MA3237 : Project #3

Due on Wednsday, 4 Apr 2014

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Question 1

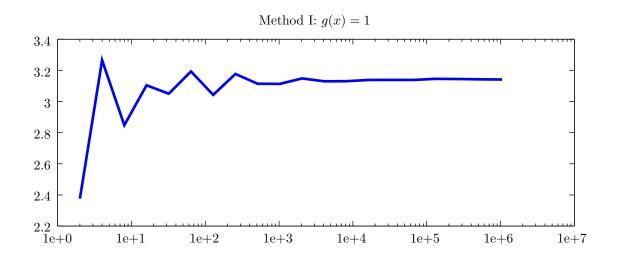
Code

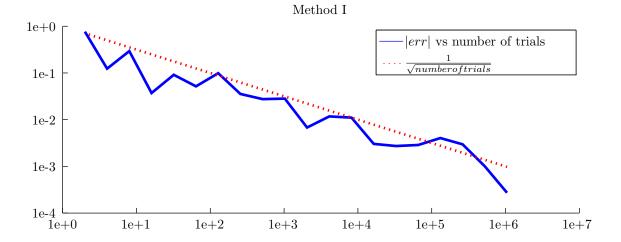
```
clear;
close all;
function I = repI(i)
         I = [];
         for j = 1:i
                  I = [I, 'I'];
         end
end
nTrials = 2.^(1:20); m = length(nTrials);
vEst = cell(3,1);
for i = 1:3
         vEst{i} = zeros(1,m);
end
rand('state',0);
\mathbf{for} \quad i = 1:m
    n=nTrials(i);
    x = rand(1,n);
    vEst\{1\}(i) = sum(4*sqrt(1-x.^2))/n;
    x = -sqrt(4 - 3*rand(1,n)) + 2;
    vEst\{2\}(i) = sum(12*sqrt(1-x.^2)./(4-2*x))/n;
    x = -\mathbf{sqrt}(1 - \mathbf{rand}(1,n)) + 1;
    vEst \{3\}(i) = sum(4*sqrt(1-x.^2)./(2-2*x))/n;
end
\operatorname{err} = \operatorname{cell}(3,1);
for i = 1:3
         err\{i\} = vEst\{i\} - pi;
end
equation = cell(3,1);
equation \{1\} = '1\$';
equation \{2\} = ' \frac{4-2x}{3} ;
equation \{3\} = '2-2x\$';
for i = 1:3
         the_plot = figure(i);
         subplot (2,1,1);
         semilogx(nTrials, vEst{i});
         title (['Method_', repI(i), ':\bot$g(x)\bot=', equation{i}]);
         subplot (2,1,2);
         loglog(nTrials,abs(err{i}));
```

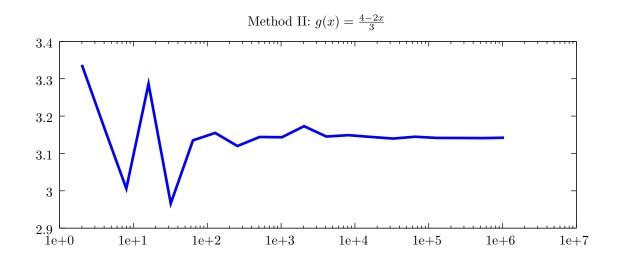
```
\label{loglog} $$ \textbf{hold} \ on; $$ \textbf{loglog}(nTrials,1./\mathbf{sqrt}(nTrials),'r:'); \ \textbf{title}(['Method_', repI(i)]) $$ \textbf{legend}('\$\abs\{err\}\_vs_number\_of\_trials','\$\frac\{1\}\{\art\{number\_of\_trials\}\}\}'); $$ \textbf{print}(the\_plot,['Method_',repI(i),'.tex'],'-S500,450','-dtex') $$ $$
```

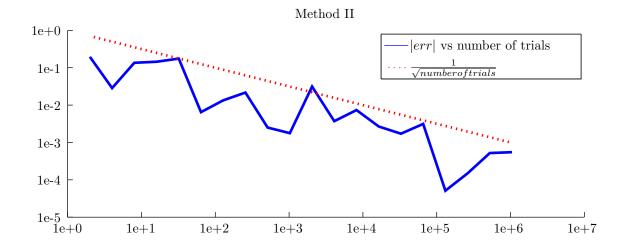
Figures

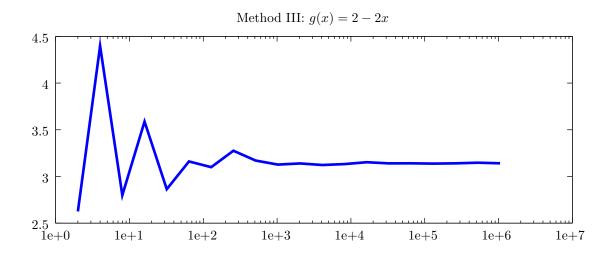
end

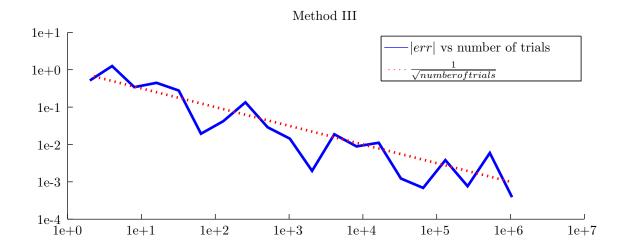












Chen Yu Question 1

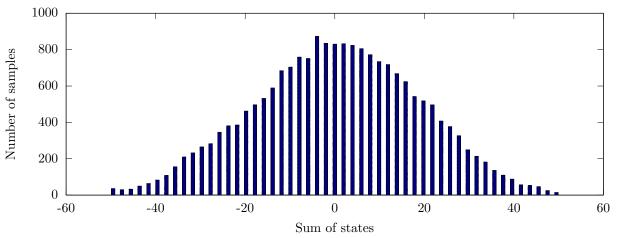
Question 2

Code

```
clear; close all;
graphics_toolkit("gnuplot");
N_{-}bins = 101;
function M = Metro_Ising (mu, N_steps, sample_rate, N)
        x = ones(N, 1);
        M = zeros(0, N_steps/sample_rate);
        for i = 1: N_steps
                 j = ceil(N*rand);
                 if j == 1
                         h = \exp(-2*mu*x(1)*(x(2)));
                 elseif j = N
                         h = \exp(-2*mu*x(N)*(x(N-1)));
                 else
                         h = \exp(-2*mu*x(j)*(x(j-1)+x(j+1)));
                 end
                 U = rand;
                 if U \le h
                         x(j) = -x(j);
                 end
                 if mod(i, 50) == 0
                         M(i/50) = sum(x);
                 end
        end
end
N_{\text{steps}} = 1e6;
sample_rate = 50;
N = 50;
%mesh = -N: floor(2*N/(N_bins - 1)):N;
\%[n, h] = hist(M, mesh);
the_plot = figure();
Mh = Metro_Ising(1, N_steps, sample_rate, N);
M_l = Metro_Ising(2, N_steps, sample_rate, N);
h_{-}plot = subplot(2,1,1);
hist (M_h, 101);
title (['Histogram_of_sum_of_states_of_high_temperature_($\mu_=_1$),
'1D Ising model with $20,000$ from $1,000,000$ states']);
xlabel('Sum_of_states');
ylabel('Number_of_samples');
1_{-}plot = subplot(2,1,2);
hist (M<sub>-</sub>l, 101);
```

Figures

Histogram of sum of states of high temperature ($\mu = 1$) 1D Ising model with 20,000 from 1,000,000 states



Histogram of sum of states of low temperature ($\mu = 2$) 1D Ising model with 20,000 from 1,000,000 states

