Reinforcement Learning

Lecture 8: Policy gradient methods

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Lecture overview



Lecture covers chapter 13 in Sutton & Barto [1] and examples from David Silver [2]

- Policy-based methods
- definition
- characteristics
- deterministic vs stochastic policies
- 2 Policy gradients
- gradient-based estimator
- Monte Carlo REINFORCE
- 3 Actor-critic methods
- definition
- algorithm
- function approximation error in AC methods
- extensions

Policy-based methods introduction



Definition: policy-based methods

Last week, we used a function approximator to estimate the value function:

$$\hat{v}(s, \mathbf{w}) \approx v_{\pi}(s),$$

and for control we estimated Q:

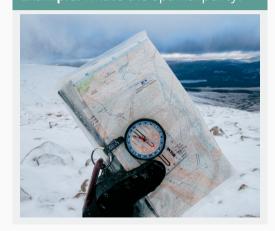
$$\hat{q}(s, a, \mathbf{w}) \approx q_{\pi}(s, a).$$

This week we will estimate policies:

$$\pi_{\theta}(a|s) = P(a|s,\theta)$$

Given a state, what's the distribution over actions?

Example: what's the optimal policy?



Policy-based methods characteristics



Policy-based RL characteristics

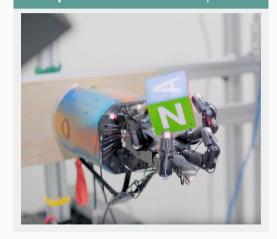
This approach has the following **advantages**:

- Can be more efficient that calculating the value function
- Better convergence guarantees
- Effective in high-dimensional or continuous action spaces
- Can learn stochastic policies

And the following disadvantages:

- Converges on local rather than global optimum
- Inefficient policy evaluation with high variance

Example: continuous action spaces •



Policy-based methods deterministic vs stochastic policies



Example: deterministic vs stochastic policies Deterministic policy for feature vectors describing the walls around a state: Stochastic policy:

Example from [2].

Policy gradients gradient estimators



Problem: ∇ through stochastic decisions

We estimate the advantage $\hat{A}(a,s)$ (or value for higher variance) for state s under a stochastic policy $\pi_{\theta}(a \mid s)$ by sampling from the policy (MC estimate).

Typically π follows a categorical distribution (softmax) or a Gaussian for continuous action spaces. We could use zeroth-order optimisation that does not require gradients (stochastic annealing, genetic algorithms, simplex downhill etc.), but this does not work well in high-dimensional spaces (e.g. with deep learning).

To optimise the policy, we need the gradient, but **sampling breaks backpropagation**!

Solution: log-derivative trick

$$\nabla_{\theta} \mathbb{E}_{\pi_{\theta}(a|x)} [\hat{A}(a,s)]$$

$$= \nabla_{\theta} \sum_{a} \pi_{\theta}(a \mid x) \hat{A}(a,s)$$

$$= \sum_{a} \pi_{\theta}(a \mid x) \frac{\nabla_{\theta} [\pi_{\theta}(a \mid x) \hat{A}(a,s)]}{\pi_{\theta}(a \mid x)}$$

$$= \sum_{a} \pi_{\theta}(a \mid x) \hat{A}(a,s) \frac{\nabla_{\theta} \pi_{\theta}(a \mid x)}{\pi_{\theta}(a \mid x)}$$

$$= \sum_{a} \pi_{\theta}(a \mid x) \hat{A}(a,s) \nabla_{\theta} \log \pi_{\theta}(a \mid x)$$

$$\approx \frac{1}{n} \sum_{a} \hat{A}(a,s) \nabla_{\theta} \log \pi_{\theta}(a \mid x)$$

$$\approx \frac{1}{n} \sum_{a \sim \pi_{\theta}(a \mid x)} \hat{A}(a,s) \nabla_{\theta} \log \pi_{\theta}(a \mid x)$$

Policy gradients Monte Carlo REINFORCE



Definition: Monte Carlo REINFORCE

REINFORCE estimates the return in the previous equation by using a Monte Carlo estimate [3].

- Initialise some arbitrary parameters θ
- Iteratively sample episodes
- Calculate the complete return from each step
- For each step again, update the gradient times the sample return

Algorithm: Monte Carlo REINFORCE

PyTorch example: 🗹

 $\begin{tabular}{ll} \# \mbox{ initialise } \theta \mbox{ with random values} \\ \pi = \mbox{PolicyNetwork}(\theta) \end{tabular}$

while(True):

sample episode following π $S_0, A_0, R_1, ..., S_{T-1}, A_{T-1}, R_T \sim \pi$

for
$$t$$
 in range $(T-1)$:

$$G_t \leftarrow \sum_{k=t+1}^{T} \gamma^{k-t-1} R_k$$

$$\theta \leftarrow \theta + \alpha \gamma^t G_t \nabla \ln \pi (A_t | S_t, \theta)$$

Actor-critic methods introduction



Definition: actor-critic methods

We combine policy gradients with action-value function approximation, using two models that may (optionally) share parameters.

• We use a **critic** to estimate the *Q* values:

$$q_{\mathbf{W}}(s,a) \approx q^{\pi_{\theta}}(s,a)$$

 We use an actor to update the policy parameters θ in the direction suggested by the critic.

Example: Actor critic



Actor-critic methods algorithm



Definition: actor-critic

Putting this together, actor-critic methods use an approximate policy gradient to adjust the actor policy in the direction that maximises the reward according to the critic:

$$\theta \leftarrow \theta + \alpha \nabla_{\theta} \log \pi_{\theta}(a|s) q_{\mathbf{w}}(s, a)$$

Algorithm: Actor-Critic (**PyTorch** ☑)

```
# initialise s, \theta, \mathbf{w} randomly # sample a \sim \pi_{\theta}(a|s) for t in range(T): sample r_t and s' from environment(s, a) sample a' \sim \pi_{\theta}(a'|s') \theta \leftarrow \theta + \alpha q_{\mathbf{w}}(s, a) \nabla_{\theta} \ln \pi_{\theta}(a|s) # update actor \delta_t = r_t + \gamma q_{\mathbf{w}}(s', a') - q_{\mathbf{w}}(s, a) # TD error \mathbf{w} \leftarrow \mathbf{w} + \alpha \delta_t \nabla_{\mathbf{w}} q_{\mathbf{w}}(s, a) # update critic a \leftarrow a', s \leftarrow s'
```

Actor-critic methods TD3



Function approximation error in actor-critic

In practice, tricks are needed to reduce function approximation in actor-critic methods. TD3 [4]:

- Dual critic networks + actor network
- Adds $\epsilon \sim \text{clip}(\mathcal{N}(0, \tilde{\sigma}), -c, c)$ to actions
- Delayed policy updates, replay buffer



Algorithm: TD3 [4]

Initialize critic networks $Q_{\theta_1}, Q_{\theta_2}$, and actor network π_ϕ with random parameters θ_1, θ_2, ϕ Initialize target networks $\theta_1' \leftarrow \theta_1, \theta_2' \leftarrow \theta_2, \phi' \leftarrow \phi$ Initialize replay buffer \mathcal{B}

for t = 1 to T do

Select action with exploration noise $a \sim \pi_{\phi}(s) + \epsilon$, $\epsilon \sim \mathcal{N}(0, \sigma)$ and observe reward r and new state s' Store transition tuple (s, a, r, s') in \mathcal{B}

Sample mini-batch of N transitions (s, a, r, s') from \mathcal{B} $\tilde{a} \leftarrow \pi_{\phi'}(s') + \epsilon, \quad \epsilon \sim \operatorname{clip}(\mathcal{N}(0, \tilde{\sigma}), -c, c)$ $y \leftarrow r + \gamma \min_{i=1,2} Q_{\theta'_i}(s', \tilde{a})$ Update critics $\theta_i \leftarrow \operatorname{argmin}_{\theta_i} N^{-1} \sum (y - Q_{\theta_i}(s, a))^2$

if $t \mod d$ then

Update ϕ by the deterministic policy gradient:

 $\nabla_{\phi}J(\phi)=N^{-1}\sum\nabla_{a}Q_{\theta_{1}}(s,a)|_{a=\pi_{\phi}(s)}\nabla_{\phi}\pi_{\phi}(s)$ Update target networks:

$$\theta_i' \leftarrow \tau \theta_i + (1 - \tau)\theta_i'$$
$$\phi' \leftarrow \tau \phi + (1 - \tau)\phi'$$

end if

Extensions and further reading



Extensions

This has introduced the foundations, hopefully now you have a good platform to read about the extensions to this.

- 1. Recommended further study (papers & code): 🗗
- 2. Recommended further study (theory & STAR):

Extensions include:

- Advantage actor critic (A3C & A2C) [5]
- Experience replay & prioritised replay [6]
- Proximal policy optimisation [7]
- Addressing Function Approximation Error in Actor-Critic Methods (TD3) [4] - recommended starter

Take Away Points



Summary

In summary:

- Policy gradients open up many new extensions
- Choose extensions to reduce variance to stabilise training
- And extensions to reduce overestimation bias of value function
- Consider regularisation to encourage exploration
- Going off-policy gives better exploration
- Its possible for the actor and critic to share some lower layer parameters, but be careful about it
- Experience replay can increase sample efficiency (where simulation is expensive)

References I



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 Reinforcement learning: An introduction (second edition). Available online . MIT press, 2018.
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References II



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