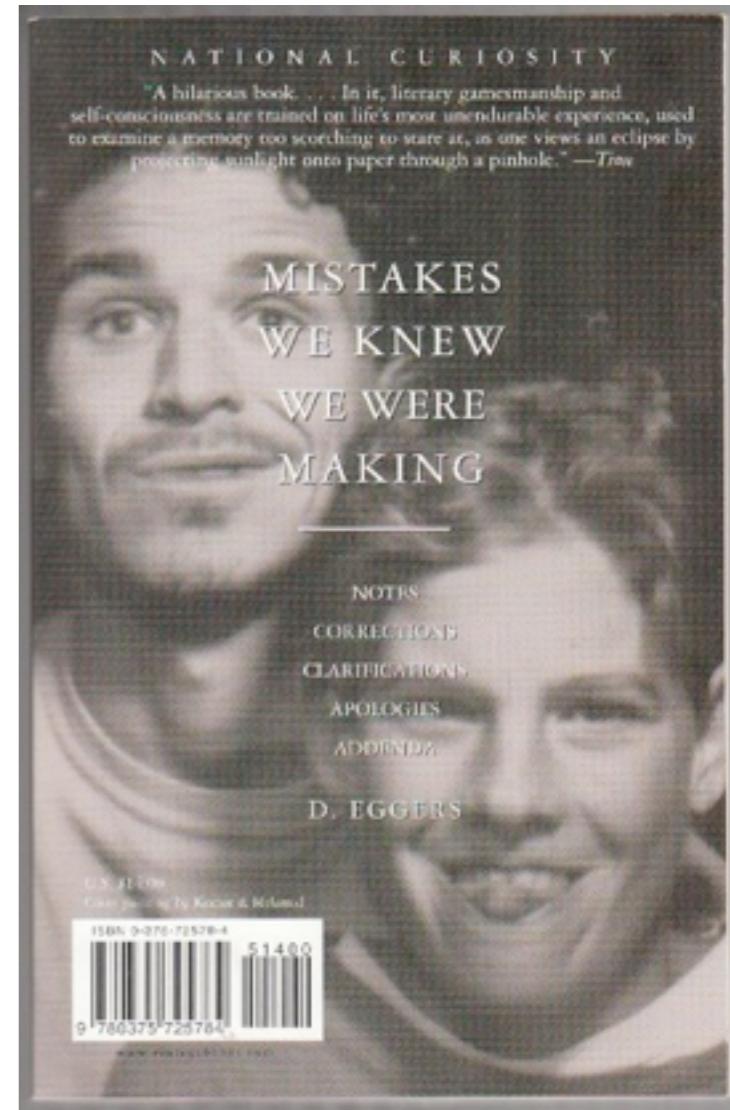


G  
O R ↑ H O  
N A ↓



# Orthogonality

- Rascal, a heartbreakin work of staggering genius ;-)
- Some mistakes we have made...
- or we are about to make...
- or not...
- have to do with orthogonality...



STICHTING  
**MATHEMATISCH CENTRUM**  
2e BOERHAAVESTRAAT 49  
**AMSTERDAM**  
—  
**REKENAFDELING**

MR 76

Orthogonal design  
and description of  
a formal language

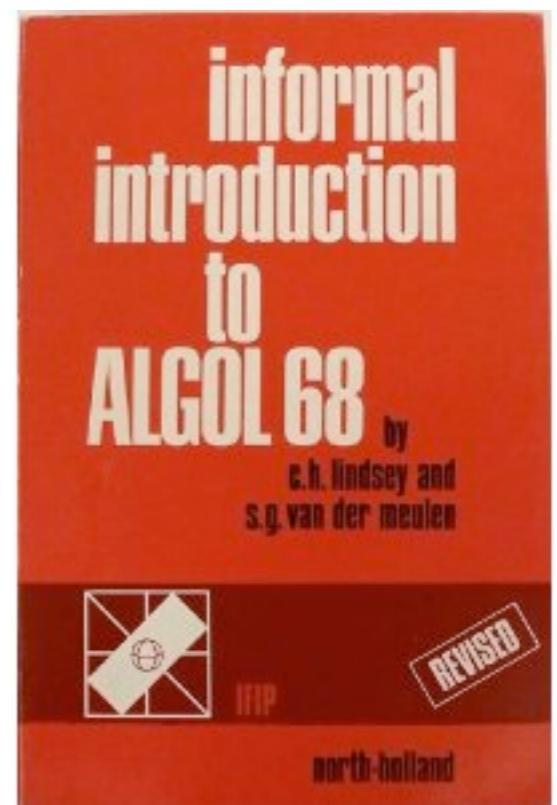
by  
A. van Wijngaarden



As to the design of a language I should like to see the definition of a language as a Cartesien product of its concepts.

# Algol 68

- procedures as params
- values as params
- values can be assigned
- so procedures can be assigned.



# Cartesian product

	assign	pass
expr	yes	yes
proc	?	yes

**STANFORD ARTIFICIAL INTELLIGENCE LABORATORY**  
**MEMO AIM - 224**

**STAN-CS-73-403**

---

**HINTS ON PROGRAMMING LANGUAGE DESIGN**

**BY**

**C. A. R. HOARE**

Another replacement of simplicity as an objective has been orthogonality of design. An example of orthogonality is the provision of complex integers, on the argument that we need reals and integers and complex reals, so why not complex integers? In the early days of hardware design, some very ingenious but arbitrary features turned up in order codes as a result of orthogonal combinations of the function bits of an instruction, on the grounds that some clever programmer would find a use for them, -- and some clever programmer always did. Hardware designers have now learned more sense; but language designers are clever programmers and have not.

# ON THE DESIGN OF PROGRAMMING LANGUAGES\*

N. WIRTH

\*Reprinted from *Proc. IFIP Congress 74*, 386-393, North-Holland, Amsterdam, North-Holland Publishing Company.

The author is with the Institut für Informatik, Eidg. Technische Hochschule, Zurich, Switzerland.

The new trend was to discover the fundamental concepts of algorithms, to extract them from their various incarnations in different language features, and to present them in a pure, distilled form, free from arbitrary and restrictive rules of applicability.

# Backfiring orthogonality

```
( real x,y;           { Declare two local variables.      }
  read((x,y));        { Read two values in them from input.   }
  if x < y then a else b { Choose one of them as the          }
  fi                  { left hand side of the assignment.    }
  ) :=                { The right hand side consists of b and  }
  b +                 { a conditionally selected second       }
  if a:= a+1; a > b   { operand. If a > b, increment a,        }
  then                { and the second operand is           }
  c:=c+1; +b          { +b, increment c in the meanwhile     }
  else                { If a is not > b, then the second      }
  c:=c-1; a           { operand is a, decrement c.            }
  fi                  { End of selection of the second operand }
```

Algol 68

HUMAN-COMPUTER INTERACTION, 1989, Volume 4, pp. 95-120  
Copyright © 1989, Lawrence Erlbaum Associates, Inc.

---

# **Testing the Principle of Orthogonality in Language Design**

**Edward M. Bowden, Sarah A. Douglas, and  
Cathryn A. Stanford**

*University of Oregon*

---

```

module Booleans
  exports
    sorts BOOL
    lexical syntax
      [\t\n]
    context-free syntax
      true
      false
      BOOL "&" BOOL
  equations
    [B1] true & true = true
    [B2] true & false = false
    [B3] false & true = false
    [B4] false & true = false

module Naturals
  imports Booleans
  exports
    sorts NAT
    context-free syntax
      "0"
      succ "(" NAT ")"
      NAT "<" NAT
    variables
      N → NAT
      M → NAT
  equations
    [N1] 0 < 0 = false
    [N2] succ (N) < 0 = false
    [N3] 0 < succ(N) = true
    [N4] succ(N) < succ(M) = N < M

```

# A bit of history...

- ASF+SDF
- “Just” two concepts
- Beautiful
- Orthogonal!
- Unusable



# Rascal

- Functional meta-programming language
- DSL implementation and program understanding/renovation
- Source code in, source code out
- Source code in the broadest sense



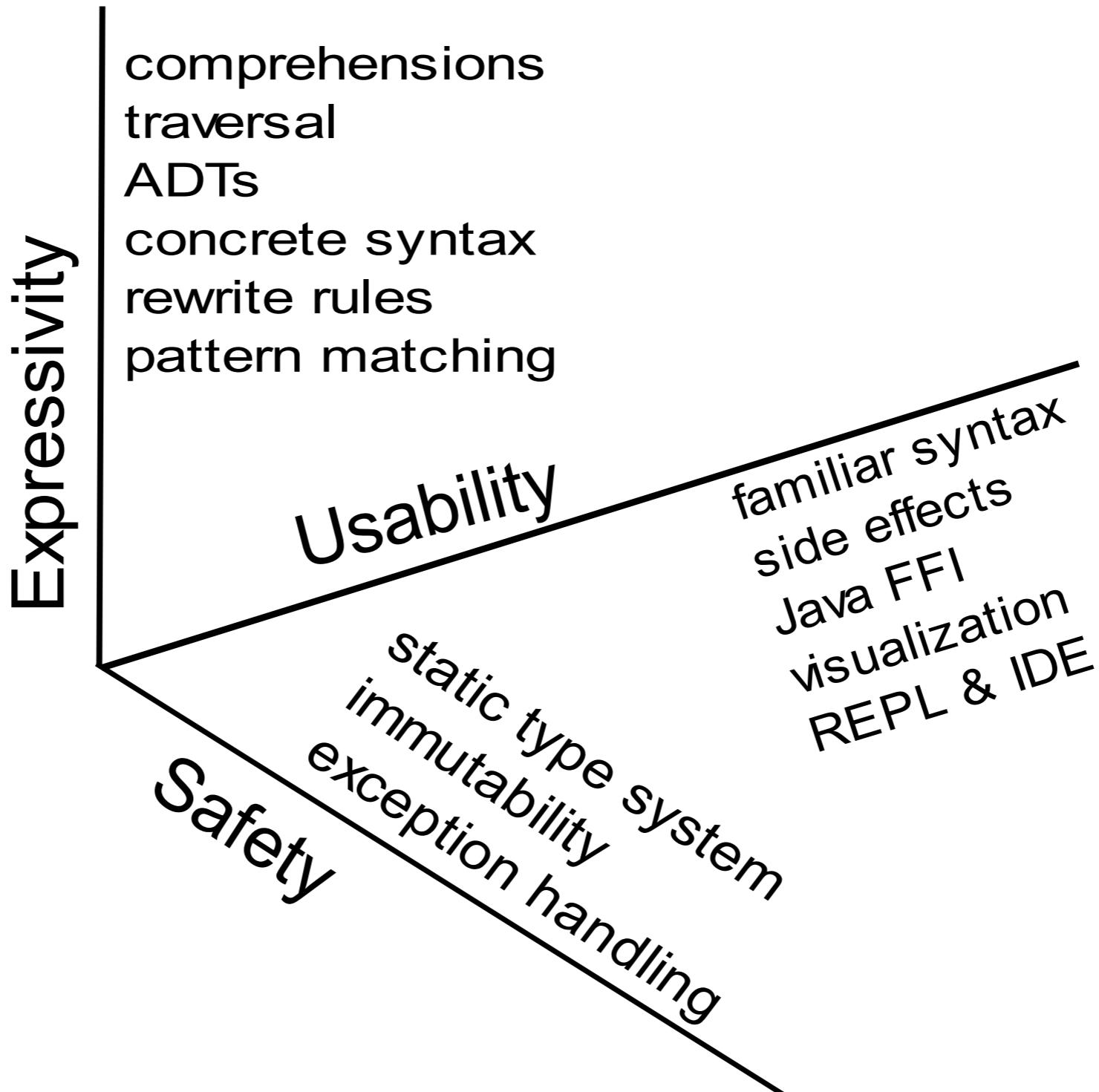
<http://www.rascal-mpl.org>

# Rascal's Unique (?) features

- Integrated context-free grammars
- Very powerful pattern matching
- Transitive closure, solve statement
- Resources (Type providers reloaded)
- Source location data type
- Built-in (randomized) testing features



<http://www.rascal-mpl.org>



# Language design

- Design = hypothesis
- Observe use in practice
- Revise design if needed
- Learn by doing!
- Today: questions more than answers

# A taste of Rascal

# Relational calculus

```
r = {  
    <"active", "waitingForDrawer">,  
    <"idle", "active">,  
    <"unlockedPanel", "idle">,  
    <"waitingForLight", "unlockedPanel">,  
    <"active", "waitingForLight">,  
    <"waitingForDrawer", "unlockedPanel">  
};
```

$r<\emptyset>;$

$r<1, \emptyset>;$

$r["active"];$

$r+;$

$r^*;$

$r \circ r$

# Relational calculus

set of tuples

```
r = {  
    <"active", "waitingForDrawer">,  
    <"idle", "active">,  
    <"unlockedPanel", "idle">,  
    <"waitingForLight", "unlockedPanel">,  
    <"active", "waitingForLight">,  
    <"waitingForDrawer", "unlockedPanel">  
};
```

$r<\emptyset>;$

$r<1, \emptyset>;$

$r["active"];$

$r+;$

$r^*;$

$r \circ r$

# Relational calculus

set of tuples

projection

$r<\emptyset>;$

$r<1, \emptyset>;$

$r["active"];$

$r+;$

$r^*;$

$r \circ r$

```
r = {  
    <"active", "waitingForDrawer">,  
    <"idle", "active">,  
    <"unlockedPanel", "idle">,  
    <"waitingForLight", "unlockedPanel">,  
    <"active", "waitingForLight">,  
    <"waitingForDrawer", "unlockedPanel">  
};
```

# Relational calculus

set of tuples

projection

$r<\emptyset>;$

invert

$r<1, \emptyset>;$

$r["active"];$

$r+;$

$r^*;$

$r \circ r$

```
r = {  
    <"active", "waitingForDrawer">,  
    <"idle", "active">,  
    <"unlockedPanel", "idle">,  
    <"waitingForLight", "unlockedPanel">,  
    <"active", "waitingForLight">,  
    <"waitingForDrawer", "unlockedPanel">  
};
```

# Relational calculus

set of tuples

projection

$r<\emptyset>;$

invert

$r<1, \emptyset>;$

$r["active"];$

right  
image

$r+;$

$r^*;$

$r \circ r$

```
r = {  
    <"active", "waitingForDrawer">,  
    <"idle", "active">,  
    <"unlockedPanel", "idle">,  
    <"waitingForLight", "unlockedPanel">,  
    <"active", "waitingForLight">,  
    <"waitingForDrawer", "unlockedPanel">  
};
```

# Relational calculus

set of tuples

projection

$r<\emptyset>;$

invert

$r<1, \emptyset>;$

transitive closure

$r+;$

$r^*;$

$r \circ r$

```
r = {  
    <"active", "waitingForDrawer">,  
    <"idle", "active">,  
    <"unlockedPanel", "idle">,  
    <"waitingForLight", "unlockedPanel">,  
    <"active", "waitingForLight">,  
    <"waitingForDrawer", "unlockedPanel">  
};
```

right  
image

# Relational calculus

set of tuples

projection

$r<\emptyset>;$

invert

$r<1, \emptyset>;$

transitive closure

$r+;$

transitive  
reflexive closure

$r^*;$

$r \circ r$

```
r = {  
    <"active", "waitingForDrawer">,  
    <"idle", "active">,  
    <"unlockedPanel", "idle">,  
    <"waitingForLight", "unlockedPanel">,  
    <"active", "waitingForLight">,  
    <"waitingForDrawer", "unlockedPanel">  
};
```

right  
image

# Relational calculus

set of tuples

projection

$r<\emptyset>;$

invert

$r<1, \emptyset>;$

transitive closure

$r+;$

transitive  
reflexive closure

$r^*;$

$r \circ r$

```
r = {  
    <"active", "waitingForDrawer">,  
    <"idle", "active">,  
    <"unlockedPanel", "idle">,  
    <"waitingForLight", "unlockedPanel">,  
    <"active", "waitingForLight">,  
    <"waitingForDrawer", "unlockedPanel">  
};
```

right  
image

relation  
composition

# Relations...

Container	Equivalent type	Operations
<code>set[tuple[...]]</code>	<code>rel</code>	<code>_o_, _+, _*, _[]</code>
<code>list[tuple[...]]</code>	<code>orel</code> 	<code>same?</code> 
<code>bag[tuple[...]]</code> 	<code>mrel</code> 	<code>same?</code> 
<code>map</code>	<code>map</code>	<code>same?</code> 

# Matching

```
int x := 3;
```

```
event(x, y) := event("a", "b");
```

```
event("c", "d") !:= event("a", "b");
```

```
[*x, 1, *y] := [5, 6, 1, 1, 1, 3, 4];
```

```
{1, *x} := {4, 5, 6, 1, 2, 3};
```

```
/transition(e, "idle") := ast;
```

```
/state(x, _, /transition(_, x)) := ast;
```

```
3 <- {1,2,3}
```

```
int x <- {1,2,3}
```

# Matching

type-based matching

```
int x := 3;
```

```
event(x, y) := event("a", "b");
```

```
event("c", "d") !:= event("a", "b");
```

```
[*x, 1, *y] := [5, 6, 1, 1, 1, 3, 4];
```

```
{1, *x} := {4, 5, 6, 1, 2, 3};
```

```
/transition(e, "idle") := ast;
```

```
/state(x, _, /transition(_, x)) := ast;
```

```
3 <- {1,2,3}
```

```
int x <- {1,2,3}
```

# Matching

type-based matching

```
int x := 3;
```

structural matching

```
event(x, y) := event("a", "b");
```

```
event("c", "d") !:= event("a", "b");
```

```
[*x, 1, *y] := [5, 6, 1, 1, 1, 3, 4];
```

```
{1, *x} := {4, 5, 6, 1, 2, 3};
```

```
/transition(e, "idle") := ast;  
/state(x, _, /transition(_, x)) := ast;
```

```
3 <- {1,2,3}
```

```
int x <- {1,2,3}
```

# Matching

type-based matching

```
int x := 3;
```

structural matching

```
event(x, y) := event("a", "b");
```

anti-matching

```
event("c", "d") !:= event("a", "b");
```

```
[*x, 1, *y] := [5, 6, 1, 1, 1, 3, 4];
```

```
{1, *x} := {4, 5, 6, 1, 2, 3};
```

```
/transition(e, "idle") := ast;  
/state(x, _, /transition(_, x)) := ast;
```

```
3 <- {1,2,3}
```

```
int x <- {1,2,3}
```

# Matching

type-based matching

```
int x := 3;
```

structural matching

```
event(x, y) := event("a", "b");
```

anti-matching

```
event("c", "d") !:= event("a", "b");
```

list matching

```
[*x, 1, *y] := [5, 6, 1, 1, 1, 3, 4];
```

```
{1, *x} := {4, 5, 6, 1, 2, 3};
```

```
/transition(e, "idle") := ast;  
/state(x, _, /transition(_, x)) := ast;
```

```
3 <- {1,2,3}
```

```
int x <- {1,2,3}
```

# Matching

type-based matching

```
int x := 3;
```

structural matching

```
event(x, y) := event("a", "b");
```

anti-matching

```
event("c", "d") !:= event("a", "b");
```

list matching

```
[*x, 1, *y] := [5, 6, 1, 1, 1, 3, 4];
```

set matching

```
{1, *x} := {4, 5, 6, 1, 2, 3};
```

```
/transition(e, "idle") := ast;  
/state(x, _, /transition(_, x)) := ast;
```

```
3 <- {1,2,3}
```

```
int x <- {1,2,3}
```

# Matching

type-based matching

```
int x := 3;
```

structural matching

```
event(x, y) := event("a", "b");
```

anti-matching

```
event("c", "d") !:= event("a", "b");
```

list matching

```
[*x, 1, *y] := [5, 6, 1, 1, 1, 3, 4];
```

set matching

```
{1, *x} := {4, 5, 6, 1, 2, 3};
```

deep matching

```
/transition(e, "idle") := ast;  
/state(x, _, /transition(_, x)) := ast;
```

```
3 <- {1,2,3}
```

```
int x <- {1,2,3}
```

# Matching

type-based matching

```
int x := 3;
```

structural matching

```
event(x, y) := event("a", "b");
```

anti-matching

```
event("c", "d") !:= event("a", "b");
```

list matching

```
[*x, 1, *y] := [5, 6, 1, 1, 1, 3, 4];
```

set matching

```
{1, *x} := {4, 5, 6, 1, 2, 3};
```

deep matching

```
/transition(e, "idle") := ast;  
/state(x, _, /transition(_, x)) := ast;
```

element matching

```
3 <- {1,2,3}  
int x <- {1,2,3}
```

# list-matching

```
rascal>for ([*x, *y] := [1,1,1,1,1,1]) println("<x> <y>");  
[] [1,1,1,1,1,1]  
[1] [1,1,1,1,1]  
[1,1] [1,1,1,1]  
[1,1,1] [1,1,1]  
[1,1,1,1] [1,1]  
[1,1,1,1,1] [1]  
[1,1,1,1,1,1] []
```

# list-matching

```
rascal>for ([*x, *y] := [1,1,1,1,1,1]) println("<x> <y>");  
[] [1,1,1,1,1,1]  
[1] [1,1,1,1,1]  
[1,1] [1,1,1,1]  
[1,1,1] [1,1,1]  
[1,1,1,1] [1,1]  
[1,1,1,1,1] [1]  
[1,1,1,1,1,1] []
```

```
rascal>for ([*x, *y] := [1,1,1,1,1,1], x == y) println("<x> <y>");  
[1,1,1] [1,1,1]
```

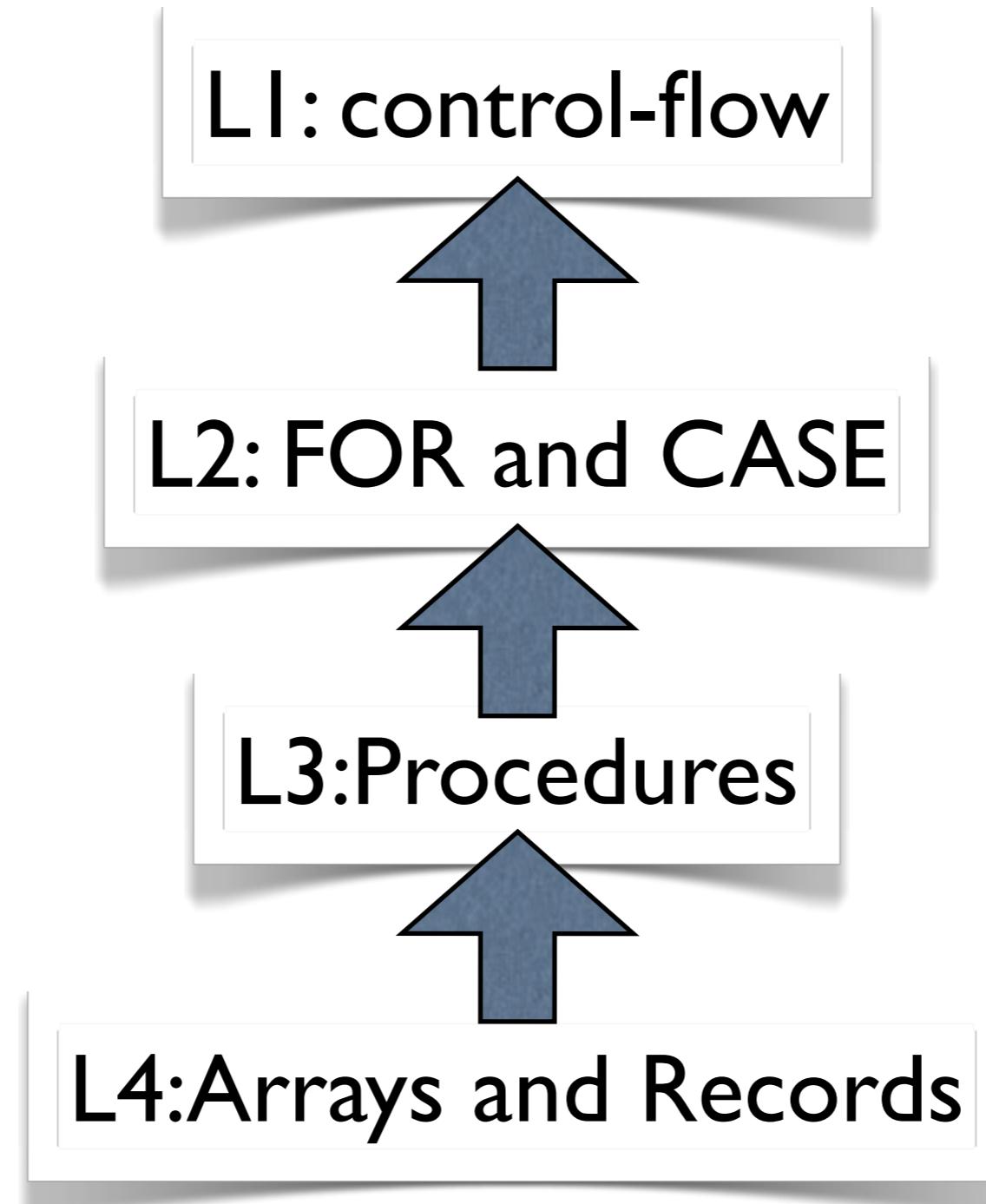
# set-matching

```
rascal>for ({*x, *y} := {1,2,3,4}) println("<x> <y>");  
{4,3,2,1} {}  
{4,3,2} {1}  
{4,3,1} {2}  
{4,3} {2,1}  
{4,2,1} {3}  
{4,2} {3,1}  
{4,1} {3,2}  
{4} {3,2,1}  
{3,2,1} {4}  
{3,2} {4,1}  
{3,1} {4,2}  
{3} {4,2,1}  
{2,1} {4,3}  
{2} {4,3,1}  
{1} {4,3,2}  
{} {4,3,2,1}
```

# Collection types

Collection	Matching
Lists	Associative
Bags	Associative, commutative 
Sets	Associative, commutative, idempotent

# Language extensibility: LDTA'11 ToolChallenge



# A simple interpreter

```
data Exp
= add(Exp lhs, Exp rhs)
| lit(int n)
;

public int eval0(Exp e) {
    switch (e) {
        case add(l, r): return eval(l) + eval(r);
        case lit(n): return n;
    }
}
```

# Extension

```
module Neg

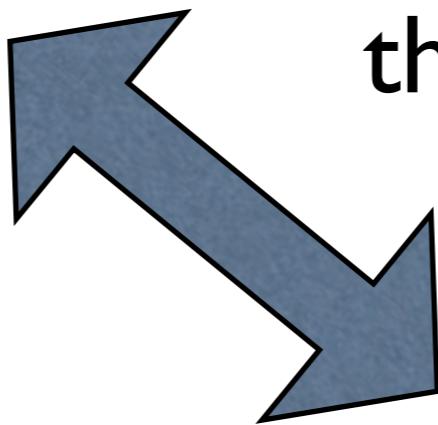
extend Add;

data Exp = neg(Exp arg);
```

# Extension

```
module Neg  
  
extend Add;  
  
data Exp = neg(Exp arg);
```

How to extend  
the interpreter?



```
public int eval0(Exp e) {  
    switch (e) {  
        case add(l, r): return eval(l) + eval(r);  
        case lit(n): return n;  
    }  
}
```

# Pattern-based dispatch

- Open up “switch”
- Allow arbitrary *patterns* in function signatures
- Liberalize overloading of functions...

# Open interpreter

```
module Add
```

```
data Exp = add(Exp lhs, Exp rhs) | lit(int n);
```

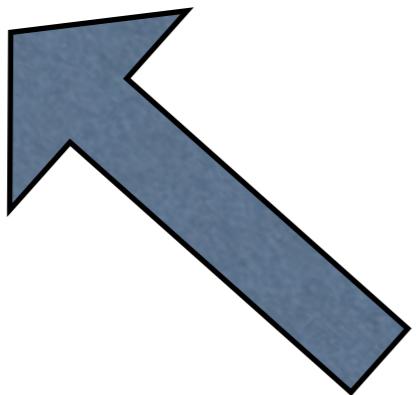
```
public int eval1(add(l, r)) = eval1(l) + eval1(r);  
public int eval1(lit(n)) = n;
```

# Open interpreter

```
module Add
```

```
data Exp = add(Exp lhs, Exp rhs) | lit(int n);
```

```
public int eval1(add(l, r)) = eval1(l) + eval1(r);  
public int eval1(lit(n)) = n;
```



```
module Neg  
extend Add;
```

```
data Exp = neg(Exp arg);
```

```
public int eval1(neg(a)) = - eval1(a);
```

# Traversal using *visit*

```
public Exp propagate0(Exp e) {  
    return innermost visit (e) {  
        case add(lit(a), lit(b)) => lit(a + b)  
    }  
}
```

# Traversal using *visit*

traversal  
strategy

```
public Exp propagate0(Exp e) {  
    return innermost visit (e) {  
        case add(lit(a), lit(b)) => lit(a + b)  
    }  
}
```

# Traversal using visit

traversal  
strategy

```
public Exp propagate0(Exp e) {  
    return innermost visit (e) {  
        case add(lit(a), lit(b)) => lit(a + b)  
    }  
}
```

structure shy

# Traversal using visit

```
public Exp propagate0(Exp e) {  
    return innermost visit (e) {  
        case add(lit(a), lit(b)) => lit(a + b)  
    }  
}
```

traversal strategy

structure shy

type preserving

Feature	“Open”
<i>switch</i>	pattern-based dispatch
<i>visit</i>	?



# Visit using functions

```
module Add
public Exp propStep(add(lit(a), lit(b))) = lit(a + b);

public Exp propagate1(Exp e) = innermost visit (e, propStep);
```

!!!

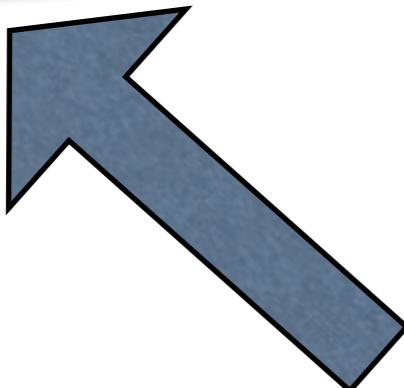


# Visit using functions

```
module Add
public Exp propStep(add(lit(a), lit(b))) = lit(a + b);

public Exp propagate1(Exp e) = innermost visit (e, propStep);
```

!!!



```
module Neg
extend Add;

public Exp propStep(neg(lit(n))) = lit(-n);
```



# Comprehensions

```
[ i | i <- [1..100], i % 2 == 0 ];
```

```
( i: i*i | i <- [1..10] );
```

```
{ <i, i*i> | i <- [1..10] };
```

# Comprehensions

list

```
[ i | i <- [1..100], i % 2 == 0 ];
```

```
( i: i*i | i <- [1..10] );
```

```
{ <i, i*i> | i <- [1..10] };
```

# Comprehensions

list

```
[ i | i <- [1..100], i % 2 == 0 ];
```

map

```
( i: i*i | i <- [1..10] );
```

```
{ <i, i*i> | i <- [1..10] };
```

# Comprehensions

list

```
[ i | i <- [1..100], i % 2 == 0 ];
```

map

```
( i: i*i | i <- [1..10] );
```

set &  
relation

```
{ <i, i*i> | i <- [1..10] };
```

# Higher-order reduce

```
public &T reduce(list[&T] l, &T init, &T(&T, &T) op) {  
    &T n = init;  
    for (e <- l)  
        n = op(e, n);  
    return n;  
}
```

Put in a library

```
public int sum1(list[int] l) =  
    reduce(l, 0, int(int e,int a) { return e + a; });
```

Clunky, needs if's  
for conditions

Ugly because of  
types and curly  
syntax

# Reducers

```
public int sum(list[int] l) =  
  ( 0 | it + x | x <- l );
```

accumulator

```
public int sumEven(list[int] l) =  
  ( 0 | it + x | x <- l, x % 2 == 0 );
```

like comprehensions

# Folds...

Type...	Collection	Tree
Preserving	comprehension	visit
Transforming	comprehension	? 
Unifying	reducer	? 

# Summarizing



- Set of tuple is a *rel*: why not *mrel* and *orel*?
- Sets and list: why not bags?
- Open switch: why not open visit?
- Folds over collections: why not over trees?

Orthogonal



pure  
hard to implement  
terse  
minimalism  
modernism  
**one-way-to-do-it**  
dead corners  
compositional  
general  
complex  
clean



Non-

ad hoc  
keyworditis  
baroque  
post-modernism  
eclectic  
**many-ways-to-do-it**  
to the point  
non-compositional  
**domain-specific**  
direct  
dirty

Domain-specific:  
Most things discussed in  
context of Rascal are  
general purpose stuff.

# Scylla & Charybdis



Algol 68,  
Smalltalk,  
Haskell

ABAP, Cobol,  
4GL etc.



- Orthogonality = design constraint
- Minimize concepts, maximize combinatorics
- More concepts => orthogonality is harder
- Trade-offs: slippery slope, turing tarpit, simplicity lost



G  
O  
N  
A  
R  
T  
H  
O

*Orthogonality* by Stefano Bertolo CC BY-NC-SA 2.0

<http://www.rascal-mpl.org>