SFWR ENG 4AA4

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Note: information from the pre-requisite, <u>SFWR ENG 3DX4</u> will not be included in this summary (although corrections will be).

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Real-Time Systems

Classifications

What happens upon failure to meet deadlines:

- Soft: performance is degraded but not destroyed
- Firm: a few times will simply degrade performance, but after may lead to system failure
- Hard: complete and catastrophic system failure
 - Safety Critical: may cause injury / death (a type of hard)
- Controller [C(s)]:
- **Input** [E(s)]:
- **Output** [U(s)]:
- U(s) = C(s)E(s)

Difference Equations

Forward difference method: derivatives using
$$f'(x) = \frac{f(x+h) - f(x)}{h}$$

Backwards Difference method: derivatives using
$$f'(x) = \frac{f(x) - f(x-h)}{h}$$

$$u[n] - u[n-1] = 48e[n] - 40e[n-1]$$

$$a\dot{U} + bU = c\dot{E} + dE$$

$$a\frac{u(kT_s)-u((k-1)T_s)}{T_s}+bu(kT_s)=c\frac{e(kT_s)-e((k-1)T_s)}{T_s}+de(kT_s)$$
 Group:

$$a\frac{u(kT_s)}{T_s} - \frac{au((k-1)T_s)}{T_s} + bu(T_s) = c\frac{e(kT_s)}{T_s} + de(kT_s) - c\frac{e((k-1)T_s)}{T_s}$$

$$\left(\frac{a}{T_s} + b\right) u(kT_s) + \left(-\frac{a}{T_s}\right) u((k-1)T_s) = \left(\frac{c}{T_s} + d\right) e(kT_s) + \left(\frac{c}{T_s}\right) e((k-1)T_s)$$

Equate each section to the values from the equation:

$$\frac{a}{T_{s}} + b = 1$$

$$b = 1 - \frac{a}{T_s}$$

$$b = 1 - 10a$$

$$\frac{a}{T} = 1$$

$$a = \frac{1}{10}$$

$$b = 0$$

$$\frac{c}{T_s} + d = 48$$

$$\boxed{d = 48 - 10c}$$

$$-\frac{c}{T_s} = -40$$

$$c = 4$$
 d = 48 - 40 = 8

$$\frac{1}{10}\dot{U} + 0U = 4\dot{E} + 8E$$

$$\frac{U}{E}(0.1s) = 4s + 8$$

$$\frac{U}{E} = \frac{4s+8}{0.1s}$$

Task optimization

Task [T]: $T_i = (p_i, r_i, e_i, d_i)$

Period [p]: time between tasks are repeatedly released

Release time [r]: time it takes to release task

Execution time [e]: slowest time task could take to be completed (but assume the tasks will take this long no matter what)

Deadline [d]: when task needs to be completed

Number of tasks [n]:

Processor Utilization [U]: used as a priority level $U = \sum_{i=1}^{n} \frac{e_i}{p_i}$

If U > 1, nothing is feasible

If $r_i = 0$ and $p_i = d_i$, then write $T_i = (p_i, e_i)$

Types of Scheduling

Static

Static Scheduling:

- task's priority is assigned before execution and does not change
- If a task misses its deadline, you mess up all the deadlines after it like an airport at Christmas
- A.K.A. Fixed priority

FIFO

First In First Out (FIFO):

• Could cause problems for tasks whose execution time is significantly shorter than the rest when there are deadlines

$$\circ$$
 E.g. $T_1 = (100, 3); T_2 = (2, 1)$

• A.K.A. First Come, First Served (FCFS)

Cyclic Executive: frame-based scheduling

- When you allocate an amount of time where a task can execute
- Can have multiple executions of the same task
- Tasks might not even fill the full frame

Schedule: the order in which tasks will be executed

Hyperperiod [H]: the entire length of a cycle, least common multiple

Harmonic: every task period evenly divides every longer period

Pre-empting: splitting a task up into multiple mini tasks. Also, if a task misses its deadline, halt the task at the deadline

Frame Size [f]:

- The best way for computers to segment the schedule in a way that it verify that the appropriate tasks have been executed
- Process: try each see which is the largest frame size that follows all the below constraints from 1 to e_{max} .
- Constraints:
 - 1. $f \ge \max_{1 \le i \le n} (e_i)$
 - 2. H% f = 0
 - 3. $2f gcd(p_i, f) \le d_i$

Least Compute Time (LCT): tasks with smallest execution times executed first

- Think greedy
- Works poorly; worse than RR

Rate Monotonic (RM): shorter period, higher priority

- Think: tasks requiring frequent attention should have higher priority
- If harmonic, feasible as long as $U \le 1$
- If non-harmonic, guaranteed feasible if $U \le n \left(2^{\frac{1}{n}} 1 \right)$
 - o If the equation fails, it still might be, so draw the whole thing to be safe.

Dynamic

Dynamic: each of the tasks' priorities can change. *Think*: while for static priorities it is constantly reevaluating which task has the highest priority, dynamic scheduling also re-evaluates the actual priorities, themselves.

The only two optimal dynamic priorities are:

- Earliest Deadline First (EDF):
 - more flexible, better U
 - o If deadlines < periods, still optimal, but determining feasibility is NP-hard
 - Always feasible if U ≤ 1
- Least Slack Theorem (LST): not as popular as EDF

Multiprocessor

Once you have multiple processors, neither EDF nor RM are guaranteed to work.

Look into first-fit algorithms

Task Interactions

Suspended: active choice, of access prevention until algorithm allows it to

Blocked: as a result of waiting for a resource to be free

How to do the timing diagrams with locks:

• $S_1 = lock(S_1)$

• $S_1^{\bullet} = \text{unlock}(S_1)$

One-shot Tasks: non-periodic tasks

Critical Section: when a task tries to acquire a shared resource already locked by another task

Priority Inversion: a method of avoiding deadlock by telling high priority tasks to share their resources with the lower priority tasks even when it's not their turn

- Allocate time, where T₁ has access to shared resource, so the time not allocated can be preempted
- Connect the pre-empted by T₁ when T₁ wants to access the resource
- Protect the resource with a semaphore
- You can make it so that tasks can use the resource even after they release the semaphore, but you risk overwriting in that time

Priority Inheritance Protocol (PIP):

- Temporarily raise the priority of a task only if and when it actually blocks a higher priority task; on leaving the critical section, the task priority reverts to its original value
- Issues:
 - o If only one shared resource, there's only one possible schedule
 - If more than one resource blocking:
 - Blocking time may be excessively long
 - Deadlock may occur
 - o If accessing multiple resources, you can only use them in the same order

Priority Ceiling Protocol (PCP): tasks entering a critical section can only access the blocked resource if it has a priority higher than the priority ceiling

- Priority Ceiling (PC): maximum priority of all tasks ever going to access a resource
- Only need to check PC when entering a critical section
- If any task needs priority higher than the priority ceiling of ALL of the semaphores currently locked, it's suspended
- Main advantages:
 - No locked resources, so free access
 - "The state of the art when resolving resource-contention issues"

- "Deadlock free for an arbitrary number of tasks with an arbitrary number of resources acted upon in an arbitrary way."
 - Deadlock: think if you and I are at a table with one fork and one knife and you need both to eat, but you take the fork and I take the knife.

Sporadic Server

Execution Budget [e_s]: periodic tasks aren't flexible...

Execution time [e_i]: ...sporadic tasks are

Deadline [d_i]: absolute deadline

Release Time [r_i]:

Set of Sporadic Tasks $[\theta]$:

Sporadic Task [S_i]:

- Non-periodic task
- (r_i, e_i, d_i)
- Typically interrupt-driven

Rules [ρ]: set of rules regulating a sporadic server

Sporadic Server $[\Phi_s]$: (p_s, e_s, θ, ρ)

Periodic Task: (ps, es) a type of sporadic server

• no expectation of when it finishes, only that a new one is queued every period

Assume:

Φ_s scheduled with T_i according to RM

We don't use K_d because it looks at the derivative regardless of the size of the error function. If your error is a sine function with a small amplitude, K_d will only take the derivative into account and it will overcompensate.

Open loop response: plant with no control

Ziegler-Nichols Tuning Rule: a PID tuning rule

Look at the open loop response. It could have a longer rise time / overshoot than preferred.

1. Tangent to curve on upslope

High sample rate \rightarrow lots of high frequency noise

Effective Utilization [δ]:

 $U = U_{periodic} + \delta U_{sporadic}$

Error bound $[\epsilon]$:

Slack [ω]:

Acceptance Test: check of stuff

$$\omega(S_k,t) = \left[\frac{d_k - t}{p_s}\right] e_s - e_k - \sum_{S_i \in \theta: d_i < d_k} e_i - \xi_i$$

- 1. If $\omega(S_k, t) < 0$, reject task
- 2. If $\omega(S_k, t) \ge 0$, need to check if already accepted sporadic tasks are adversely affected, i.e. $\omega(S_j, t) e_k \ge 0$ holds for all $S_j \in \theta$ with $d_i \ge d_k$.

The set θ is maintained dynamically.

Clocks

Computer Clock [C]:

Standard Clock [Cs]: perfect clock; has real time

Attributes:

- Correctness
- Bounded Drift
- Monotonicity
- Chronoscopicity

(EPS): a bounded/maximum difference between the clock time and the real time $|C(t) - C_S(t)| \le EPS$

Reset time [r]: the real time you set the clock to when you reset it

Drift [E]: rate of change of the clock value away from a perfect clock (each second)

• There's usually a reason why a clock drifts

Drift Bound [ρ]: maximum drift

$$\left| \frac{\mathrm{d}C(t)}{\mathrm{d}t} - 1 \right| \le \rho$$

Reset Error [ɛ]: error between actual time and time clock was set to at reset

Total Error [E]: $E(t) = \varepsilon + drift_since_reset$ $drift_since_reset \le \rho(C(t) - r)$ $E(t) = \rho(C(t) - r) + \varepsilon \le EPS$ $C(t) - r \le (EPS - \varepsilon)/\rho$

Real time will be within this interval – [C(t) - E(t), C(t) + E(t)]

Monotonicity: Clock will always have a consistent spacing and will only move in one order (forward / backwards)

SSL certs will fail signature if your clock is wrong as to ensure this

Chronoscopicity [y]: maximum changing drift

second derivative of stuff $\left| \frac{\mathrm{d}^2 C(t)}{\mathrm{d}t^2} \right| \leq \gamma$

Cristian's Algorithm

Minimum Latency [T_{min}]:

Request Send Time [T₀]:

Request Receive Time [T₁]:

Server Time $[T_{server}]$: time returned by the server

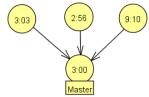
$$T_{\text{new}} = T_{\text{server}} + \frac{T_1 - T_0}{2}$$

Accuracy is
$$\pm \frac{T_1 - T_0}{2} - T_{\min}$$

Berkeley

Not often used, but useful for learning

1. Elect 1 node to be the **master**, the one that runs the algorithm



- 2. Finds the average of the nodes. However, that's probably going to find a value that isn't near any of them.
- 3. Eliminate the outliers:
 - a. Standard deviation: the more outliers, the harder to remove them, i.e. $\sqrt{1/2} \times \Sigma(x_i \mu)^2$
 - b. Mediar
 - c. **Maximum deviation**: maximum clock drift × time since last synchronization; sometimes it's good to use physical limitations as the minimum check to ensure accuracy

d.

PID Control

Plant [G(s)]: a transfer function, e.g. $\frac{1}{s^2 + 10s + 20}$

Remember this from 3DX4? Most of the stuff is still there, so refer to that. More here. Each of the K's represent a different error or gain

4 types of controllers [P(s)]:

• Proportional Controller (P),(PC):
$$\frac{K_p}{s^2 + 10s + (20 + K_p)}$$

• Proportional Integral (PI):
$$\frac{K_p s + K_i}{s^3 + 10s^2 + \left(20 + K_p s + K_i\right)}$$

- Proportional Derivative (PD): $\frac{K_d s + K_p}{s^2 + \left(10 + K_d\right) s + \left(20 + K_p\right)}$
- Proportional Integral Derivative (PID): $\frac{K_p s + K_i + s^2 K_d}{s \left(s^2 + a s + b\right) + K_p s + K_i + s^2 K_d}$

$$\frac{K_d s^2 + K_p s + K_i}{s^3 + (10 + K_d) s^2 + (20 + K_p) s + K_i}$$

$$u(t) = K_p e(t) + K_d \dot{e}(t) + K_i \int_0^t e(v) dv$$

Dominant pole: largest magnitude

Sampling

Good sampling rate is 10-20× the bandwidth

 $1Hz = 2\pi rad$

$$T_s \approx \frac{\text{dominant pole } \frac{rad}{s}}{2\pi rad}$$

Designing a PID Controller

- 1. Obtain an open-loop response and determine what needs to be improved
- 2. Add K_p to improve the rise time
- 3. Add K_d to improve the overshoot
- 4. Add K_i to eliminate the steady-state error
- 5. Adjust each of K_p , K_d , and K_i until you obtain a desired overall response. You can always refer to the table below to find out which controller controls what characteristics.

Increasing this	RISE TIME	OVERSHOOT	SETTLING TIME	S-S ERROR
Kp	Decrease	Increase	Small Change	Decrease
K _d	Small Change	Decrease	Decrease	No Change
K _i	Decrease	Increase	Increase	Eliminate

Ziegler-Nichols Tuning Rule:

- a plant with neither integrators nor dominant complex-conjugate pairs
- Look at the *open loop response*. It could have a longer rise time / overshoot than preferred.
- Tangent to curve on upslope
- For PID controllers

Noise frequency $[\omega_n]$:

Noise amplitude [a_n]:

Open loop: plant with no control

Closed loop:
$$H(s) = \frac{C(s)G(s)}{1 + C(s)G(s)}$$

$$H(s) = K_C \frac{\prod_{i=0}^{N} (s - z_i)}{\prod_{j=0}^{M} (s - p_j)}$$

$$C(s) = K_D s + K_P + \frac{K_I}{s}$$

So, you need to rearrange your H(s) that is in the first formula to look more like the second formula

Jitter

Jitter [J]: a delay

Relative Jitter: difference in response time between current and previous response times

 $\max_{k} |R_{i,k+1} - R_{i,k}|$

Absolute Jitter: difference between largest response time and smallest response time

max_k R_{i,k} - min_k R_{i,k}

Absolute jitter ≥ relative jitter

Fail

- **Fail-safe**: in the event of a specific type of failure, responds in a way that will cause no harm, or at least a minimum of harm, to other devices or to personnel
- Fail-stop: detects exceptions, but doesn't worry about handling them or raising them
 - failure in one component might not be visible until it leads to failure in another component
- Fail-fast: when a problem occurs, a fail-fast system fails immediately

Voting Schemes

Plurality [k]: number of votes needed for a majority

- Median voter: chooses median value as correct output (for this example, 2.00)
- Majority voter: given observations, d_i, and tolerance ε, i.e. willingness for error in *correct* value:
 - 1. Construct sets, P_k : $x \in P_k \leftrightarrow |x y| \le \varepsilon$ for all $y \in P_k$, where P_k has all elements within ε of each other, P_k is maximal, i.e. cannot add any points to it
 - 2. Choose P_k with largest $|P_k|$, where $|P_k| = \text{len}(P_k)$
 - If $|P_k| > floor(N/2)$: choose any one of P_k as *correct* value or a combination of many
 - Else, no result
 - e.g. Choose:
 - $\varepsilon = 0.1$
 - $P_1 = \{2.00, 2.01, 1.98, 2.05\} => |P_1| = 4 > floor(5/2) \leftarrow majority$ chooses value in P_k
 - $P_2 = \{1.80\}$

• What is the minimum value of ε that leads to the majority voter outputting a value?

 $\varepsilon = 0.03$ (i.e. range of 2.00, 2.01, 1.98); d_1 , d_2 , d_3 all satisfy $|d_i - d_j| \le 0.03$

• **K-plurality**: make a section of size k

Modular Redundancy (MR): when you have multiple separate redundant systems **Triple Modular Redundancy (TMR)**: having 3 systems with the same purpose running together. This ensures that if a system is not working properly, the things it outputs is compared against the other 2 systems and can be verified as wrong

Cold spare: a redundant system that is off until needed

Warm spare: a redundant system that is in a standby state until needed

Hot spare: a redundant system that is functional, on, and actively collaborating with the primary system

Byzantine General's Problem: useful for sensors with noisy values

n ≥ 3t + 1

[n]: number of generals

[t]: number of traitorous generals

Best Case Execution Time (BCET): Worst Case Execution Time (WCET):

(BCET^): estimation of BCET (WCET^): estimation of WCET BCET^ < BCET < WCET, WCET^

A lot of these problems are based on binomial

Information Redundancy

e.g. 1101100_, '_' is a parity or checksum, where 1's are even for even parity and odd for odd parity.

- Can detect single bit errors
- Cannot correct errors
- Adding more bits can also allow for correction
- Used in all Communication pRotoCols (CRC)