# SFWR ENG 4AA4

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Note: information from the pre-requisite, <u>SFWR ENG 3DX4</u> will not be included in this summary (although corrections will be).

# Contents

Real-Time Systems	2
Classifications	2
Difference Equations	2
e.g.)	2
Task optimization	3
Types of Scheduling	3
Static	3
FIFO	3
Dynamic	4
Multiprocessor	5
Task Interactions	5
Sporadic Server	6
Clocks	7
Cristian's Algorithm	8
Berkeley	8
PID Control	8
Sampling	9
Designing a PID Controller	9
Jitter	10
Fail	10
Voting Schemes	10
Information Redundancy	11

# Real-Time Systems

#### Classifications

What happens upon failure to meet deadlines:

- Soft: performance is degraded but not destroyed
- Firm: a few times will simply degrade performance, but after may lead to system failure
- Hard: complete and catastrophic system failure
  - Safety Critical: may cause injury / death (a type of hard)
- Controller [C(s)]:
- **Input** [E(s)]:
- **Output** [U(s)]:
- U(s) = C(s)E(s)

## **Difference Equations**

Forward difference method: derivatives using 
$$f'(x) = \frac{f(x+h) - f(x)}{h}$$

Backwards Difference method: derivatives using 
$$f'(x) = \frac{f(x) - f(x-h)}{h}$$

$$u[n] - u[n-1] = 48e[n] - 40e[n-1]$$

$$a\dot{U} + bU = c\dot{E} + dE$$

$$a\frac{u(kT_s)-u((k-1)T_s)}{T_s}+bu(kT_s)=c\frac{e(kT_s)-e((k-1)T_s)}{T_s}+de(kT_s)$$
 Group:

$$a\frac{u(kT_s)}{T_s} - \frac{au((k-1)T_s)}{T_s} + bu(T_s) = c\frac{e(kT_s)}{T_s} + de(kT_s) - c\frac{e((k-1)T_s)}{T_s}$$

$$\left(\frac{a}{T_s} + b\right) u(kT_s) + \left(-\frac{a}{T_s}\right) u((k-1)T_s) = \left(\frac{c}{T_s} + d\right) e(kT_s) + \left(\frac{c}{T_s}\right) e((k-1)T_s)$$

Equate each section to the values from the equation:

$$\frac{a}{T_{s}} + b = 1$$

$$b = 1 - \frac{a}{T_s}$$

$$b = 1 - 10a$$

$$\frac{a}{T_{\cdot}} = 1$$

$$a = \frac{1}{10}$$

$$b = 0$$

$$\frac{c}{T_s} + d = 48$$

$$d = 48 - 10c$$

$$-\frac{c}{T_s} = -40$$

$$c = 4$$
 d = 48 – 40 = 8

$$\frac{1}{10}\dot{U} + 0U = 4\dot{E} + 8E$$

$$\frac{U}{E}(0.1s) = 4s + 8$$

$$\frac{U}{E} = \frac{4s+8}{0.1s}$$

# Task optimization

Task [T]:  $T_i = (p_i, r_i, e_i, d_i)$ 

Period [p]: time between tasks are repeatedly released

Release time [r]: time it takes to release task

**Execution time** [e]: slowest time task could take to be completed (but assume the tasks will take this long no matter what)

Deadline [d]: when task needs to be completed

Number of tasks [n]:

**Processor Utilization** [U]: used as a priority level  $U = \sum_{i=1}^{n} \frac{e_i}{p_i}$ 

If U > 1, nothing is feasible

If  $r_i = 0$  and  $p_i = d_i$ , then write  $T_i = (p_i, e_i)$ 

# Types of Scheduling

#### Static

#### **Static Scheduling:**

- task's priority is assigned before execution and does not change
- If a task misses its deadline, you mess up all the deadlines after it like an airport at Christmas
- A.K.A. Fixed priority

#### **FIFO**

#### First In First Out (FIFO):

• Could cause problems for tasks whose execution time is significantly shorter than the rest when there are deadlines

$$\circ$$
 E.g.  $T_1 = (100, 3); T_2 = (2, 1)$ 

• A.K.A. First Come, First Served (FCFS)

Cyclic Executive: frame-based scheduling

- When you allocate an amount of time where a task can execute
- Can have multiple executions of the same task
- Tasks might not even fill the full frame

Schedule: the order in which tasks will be executed

Hyperperiod [H]: the entire length of a cycle, least common multiple

Harmonic: every task period evenly divides every longer period

**Pre-empting**: splitting a task up into multiple mini tasks. Also, if a task misses its deadline, halt the task at the deadline

#### Frame Size [f]:

- The best way for computers to segment the schedule in a way that it verify that the appropriate tasks have been executed
- Process: try each see which is the largest frame size that follows all the below constraints from 1 to  $e_{\text{max}}$ .
- Constraints:
  - 1.  $f \ge \max(e_i)$
  - 2. H% f = 0
  - 3.  $2f gcd(p_i, f) \le d_i$

Least Compute Time (LCT): tasks with smallest execution times executed first

- Think greedy
- Works poorly; worse than RR

Rate Monotonic (RM): shorter period, higher priority

- Think: tasks requiring frequent attention should have higher priority
- If harmonic, feasible as long as  $U \le 1$
- If non-harmonic, guaranteed feasible if  $U \le n \left( 2^{\frac{1}{n}} 1 \right)$ 
  - o If the equation fails, it still might be, so draw the whole thing to be safe.

#### Dynamic

**Dynamic**: each of the tasks' priorities can change. *Think*: while for static priorities it is constantly reevaluating which task has the highest priority, dynamic scheduling also re-evaluates the actual priorities, themselves.

The only two optimal dynamic priorities are:

- Earliest Deadline First (EDF):
  - more flexible, better U
  - o If deadlines < periods, still optimal, but determining feasibility is NP-hard
  - Always feasible if U ≤ 1
- Least Slack Theorem (LST): not as popular as EDF

#### Multiprocessor

Once you have multiple processors, neither EDF nor RM are guaranteed to work.

Look into first-fit algorithms

## Task Interactions

Suspended: active choice, of access prevention until algorithm allows it to

**Blocked**: as a result of waiting for a resource to be free

How to do the timing diagrams with locks:

•  $S_1 = lock(S_1)$ 

•  $S_1^* = \text{unlock}(S_1)$ 

One-shot Tasks: non-periodic tasks

Critical Section: when a task tries to acquire a shared resource already locked by another task

**Priority Inversion**: a method of avoiding deadlock by telling high priority tasks to share their resources with the lower priority tasks even when it's not their turn

- Allocate time, where T<sub>1</sub> has access to shared resource, so the time not allocated can be preempted
- Connect the pre-empted by T<sub>1</sub> when T<sub>1</sub> wants to access the resource
- Protect the resource with a semaphore
- You can make it so that tasks can use the resource even after they release the semaphore, but you risk overwriting in that time

#### **Priority Inheritance Protocol (PIP)**:

- Temporarily raise the priority of a task only if and when it actually blocks a higher priority task; on leaving the critical section, the task priority reverts to its original value
- Issues:
  - o If only one shared resource, there's only one possible schedule
  - If more than one resource blocking:
    - Blocking time may be excessively long
    - Deadlock may occur
  - o If accessing multiple resources, you can only use them in the same order

**Priority Ceiling Protocol (PCP)**: tasks entering a critical section can only access the blocked resource if it has a priority higher than the priority ceiling

- Priority Ceiling (PC): maximum priority of all tasks ever going to access a resource
- Only need to check PC when entering a critical section
- If any task needs priority higher than the priority ceiling of ALL of the semaphores currently locked, it's suspended
- Main advantages:
  - No locked resources, so free access
  - "The state of the art when resolving resource-contention issues"

- "Deadlock free for an arbitrary number of tasks with an arbitrary number of resources acted upon in an arbitrary way."
  - **Deadlock**: think if you and I are at a table with one fork and one knife and you need both to eat, but you take the fork and I take the knife.

# **Sporadic Server**

**Execution Budget** [e<sub>s</sub>]: periodic tasks aren't flexible...

**Execution time** [e<sub>i</sub>]: ...sporadic tasks are

Deadline [d<sub>i</sub>]: absolute deadline

**Release Time** [r<sub>i</sub>]: delay before the task is released to be executed

#### **Set of Sporadic Tasks** $[\theta]$ :

Sporadic Task [S<sub>i</sub>]:

- Non-periodic task (a.k.a. aperiodic)
- (r<sub>i</sub>, e<sub>i</sub>, d<sub>i</sub>)
- Typically interrupt-driven

**Rules** [ρ]: set of rules regulating a sporadic server

**Sporadic Server**  $[\Phi_s]$ :  $(p_s, e_s, \theta, \rho)$ 

Periodic Task: (ps, es) a type of sporadic server

• no expectation of when it finishes, only that a new one is gueued every period

#### Assume:

Φ<sub>s</sub> scheduled with T<sub>i</sub> according to RM

We don't use K<sub>d</sub> because it looks at the derivative regardless of the size of the error function. If your error is a sine function with a small amplitude, K<sub>d</sub> will only take the derivative into account and it will overcompensate.

Open loop response: plant with no control

#### Ziegler-Nichols Tuning Rule: a PID tuning rule

Look at the open loop response. It could have a longer rise time / overshoot than preferred.

1. Tangent to curve on upslope

High sample rate  $\rightarrow$  lots of high frequency noise

#### **Effective Utilization** [ $\delta$ ]:

 $U = U_{periodic} + \delta U_{sporadic}$ 

Error bound  $[\epsilon]$ :

Slack [ω]:

Acceptance Test: check of stuff

$$\omega(S_k,t) = \left[\frac{d_k - t}{p_s}\right] e_s - e_k - \sum_{S_i \in \theta: d_i < d_k} e_i - \xi_i$$

- 1. If  $\omega(S_k, t) < 0$ , reject task
- 2. If  $\omega(S_k, t) \ge 0$ , need to check if already accepted sporadic tasks are adversely affected, i.e.  $\omega(S_j, t) e_k \ge 0$  holds for all  $S_j \in \theta$  with  $d_i \ge d_k$ .

The set  $\theta$  is maintained dynamically.

#### Clocks

Computer Clock [C]:

Standard Clock [Cs]: perfect clock; has real time

Attributes:

- Correctness
- Bounded Drift
- Monotonicity
- Chronoscopicity

**(EPS)**: a bounded/maximum difference between the clock time and the real time  $|C(t) - C_s(t)| \le EPS$ 

**Reset time** [r]: the real time you set the clock to when you reset it

Drift [E]: rate of change of the clock value away from a perfect clock (each second)

• There's usually a reason why a clock drifts

**Drift Bound** [ρ]: maximum drift

$$\left| \frac{\mathrm{d}C(t)}{\mathrm{d}t} - 1 \right| \le \rho$$

Reset Error [ɛ]: error between actual time and time clock was set to at reset

**Total Error** [E]:  $E(t) = \varepsilon + drift\_since\_reset$   $drift\_since\_reset \le \rho(C(t) - r)$   $E(t) = \rho(C(t) - r) + \varepsilon \le EPS$   $C(t) - r \le (EPS - \varepsilon)/\rho$ 

Real time will be within this interval – [C(t) - E(t), C(t) + E(t)]

**Monotonicity**: Clock will always have a consistent spacing and will only move in one order (forward / backwards)

SSL certs will fail signature if your clock is wrong as to ensure this

**Chronoscopicity** [y]: maximum changing drift

second derivative of stuff  $\left| \frac{\mathrm{d}^2 C(t)}{\mathrm{d}t^2} \right| \leq \gamma$ 

# Cristian's Algorithm

Minimum Latency [T<sub>min</sub>]:

**Request Send Time** [T<sub>0</sub>]:

**Request Receive Time** [T<sub>1</sub>]:

**Server Time**  $[T_{server}]$ : time returned by the server

$$T_{\text{new}} = T_{\text{server}} + \frac{T_1 - T_0}{2}$$

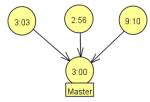
Accuracy is  $\pm \frac{T_1 - T_0}{2} - T_{\min}$ 

#### **Round Trip Time (RTT)**:

#### Berkeley

Not often used, but useful for learning

1. Elect 1 node to be the master, the one that runs the algorithm



- 2. Finds the average of the nodes. However, that's probably going to find a value that isn't near any of them.
- 3. Eliminate the outliers:
  - a. Standard deviation: the more outliers, the harder to remove them, i.e.  $\sqrt{1/2} \times \Sigma(x_i \mu)^2$
  - b. Median
  - c. **Maximum deviation**: maximum clock drift × time since last synchronization; sometimes it's good to use physical limitations as the minimum check to ensure accuracy

d.

### PID Control

**Plant** [G(s)]: a transfer function, e.g.  $\frac{1}{s^2 + 10s + 20}$ 

Remember this from 3DX4? Most of the stuff is still there, so refer to that. <u>More here</u>. Each of the K's represent a different error or gain

4 types of controllers [P(s)]:

• Proportional Controller (P),(PC):  $\frac{K_p}{s^2 + 10s + (20 + K_p)}$ 

- Proportional Integral (PI):  $\frac{K_p s + K_i}{s^3 + 10s^2 + \left(20 + K_p s + K_i\right)}$
- Proportional Derivative (PD):  $\frac{K_d s + K_p}{s^2 + (10 + K_d) s + (20 + K_p)}$
- Proportional Integral Derivative (PID):  $\frac{K_p s + K_i + s^2 K_d}{s \left(s^2 + a s + b\right) + K_p s + K_i + s^2 K_d}$

$$\frac{K_d s^2 + K_p s + K_i}{s^3 + (10 + K_d) s^2 + (20 + K_p) s + K_i}$$

$$u(t) = K_p e(t) + K_d \dot{e}(t) + K_i \int_0^t e(v) dv$$

Dominant pole: largest magnitude

### Sampling

Good sampling rate is 10-20× the bandwidth

 $1Hz = 2\pi rad$ 

$$T_s \approx \frac{\text{dominant pole} \frac{rad}{s}}{2\pi rad}$$

## Designing a PID Controller

- 1. Obtain an open-loop response and determine what needs to be improved
- 2. Add  $K_p$  to improve the rise time
- 3. Add K<sub>d</sub> to improve the overshoot
- 4. Add K<sub>i</sub> to eliminate the steady-state error
- 5. Adjust each of K<sub>p</sub>, K<sub>d</sub>, and K<sub>i</sub> until you obtain a desired overall response. You can always refer to the table below to find out which controller controls what characteristics.

Increasing this	RISE TIME	OVERSHOOT	SETTLING TIME	S-S ERROR
Kp	Decrease	Increase	Small Change	Decrease
K <sub>d</sub>	Small Change	Decrease	Decrease	No Change
K <sub>i</sub>	Decrease	Increase	Increase	Eliminate

#### **Ziegler-Nichols Tuning Rule:**

- a plant with neither integrators nor dominant complex-conjugate pairs
- Look at the open loop response. It could have a longer rise time / overshoot than preferred.
- Tangent to curve on upslope
- For PID controllers

Noise frequency  $[\omega_n]$ :

**Noise amplitude** [a<sub>n</sub>]:

Open loop: plant with no control

Closed loop: 
$$H(s) = \frac{C(s)G(s)}{1 + C(s)G(s)}$$

$$H(s) = K_C \frac{\prod_{i=0}^{N} (s - z_i)}{\prod_{j=0}^{M} (s - p_j)}$$

$$C(s) = K_D s + K_P + \frac{K_I}{s}$$

So, you need to rearrange your H(s) that is in the first formula to look more like the second formula

### **Jitter**

Jitter [J]: a delay

Relative Jitter: difference in response time between current and previous response times

 $\max_{k} |R_{i,k+1} - R_{i,k}|$ 

Absolute Jitter: difference between largest response time and smallest response time

max<sub>k</sub> R<sub>i,k</sub> - min<sub>k</sub> R<sub>i,k</sub>

Absolute jitter ≥ relative jitter

#### Fail

- **Fail-safe**: in the event of a specific type of failure, responds in a way that will cause no harm, or at least a minimum of harm, to other devices or to personnel
- Fail-stop: detects exceptions, but doesn't worry about handling them or raising them
  - failure in one component might not be visible until it leads to failure in another component
- Fail-fast: when a problem occurs, a fail-fast system fails immediately

# **Voting Schemes**

Plurality [k]: number of votes needed for a majority

- Median voter: chooses median value as correct output (for this example, 2.00)
- Majority voter: given observations, d<sub>i</sub>, and tolerance ε, i.e. willingness for error in correct value:
  - 1. Construct sets,  $P_k$ :  $x \in P_k \leftrightarrow |x y| \le \varepsilon$  for all  $y \in P_k$ , where  $P_k$  has all elements within  $\varepsilon$  of each other,  $P_k$  is maximal, i.e. cannot add any points to it
  - 2. Choose  $P_k$  with largest  $|P_k|$ , where  $|P_k| = \text{len}(P_k)$ 
    - If  $|P_k| > floor(N/2)$ : choose any one of  $P_k$  as *correct* value or a combination of many
    - Else, no result
    - e.g. Choose:
      - $\varepsilon = 0.1$
      - $P_1 = \{2.00, 2.01, 1.98, 2.05\} => |P_1| = 4 > floor(5/2) \leftarrow majority$  chooses value in  $P_k$
      - $P_2 = \{1.80\}$

• What is the minimum value of  $\epsilon$  that leads to the majority voter outputting a value?

 $\varepsilon = 0.03$  (i.e. range of 2.00, 2.01, 1.98);  $d_1$ ,  $d_2$ ,  $d_3$  all satisfy  $|d_i - d_j| \le 0.03$ 

• K-plurality: make a section of size k

**Modular Redundancy (MR)**: when you have multiple separate redundant systems **Triple Modular Redundancy (TMR)**: having 3 systems with the same purpose running together. This ensures that if a system is not working properly, the things it outputs is compared against the other 2 systems and can be verified as wrong

Cold spare: a redundant system that is off until needed

Warm spare: a redundant system that is in a standby state until needed

Hot spare: a redundant system that is functional, on, and actively collaborating with the primary system

Byzantine General's Problem: useful for sensors with noisy values

n ≥ 3t + 1

[n]: number of generals

[t]: number of traitorous generals

A lot of these problems are based on binomial

#### Information Redundancy

e.g. 1101100\_, '\_' is a **parity** or **checksum**, where the number of 1's are identified as even (1) for **even parity** and odd (0) for **odd parity**.

- Can detect single bit errors
- Cannot correct errors
- Adding more bits can also allow for correction
- Used in all Communication pRotoCols (CRC)

#### **Execution Time**

Underestimate the time

Best Case Execution Time (BCET): Worst Case Execution Time (WCET):

(BCET^): estimation of BCET (WCET^): estimation of WCET BCET^ < BCET < WCET, WCET^

# Natural Language Standards

Should: soft requirement Shall: hard requirement