows a non-normal (studentized or t) distribution that depends on degrees of freedom. Here, df = N - 2 = 8 - 2 = 6. A twith 6 df that equals 2.309 has a two-tailed probability (p) of .060, a finding that is not statistically significant.

The pooled (or weighted average) Std. Deviation of the groups can be determined from the group descriptive statistics:

$$SD_{WITHIN} = \sqrt{\frac{(SD_1^2)(df_1) + (SD_2^2)(df_2)}{df_1 + df_2}} = \sqrt{\frac{(2.449^2)(3) + (2.449^2)(3)}{3+3}} = 2.449$$

Cohen's "d" provides a standardized effect size for the difference between the two means:

$$d = \frac{M_{DIFF}}{SD_{WITHIN}} = \frac{4.000}{2.449} = 1.633$$

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OneWay ANOVA

- > ### Descriptive Statistics
- > by (Outcome, Factor, sd)
- > mean (Outcome)

[1] 5

These values of the group statistics are calculated separately for each group. They are not identical to the values obtained from analyzing the variable as a whole.

A grand mean can be determined by taking the weighted average of all of the group means:

$$M_{TOTAL} = \frac{\sum n(M_{GROUP})}{N} = \frac{4(2) + 4(6) + 4(7)}{4 + 4 + 4} = 5.000$$

> tapply(Outcome, Factor, function(x) c(length(x), mean(x), sd(x)))

```
$`1
[1] 4.00000 2.00000 2.44949
[1] 4.00000 6.00000 2.44949
```

- [1] 4.00000 7.00000 2.44949
- > ### Inferential Statistics
- > summary(Results)

Residuals

value Fr(>F) Df Sum Sq Mean Sq F Factor 4.667 0.0407 28

The "F" statistic is a ratio of the between and within group variance estimates:

$$F = \frac{MS_{BETWEEN}}{MS_{WITHIN}} = \frac{28.000}{6.000} = 4.667$$

An F with 2 and 9 df that equals 4.667 has a two-tailed probability (p) of .041, a statistically significant finding.

The "n²" statistic is a ratio of the between group and the total group variability ("Sum of Squares") estimates:

$$\eta^{2} = \frac{SS_{BETWEEN}}{SS_{TOTAL}} = \frac{SS_{BETWEEN}}{SS_{BETWEEN} + SS_{WITHIN}} = \frac{56.000}{56.000 + 54.000} = 0.509$$

Thus, 50.9% of the total variability among all of the scores in the study is accounted for by group membership.

"Factor" statistics are a function of the differences among the groups:

$$SS_{BETWEEN} = \sum n(M_{GROUP} - M_{TOTAL})^2$$

$$SS_{BETWEEN} = 4(2-5)^2 + 4(6-5)^2 + 4(7-5)^2 = 56.000$$

The degrees of freedom ("df") are a function of the number of groups:

$$df_{BETWEEN} = \#groups - 1 = 2$$

The "Mean Square" is the ratio of the "Sum of Squares" to the "df":

$$MS_{BETWEEN} = \frac{SS_{BETWEEN}}{df_{BETWEEN}} = \frac{56.000}{2} = 28.000$$

"Residual" statistics are a function of the within group variabilities. Because SS for each group equals 2.00 $(SS = SD^2 \times df)$:

$$SS_{WITHIN} = SS_1 + SS_2 + SS_3$$

= 18.000 + 18.000 + 18.000
= 54.000

The degrees of freedom ("df") are a function of the number of people in each group:

$$df_{WITHIN} = df_1 + df_2 + df_3 = 9$$

The "Mean Square" is the ratio of the "Sum of Squares" to the "df":

$$MS_{WITHIN} = \frac{SS_{WITHIN}}{df_{WITHIN}} = \frac{54.000}{9} = 6.000$$

Post Hoc Comparisons

- > ### Descriptive Statistics
- > by (Outcome, Factor, sd)
- > mean (Outcome)
- [1] 5

```
> tapply(Outcome, Factor, function(x) c(length(x), mean(x), sd(x)))
```

```
$`1`
[1] 4.00000 2.00000 2.44949
$`2`
[1] 4.00000 6.00000 2.44949
$`3`
[1] 4.00000 7.00000 2.44949
```

- > ### Inferential Statistics
- > TukeyHSD (Results)

Tukey multiple comparisons of means 95% family-wise confidence level

Fit: aov(formula = Outcome ~ Factor)

\$Factor

```
diff lwr upr p adj
2-1 4 -0.8358956 8.835896 0.1055254
3-1 5 0.1641044 9.835896 0.0431300
3-2 1 -3.8358956 5.835896 0.8352889
```

These values of the group statistics are calculated separately for each group. They are not identical to the values obtained from analyzing the variable as a whole.

A grand mean can be determined by taking the weighted average of all of the group means:

$$M_{TOTAL} = \frac{\sum n(M_{GROUP})}{N} = \frac{4(2) + 4(6) + 4(7)}{4 + 4 + 4} = 5.000$$

The "Standard Errors" are for the difference between the two group means. The values are a function of the MS_{WITHIN} (from the ANOVA) and the sample sizes:

$$SE_{DIFF} = \sqrt{\left(\frac{MS_{WITHIN}}{n_{GROUP}}\right) + \left(\frac{MS_{WITHIN}}{n_{GROUP}}\right)} = \sqrt{\left(\frac{6}{4}\right) + \left(\frac{6}{4}\right)} = 1.732$$

In this case, because all groups are of the same size, the standard error for each comparison is the same.

An HSD value is conceptually similar to a *t* statistic in that it is a function of the "Diff" and the "SE". For the first comparison in the example:

$$HSD = \frac{M_2 - M_1}{SE_{DIFF}} = \frac{4.000}{1.732} = 2.309$$

The "p adj" column provides the probability of the HSD statistic. An HSD of -2.309 (with 2 df_{BETWEEN} and 9 df_{WITHIN} like in the ANOVA source table) has a two-tailed probability (p) of .106, a finding that is not statistically significant.

This section provides confidence intervals around (centered on) the Mean Differences. Calculation requires the appropriate critical value. Specifically, the HSD statistic (with 2 df_{BETWEEN} and 9 df_{WITHIN}) that has a probability of .05 equals 3.068. For the first comparison in the example:

$$CI_{DIFF} = M_{DIFF} \pm (HSD_{CRITICAL})(SE_{DIFF})$$

 $CI_{DIFF} = 4.000 \pm (2.792)(1.732)$

Thus, the estimates that the true population mean difference is somewhere between -8.836 and 0.836 (knowing that the estimate could be incorrect).

Repeated Measures ANOVA

- > ### Descriptive Statistics
- > lapply(RepeatedData, function(x) c(length(x), mea

These descriptive statistics are calculated separately for each level or condition. Because sample sizes are equal, a grand mean can be determined by averaging these two level means:

$$M_{TOTAL} = (M_{LEVEL} + M_{LEVEL})/2 = (2.000 + 6.000)/2 = 4.000$$

\$Outcome1 [1] 4.00000 2.00000 2.44949 \$Outcome2 [1] 4.00000 6.00000 2.44949

> ### Inferential Statistics

> summary(Results)

Error: factor (Subject)

Error: Within

Signif. codes: 0 '*** 0.001 '** 0.01 '*' 0.05

The statistics for the effect ("Factor") are functions of the means of the levels or conditions and the sample sizes:

$$SS_{EFFECT} = \sum_{LEVEL} (M_{LEVEL} - M_{TOTAL})^2$$

$$SS_{EFFECT} = 4(2.0 - 4.0)^2 + 4(6.0 - 4.0)^2 = 32.000$$

$$df_{EFFECT} = \#levels - 1 = 1$$

The "Mean Square" is the usual ratio of the Sum of Squares to the degrees of freedom.

$$MS_{EFFECT} = \frac{SS_{EFFECT}}{df_{FFFECT}} = \frac{32.000}{1} = 32.000$$

Between-subjects error refers to the average differences across the participants of the study. This Sum of Squares is not easily determined from the summary statistics output, but rather from the data (and the calculations are therefore not shown here). However:

$$df_{SUBIECTS} = \#subjects - 1 = 3$$

The "Mean Square" is the usual ratio of the Sum of Squares to the degrees of freedom.

The within-subjects "Error" is a function of variabilities of the separate levels or conditions of the factor and the "between-subjects error" given above. Because SS for each level can be determined ($SS = SD^2 \times df$, which equals 18.000 for each of the two outcomes):

$$SS_{ERROR} = SS_1 + SS_2 - SS_{SUBJECTS}$$

 $SS_{ERROR} = 18.000 + 18.000 - 27.000 = 9.000$
 $df_{ERROR} = df_1 + df_2 - df_{SUBJECTS} = 3 + 3 - 3 = 3.000$

The "Mean Square" is the usual ratio of the Sum of Squares to the degrees of freedom.

The "F" statistic is a ratio of the effect and within-subjects error variance estimates:

$$F = \frac{MS_{EFFECT}}{MS_{ERROR}} = \frac{32.000}{3.000} = 10.667$$

An F with 1 and 3 df that equals 10.667 has a two-tailed probability of .047, a statistically significant finding.

The partial " η^2 " statistic is a ratio of the effect and the total group variability ("Sum of Squares") estimates:

$$Partial \ \eta^2 = \frac{SS_{EFFECT}}{SS_{EFFECT} + SS_{ERROR}}$$

$$Partial \ \eta^2 = \frac{32.000}{32.000 + 9.000} = 0.780$$

Thus, 78.0% of the variability in Outcome scores (after removing individual differences) is accounted for by the repeated measures.

Factorial ANOVA

```
> ### Descriptive Statistics
```

```
> Results <- aov(Outcome~FactorA*FactorB)</pre>
```

> mode1.tables(Results, "means")

Tables of means Grand mean 5

FactorA FactorA A1 A2 4 6

FactorB FactorB B1 B2 4.5 5.5

FactorA: FactorB
FactorB
FactorA B1 B2
A1 2 6
A2 7 5

> tapply(Outcome, list(FactorA, FactorB), sd)

B1 B2 A1 2.44949 2.44949 A2 2.44949 2.44949

> ### Inferential Statistics

> summary(Results)

These descriptive statistics are calculated separately for each group or condition. A level (marginal) mean can be determined by taking the weighted average of the appropriate group means. For example, the marginal mean for Level 1 of Factor A:

$$M_{LEVEL} = \frac{\sum n(M_{GROUP})}{n_{LEVEL}} = \frac{4(2) + 4(7)}{8} = 4.500$$

A grand mean can be determined by taking the weighted average of all of the group means:

$$M_{TOTAL} = \frac{\sum n(M_{GROUP})}{N} = \frac{4(2) + 4(7) + 4(6) + 4(5)}{4 + 4 + 4 + 4} = 5.000$$

Overall, all of the between-group variability is a function of the group means and sample sizes:

$$SS_{MODEL} = \sum_{MODEL} n(M_{GROUP} - M_{TOTAL})^2 = 4(2-5)^2 + 4(7-5)^2 + 4(6-5)^2 + 4(5-5)^2 = 56.000$$

$$df_{MODEL} = \#groups - 1 = 3$$

The statistics for the effects of "Factor A" and Factor B" are functions of the level (marginal) means and sample sizes. For "Factor B":

$$SS_{FACTORB} = \sum_{n} n(M_{LEVEL} - M_{TOTAL})^2 = 8(4.5 - 5)^2 + 8(5.5 - 5)^2 = 4.000$$

 $df_{FACTORB} = \#levels - 1 = 2 - 1 = 1$

The "Factor A * Factor B" (interaction) statistics reflect the between- group variability not accounted for by the factors:

$$SS_{INTERACTION} = SS_{MODEL} - SS_{FACTORA} - SS_{FACTORB} == 56.000 - 4.000 - 16.000 = 36.000$$

$$df_{INTERACTION} = df_A \times df_B = 1$$

"Residual" (error) statistics are a function of the within group variabilities. Because SS for each group can be determined ($SS = SD^2 x df$):

$$SS_{ERROR} = SS_1 + SS_2 + SS_3 + SS_4 = 18.000 + 18.000 + 18.000 + 18.000 = 72.000$$

 $df_{ERROR} = df_1 + df_2 + df_3 + df_4 = 12$

The "F" statistic is a ratio of the effect and within group (error) variance estimates. For "Factor B":

$$F_{FACTORB} = \frac{MS_{FACTORB}}{MS_{ERROR}} = \frac{16.0}{6.0} = 2.667$$

An *F* with 1 and 12 *df* that equals 2.667 has a two-tailed probability of .128, which is not statistically significant.