

# SFWR ENG 4E03

Fall 2015

Note: material covered in [Stats 3Y03 Summary](#) will not be covered in this summary

**Expected Value** [ $\mu$ ]: definition of expected (NOT RIGHT!!)

**Poisson parameter** [ $\lambda$ ]:

**Exponential distribution**: not always for time

**Probability Distribution Function (PDF)**:

**Cumulative Distribution Function (CDF)**:

**Uniform Distribution**: no memoryless property

**Exponential Distribution**:

- Memoryless
- Either CDF or PDF of original equation  $F = 1 - e^{-\lambda x}$

*Think chemistry, i.e. cancelling units*

**Device** [ $i$ ]:

[ $k$ ]: total number of devices

**Service Time** [ $S$ ]: time to complete specific job

**Visitation** [ $V$ ]: given or projected visits/jobs (closed system); cannot be calculated

[ $E(V)$ ]: calculated visit/job ratio

**Demand** [ $D$ ]: total service demand

$$D_i = E[S_i] \cdot V_i$$

$$D = \sum_{i=0}^k D_i$$

**Time in system** [ $T$ ]: expected time the job is in the system

**Response Time** [ $R$ ]:

**Total Jobs** [ $N$ ]:

$$E[T] = \frac{N}{X}$$

$$E[N] = \lambda E[T], \lambda = X$$

**Think time** [ $Z$ ]: time it takes the user to put a request in and start, it's kinda like the frequency that users put in requests (seconds / request)

$$E[Z] = E[T] - E[R]$$

If  $E[Z] = 0$ ,  $R = N$

$$E[N] = \lambda E[R], \lambda = X$$

$$E[T] \geq \max(D, ND_{\max} - E[Z])$$

**Throughput** [ $X$ ]: out-rate, jobs / hour of full system

$$X \leq \min \left( \frac{1}{D_{\max}}, \frac{N}{D + E[Z]} \right)$$

Note:  $\frac{1}{D_{\max}}$  and  $\frac{N}{D + E[Z]}$  converge at their lowest point, so equate them

$[X_i]$ : throughput of individual component

$$X_i = E[V_i]X$$

**Utilization**  $[\rho]$ : ratio that the time is busy

$$\rho_i = X_i E[S_i]$$

$$\rho_i = XD_i$$