# Comparing Models for the Prediction of Home Prices

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## Abstract

Being able to accurately predict housing prices is critical to many industries. Recently, analysts have attempted to improve price prediction with enhanced statistical techniques. In this paper, we take a more comparative approach, examining 6 standard regression techniques (OLS, ridge, lasso, elastic net, random forest and gradient boosting) to assess the best performance. We used a kaggle dataset (https://www.kaggle.com/c/house-prices-advanced-regression-techniques) in order to test the performance of the model. We found Lasso to be the best predictor, which we speculate is because the dataset has a high number of predictors relative to the number of observations.

Keywords: Regression, OLS, Ridge, Lasso, elastic net, random forest, gradient boosting, home prices

### Introduction

In this paper we analyze housing prices by comparing three prediction methodologies: OLS, ridge, lasso, elastic net, random forest and gradient boosting. The purpose is to compare the methodologies and draw conclusions about which are most effective and why. Regression alone is not necessarily the optimal strategy for predicting housing prices.<sup>1</sup> However, when data sets and/or analysis resources are limited, regression can perform adequately.

### Background and Literature Review

The ability to accurately predict home prices is of tremendous value to a number of industries, including investors, real estate agents, and municipalities who depend upon property tax revenue. Predictive models for home prices fall roughly into two kinds. First, there are those which predict market trends, busts, and booms. These predictions rely mainly on time series data and analysis of housing prices in the aggregate.

<sup>&</sup>lt;sup>1</sup>1 Li, 2021

The other type of prediction involves the capacity to predict individual house prices from a set of factors.

These usually employ some form of regression and/or machine learning.<sup>2</sup>

For either sort of prediction, there is no consensus about the best method. Many researchers have sought to enhance the traditional models with other methodologies.<sup>3</sup> For example, Guan et. al. propose a "data stream" approach in which past sale records are treated as an evolving datastream.<sup>4</sup> Li et. al. introduce a "grey seasonal model" in which seasonal fluctuations are modeled using grey systems theory, which incorporates uncertainty.<sup>5</sup> Alfiyatin, et. el. use particle swarm optimization (PSO) to select independent variables.<sup>6</sup> (PSO is an optimization system in which population is initialized with random solutions and searches for optima by updating generations.) Finally, Liu et.al incorporate both spatial and temporal autocorrelation in their models by analyzing experience-based submarkets identified by real estate professionals.<sup>7</sup>

All of these researchers report that their innovations improve their regression models. Indeed, any real estate agent can tell you that a predictive model can be improved simply by knowing what other houses in the neighborhood sold for. The problem is, the data at the center of these enhancements is not always available. The researcher may have home sales from only a short time span, and neighborhoods that are not defined by real estate experts but by traditional boundary lines which may contain a mix of house types. Even when data is available, the complex models proposed may be computationally expensive and/or require data analysis expertise that is not generally available.

In this project we approach the question comparatively. Restricting ourselves to regression models, we compare six types of regression: OLS, ridge, lasso, elastic net, random forest and gradient boosting. The data is drawn from the Advanced Regression Techniques housing data set for Ames, Iowa. We test the accuracy of our models by submitting each to the Kaggle competition to see how they perform. We then discuss the merits of the different sorts of approaches.

#### Modeling

We are modeling a data set containing 1460 records of houses sold in the Ames, Iowa area between 2006 and 2010. The variables are mostly related to house features, such as square footage, the presence of a pool, etc. The response variable, "SalePrice", is a continuous variable representing the sale price of the house in thousands of dollars.

<sup>&</sup>lt;sup>2</sup>2 Journal, 2019

<sup>&</sup>lt;sup>3</sup>3 Wu, 2020

<sup>&</sup>lt;sup>4</sup>4 Guan, 2021

<sup>&</sup>lt;sup>5</sup>5 Li, 2021

<sup>&</sup>lt;sup>6</sup>6 Alfiyatin, 2017

<sup>&</sup>lt;sup>7</sup>7 Liu, X. 2012

We examine the data:

# 1. Dataset Description

# A. Summary Statistics

```
##
          Ιd
                        MSSubClass
                                          MSZoning
                                                       LotFrontage
##
    Min.
          :
               1.0
                      Min.
                             : 20.0
                                       C (all):
                                                 10
                                                      Min.
                                                              : 21.00
    1st Qu.: 365.8
                      1st Qu.: 20.0
##
                                       F۷
                                                 65
                                                       1st Qu.: 59.00
    Median : 730.5
                      Median: 50.0
                                                      Median : 69.00
##
                                       RH
                                                 16
##
    Mean
           : 730.5
                      Mean
                             : 56.9
                                       RL
                                              :1151
                                                      Mean
                                                              : 70.05
                      3rd Qu.: 70.0
                                                      3rd Qu.: 80.00
##
    3rd Qu.:1095.2
                                       RM
                                              : 218
##
    Max.
           :1460.0
                      Max.
                             :190.0
                                                      Max.
                                                              :313.00
##
                                                      NA's
                                                              :259
##
       LotArea
                       Street
                                   Alley
                                               LotShape LandContour Utilities
                                                                63
          : 1300
                      Grvl:
                              6
                                  Grv1: 50
                                               IR1:484
                                                          Bnk:
                                                                      AllPub: 1459
##
    Min.
##
    1st Qu.: 7554
                      Pave:1454
                                  Pave:
                                         41
                                               IR2: 41
                                                          HLS:
                                                                50
                                                                      NoSeWa:
                                                                                 1
   Median: 9478
                                  NA's:1369
                                               IR3: 10
                                                                36
##
                                                          Low:
          : 10517
##
    Mean
                                               Reg:925
                                                          Lvl:1311
##
    3rd Qu.: 11602
           :215245
##
    Max.
##
      LotConfig
                                Neighborhood
                                                                Condition2
##
                   LandSlope
                                                Condition1
    Corner: 263
                   Gtl:1382
                               NAmes :225
                                              Norm
                                                      :1260
                                                              Norm
                                                                     :1445
##
    CulDSac: 94
                   Mod:
                          65
                               CollgCr:150
                                              Feedr
                                                        81
                                                              Feedr
                                                                         6
##
    FR2
              47
                          13
                               OldTown:113
                                                        48
##
                    Sev:
                                              Artery:
                                                              Artery:
                                                                         2
##
    FR3
               4
                               Edwards:100
                                              RRAn
                                                        26
                                                              PosN
                                                                         2
    Inside:1052
                               Somerst: 86
##
                                              PosN
                                                     :
                                                        19
                                                              RRNn
                                                                          2
                               Gilbert: 79
                                              RRAe
                                                              PosA
##
                                                        11
                                                                          1
##
                               (Other):707
                                              (Other):
                                                       15
                                                              (Other):
                                                                          2
                     HouseStyle
                                                                      YearBuilt
##
      BldgType
                                  OverallQual
                                                    OverallCond
    1Fam :1220
                   1Story :726
                                         : 1.000
                                                           :1.000
                                                                    Min.
                                                                            :1872
                                 Min.
                                                   Min.
##
##
    2fmCon:
             31
                  2Story :445
                                 1st Qu.: 5.000
                                                   1st Qu.:5.000
                                                                    1st Qu.:1954
                                 Median : 6.000
                                                   Median :5.000
    Duplex:
             52
                   1.5Fin :154
                                                                    Median:1973
##
```

```
Twnhs: 43
                  SLvl
                         : 65
                                        : 6.099
                                                          :5.575
##
                                 Mean
                                                   Mean
                                                                    Mean
                                                                           :1971
    TwnhsE: 114
                  SFoyer: 37
                                                   3rd Qu.:6.000
                                                                    3rd Qu.:2000
##
                                 3rd Qu.: 7.000
##
                  1.5Unf : 14
                                 Max.
                                        :10.000
                                                   Max.
                                                          :9.000
                                                                    Max.
                                                                           :2010
##
                   (Other): 19
##
     YearRemodAdd
                     RoofStyle
                                      RoofMatl
                                                    Exterior1st
                                                                  Exterior2nd
    Min.
           :1950
                   Flat
                           : 13
                                   CompShg: 1434
                                                   VinylSd:515
                                                                 VinylSd:504
##
##
    1st Qu.:1967
                   Gable :1141
                                   Tar&Grv:
                                             11
                                                   HdBoard:222
                                                                 MetalSd:214
    Median:1994
                                   WdShngl:
##
                   Gambrel: 11
                                              6
                                                   MetalSd:220
                                                                 HdBoard:207
           :1985
                                                   Wd Sdng:206
##
    Mean
                   Hip
                           : 286
                                   WdShake:
                                              5
                                                                 Wd Sdng:197
##
    3rd Qu.:2004
                   Mansard:
                               7
                                   ClyTile:
                                                   Plywood:108
                                                                 Plywood:142
##
    Max.
           :2010
                   Shed
                               2
                                   Membran:
                                                   CemntBd: 61
                                                                 CmentBd: 60
                                               1
                                   (Other):
                                               2
                                                   (Other):128
                                                                 (Other):136
##
##
      MasVnrType
                    MasVnrArea
                                    ExterQual ExterCond Foundation BsmtQual
    BrkCmn : 15
                                                     3
##
                  Min.
                              0.0
                                    Ex: 52
                                               Ex:
                                                         BrkTil:146
                                                                       Ex
                                                                          :121
    BrkFace:445
                  1st Qu.:
                              0.0
                                                    28
                                                         CBlock:634
##
                                    Fa: 14
                                              Fa:
                                                                      Fa
                                                                          : 35
##
    None
           :864
                  Median :
                              0.0
                                    Gd:488
                                              Gd: 146
                                                         PConc:647
                                                                       Gd
                                                                           :618
           :128
                         : 103.7
                                    TA:906
##
    Stone
                  Mean
                                              Po:
                                                     1
                                                         Slab : 24
                                                                          :649
                                                                       TA
                  3rd Qu.: 166.0
                                               TA:1282
##
    NA's
           : 8
                                                         Stone: 6
                                                                       NA's: 37
##
                  Max.
                          :1600.0
                                                         Wood: 3
##
                  NA's
                          :8
    BsmtCond
                BsmtExposure BsmtFinType1
##
                                              BsmtFinSF1
                                                             BsmtFinType2
                    :221
                              ALQ :220
                                                             ALQ: 19
##
    Fa:
          45
                Αv
                                           Min.
                                                 :
                                                       0.0
##
    Gd
           65
                Gd
                    :134
                              BLQ :148
                                           1st Qu.:
                                                       0.0
                                                             BLQ :
                                           Median : 383.5
##
    Ро
            2
                Mn
                    :114
                              GLQ :418
                                                             GLQ: 14
                              LwQ : 74
##
    TA:1311
                No
                    :953
                                           Mean
                                                   : 443.6
                                                             LwQ:
                              Rec :133
                                           3rd Qu.: 712.2
##
    NA's: 37
                NA's: 38
                                                             Rec : 54
##
                              Unf :430
                                           Max.
                                                   :5644.0
                                                             Unf :1256
                              NA's: 37
                                                             NA's: 38
##
                                         {\tt TotalBsmtSF}
##
      BsmtFinSF2
                         BsmtUnfSF
                                                           Heating
                                                                        HeatingQC
               0.00
                                  0.0
                                               :
                                                          Floor:
                                                                        Ex:741
##
    Min.
                      Min.
                              :
                                        Min.
                                                    0.0
                                                                   1
                                                                       Fa: 49
    1st Qu.:
               0.00
                      1st Qu.: 223.0
                                        1st Qu.: 795.8
                                                          GasA :1428
##
##
    Median :
               0.00
                      Median : 477.5
                                        Median : 991.5
                                                          GasW :
                                                                 18
                                                                        Gd:241
              46.55
                              : 567.2
                                                :1057.4
                                                                   7
                                                                        Po: 1
##
    Mean
                      Mean
                                        Mean
                                                          Grav :
```

```
3rd Qu.: 808.0
                                     3rd Qu.:1298.2 OthW:
   3rd Qu.:
             0.00
                                                                 TA:428
##
          :1474.00
                    Max.
                           :2336.0
                                    Max. :6110.0
                                                     Wall:
   Max.
##
   CentralAir Electrical
                            X1stFlrSF
                                          X2ndFlrSF
                                                       LowQualFinSF
##
   N: 95
              FuseA: 94
                          Min. : 334
                                        Min. :
                                                       Min.
                                                              : 0.000
##
                                                   0
   Y:1365
              FuseF: 27
                          1st Qu.: 882
                                        1st Qu.:
                                                       1st Qu.: 0.000
##
                                                   0
##
              FuseP:
                      3
                          Median :1087
                                        Median :
                                                       Median : 0.000
                          Mean :1163
                                        Mean : 347
##
              Mix : 1
                                                       Mean : 5.845
                          3rd Qu.:1391
##
              SBrkr:1334
                                        3rd Qu.: 728
                                                       3rd Qu.: 0.000
##
              NA's :
                     1
                          Max.
                                 :4692
                                        Max.
                                              :2065
                                                       Max. :572.000
##
                  BsmtFullBath
                                   BsmtHalfBath
                                                      FullBath
##
     GrLivArea
##
   Min. : 334
                 Min.
                        :0.0000
                                  Min. :0.00000
                                                   Min. :0.000
                                  1st Qu.:0.00000
##
   1st Qu.:1130
                 1st Qu.:0.0000
                                                   1st Qu.:1.000
   Median:1464
                 Median :0.0000
                                  Median :0.00000
                                                   Median :2.000
##
##
   Mean :1515
                 Mean
                        :0.4253
                                  Mean
                                       :0.05753
                                                   Mean :1.565
##
   3rd Qu.:1777
                  3rd Qu.:1.0000
                                  3rd Qu.:0.00000
                                                   3rd Qu.:2.000
##
   Max.
          :5642
                  Max.
                        :3.0000
                                  Max.
                                        :2.00000
                                                   Max.
                                                          :3.000
##
##
      HalfBath
                    {\tt BedroomAbvGr}
                                  KitchenAbvGr
                                                  KitchenQual TotRmsAbvGrd
          :0.0000
                    Min. :0.000
                                   Min. :0.000
##
   Min.
                                                  Ex:100
                                                             Min. : 2.000
   1st Qu.:0.0000
                    1st Qu.:2.000
                                   1st Qu.:1.000
                                                             1st Qu.: 5.000
##
                                                  Fa: 39
   Median :0.0000
                    Median :3.000
                                   Median :1.000
                                                  Gd:586
                                                             Median : 6.000
##
##
   Mean :0.3829
                    Mean :2.866
                                   Mean :1.047
                                                  TA:735
                                                             Mean : 6.518
   3rd Qu.:1.0000
                    3rd Qu.:3.000
                                   3rd Qu.:1.000
                                                              3rd Qu.: 7.000
##
##
   Max.
          :2.0000
                    Max.
                          :8.000
                                   Max.
                                          :3.000
                                                              Max.
                                                                    :14.000
##
   Functional
                Fireplaces
                              FireplaceQu GarageType
                                                      GarageYrBlt
##
##
   Maj1: 14
               Min. :0.000
                              Ex : 24
                                          2Types: 6
                                                       Min. :1900
               1st Qu.:0.000
                                         Attchd:870
##
   Maj2:
          5
                              Fa : 33
                                                       1st Qu.:1961
   Min1: 31
              Median :1.000
                              Gd :380
                                         Basment: 19
                                                       Median:1980
##
   Min2:
          34
               Mean :0.613
                              Po : 20
                                         BuiltIn: 88
                                                       Mean :1979
   Mod: 15
               3rd Qu.:1.000
                              TA :313
                                                       3rd Qu.:2002
##
                                         CarPort: 9
```

```
Sev: 1
                     :3.000
                              NA's:690
                                         Detchd:387
                                                             :2010
               Max.
                                                      Max.
                                         NA's
                                                : 81
                                                       NA's
                                                             :81
##
   Typ: 1360
                  GarageCars
                                 GarageArea
   GarageFinish
                                               GarageQual
                                                          GarageCond
   Fin :352
                Min. :0.000
                               Min. :
                                         0.0
                                               Ex
                                                      3
                                                          Ex
                                                             :
                                                                  2
##
   RFn:422
                1st Qu.:1.000
                               1st Qu.: 334.5
                                               Fa :
                                                      48
                                                          Fa
##
   Unf :605
               Median :2.000
                               Median : 480.0
                                               Gd : 14
                                                          Gd:
                                                                  9
##
   NA's: 81
                Mean :1.767
                               Mean : 473.0
                                               Ро
                                                  : 3
                                                          Ро
                3rd Qu.:2.000
                               3rd Qu.: 576.0
                                               TA :1311
##
                                                          TA:1326
                                               NA's: 81
##
                Max.
                      :4.000
                               Max.
                                      :1418.0
                                                          NA's: 81
##
               WoodDeckSF
                               OpenPorchSF
                                              EnclosedPorch
   PavedDrive
                                                               X3SsnPorch
   N: 90
              Min. : 0.00
                              Min. : 0.00
                                              Min. : 0.00
##
                                                              Min. : 0.00
##
   P: 30
              1st Qu.: 0.00
                              1st Qu.: 0.00
                                              1st Qu.: 0.00
                                                              1st Qu.: 0.00
   Y:1340
              Median: 0.00
                              Median : 25.00
                                              Median: 0.00
##
                                                              Median: 0.00
##
              Mean
                   : 94.24
                                    : 46.66
                                              Mean : 21.95
                                                                   : 3.41
                              Mean
                                                              Mean
##
              3rd Qu.:168.00
                              3rd Qu.: 68.00
                                              3rd Qu.: 0.00
                                                              3rd Qu.: 0.00
                    :857.00
                                     :547.00
                                                                     :508.00
##
              Max.
                              Max.
                                                     :552.00
                                                              Max.
                                              Max.
##
                                                            MiscFeature
                      PoolArea
                                     PoolQC
##
    ScreenPorch
                                                  Fence
##
   Min.
        : 0.00
                   Min. : 0.000
                                    Ex:
                                            2
                                                GdPrv: 59
                                                            Gar2:
                                                                    2
   1st Qu.: 0.00
                   1st Qu.: 0.000
                                                GdWo :
                                                            Othr:
                                                                    2
##
                                    Fa :
                                                       54
                   Median : 0.000
   Median: 0.00
                                                MnPrv: 157
                                                            Shed:
                                                                   49
##
                                    Gd:
##
   Mean
        : 15.06
                   Mean
                         : 2.759
                                     NA's:1453
                                                MnWw :
                                                            TenC:
   3rd Qu.: 0.00
                   3rd Qu.: 0.000
                                                NA's :1179
##
                                                            NA's:1406
##
   Max.
          :480.00
                   Max.
                          :738.000
##
      MiscVal
                         MoSold
                                         YrSold
                                                      SaleType
##
              0.00
                     Min. : 1.000
                                     Min. :2006
                                                    WD
                                                           :1267
   Min. :
##
   1st Qu.:
            0.00
                     1st Qu.: 5.000
                                      1st Qu.:2007
                                                    New
                                                           : 122
   Median :
            0.00
                                     Median:2008
                     Median : 6.000
                                                    COD
##
                                                             43
              43.49
                                     Mean :2008
##
   Mean :
                     Mean : 6.322
                                                    ConLD
                                                              9
   3rd Qu.:
                     3rd Qu.: 8.000
              0.00
                                      3rd Qu.:2009
                                                    ConLI :
                                                              5
   Max. :15500.00
                     Max. :12.000
                                     Max. :2010
                                                              5
##
                                                    ConLw :
```

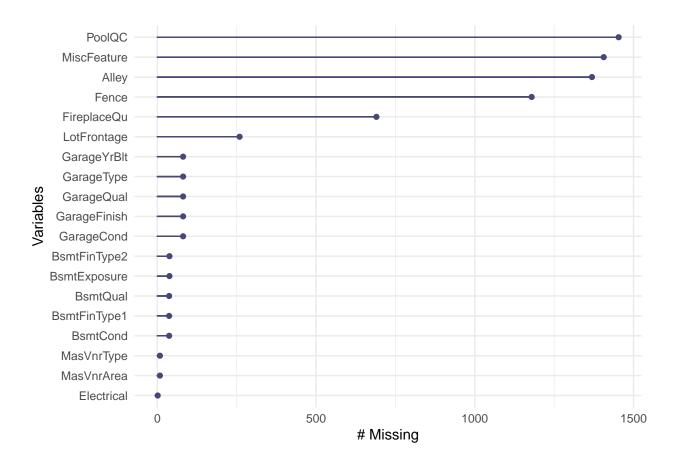
```
(Other):
##
                                                                 9
   SaleCondition
                    SalePrice
##
##
   Abnorml: 101
                  Min.
                          : 34900
   AdjLand:
                  1st Qu.:129975
##
              4
   Alloca: 12
                  Median :163000
##
   Family: 20
##
                  Mean
                         :180921
##
   Normal:1198
                  3rd Qu.:214000
##
   Partial: 125
                  Max.
                         :755000
##
                   1460 obs. of 81 variables:
  'data.frame':
                  : int 1 2 3 4 5 6 7 8 9 10 ...
##
   $ Id
##
   $ MSSubClass
                  : int 60 20 60 70 60 50 20 60 50 190 ...
                  : Factor w/ 5 levels "C (all)", "FV", ...: 4 4 4 4 4 4 4 4 5 4 ...
##
   $ MSZoning
   $ LotFrontage
                  : int 65 80 68 60 84 85 75 NA 51 50 ...
##
                  : int 8450 9600 11250 9550 14260 14115 10084 10382 6120 7420 ...
##
   $ LotArea
   $ Street
                  : Factor w/ 2 levels "Grvl", "Pave": 2 2 2 2 2 2 2 2 2 ...
##
                  $ Alley
##
   $ LotShape
                  : Factor w/ 4 levels "IR1", "IR2", "IR3", ...: 4 4 1 1 1 1 4 1 4 4 ....
##
                  : Factor w/ 4 levels "Bnk", "HLS", "Low", ...: 4 4 4 4 4 4 4 4 4 4 ...
##
   $ LandContour
   $ Utilities
                  : Factor w/ 2 levels "AllPub", "NoSeWa": 1 1 1 1 1 1 1 1 1 1 ...
##
                  : Factor w/ 5 levels "Corner", "CulDSac", ...: 5 3 5 1 3 5 5 1 5 1 ...
   $ LotConfig
   $ LandSlope
                  : Factor w/ 3 levels "Gtl", "Mod", "Sev": 1 1 1 1 1 1 1 1 1 1 ...
##
   $ Neighborhood : Factor w/ 25 levels "Blmngtn", "Blueste",..: 6 25 6 7 14 12 21 17 18 4 ...
##
                  : Factor w/ 9 levels "Artery", "Feedr", ...: 3 2 3 3 3 3 5 1 1 ...
   $ Condition1
##
##
   $ Condition2
                  : Factor w/ 8 levels "Artery", "Feedr", ...: 3 3 3 3 3 3 3 3 1 ...
                  : Factor w/ 5 levels "1Fam", "2fmCon", ...: 1 1 1 1 1 1 1 1 2 ...
   $ BldgType
##
                  : Factor w/ 8 levels "1.5Fin", "1.5Unf", ...: 6 3 6 6 6 1 3 6 1 2 ....
##
   $ HouseStyle
##
   $ OverallQual : int 7 6 7 7 8 5 8 7 7 5 ...
##
   $ OverallCond : int 5 8 5 5 5 5 6 5 6 ...
   $ YearBuilt
                  : int 2003 1976 2001 1915 2000 1993 2004 1973 1931 1939 ...
##
   $ YearRemodAdd : int 2003 1976 2002 1970 2000 1995 2005 1973 1950 1950 ...
##
   $ RoofStyle
                  : Factor w/ 6 levels "Flat", "Gable", ...: 2 2 2 2 2 2 2 2 2 2 ...
```

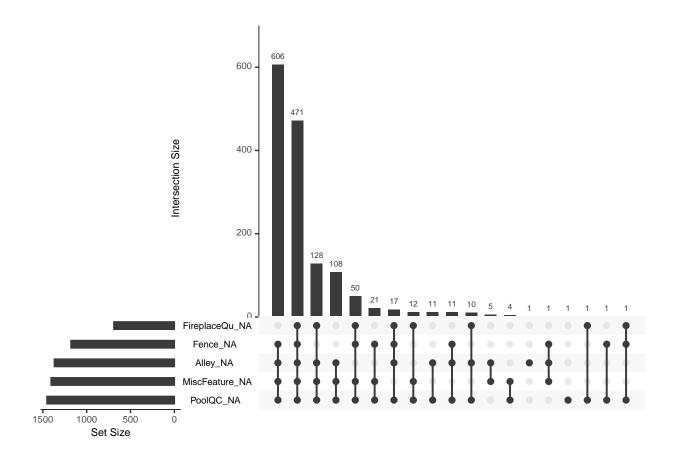
```
$ RoofMatl
                   : Factor w/ 8 levels "ClyTile", "CompShg",...: 2 2 2 2 2 2 2 2 2 2 ...
                  : Factor w/ 15 levels "AsbShng", "AsphShn", ...: 13 9 13 14 13 13 13 7 4 9 ...
##
   $ Exterior1st
##
   $ Exterior2nd
                  : Factor w/ 16 levels "AsbShng", "AsphShn", ...: 14 9 14 16 14 14 14 7 16 9 ...
                   : Factor w/ 4 levels "BrkCmn", "BrkFace", ...: 2 3 2 3 2 3 4 4 3 3 ...
   $ MasVnrType
##
   $ MasVnrArea
                   : int 196 0 162 0 350 0 186 240 0 0 ...
##
                   : Factor w/ 4 levels "Ex", "Fa", "Gd", ...: 3 4 3 4 3 4 3 4 4 4 ...
##
   $ ExterQual
##
   $ ExterCond
                   : Factor w/ 5 levels "Ex", "Fa", "Gd", ...: 5 5 5 5 5 5 5 5 5 5 5 ...
##
   $ Foundation
                   : Factor w/ 6 levels "BrkTil", "CBlock", ...: 3 2 3 1 3 6 3 2 1 1 ...
   $ BsmtQual
                   : Factor w/ 4 levels "Ex", "Fa", "Gd", ...: 3 3 3 4 3 3 1 3 4 4 ...
##
##
   $ BsmtCond
                   : Factor w/ 4 levels "Fa", "Gd", "Po", ...: 4 4 4 2 4 4 4 4 4 4 ...
   $ BsmtExposure : Factor w/ 4 levels "Av", "Gd", "Mn", ...: 4 2 3 4 1 4 1 3 4 4 ...
##
   $ BsmtFinType1 : Factor w/ 6 levels "ALQ", "BLQ", "GLQ", ...: 3 1 3 1 3 3 3 1 6 3 ...
##
##
   $ BsmtFinSF1
                   : int 706 978 486 216 655 732 1369 859 0 851 ...
   $ BsmtFinType2 : Factor w/ 6 levels "ALQ", "BLQ", "GLQ", ...: 6 6 6 6 6 6 6 6 2 6 6 ...
##
                   : int 0000003200...
   $ BsmtFinSF2
##
##
   $ BsmtUnfSF
                   : int 150 284 434 540 490 64 317 216 952 140 ...
                   : int 856 1262 920 756 1145 796 1686 1107 952 991 ...
   $ TotalBsmtSF
##
                   : Factor w/ 6 levels "Floor", "GasA", ...: 2 2 2 2 2 2 2 2 2 ...
   $ Heating
##
##
   $ HeatingQC
                   : Factor w/ 5 levels "Ex", "Fa", "Gd", ...: 1 1 1 3 1 1 1 1 3 1 ...
   $ CentralAir
                   : Factor w/ 2 levels "N", "Y": 2 2 2 2 2 2 2 2 2 2 ...
##
                   : Factor w/ 5 levels "FuseA", "FuseF", ...: 5 5 5 5 5 5 5 5 5 2 5 ...
##
   $ Electrical
   $ X1stFlrSF
                   : int 856 1262 920 961 1145 796 1694 1107 1022 1077 ...
##
   $ X2ndFlrSF
                   : int 854 0 866 756 1053 566 0 983 752 0 ...
##
   $ LowQualFinSF : int 0 0 0 0 0 0 0 0 0 ...
##
   $ GrLivArea
                   : int 1710 1262 1786 1717 2198 1362 1694 2090 1774 1077 ...
##
   $ BsmtFullBath : int 1 0 1 1 1 1 1 1 0 1 ...
##
   $ BsmtHalfBath : int 0 1 0 0 0 0 0 0 0 ...
##
                   : int 2 2 2 1 2 1 2 2 2 1 ...
   $ FullBath
##
##
   $ HalfBath
                   : int 1010110100...
   $ BedroomAbvGr : int 3 3 3 3 4 1 3 3 2 2 ...
##
   $ KitchenAbvGr : int    1 1 1 1 1 1 1 2 2 ...
##
   $ KitchenQual : Factor w/ 4 levels "Ex", "Fa", "Gd", ...: 3 4 3 3 3 4 3 4 4 4 ...
   $ TotRmsAbvGrd : int 8 6 6 7 9 5 7 7 8 5 ...
```

```
##
    $ Functional
                   : Factor w/ 7 levels "Maj1", "Maj2", ...: 7 7 7 7 7 7 7 7 3 7 ...
    $ Fireplaces
                   : int 0 1 1 1 1 0 1 2 2 2 ...
##
                   : Factor w/ 5 levels "Ex", "Fa", "Gd", ...: NA 5 5 3 5 NA 3 5 5 5 ...
##
    $ FireplaceQu
    $ GarageType
                   : Factor w/ 6 levels "2Types", "Attchd", ...: 2 2 2 6 2 2 2 6 2 ...
##
    $ GarageYrBlt
                          2003 1976 2001 1998 2000 1993 2004 1973 1931 1939 ...
##
    $ GarageFinish : Factor w/ 3 levels "Fin", "RFn", "Unf": 2 2 2 3 2 3 2 2 3 2 ...
##
##
    $ GarageCars
                   : int
                          2 2 2 3 3 2 2 2 2 1 ...
##
    $ GarageArea
                         548 460 608 642 836 480 636 484 468 205 ...
                   : Factor w/ 5 levels "Ex", "Fa", "Gd", ...: 5 5 5 5 5 5 5 5 2 3 ....
    $ GarageQual
##
##
    $ GarageCond
                   : Factor w/ 5 levels "Ex", "Fa", "Gd", ...: 5 5 5 5 5 5 5 5 5 5 ...
    $ PavedDrive
                   : Factor w/ 3 levels "N", "P", "Y": 3 3 3 3 3 3 3 3 3 3 ...
##
    $ WoodDeckSF
                   : int 0 298 0 0 192 40 255 235 90 0 ...
##
##
    $ OpenPorchSF
                   : int 61 0 42 35 84 30 57 204 0 4 ...
    $ EnclosedPorch: int 0 0 0 272 0 0 0 228 205 0 ...
##
                   : int 000003200000...
    $ X3SsnPorch
##
##
    $ ScreenPorch
                   : int
                         0 0 0 0 0 0 0 0 0 0 ...
    $ PoolArea
                   : int 0000000000...
##
                   : Factor w/ 3 levels "Ex", "Fa", "Gd": NA ...
##
    $ PoolQC
##
    $ Fence
                   : Factor w/ 4 levels "GdPrv", "GdWo", ...: NA ...
##
    $ MiscFeature
                   : Factor w/ 4 levels "Gar2", "Othr", ...: NA NA NA NA NA NA 3 NA 3 NA NA ...
                          0 0 0 0 0 700 0 350 0 0 ...
##
    $ MiscVal
    $ MoSold
                          2 5 9 2 12 10 8 11 4 1 ...
##
                   : int
    $ YrSold
                          2008 2007 2008 2006 2008 2009 2007 2009 2008 2008 ...
##
                   : Factor w/ 9 levels "COD", "Con", "ConLD", ...: 9 9 9 9 9 9 9 9 9 ...
##
    $ SaleType
    $ SaleCondition: Factor w/ 6 levels "Abnorml", "AdjLand",..: 5 5 5 1 5 5 5 5 1 5 ...
                   : int 208500 181500 223500 140000 250000 143000 307000 200000 129900 118000 ...
##
    $ SalePrice
```

The dataset consists of 1460 observations and 81 variables, some numeric and some categorical. The target variable has a minimum of 34,950 and a maximum of 7,550,000. The low median compared to the mean suggests some skew.

### **B.** Missing values There are missing values scattered throughout the dataset. We analyse them:





A few categorical features like fireplace, fence, etc. take up the bulk of missings. They do not appear to be important enough to retain so we delete them (FireplaceQu, Fence, Alley, MiscFeature, PoolQC, and LotFrontage). We impute the mean for the rest.

- **C. Create dummy variables** Now we create dummy variables for all of the character variables. Categorical NA's will be handled by adding a dummy variable for NA.
- **D.** Reconcile training and test sets We check if the dataset is missing columns from the test dataset and if so, drop them from the training set. This way we don't risk making predictions on training set variables not found in the test set.
- **E. Multicollinearity** We examine multicollinearity in the dataset. We look at all of the pairs of correlations over .8 There are 24 pairs.

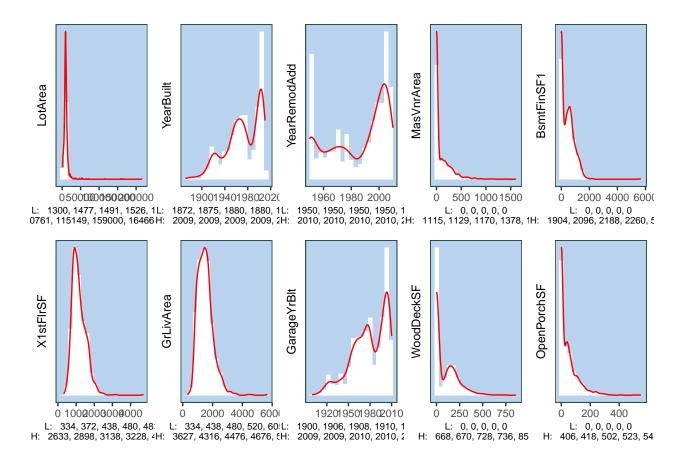
##	3	GrLivArea	${\tt TotRmsAbvGrd}$	0.8254894
##	5	GarageCars	GarageArea	0.8824754
##	7	MSZoning_FV	Neighborhood_Somerst	0.8628071
##	9	RoofStyle_Flat	RoofMatl_Tar.Grv	0.8349139
##	11	Exterior1st_AsbShng	Exterior2nd_AsbShng	0.8479167
##	12	Exterior1st_CemntBd	Exterior2nd_CmentBd	0.9741711
##	13	Exterior1st_HdBoard	Exterior2nd_HdBoard	0.8832714
##	14	Exterior1st_MetalSd	Exterior2nd_MetalSd	0.9730652
##	15	Exterior1st_Wd.Sdng	Exterior2nd_Wd.Sdng	0.8592439
##	21	Foundation_Slab	${\tt BsmtQual\_NA}$	0.8017334
##	22	Foundation_Slab	${\tt BsmtCond\_NA}$	0.8017334
##	23	Foundation_Slab	${\tt BsmtFinType1\_NA}$	0.8017334
##	25	${\tt BsmtQual\_NA}$	${\tt BsmtCond\_NA}$	1.0000000
##	26	${\tt BsmtQual\_NA}$	${\tt BsmtExposure\_NA}$	0.9864076
##	27	${\tt BsmtQual\_NA}$	${\tt BsmtFinType1\_NA}$	1.0000000
##	28	${\tt BsmtQual\_NA}$	${\tt BsmtFinType2\_NA}$	0.9864076
##	31	${\tt BsmtCond\_NA}$	${\tt BsmtExposure\_NA}$	0.9864076
##	32	${\tt BsmtCond\_NA}$	${\tt BsmtFinType1\_NA}$	1.0000000
##	33	${\tt BsmtCond\_NA}$	${\tt BsmtFinType2\_NA}$	0.9864076
##	36	${\tt BsmtExposure\_NA}$	${\tt BsmtFinType1\_NA}$	0.9864076
##	37	${\tt BsmtExposure\_NA}$	BsmtFinType2_NA	0.9729810
##	42	${\tt BsmtFinType1\_NA}$	${\tt BsmtFinType2\_NA}$	0.9864076
##	47	SaleType_New	SaleCondition_Partial	0.9868190

Most of the pairs make sense - siding on the first floor will match siding on the second floor, the number of cars a garage can hold will be related to its area. We will address the multicollinearity more closely when we run the analysis.

# 2. Transformations

A. Log of SalePrice The skew in the dependent variable suggests a log transformation.

B. Other transformations A number of histograms suggest issues with some of the independent variables.



We can see some transformations might be useful. We: 1. Add a dummy variable to mark YearBuilt before and after 1920 2. We set YearRemodAdd = 1950 to 0, and create a dummy variable YearRemodUnknown to track it 3. We add dummies for NoFinBsmt, HasDeck, and HasPorch 4. We eliminate outliers by setting GrLivArea<4000

#### 3. Model and Predict:

**A. Base Model** We run an OLS regression using the stepAIC algorithm to minimize AIC.

```
##
## Call:
## lm(formula = SalePrice ~ Id + LotArea + OverallQual + OverallCond +
## YearBuilt + YearRemodAdd + BsmtFinSF1 + BsmtFinSF2 + BsmtUnfSF +
## X1stFlrSF + X2ndFlrSF + LowQualFinSF + BsmtFullBath + FullBath +
## HalfBath + KitchenAbvGr + Fireplaces + GarageCars + GarageArea +
## WoodDeckSF + OpenPorchSF + EnclosedPorch + X3SsnPorch + ScreenPorch +
```

```
PoolArea + MSZoning_C..all. + MSZoning_RM + Street_Grvl +
##
##
       LotConfig_CulDSac + LandSlope_Sev + Neighborhood_BrkSide +
##
       Neighborhood_ClearCr + Neighborhood_Crawfor + Neighborhood_Edwards +
##
       Neighborhood IDOTRR + Neighborhood MeadowV + Neighborhood Mitchel +
##
       Neighborhood_NWAmes + Neighborhood_NoRidge + Neighborhood_NridgHt +
##
       Neighborhood_Somerst + Neighborhood_StoneBr + Condition1_Artery +
##
       Condition1_RRAe + Condition1_RRAn + BldgType_Duplex + BldgType_Twnhs +
##
       BldgType_TwnhsE + RoofStyle_Flat + Exterior1st_BrkComm +
       Exterior1st BrkFace + Exterior1st CemntBd + Exterior1st HdBoard +
##
##
       Exterior1st_Plywood + Exterior1st_Wd.Sdng + Exterior2nd_CmentBd +
##
       Exterior2nd_Wd.Sdng + MasVnrType_BrkCmn + MasVnrType_Stone +
       ExterCond_Ex + ExterCond_Fa + ExterCond_Gd + Foundation_Stone +
##
##
       Foundation_Wood + BsmtQual_Ex + BsmtCond_Fa + BsmtCond_Po +
##
       BsmtExposure_Gd + BsmtFinType2_BLQ + BsmtFinType2_GLQ + Heating_GasW +
##
       Heating_Grav + Heating_Wall + CentralAir_N + KitchenQual_Ex +
##
       Functional_Maj1 + Functional_Maj2 + Functional_Min1 + Functional_Min2 +
##
       Functional_Mod + Functional_Sev + GarageType_2Types + GarageType_NA +
       GarageQual_Fa + GarageQual_Po + GarageCond_Fa + GarageCond_Po +
##
##
       PavedDrive_N + SaleType_CWD + SaleType_Con + SaleType_ConLD +
##
       SaleType_ConLw + SaleType_New + SaleType_Oth + SaleCondition_Abnorml +
       SaleCondition_Family + SaleCondition_Partial + BuiltAfter1920 +
##
       YearRemodUnknown, data = df)
##
##
## Residuals:
##
        Min
                  1Q
                      Median
                                    3Q
                                            Max
## -0.67671 -0.04919 0.00285 0.05111 0.46324
##
## Coefficients:
##
                           Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                          4.497e+00 5.680e-01
                                                 7.918 4.97e-15 ***
## Id
                         -9.095e-06 6.429e-06 -1.415 0.157355
## LotArea
                          2.600e-06 3.859e-07
                                                 6.738 2.37e-11 ***
## OverallQual
                          4.738e-02 3.865e-03 12.258 < 2e-16 ***
```

```
## OverallCond
                          3.739e-02 3.501e-03 10.681 < 2e-16 ***
## YearBuilt
                          2.426e-03 2.618e-04
                                                 9.267 < 2e-16 ***
## YearRemodAdd
                          8.239e-04 2.532e-04
                                                 3.255 0.001164 **
## BsmtFinSF1
                          1.614e-04 1.476e-05 10.936 < 2e-16 ***
## BsmtFinSF2
                          1.153e-04 2.312e-05
                                                 4.986 6.98e-07 ***
## BsmtUnfSF
                                                 7.548 8.09e-14 ***
                          9.846e-05 1.305e-05
## X1stFlrSF
                          2.669e-04 1.638e-05
                                                16.293 < 2e-16 ***
## X2ndFlrSF
                          2.570e-04 1.274e-05
                                                20.169 < 2e-16 ***
## LowQualFinSF
                          2.394e-04 5.854e-05
                                                 4.090 4.58e-05 ***
## BsmtFullBath
                          2.752e-02 7.453e-03
                                                 3.693 0.000231 ***
## FullBath
                          1.898e-02 8.570e-03
                                                 2.215 0.026912 *
## HalfBath
                          1.867e-02 8.196e-03
                                                 2.277 0.022926 *
## KitchenAbvGr
                         -5.083e-02 1.895e-02
                                               -2.683 0.007388 **
## Fireplaces
                          1.974e-02 5.418e-03
                                                 3.643 0.000279 ***
                                                 3.351 0.000827 ***
## GarageCars
                          3.053e-02 9.111e-03
## GarageArea
                          6.558e-05 3.021e-05
                                                 2.171 0.030083 *
## WoodDeckSF
                          8.737e-05 2.401e-05
                                                 3.639 0.000284 ***
                                                 2.264 0.023702 *
## OpenPorchSF
                          1.055e-04 4.660e-05
## EnclosedPorch
                          1.094e-04 5.013e-05
                                                 2.182 0.029263 *
## X3SsnPorch
                          1.885e-04 9.255e-05
                                                 2.037 0.041878 *
## ScreenPorch
                                                 4.518 6.78e-06 ***
                          2.295e-04 5.078e-05
## PoolArea
                          1.175e-04 7.820e-05
                                                 1.503 0.133101
## MSZoning_C..all.
                         -4.260e-01 4.027e-02 -10.580 < 2e-16 ***
## MSZoning_RM
                         -6.101e-02 1.060e-02 -5.756 1.06e-08 ***
## Street Grvl
                         -8.150e-02 4.677e-02 -1.742 0.081684 .
## LotConfig_CulDSac
                          3.232e-02 1.157e-02
                                                 2.793 0.005289 **
## LandSlope_Sev
                         -1.274e-01 3.958e-02 -3.218 0.001323 **
## Neighborhood_BrkSide
                         5.767e-02 1.588e-02
                                                 3.631 0.000293 ***
## Neighborhood_ClearCr
                          5.267e-02 2.233e-02
                                                 2.358 0.018517 *
## Neighborhood_Crawfor
                          1.453e-01 1.659e-02
                                                 8.760 < 2e-16 ***
## Neighborhood_Edwards -3.461e-02 1.193e-02 -2.901 0.003782 **
## Neighborhood_IDOTRR
                         3.522e-02 2.210e-02
                                                 1.593 0.111325
## Neighborhood_MeadowV -1.180e-01 3.263e-02 -3.617 0.000309 ***
```

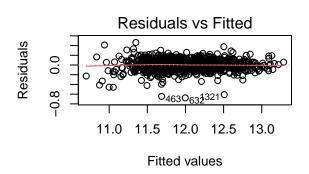
```
## Neighborhood_Mitchel -2.182e-02 1.573e-02 -1.387 0.165621
## Neighborhood_NWAmes
                        -2.698e-02 1.351e-02 -1.997 0.046026 *
## Neighborhood_NoRidge
                         5.057e-02 1.853e-02
                                                2.729 0.006443 **
## Neighborhood_NridgHt
                                                3.789 0.000158 ***
                         6.080e-02 1.605e-02
## Neighborhood_Somerst
                        4.679e-02 1.377e-02
                                                3.399 0.000696 ***
                                                5.449 6.00e-08 ***
## Neighborhood_StoneBr
                        1.244e-01 2.282e-02
## Condition1_Artery
                        -6.968e-02 1.609e-02
                                               -4.331 1.60e-05 ***
                                               -3.774 0.000168 ***
## Condition1_RRAe
                        -1.178e-01 3.122e-02
## Condition1_RRAn
                        -3.755e-02 2.077e-02 -1.808 0.070808 .
## BldgType_Duplex
                        -4.643e-02 2.187e-02 -2.123 0.033904 *
## BldgType_Twnhs
                        -9.935e-02 1.853e-02 -5.362 9.68e-08 ***
## BldgType_TwnhsE
                        -3.713e-02 1.224e-02 -3.034 0.002460 **
## RoofStyle_Flat
                         6.984e-02 3.551e-02
                                                1.967 0.049422 *
## Exterior1st_BrkComm
                        -2.137e-01 7.879e-02 -2.712 0.006775 **
## Exterior1st_BrkFace
                         3.442e-02 1.680e-02
                                                2.049 0.040636 *
## Exterior1st_CemntBd
                        -9.097e-02 6.111e-02 -1.489 0.136825
## Exterior1st_HdBoard
                        -3.707e-02 8.732e-03
                                              -4.246 2.33e-05 ***
## Exterior1st_Plywood
                        -3.344e-02 1.206e-02 -2.772 0.005649 **
                        -6.159e-02 1.661e-02 -3.707 0.000218 ***
## Exterior1st_Wd.Sdng
## Exterior2nd_CmentBd
                        8.753e-02 6.156e-02
                                                1.422 0.155343
## Exterior2nd_Wd.Sdng
                         4.423e-02 1.637e-02
                                                2.702 0.006970 **
## MasVnrType_BrkCmn
                        -5.277e-02 2.780e-02 -1.898 0.057862 .
## MasVnrType_Stone
                         2.179e-02 1.121e-02
                                                1.944 0.052089 .
## ExterCond_Ex
                         1.013e-01 6.055e-02
                                                1.672 0.094696 .
## ExterCond Fa
                        -3.659e-02 2.264e-02
                                               -1.616 0.106303
## ExterCond_Gd
                        -1.809e-02 9.700e-03
                                              -1.864 0.062477 .
                         1.026e-01 4.444e-02
                                                2.309 0.021089 *
## Foundation_Stone
## Foundation_Wood
                        -1.391e-01 5.955e-02 -2.336 0.019641 *
## BsmtQual_Ex
                         2.848e-02 1.331e-02
                                                2.140 0.032529 *
## BsmtCond_Fa
                        -3.251e-02 1.692e-02 -1.922 0.054858 .
## BsmtCond_Po
                         1.691e-01 9.088e-02
                                                1.861 0.062987 .
## BsmtExposure_Gd
                         5.052e-02 1.093e-02
                                                4.621 4.19e-06 ***
## BsmtFinType2_BLQ
                        -3.235e-02 1.922e-02 -1.683 0.092602 .
```

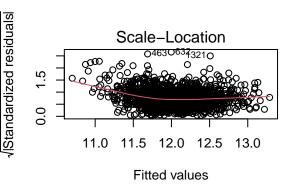
```
## BsmtFinType2_GLQ
                         5.425e-02 3.079e-02
                                               1.762 0.078250 .
## Heating_GasW
                         5.224e-02 2.727e-02
                                               1.916 0.055622 .
## Heating_Grav
                        -1.477e-01 4.379e-02 -3.372 0.000766 ***
## Heating Wall
                         8.911e-02 5.559e-02
                                               1.603 0.109163
## CentralAir_N
                        -6.317e-02 1.427e-02 -4.426 1.04e-05 ***
                         6.301e-02 1.374e-02
                                               4.587 4.92e-06 ***
## KitchenQual_Ex
## Functional_Maj1
                        -9.671e-02 2.996e-02 -3.228 0.001278 **
## Functional_Maj2
                        -3.104e-01 4.978e-02 -6.237 5.96e-10 ***
## Functional Min1
                        -4.847e-02 1.949e-02 -2.487 0.013004 *
## Functional_Min2
                        -3.440e-02 1.879e-02 -1.830 0.067441 .
                        -1.175e-01 2.820e-02 -4.167 3.28e-05 ***
## Functional_Mod
## Functional_Sev
                        -4.125e-01 1.119e-01 -3.685 0.000238 ***
                        -8.141e-02 4.455e-02 -1.827 0.067892 .
## GarageType_2Types
## GarageType_NA
                        -4.205e-02 1.710e-02 -2.459 0.014066 *
## GarageQual_Fa
                        -3.572e-02 1.914e-02 -1.866 0.062228 .
## GarageQual_Po
                        -1.359e-01 8.849e-02 -1.536 0.124782
## GarageCond_Fa
                        -3.201e-02 2.103e-02 -1.522 0.128259
## GarageCond_Po
                         1.079e-01 5.623e-02
                                               1.919 0.055189 .
## PavedDrive_N
                        -1.862e-02 1.352e-02 -1.378 0.168529
## SaleType_CWD
                         8.151e-02 5.230e-02
                                               1.559 0.119343
## SaleType_Con
                         1.233e-01 7.211e-02
                                               1.710 0.087502 .
                                               3.645 0.000277 ***
## SaleType_ConLD
                         1.333e-01 3.657e-02
## SaleType_ConLw
                         6.869e-02 4.704e-02
                                               1.460 0.144458
## SaleType_New
                         1.772e-01 6.258e-02
                                               2.832 0.004696 **
## SaleType_Oth
                         8.899e-02 5.994e-02
                                               1.485 0.137864
## SaleCondition_Abnorml -6.940e-02 1.128e-02 -6.150 1.02e-09 ***
## SaleCondition_Family -4.724e-02 2.339e-02 -2.020 0.043582 *
## SaleCondition_Partial -1.311e-01 6.197e-02 -2.116 0.034563 *
## BuiltAfter1920
                        -2.748e-02 1.554e-02 -1.768 0.077271 .
## YearRemodUnknown
                        1.598e+00 5.011e-01
                                               3.188 0.001464 **
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
```

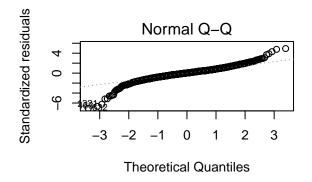
```
## Residual standard error: 0.09995 on 1356 degrees of freedom
## Multiple R-squared: 0.9406, Adjusted R-squared: 0.9363
## F-statistic: 217.1 on 99 and 1356 DF, p-value: < 2.2e-16
##
   [1] "VIF Analysis"
                      Ιd
                                       LotArea
                                                         OverallQual
##
                1.070446
                                      2.109227
                                                            4.082242
             OverallCond
                                                        YearRemodAdd
##
                                     YearBuilt
                2.214804
                                      9.101482
                                                         3969.919813
##
##
              BsmtFinSF1
                                    BsmtFinSF2
                                                           BsmtUnfSF
                5.870162
                                      2.030635
                                                            4.846297
##
                                                        LowQualFinSF
               X1stFlrSF
                                     X2ndFlrSF
##
##
                5.329108
                                      4.402165
                                                            1.183029
            BsmtFullBath
##
                                      FullBath
                                                            HalfBath
                                                            2.470764
                2.165471
                                      3.208325
##
            KitchenAbvGr
                                    Fireplaces
                                                          GarageCars
                2.544832
                                      1.752755
                                                            6.732297
##
              GarageArea
                                    WoodDeckSF
                                                         OpenPorchSF
##
                5.970826
                                      1.315971
                                                            1.350534
##
##
           EnclosedPorch
                                    X3SsnPorch
                                                         ScreenPorch
                1.370222
                                      1.074979
                                                            1.170604
##
##
                PoolArea
                              MSZoning_C..all.
                                                         MSZoning_RM
                1.114980
                                      1.611695
                                                            2.083850
##
             Street_Grvl
                             LotConfig_CulDSac
                                                       LandSlope_Sev
##
                1.308506
                                      1.178051
                                                            2.020225
    Neighborhood_BrkSide
                          Neighborhood_ClearCr Neighborhood_Crawfor
##
                1.406034
                                      1.371166
                                                            1.355105
    Neighborhood_Edwards
                           ##
                1.302697
                                      1.763348
                                                            1.790537
    Neighborhood Mitchel
                           Neighborhood_NWAmes Neighborhood_NoRidge
##
                1.172639
                                      1.266834
                                                            1.305002
    Neighborhood_NridgHt
                          Neighborhood_Somerst Neighborhood_StoneBr
##
                1.879891
                                      1.535288
                                                            1.281182
```

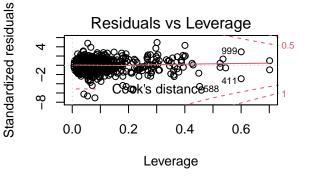
##	Condition1_Artery	Condition1_RRAe	Condition1_RRAn
##	1.202671	1.065123	1.102368
##	BldgType_Duplex	BldgType_Twnhs	BldgType_TwnhsE
##	2.399890	1.434197	1.575527
##	RoofStyle_Flat	Exterior1st_BrkComm	Exterior1st_BrkFace
##	1.626001	1.240871	1.363344
##	Exterior1st_CemntBd	Exterior1st_HdBoard	Exterior1st_Plywood
##	21.501494	1.430582	1.456569
##	Exterior1st_Wd.Sdng	Exterior2nd_CmentBd	Exterior2nd_Wd.Sdng
##	4.865587	21.475610	4.567847
##	MasVnrType_BrkCmn	MasVnrType_Stone	ExterCond_Ex
##	1.148006	1.447534	1.098791
##	ExterCond_Fa	${\tt ExterCond\_Gd}$	Foundation_Stone
##	1.408762	1.237170	1.181241
##	Foundation_Wood	${\tt BsmtQual\_Ex}$	BsmtCond_Fa
##	1.062645	1.907796	1.249316
##	BsmtCond_Po	${\tt BsmtExposure\_Gd}$	BsmtFinType2_BLQ
##	1.651124	1.426619	1.192674
##	${\tt BsmtFinType2\_GLQ}$	Heating_GasW	Heating_Grav
##	1.315372	1.323281	1.336804
##	Heating_Wall	CentralAir_N	KitchenQual_Ex
##	1.233841	1.811117	1.693583
##	Functional_Maj1	Functional_Maj2	Functional_Min1
##	1.245837	1.235746	1.153368
##	Functional_Min2	$Functional\_Mod$	Functional_Sev
##	1.173951	1.181688	1.253489
##	<pre>GarageType_2Types</pre>	${\tt GarageType\_NA}$	GarageQual_Fa
##	1.187210	2.238917	1.702411
##	GarageQual_Po	<pre>GarageCond_Fa</pre>	<pre>GarageCond_Po</pre>
##	2.346550	1.512048	2.204323
##	PavedDrive_N	SaleType_CWD	SaleType_Con
##	1.543691	1.092156	1.039413
##	SaleType_ConLD	SaleType_ConLw	SaleType_New

```
##
                1.197037
                                       1.103716
                                                             43.157779
            SaleType_Oth SaleCondition_Abnorml SaleCondition_Family
##
                                       1.186853
                                                              1.079773
##
## SaleCondition_Partial
                                                      YearRemodUnknown
                                 BuiltAfter1920
##
               43.285823
                                       2.622103
                                                           3926.926004
```









##
## studentized Breusch-Pagan test
##
## data: step3
## BP = 270.14, df = 99, p-value < 2.2e-16
##
##</pre>

## Shapiro-Wilk normality test

## NULL

##

```
## data: step3$residuals
## W = 0.93874, p-value < 2.2e-16
##
## [1] "AIC: -2476.10190734742"
##
## Call:
## lm(formula = SalePrice ~ Id + LotArea + OverallQual + OverallCond +
##
       YearBuilt + YearRemodAdd + BsmtFinSF1 + BsmtFinSF2 + BsmtUnfSF +
       X1stFlrSF + X2ndFlrSF + LowQualFinSF + BsmtFullBath + FullBath +
##
##
       HalfBath + KitchenAbvGr + Fireplaces + GarageCars + GarageArea +
##
       WoodDeckSF + OpenPorchSF + EnclosedPorch + X3SsnPorch + ScreenPorch +
##
       PoolArea + MSZoning_C..all. + MSZoning_RM + Street_Grvl +
##
       LotConfig_CulDSac + LandSlope_Sev + Neighborhood_BrkSide +
##
       Neighborhood ClearCr + Neighborhood Crawfor + Neighborhood Edwards +
       Neighborhood_IDOTRR + Neighborhood_MeadowV + Neighborhood_Mitchel +
##
##
       Neighborhood_NWAmes + Neighborhood_NoRidge + Neighborhood_NridgHt +
##
       Neighborhood_Somerst + Neighborhood_StoneBr + Condition1_Artery +
##
       Condition1_RRAe + Condition1_RRAn + BldgType_Duplex + BldgType_Twnhs +
##
       BldgType TwnhsE + RoofStyle Flat + Exterior1st BrkComm +
##
       Exterior1st_BrkFace + Exterior1st_CemntBd + Exterior1st_HdBoard +
       Exterior1st_Plywood + Exterior1st_Wd.Sdng + Exterior2nd_CmentBd +
##
##
       Exterior2nd_Wd.Sdng + MasVnrType_BrkCmn + MasVnrType_Stone +
##
       ExterCond_Ex + ExterCond_Fa + ExterCond_Gd + Foundation_Stone +
##
       Foundation_Wood + BsmtQual_Ex + BsmtCond_Fa + BsmtCond_Po +
##
       BsmtExposure_Gd + BsmtFinType2_BLQ + BsmtFinType2_GLQ + Heating_GasW +
##
       Heating_Grav + Heating_Wall + CentralAir_N + KitchenQual_Ex +
       Functional_Maj1 + Functional_Maj2 + Functional_Min1 + Functional_Min2 +
##
##
       Functional_Mod + Functional_Sev + GarageType_2Types + GarageType_NA +
##
       GarageQual_Fa + GarageQual_Po + GarageCond_Fa + GarageCond_Po +
       PavedDrive_N + SaleType_CWD + SaleType_Con + SaleType_ConLD +
##
##
       SaleType_ConLw + SaleType_New + SaleType_Oth + SaleCondition_Abnorm1 +
##
       SaleCondition_Family + SaleCondition_Partial + BuiltAfter1920 +
```

```
##
       YearRemodUnknown, data = df)
##
## Residuals:
       Min
                 1Q
                      Median
                                    3Q
##
                                           Max
  -0.67671 -0.04919 0.00285 0.05111 0.46324
##
## Coefficients:
##
                           Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         4.497e+00 5.680e-01
                                                7.918 4.97e-15 ***
## Id
                         -9.095e-06 6.429e-06 -1.415 0.157355
## LotArea
                         2.600e-06 3.859e-07
                                                 6.738 2.37e-11 ***
## OverallQual
                         4.738e-02 3.865e-03 12.258 < 2e-16 ***
## OverallCond
                         3.739e-02 3.501e-03 10.681 < 2e-16 ***
## YearBuilt
                          2.426e-03 2.618e-04
                                                 9.267 < 2e-16 ***
## YearRemodAdd
                                                 3.255 0.001164 **
                         8.239e-04 2.532e-04
## BsmtFinSF1
                         1.614e-04 1.476e-05 10.936 < 2e-16 ***
## BsmtFinSF2
                          1.153e-04 2.312e-05
                                                 4.986 6.98e-07 ***
## BsmtUnfSF
                         9.846e-05 1.305e-05
                                                 7.548 8.09e-14 ***
                          2.669e-04 1.638e-05
## X1stFlrSF
                                               16.293 < 2e-16 ***
## X2ndFlrSF
                          2.570e-04 1.274e-05 20.169 < 2e-16 ***
## LowQualFinSF
                                                 4.090 4.58e-05 ***
                          2.394e-04 5.854e-05
## BsmtFullBath
                                                 3.693 0.000231 ***
                          2.752e-02 7.453e-03
## FullBath
                          1.898e-02 8.570e-03
                                                 2.215 0.026912 *
                          1.867e-02 8.196e-03
## HalfBath
                                                 2.277 0.022926 *
## KitchenAbvGr
                         -5.083e-02 1.895e-02
                                               -2.683 0.007388 **
## Fireplaces
                         1.974e-02 5.418e-03
                                                 3.643 0.000279 ***
## GarageCars
                         3.053e-02 9.111e-03
                                                 3.351 0.000827 ***
                                                 2.171 0.030083 *
## GarageArea
                          6.558e-05 3.021e-05
## WoodDeckSF
                          8.737e-05 2.401e-05
                                                 3.639 0.000284 ***
## OpenPorchSF
                         1.055e-04 4.660e-05
                                                 2.264 0.023702 *
## EnclosedPorch
                         1.094e-04 5.013e-05
                                                 2.182 0.029263 *
## X3SsnPorch
                         1.885e-04 9.255e-05
                                                 2.037 0.041878 *
## ScreenPorch
                          2.295e-04 5.078e-05
                                                 4.518 6.78e-06 ***
```

```
## PoolArea
                         1.175e-04 7.820e-05
                                                1.503 0.133101
## MSZoning_C..all.
                        -4.260e-01 4.027e-02 -10.580 < 2e-16 ***
## MSZoning_RM
                        -6.101e-02 1.060e-02 -5.756 1.06e-08 ***
## Street Grvl
                        -8.150e-02 4.677e-02 -1.742 0.081684 .
## LotConfig_CulDSac
                         3.232e-02 1.157e-02
                                                2.793 0.005289 **
                        -1.274e-01 3.958e-02 -3.218 0.001323 **
## LandSlope_Sev
## Neighborhood_BrkSide
                         5.767e-02 1.588e-02
                                                3.631 0.000293 ***
## Neighborhood_ClearCr
                         5.267e-02 2.233e-02
                                                2.358 0.018517 *
                         1.453e-01 1.659e-02
## Neighborhood_Crawfor
                                                8.760 < 2e-16 ***
## Neighborhood_Edwards
                        -3.461e-02 1.193e-02
                                               -2.901 0.003782 **
## Neighborhood_IDOTRR
                         3.522e-02 2.210e-02
                                                1.593 0.111325
## Neighborhood_MeadowV
                        -1.180e-01 3.263e-02
                                               -3.617 0.000309 ***
## Neighborhood_Mitchel
                        -2.182e-02 1.573e-02
                                              -1.387 0.165621
## Neighborhood_NWAmes
                        -2.698e-02 1.351e-02 -1.997 0.046026 *
## Neighborhood_NoRidge
                         5.057e-02 1.853e-02
                                                2.729 0.006443 **
## Neighborhood_NridgHt
                         6.080e-02 1.605e-02
                                                3.789 0.000158 ***
## Neighborhood_Somerst
                                                3.399 0.000696 ***
                         4.679e-02 1.377e-02
## Neighborhood_StoneBr
                         1.244e-01 2.282e-02
                                                5.449 6.00e-08 ***
## Condition1_Artery
                        -6.968e-02 1.609e-02
                                               -4.331 1.60e-05 ***
## Condition1_RRAe
                        -1.178e-01 3.122e-02 -3.774 0.000168 ***
## Condition1_RRAn
                        -3.755e-02 2.077e-02
                                               -1.808 0.070808 .
## BldgType_Duplex
                        -4.643e-02 2.187e-02 -2.123 0.033904 *
## BldgType_Twnhs
                        -9.935e-02 1.853e-02 -5.362 9.68e-08 ***
## BldgType_TwnhsE
                        -3.713e-02 1.224e-02 -3.034 0.002460 **
## RoofStyle Flat
                         6.984e-02 3.551e-02
                                                1.967 0.049422 *
## Exterior1st_BrkComm
                        -2.137e-01 7.879e-02 -2.712 0.006775 **
                         3.442e-02 1.680e-02
                                                2.049 0.040636 *
## Exterior1st_BrkFace
## Exterior1st_CemntBd
                        -9.097e-02 6.111e-02 -1.489 0.136825
## Exterior1st_HdBoard
                        -3.707e-02 8.732e-03 -4.246 2.33e-05 ***
## Exterior1st_Plywood
                        -3.344e-02 1.206e-02 -2.772 0.005649 **
## Exterior1st_Wd.Sdng
                        -6.159e-02 1.661e-02 -3.707 0.000218 ***
## Exterior2nd_CmentBd
                         8.753e-02 6.156e-02
                                                1.422 0.155343
## Exterior2nd_Wd.Sdng
                         4.423e-02 1.637e-02
                                                2.702 0.006970 **
```

```
## MasVnrType_BrkCmn
                        -5.277e-02 2.780e-02 -1.898 0.057862 .
## MasVnrType_Stone
                         2.179e-02 1.121e-02
                                                1.944 0.052089 .
## ExterCond_Ex
                         1.013e-01 6.055e-02
                                                1.672 0.094696 .
                        -3.659e-02 2.264e-02 -1.616 0.106303
## ExterCond Fa
## ExterCond_Gd
                        -1.809e-02 9.700e-03 -1.864 0.062477 .
                                                2.309 0.021089 *
## Foundation_Stone
                         1.026e-01 4.444e-02
## Foundation_Wood
                        -1.391e-01 5.955e-02 -2.336 0.019641 *
## BsmtQual_Ex
                         2.848e-02 1.331e-02
                                                2.140 0.032529 *
## BsmtCond Fa
                        -3.251e-02 1.692e-02 -1.922 0.054858 .
## BsmtCond_Po
                         1.691e-01 9.088e-02
                                                1.861 0.062987 .
## BsmtExposure_Gd
                         5.052e-02 1.093e-02
                                                4.621 4.19e-06 ***
## BsmtFinType2_BLQ
                        -3.235e-02 1.922e-02 -1.683 0.092602 .
## BsmtFinType2_GLQ
                         5.425e-02 3.079e-02
                                                1.762 0.078250 .
## Heating_GasW
                         5.224e-02 2.727e-02
                                                1.916 0.055622 .
## Heating_Grav
                        -1.477e-01 4.379e-02 -3.372 0.000766 ***
## Heating_Wall
                         8.911e-02 5.559e-02
                                                1.603 0.109163
## CentralAir_N
                        -6.317e-02 1.427e-02 -4.426 1.04e-05 ***
## KitchenQual_Ex
                         6.301e-02 1.374e-02
                                                4.587 4.92e-06 ***
## Functional_Maj1
                        -9.671e-02 2.996e-02 -3.228 0.001278 **
                        -3.104e-01 4.978e-02 -6.237 5.96e-10 ***
## Functional_Maj2
## Functional_Min1
                        -4.847e-02 1.949e-02 -2.487 0.013004 *
## Functional_Min2
                        -3.440e-02 1.879e-02 -1.830 0.067441 .
## Functional_Mod
                        -1.175e-01 2.820e-02 -4.167 3.28e-05 ***
## Functional_Sev
                        -4.125e-01 1.119e-01 -3.685 0.000238 ***
## GarageType_2Types
                        -8.141e-02 4.455e-02 -1.827 0.067892 .
## GarageType_NA
                        -4.205e-02 1.710e-02 -2.459 0.014066 *
## GarageQual_Fa
                        -3.572e-02 1.914e-02 -1.866 0.062228 .
## GarageQual_Po
                        -1.359e-01 8.849e-02 -1.536 0.124782
## GarageCond_Fa
                        -3.201e-02 2.103e-02 -1.522 0.128259
## GarageCond_Po
                         1.079e-01 5.623e-02
                                                1.919 0.055189 .
## PavedDrive_N
                        -1.862e-02 1.352e-02 -1.378 0.168529
## SaleType_CWD
                         8.151e-02 5.230e-02
                                                1.559 0.119343
## SaleType_Con
                         1.233e-01 7.211e-02
                                                1.710 0.087502 .
```

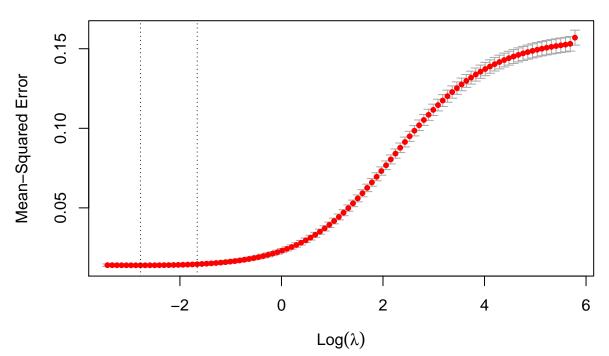
```
## SaleType_ConLD
                                                3.645 0.000277 ***
                         1.333e-01 3.657e-02
                                                1.460 0.144458
## SaleType_ConLw
                         6.869e-02 4.704e-02
## SaleType_New
                         1.772e-01 6.258e-02
                                                2.832 0.004696 **
## SaleType_Oth
                         8.899e-02 5.994e-02
                                                1.485 0.137864
## SaleCondition_Abnorml -6.940e-02 1.128e-02 -6.150 1.02e-09 ***
## SaleCondition_Family -4.724e-02 2.339e-02 -2.020 0.043582 *
## SaleCondition_Partial -1.311e-01 6.197e-02
                                              -2.116 0.034563 *
## BuiltAfter1920
                        -2.748e-02 1.554e-02 -1.768 0.077271 .
                                                3.188 0.001464 **
                         1.598e+00 5.011e-01
## YearRemodUnknown
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 0.09995 on 1356 degrees of freedom
## Multiple R-squared: 0.9406, Adjusted R-squared: 0.9363
## F-statistic: 217.1 on 99 and 1356 DF, p-value: < 2.2e-16
```

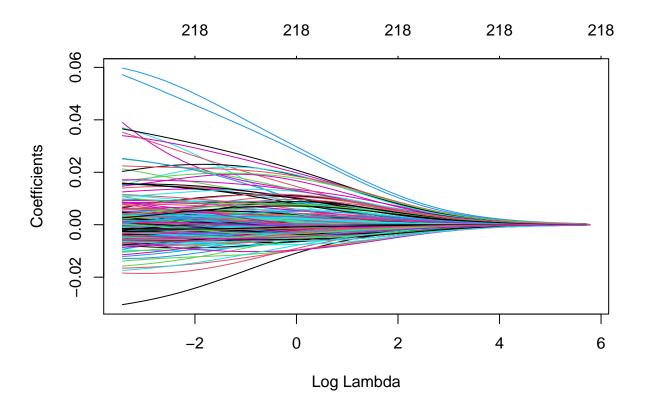
Now we make predictions

We achieve a score of .14586 on kaggle. This puts us in the 60th percentile.

**B. Ridge regression:** R makes it easy to find the best lambda by using kfold validation. Below are the results of our ridge regression analysis. Unlike stepAIC, ridge regression will retain all of the variables.







##	219	x	1	sparse	Matrix	of	class	"dgCMatrix"
##								s0
##	(Int	er	ce	ept)		1.	. 202194	le+01
##	Id					-3.	.316167	′e-03
##	MSSt	1b(	Cla	ass		-1.	. 220442	2e-03
##	LotA	٩re	ea			1.	. 893276	Se-02
##	Over	ra]	10	Qual		5.	. 585056	Se-02
##	Over	ra]	10	Cond		3.	.307967	re-02
##	Year	rΒι	ıi]	Lt		2.	.921600	)e-02
##	Year	cRe	emo	odAdd		8.	. 396676	Se-03
##	MasV	/nr	:A:	rea		4.	. 463805	5e-03
##	Bsmt	Fi	nS	SF1		2.	. 321538	Be-02
##	Bsmt	Fi	nS	SF2		3.	. 394083	Be-03
##	Bsmt	Ur	ıfS	SF		5.	.868867	'e-03
##	Tota	alE	Bsi	ntSF		3.	. 205511	le-02

X1stFlrSF	3.398655e-02
X2ndFlrSF	3.074557e-02
LowQualFinSF	1.455037e-03
GrLivArea	5.219902e-02
BsmtFullBath	1.503678e-02
BsmtHalfBath	8.263591e-04
FullBath	2.215637e-02
HalfBath	1.461155e-02
BedroomAbvGr	1.862441e-03
KitchenAbvGr	-1.237620e-02
TotRmsAbvGrd	1.832210e-02
Fireplaces	1.635576e-02
GarageYrBlt	8.430868e-03
GarageCars	2.208106e-02
GarageArea	1.816561e-02
WoodDeckSF	9.495562e-03
OpenPorchSF	5.407171e-03
EnclosedPorch	5.396358e-03
X3SsnPorch	5.918845e-03
ScreenPorch	1.087578e-02
PoolArea	5.224207e-03
MiscVal	-1.893104e-03
MoSold	-7.361292e-04
YrSold	-1.847161e-03
MSZoning_Call.	-2.818916e-02
MSZoning_FV	7.785702e-03
MSZoning_RM	-1.298121e-02
Street_Grvl	-5.527020e-03
LotShape_IR1	1.066411e-03
LotShape_IR2	4.638174e-03
LotShape_IR3	1.459866e-03
LandContour_Bnk	-1.353820e-03
LandContour_HLS	2.920167e-03
	X2ndFlrSF LowQualFinSF GrLivArea BsmtFullBath BsmtHalfBath FullBath HalfBath BedroomAbvGr KitchenAbvGr TotRmsAbvGrd Fireplaces GarageYrBlt GarageCars GarageArea WoodDeckSF OpenPorchSF EnclosedPorch X3SsnPorch ScreenPorch PoolArea MiscVal MoSold YrSold MSZoning_Call. MSZoning_FV MSZoning_RM Street_Grvl LotShape_IR1 LotShape_IR2 LotShape_IR3 LandContour_Bnk

##	LandContour_Low	-1.090528e-03
##	LotConfig_Corner	2.845655e-03
##	LotConfig_CulDSac	9.062037e-03
##	LotConfig_FR2	-5.179079e-03
##	LotConfig_FR3	-1.621573e-03
##	LandSlope_Mod	2.208949e-03
##	LandSlope_Sev	-7.297180e-03
##	Neighborhood_Blmngtn	-6.953252e-05
##	Neighborhood_Blueste	-2.935210e-03
##	Neighborhood_BrDale	-8.574068e-03
##	Neighborhood_BrkSide	6.155806e-03
##	${\tt Neighborhood\_ClearCr}$	5.698727e-03
##	${\tt Neighborhood\_Crawfor}$	2.352916e-02
##	Neighborhood_Edwards	-9.885964e-03
##	Neighborhood_Gilbert	7.866620e-04
##	Neighborhood_IDOTRR	-2.564449e-03
##	${\tt Neighborhood\_MeadowV}$	-1.860140e-02
##	${\tt Neighborhood\_Mitchel}$	-4.492634e-03
##	Neighborhood_NPkVill	-1.720593e-03
##	Neighborhood_NWAmes	-5.253035e-03
##	Neighborhood_NoRidge	1.338503e-02
##	${\tt Neighborhood\_NridgHt}$	1.505907e-02
##	${\tt Neighborhood\_OldTown}$	-6.906287e-03
##	Neighborhood_SWISU	2.222073e-03
##	Neighborhood_Sawyer	-3.956776e-03
##	Neighborhood_SawyerW	3.338802e-03
##	Neighborhood_Somerst	8.494840e-03
##	Neighborhood_StoneBr	1.509195e-02
##	Neighborhood_Timber	2.700942e-03
##	Neighborhood_Veenker	4.898939e-03
##	Condition1_Artery	-1.112093e-02
##	Condition1_PosA	-1.514734e-03
##	Condition1_PosN	-1.596212e-03

##	Condition1_RRAe	-7.061452e-03
##	Condition1_RRAn	-4.276013e-03
##	Condition1_RRNe	-1.093182e-03
##	Condition1_RRNn	2.407893e-04
##	Condition2_Artery	-2.773141e-03
##	Condition2_Feedr	9.605498e-04
##	Condition2_PosA	1.834850e-03
##	Condition2_PosN	-2.011688e-03
##	BldgType_2fmCon	2.964283e-04
##	BldgType_Duplex	-7.780375e-03
##	BldgType_Twnhs	-9.402093e-03
##	BldgType_TwnhsE	-5.771063e-03
##	HouseStyle_1.5Fin	4.654782e-03
##	HouseStyle_1.5Unf	2.673297e-03
##	HouseStyle_2.5Unf	4.151987e-03
##	HouseStyle_SFoyer	-1.464736e-04
##	HouseStyle_SLvl	4.438741e-05
##	RoofStyle_Flat	6.634384e-03
##	RoofStyle_Gambrel	1.404284e-03
##	RoofStyle_Hip	6.641289e-04
##	RoofStyle_Mansard	3.335277e-03
##	RoofStyle_Shed	3.566185e-03
##	RoofMatl_Tar.Grv	-3.690499e-03
##	RoofMatl_WdShake	9.022830e-04
##	RoofMatl_WdShngl	5.057080e-03
##	Exterior1st_AsbShng	2.512051e-04
##	Exterior1st_AsphShn	-4.090004e-05
##	Exterior1st_BrkComm	-7.193092e-03
##	Exterior1st_BrkFace	1.033384e-02
##	Exterior1st_CBlock	-2.707114e-04
##	Exterior1st_CemntBd	-1.295719e-03
##	Exterior1st_HdBoard	-7.948707e-03
##	Exterior1st_MetalSd	-2.068717e-03

##	Exterior1st_Plywood	-4.989657e-03
##	Exterior1st_Stucco	1.456822e-03
##	Exterior1st_Wd.Sdng	-1.036136e-02
##	Exterior1st_WdShing	-3.589031e-03
##	Exterior2nd_AsbShng	-3.280628e-03
##	Exterior2nd_AsphShn	8.795836e-04
##	Exterior2nd_Brk.Cmn	-1.936721e-03
##	Exterior2nd_BrkFace	-5.905631e-03
##	Exterior2nd_CBlock	-2.688550e-04
##	Exterior2nd_CmentBd	1.735964e-03
##	Exterior2nd_HdBoard	-7.017346e-03
##	Exterior2nd_ImStucc	-7.981273e-04
##	Exterior2nd_MetalSd	-2.238328e-03
##	Exterior2nd_Plywood	-6.822890e-03
##	Exterior2nd_Stone	-1.609856e-03
##	Exterior2nd_Stucco	-1.137528e-03
##	Exterior2nd_Wd.Sdng	-5.344159e-04
##	Exterior2nd_Wd.Shng	-3.570795e-03
##	MasVnrType_BrkCmn	-6.458243e-03
##	MasVnrType_NA	-1.812043e-03
##	MasVnrType_Stone	6.463089e-03
##	ExterQual_Ex	2.235792e-03
##	ExterQual_Fa	-1.532623e-03
##	ExterCond_Ex	2.744351e-03
##	ExterCond_Fa	-5.985140e-03
##	ExterCond_Gd	-3.107162e-03
##	ExterCond_Po	-2.937623e-03
##	Foundation_BrkTil	-3.913867e-03
##	Foundation_Slab	-1.827664e-03
##	Foundation_Stone	4.366354e-03
##	Foundation_Wood	-4.061401e-03
##	BsmtQual_Ex	1.168843e-02
##	BsmtQual_Fa	1.667580e-04

BsmtQual_NA	-8.707477e-04
BsmtCond_Fa	-5.883071e-03
BsmtCond_Gd	1.737232e-03
BsmtCond_NA	-5.556071e-04
BsmtCond_Po	2.419696e-03
BsmtExposure_Av	5.234627e-03
BsmtExposure_Gd	1.558444e-02
BsmtExposure_Mn	4.357142e-03
BsmtExposure_NA	-7.403299e-04
BsmtFinType1_ALQ	-3.363694e-03
BsmtFinType1_BLQ	-6.627262e-03
BsmtFinType1_LwQ	-5.481796e-03
BsmtFinType1_NA	-3.027530e-04
BsmtFinType1_Unf	-4.652304e-03
BsmtFinType2_ALQ	1.262671e-03
BsmtFinType2_BLQ	-6.504581e-03
BsmtFinType2_GLQ	4.993026e-03
BsmtFinType2_NA	-1.054292e-03
BsmtFinType2_Rec	-2.637787e-03
Heating_GasW	6.000639e-03
Heating_Grav	-9.456538e-03
Heating_Wall	2.946812e-03
HeatingQC_Fa	-2.119679e-03
HeatingQC_Gd	-3.263399e-03
HeatingQC_Po	-2.113756e-03
CentralAir_N	-1.613808e-02
Electrical_FuseA	1.827542e-04
Electrical_FuseF	1.142244e-03
Electrical_FuseP	-1.829331e-03
KitchenQual_Ex	1.705759e-02
KitchenQual_Fa	1.002915e-04
Functional_Maj1	-6.519887e-03
Functional_Maj2	-1.458709e-02
	BsmtCond_Fa BsmtCond_Gd BsmtCond_NA BsmtCond_Po BsmtExposure_Av BsmtExposure_Gd BsmtExposure_Mn BsmtExposure_NA BsmtFinType1_ALQ BsmtFinType1_BLQ BsmtFinType1_LwQ BsmtFinType1_Unf BsmtFinType2_ALQ BsmtFinType2_BLQ BsmtFinType2_BLQ BsmtFinType2_Rec Heating_GasW Heating_Grav Heating_Wall HeatingQC_Fa HeatingQC_Po CentralAir_N Electrical_FuseA Electrical_FuseF Electrical_FuseP KitchenQual_Ex KitchenQual_Ex KitchenQual_Fa Functional_Maj1

##	Functional_Min1	-4.510770e-03
##	Functional_Min2	-6.020738e-03
##	Functional_Mod	-7.597360e-03
##	Functional_Sev	-6.813091e-03
##	<pre>GarageType_2Types</pre>	-5.564597e-03
##	<pre>GarageType_Basment</pre>	-1.708063e-03
##	<pre>GarageType_BuiltIn</pre>	1.362803e-03
##	<pre>GarageType_CarPort</pre>	-8.057846e-04
##	<pre>GarageType_Detchd</pre>	-8.014494e-03
##	<pre>GarageType_NA</pre>	-3.602695e-03
##	GarageFinish_Fin	4.571995e-03
##	GarageFinish_NA	-3.459337e-03
##	GarageQual_Fa	-4.233673e-03
##	GarageQual_Gd	3.634157e-03
##	GarageQual_NA	-3.349563e-03
##	GarageQual_Po	-9.464443e-04
##	GarageCond_Ex	5.371144e-04
##	GarageCond_Fa	-4.888778e-03
##	GarageCond_Gd	-6.181713e-04
##	GarageCond_NA	-3.375997e-03
##	GarageCond_Po	4.154394e-03
##	PavedDrive_N	-6.128714e-03
##	PavedDrive_P	-2.954823e-03
##	SaleType_COD	-5.850902e-04
##	SaleType_CWD	3.857856e-03
##	SaleType_Con	3.469501e-03
##	SaleType_ConLD	7.285072e-03
##	SaleType_ConLI	-1.536375e-03
##	SaleType_ConLw	2.940252e-03
##	SaleType_New	9.316847e-03
##	SaleType_Oth	3.430097e-03
##	SaleCondition_Abnorml	-1.638142e-02
##	SaleCondition_AdjLand	9.840009e-04

## SaleCondition\_Alloca -1.718252e-03
## SaleCondition\_Family -6.308048e-03
## SaleCondition\_Partial 5.022071e-03
## BuiltAfter1920 2.075557e-03
## YearRemodUnknown -6.790909e-03
## NoFinBsmt -4.420746e-03
## HasDeck 3.695499e-03
## HasPorch 8.224311e-03

We predict values based on our Ridge regressions.

Despite the large number of independent variables, ridge regression performs better, with a score of .14047. This puts us at 1690 out of 4216 individuals.

C. Lasso Regression To perform Lasso regression, first we define the predictor and response variables for the training dataset. Similarly to the Ridge model, we'll use the glmnet library, which makes it easy to use k-fold cross-validation to find the optimal value for lambda. Next, we find the coefficients for the Lasso model using our optimized lambda. Lastly, we predict new values using our optimized Lasso model. Here is our lambda:

#### ## [1] 0.003398183

We try Lasso with both scaled and unscaled data. Because lasso incorporates a penalty based on the size of the coefficients, we expect the scaled data to perform better, and it does. Our lasso regression gives us a .1375, which outperforms ridge.

**D. Elastic Net Regression** In order to form elastic net, first, build a control model. Next, train the elastic net regression model. Then we optimize the elastic net model based on tuning parameters selected from model training.

Our elastic net result falls between ridge and lasso.

E. Tree based models: Random Forest and Gradient Boosting Our final models are Random Forest and Gradient Boosting.

Below are the top variables for our Gradient Boosting model:

var	rel.inf
OverallQual	56.1959140
GrLivArea	19.1380158
${\bf TotalBsmtSF}$	5.0768487
GarageCars	4.1497417
YearBuilt	3.6828566
GarageArea	2.3485607
$CentralAir\_N$	2.0469328
X1stFlrSF	1.5821608
${\bf BsmtFinSF1}$	1.2926779
Fireplaces	1.0187212
$BsmtQual\_Ex$	0.7572699
${\bf Year RemodAdd}$	0.7157811
${\rm MSZoning}\_{\rm RM}$	0.5741999
OverallCond	0.5443683
X2ndFlrSF	0.3494080
LotArea	0.1262086
HalfBath	0.1035937
NoFinBsmt	0.0919161
FullBath	0.0862303
${\tt GarageType\_Detchd}$	0.0686628
	OverallQual GrLivArea TotalBsmtSF GarageCars YearBuilt GarageArea CentralAir_N X1stFlrSF BsmtFinSF1 Fireplaces BsmtQual_Ex YearRemodAdd MSZoning_RM OverallCond X2ndFlrSF LotArea HalfBath NoFinBsmt FullBath

Below is the output from our random forest model:

Our Random Forest model does not improve our score, but Gradient Boosting does. We land on .12786, which puts us in the 80th percentile.

# Discussion and Conclusions

Ordinary Least Squares is a regression technique with a long history of use as a predictive model. However, standard measures of fit (like  $R^2$ ) will always increase (or stay the same) as you add independent variables. This can result in models which incorporate noise - in other words, overfit the data so that idiosyncrasies in

the training set affect predictions in the test set. Other methods of measuring fit, such as adjusted R<sup>2</sup> and AIC, help mitigate the overfitting effect by penalizing the addition of factors.

More recently, other techniques which employ regularization have been introduced to deal with overfit. For example, in ridge regression, we reduce the sum of our coefficients, not the number of variables. We do this by introducing a penalty in the loss function represented by the squared sum of the coefficients themselves, multiplied by a factor (designated as lambda) which allows us to control the degree to which the size of the coefficients matters. If lambda is zero, there is no difference between ridge regression and OLS.

Ridge regression will keep all the variables but may significantly reduce the coefficients for some. Lasso regression is similar in that it employs a constraint where the sum of the absolute value of the coefficients is less than a fixed value. Lasso regression may drop coefficients altogether to stay under the constraint.

Elastic Net regression is a hybrid approach that blends both of the penalizations of lasso and ridge methods. An alpha parameter weights which penalty to emphasize - lasso or ridge.

Random Forest (RF) and Gradient Boosting (GB) both rely on decision trees. Decision trees incorporate sequential choice-point steps, providing different outcomes for each choice-point. Decision trees have the advantage that they do not make assumptions that the dependent variable is linearly related to the independent variables. In addition, RF and GB both combine multiple trees so the results are averages of many samples, which improves their predictability. However, the results may be difficut to interpret.

RF and BG handle the combination of trees differently. RF builds each tree independently and averages at the end. BG proceeds in a stage-wise manner, improving the performance of weak learners as you go. This can result in better performance.

Our dataset has features that lend to overfitting. Most significant of these is the high number of potential independent variables (over 200 once the dummy variables are created.) Multicollinearity is also a problem, though less than we might have expected.

We used stepAIC to fit our OLS model. StepAIC uses backward substitution to find the best model with the lowest AIC. With an adjusted R<sup>2</sup> of over 90% overfitting was expected. However, even with an overfit model our predictions performed at the 60th percentile on the Kaggle.

Because of the large number of potential predictors, ridge (and by extension elastic net) were not as good candidates as Lasso - however, potential issues with collinearity actually favored ridge. We found that Lasso improved our score the most of the regression-based models, followed be elastic net (which is a compromise between lasso and ridge), followed by ridge. All were improvements over OLS - however, the improvements were not dramatic.

Gradient boosting had the most success. Because gradient boosting is a machine-learning technique in which the model receives direct feedback with each iteration, it can often do a better job of predicting than the other models. However, if we were looking for insight into the data, GB is something of a "black box" which makes interpretation difficult.

Our gradient boosting model relied on a few key variables - overall quality, size, number of cars and year built. The fact that number of cars and size of garage both featured prominently suggests we could have improved the model by eliminating some multicollinearity (the two are highly correlated).

In conclusion, it is important to keep in mind that while regularization improved our model, the base OLS model also performed adequately, so regularization, while important, may in some cases improve models at the margin. It is also important to recognize the strengths of each of the techniques and use the appropriate one for the situation.

#### References

Alfiyatin, A. N. (2017, December 1). Modeling House Price Prediction using Regression Analysis and Particle Swarm Optimization Case Study: Malang, East Java, Indonesia. Https://Thesai.Org/. https://thesai.org/Publications/ViewPaper?Volume=8&Issue=10&Code=IJACSA&SerialNo=42

Guan, J. (2021, November 12). Predicting home sale prices: A review of existing methods and illustration of data stream methods for improved performance. University of Louisville College of Business. https://business.louisville.edu/faculty-research/research-publications/predicting-home-sale-prices-a-review-of-existing-methods-and-illustration-of-data-stream-methods-for-improved-performance/

Journal, I. (2019, May 4). Predicting housing prices using advanced regression techniques. Ijariit Journal - Academia.Edu. https://www.academia.edu/39014594/Predicting\_housing\_prices\_using\_advanced\_regression\_techniques#:%7E:text=There%20are%20various%20techniques%20for%20predicting%20house%20prices.,have%20an%20impact%20on%20a%20topic%20of%

Kennedy, J. (2014, June 11). Particle swarm optimization. Https://Www.Academia.Edu. https://www.academia.edu/1446115/Particle swarm optimization

Li, D. (2021, July 3). Prediction of China's Housing Price Based on a Novel Grey Seasonal Model. Www.Hindawi.Com. https://www.hindawi.com/journals/mpe/2021/5541233/ Liu, S. (2011, September 1). A brief introduction to Grey systems theory. Https://Www.Researchgate.Net.

https://www.researchgate.net/publication/252052256\_A\_brief\_introduction\_to\_Grey\_systems\_theory

Wu, Z., et. al., (2020, November 5). Prediction of California House Price Based on Multiple Linear Regression | Francis Academic Press. Https://Www.Academia.Edu/. https://francis-press.com/papers/2868