

COMP3667: Reinforcement learning practical 6

Temporal-Difference Learning

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This is the version *with* answers!

1 Overview

Welcome to the sixth reinforcement learning practical. In this practical, we will be experimenting with different TD methods to better understand their characteristics, advantages, and drawbacks. In particular, we will

- evaluate on-policy SARSA(0) and off-policy Q -Learning
- experiment with n -step TD learning
- compare the performance of these methods in different environments
- understand when/how/why they may fail to work and how to fix them.

2 Setup

For this practical, you will need a basic Python environment with `numpy`, `matplotlib`, and OpenAI `gym` (version 0.20.0). You will not need a GPU. [</> copy code](#)

```
1 !pip install 'gym[box2d]==0.20.0'
2 import gym
3 import numpy as np
4 import matplotlib.pyplot as plt
5 import matplotlib.font_manager
6 import itertools
7 from IPython import display
```

As before, we will use different versions of the frozen lake gym environment: [</> copy code](#)

```
1 name = 'FrozenLake-v1'
2 env = gym.make(name, is_slippery=False) # 4x4
3 env = gym.make(name, map_name="8x8", is_slippery=False) # 8x8
4 env = gym.make(name, desc=["SFHH",
5                             "HFFH",
6                             "HHFF",
7                             "HHHG",], is_slippery=False) # custom
8 env.seed(742)
9 env.action_space.seed(742)
10 LEFT, DOWN, RIGHT, UP = 0, 1, 2, 3
```

You can use this function (slightly modified from previous practicals) for plotting the environment [</> copy code](#)

```
1 def plot(env, v=None, policy=None, col_ramp=1, dpi=175, draw_vals=False, mark_ice=True):
2     # set up plot
3     plt.rcParams['figure.dpi'] = dpi
4     plt.rcParams.update({'axes.edgecolor': (0.32,0.36,0.38)})
5     plt.rcParams.update({'font.size': 4 if env.env.nrow == 8 else 7})
6     gray = np.array((0.32,0.36,0.38))
7     plt.figure(figsize=(3, 3))
```

```

8     ax = plt.gca()
9     ax.set_xticks(np.arange(env.env.ncol)-.5)
10    ax.set_yticks(np.arange(env.env.nrow)-.5)
11    ax.set_xticklabels([])
12    ax.set_yticklabels([])
13    plt.grid(color=(0.42,0.46,0.48), linestyle=':')
14    ax.set_axisbelow(True)
15    ax.tick_params(color=(0.42,0.46,0.48),
16                  which='both', top='off', left='off', right='off', bottom='off')
17    # use zero value as dummy if not provided
18    if v is None:
19        v = np.zeros(env.nS)
20    # plot values
21    plt.imshow(1-v.reshape(env.env.nrow,env.env.ncol)**col_ramp,
22              cmap='gray', interpolation='none',
23              clim=(0,1), zorder=-1)
24    # go through states
25    for s in range(env.nS):
26        x, y = s % env.env.nrow, s // env.env.ncol
27        # print numeric values
28        if draw_vals and v[s] > 0:
29            vstr = '{0:.1e}'.format(v[s]) if env.env.nrow == 8 else '{0:.6f}'.format(v[s])
30            plt.text(x - 0.45, y + 0.45, vstr, color=(0.2, 0.8, 0.2), fontname='Sans')
31        # mark ice, start, goal
32        if env.desc.tolist()[y][x] == b'F':
33            plt.text(x-0.45,y-0.3, 'ice', color=(0.5, 0.6, 1), fontname='Sans')
34            if mark_ice:
35                ax.add_patch(plt.Circle((x, y), 0.2, color=(0.7, 0.8, 1), zorder=0))
36        elif env.desc.tolist()[y][x] == b'S':
37            plt.text(x-0.45,y-0.3, 'start',color=(0.2,0.5,0.5), fontname='Sans',
38                  weight='bold')
39        elif env.desc.tolist()[y][x] == b'G':
40            plt.text(x-0.45,y-0.3, 'goal', color=(0.7,0.2,0.2), fontname='Sans',
41                  weight='bold')
42            continue # don't plot policy for goal state
43        else:
44            continue # don't plot policy for holes
45        # plot policy
46        def plot_arrow(x, y, dx, dy, v, scale=0.4):
47            plt.arrow(x, y, scale * float(dx), scale * float(dy), color=gray+0.2*(1-v),
48                    head_width=0.1, head_length=0.1, zorder=1)
49        if policy is not None:
50            if policy[s, 0] > 0.0: plot_arrow(x, y, -policy[s, 0],      0., v[s]) # left
51            if policy[s, 1] > 0.0: plot_arrow(x, y,      0., policy[s, 1], v[s]) # down
52            if policy[s, 2] > 0.0: plot_arrow(x, y, policy[s, 2],      0., v[s]) # right
53            if policy[s, 3] > 0.0: plot_arrow(x, y,      0., -policy[s, 3], v[s]) # up
54    plt.show()

```

and these two helper classes to define hard-coded policies or policies using Q -values

[</> copy code](#)

```

1  class QPolicy:
2      def __init__(self, Q, epsilon, values=False):
3          self.Q = Q
4          self.epsilon = epsilon
5          self.values = values
6      def sample(self, state):
7          if np.random.rand() > self.epsilon:
8              best_actions = np.argwhere(self.Q[state]==np.max(self.Q[state])).flatten()
9              return np.random.choice(best_actions)
10         else:

```

```

11         return env.action_space.sample()
12     def __getitem__(self, item):
13         state, action = item
14         if self.values:
15             return self.Q[state, action] / (self.Q[state].sum() + 1e-10)
16         else:
17             best_actions = np.argwhere(self.Q[state]==np.max(self.Q[state])).flatten()
18             p = int(action in best_actions) / len(best_actions)
19             return (1 - self.epsilon) * p + self.epsilon / len(self.Q[state])
20 class HardCodedPolicy:
21     def __init__(self, state_action_map):
22         self.state_action_map = state_action_map
23     def sample(self, state):
24         if state in self.state_action_map:
25             return np.random.choice(self.state_action_map[state])
26         else:
27             return np.random.choice(4)
28     def __getitem__(self, item):
29         state, action = item
30         if state in self.state_action_map:
31             if action in self.state_action_map[state]:
32                 return 1 / len(self.state_action_map[state])
33             else:
34                 return 0
35         else:
36             return 1 / 4

```

Finally, these functions can be used to plot the learning progress

[copy code](#)

```

1  # (using global variables in functions)
2  def update_plot(mod):
3      reward_list[experiment_id].append(reward_sum)
4      aoc[experiment_id] += reward_sum
5      test_reward_list[experiment_id].append(test_reward_sum)
6      test_aoc[experiment_id] += test_reward_sum
7      if episode % mod == 0:
8          plot_data[experiment_id].append([episode,
9                                          np.array(reward_list[experiment_id]).mean(),
10                                         np.array(test_reward_list[experiment_id]).mean()])
11
12      reward_list[experiment_id] = []
13      test_reward_list[experiment_id] = []
14      for i in range(len(plot_data)):
15          color=next(plt.gca()._get_lines.prop_cycler)['color']
16          plt.plot([x[0] for x in plot_data[i]],
17                  [x[1] for x in plot_data[i]],
18                  '-', color=color,
19                  label=f"{plot_labels[i]}, AOC: {aoc[i]}|{test_aoc[i]}")
20          plt.plot([x[0] for x in plot_data[i]],
21                  [x[2] for x in plot_data[i]], '--', color=color)
22      plt.xlabel('Episode number')
23      plt.ylabel('Episode reward')
24      plt.legend()
25      display.clear_output(wait=True)
26      plt.show()
27  def next_experiment():
28      reward_list.append([])
29      aoc.append(0)
30      test_reward_list.append([])
31      test_aoc.append(0)
32      plot_data.append([])

```

```
return experiment_id + 1
```

using the following global variables (re-evaluate this cell to reset them)

[copy code](#)

```
1 reward_list = [[]]
2 aoc = [0]
3 test_reward_list = [[]]
4 test_aoc = [0]
5 plot_data = [[]]
6 plot_labels = []
7 experiment_id = 0
```

3 On-policy and off-policy learning with TD(0)

Recap TD Learning

Remember our 0-step temporal difference (TD) targets from the lecture, which can be computed for any (also partial) episodes

$$\begin{aligned}
 V_\pi(s_t) &= \sum_{a_t \in \mathcal{A}} \pi(a_t | s_t) \sum_{s_{t+1} \in \mathcal{S}} p(s_{t+1} | s_t, a_t) \left[\mathcal{R}_{s_t s_{t+1}}^{a_t} + \gamma V_\pi(s_{t+1}) \right] \\
 &= \mathbb{E}_{a_t \sim \pi(a_t | s_t)} \mathbb{E}_{s_{t+1} \sim p(s_{t+1} | s_t, a_t)} \left[\mathcal{R}_{s_t s_{t+1}}^{a_t} + \gamma V_\pi(s_{t+1}) \right] \\
 &\approx \underbrace{\mathcal{R}_{s_t s_{t+1}}^{a_t} + \gamma V_\pi(s_{t+1})}_{\text{TD(0) target}} \\
 Q_{\pi^*}(s_t, a_t) &= \sum_{s_{t+1} \in \mathcal{S}} p(s_{t+1} | s_t, a_t) \left[\mathcal{R}_{s_t s_{t+1}}^{a_t} + \gamma \sum_{a_{t+1} \in \mathcal{A}} \pi^*(a_{t+1} | s_{t+1}) Q_{\pi^*}(s_{t+1}, a_{t+1}) \right] \\
 &= \mathbb{E}_{s_{t+1} \sim p(s_{t+1} | s_t, a_t)} \left[\mathcal{R}_{s_t s_{t+1}}^{a_t} + \gamma \mathbb{E}_{a_{t+1} \sim \pi^*(a_{t+1} | s_{t+1})} Q_{\pi^*}(s_{t+1}, a_{t+1}) \right] \\
 &\approx \underbrace{\mathcal{R}_{s_t s_{t+1}}^{a_t} + \gamma Q_{\pi^*}(s_{t+1}, a_{t+1})}_{\text{TD(0) target}} .
 \end{aligned}$$

At a particular time t we are in state s_t and take action $a_t \sim \pi(a_t | s_t)$ sampled from the policy π . We then end up in state $s_{t+1} \sim p(s_{t+1} | s_t, a_t)$ based on the environment's transition function. If we are interested in learning state-action values (i.e. solving the control problem), we additionally need to consider the following action $a_{t+1} \sim \pi^*(a_{t+1} | s_{t+1})$ based on the policy π^* that we want to learn or evaluate.

The TD(0) targets are noisy “snapshots” of how the values should look like based on the current transition at time t . The difference between the TD target and our current value estimate gives us a noisy TD error signal that tells us “how far off” our estimates are. This can be used to update our value estimates with a learning rate α (similar to SGD) to improve them

$$\begin{aligned}
 V_\pi(s_t) &\leftarrow V_\pi(s_t) + \alpha \left[\underbrace{\mathcal{R}_{s_t s_{t+1}}^{a_t} + \gamma V_\pi(s_{t+1})}_{\text{TD(0) target}} - V_\pi(s_t) \right] \\
 Q_{\pi^*}(s_t, a_t) &\leftarrow Q_{\pi^*}(s_t, a_t) + \alpha \left[\underbrace{\mathcal{R}_{s_t s_{t+1}}^{a_t} + \gamma Q_{\pi^*}(s_{t+1}, a_{t+1})}_{\text{TD(0) target}} - Q_{\pi^*}(s_t, a_t) \right] .
 \end{aligned}$$

On-policy SARSA(0)

We can evaluate and improve our policy “on the go”. This is called *on-policy* learning and it means that the policy π we use for sampling is the same as the policy π^* we are evaluating and learning.

Exercise

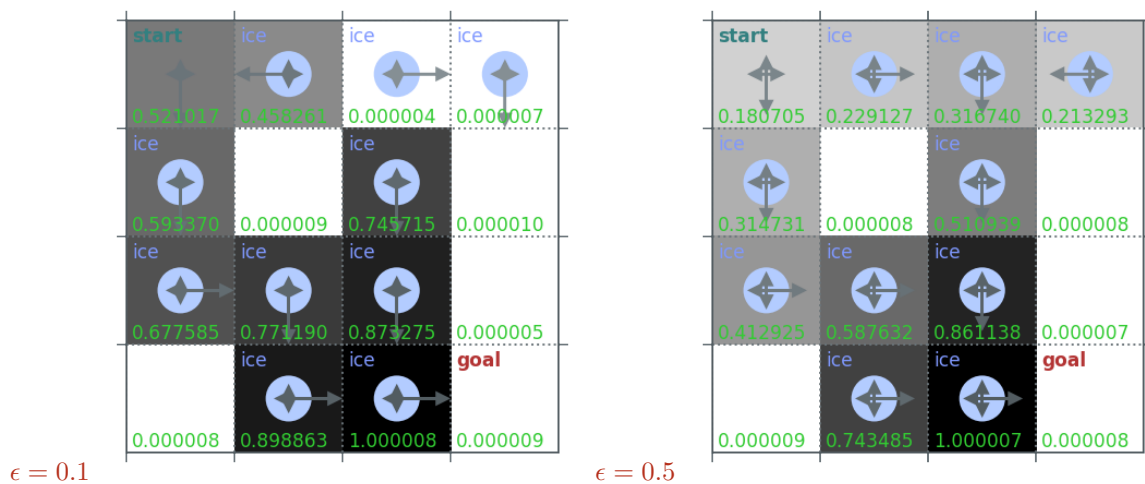
- Implement SARSA(0) by filling in the TD(0) targets and updates in the skeleton below. (The rest of the skeleton is for collecting episodes, evaluating the learned policy and plotting everything. The dashed line is the reward for the learned policy, the solid line is for the sampling policy.)

- Run a couple of evaluations with different values for the learning rate **alpha** and the exploration **epsilon** on the 4x4 environment. Use both “noisy” and “neutral” initialisations for Q (commenting in/out the respective lines in the code). What effects do you observe? With what parameters does the agent learn best?

Generally, learning occurs as a “jump”. Once the agent improves, it jumps directly to the level of its final performance (this is because there is only one simple goal state; either it knows how to get there or not). “Good” learning performance means that the agent makes that jump early (with a high probability). The best performance is achieved with intermediate values for both learning rate and exploration.

Learning rate alpha: Very large (approaching 1) and very low (below 0.01) learning rates are detrimental. Large learning rates make the convergence unstable; small learning rates are not a problem with a “neutral” initialisation but delay learning with a “noisy” initialisation.

Exploration epsilon: Generally, higher exploration results in a lower final performance because the agent does not act optimally. With “neutral” initialisation, little exploration is not detrimental (the policy chooses random actions if all values are zero; if they are not zero anymore, the agent has found the solution and we do not need to explore; this is again due to having only a single goal state). With a “noisy” initialisation, little exploration delays or prevents learning. Little exploration may also results in some states of the environment not being explored (if they are not on the found “solution path”) and thus not having a good policy for these states.



[copy code](#)

```

1  # parameters
2  num_episodes = 3000
3  alpha = 0.1
4  gamma = 0.9
5  epsilon = 0.5
6
7  Q = np.random.uniform(0, 1e-5, [env.observation_space.n, env.action_space.n]) # noisy
8  Q = np.zeros([env.observation_space.n, env.action_space.n]) # neutral
9  V = np.zeros([env.observation_space.n])
10
11 # policies
12 sample_policy = QPolicy(Q, epsilon)
13 learned_policy = sample_policy
14 plot_labels.append(f"SARSA (alpha={alpha}, epsilon={epsilon})")
15
16 for episode in range(num_episodes):
17     state = env.reset()
18     reward_sum = 0
19     # learning a policy
20     for t in itertools.count():
21         action = sample_policy.sample(state)
22         next_state, reward, done, _ = env.step(action)
23         next_action = learned_policy.sample(next_state)

```

```

24     # TD(0) targets
25     v_target = ...                # FILL IN HERE!
26     q_target = ...                # FILL IN HERE!
27     # updates
28     s, a = state, action
29     V[s] += ...                    # FILL IN HERE!
30     Q[s, a] += ...                # FILL IN HERE!
31
32     reward_sum += reward
33     if done:
34         break
35     state = next_state
36
37     # testing the learned policy
38     state = env.reset()
39     test_reward_sum = 0
40     while True:
41         action = learned_policy.sample(state)
42         next_state, reward, done, _ = env.step(action)
43         test_reward_sum += reward
44         state = next_state
45         if done:
46             break
47
48     update_plot(int(np.ceil(num_episodes / 20)))
49
50 env.close()
51 experiment_id = next_experiment()
52 print("Sampling policy and values")
53 plot(env, v=V, policy=sample_policy, draw_vals=True)
54 print("Learned policy and optimal/max values")
55 plot(env, v=Q.max(axis=1), policy=learned_policy, draw_vals=True)

```

Answer:

[copy code](#)

```

1  # TD(0) targets
2  v_target = reward + gamma * V[next_state]
3  q_target = reward + gamma * Q[next_state, next_action]
4  # updates
5  s, a = state, action
6  V[s] += alpha * (v_target - V[s])
7  Q[s, a] += alpha * (q_target - Q[s, a])

```

Off-policy Q-Learning

Sometimes, we would like to generate samples with one policy π (typically an exploratory policy) but then use the samples to learn another policy π^* (typically a near-optimal policy). This is possible with *off-policy* methods, such as Q-Learning.

3.0.1 Exercise

- Implement Q-Learning by using a different policy for the `learned_policy` (with lower `epsilon`) then for the `sample_policy`.
 - *Note:* Strictly speaking, the `sample_policy` does not change in Q-Learning. You can achieve this by using `epsilon=1` in the `sample_policy` to select actions randomly. For other values of `epsilon`, the `sample_policy` “peeks” into the values of the learned policy, which lets it profit from that learning (but is not a clean implementation).
 - *Bonus exercise:* Learn the `sample_policy` using SARSA(0) while learning the `learned_policy` with Q-Learning (this requires maintaining two copies of values estimates, performing separate updates for both etc).

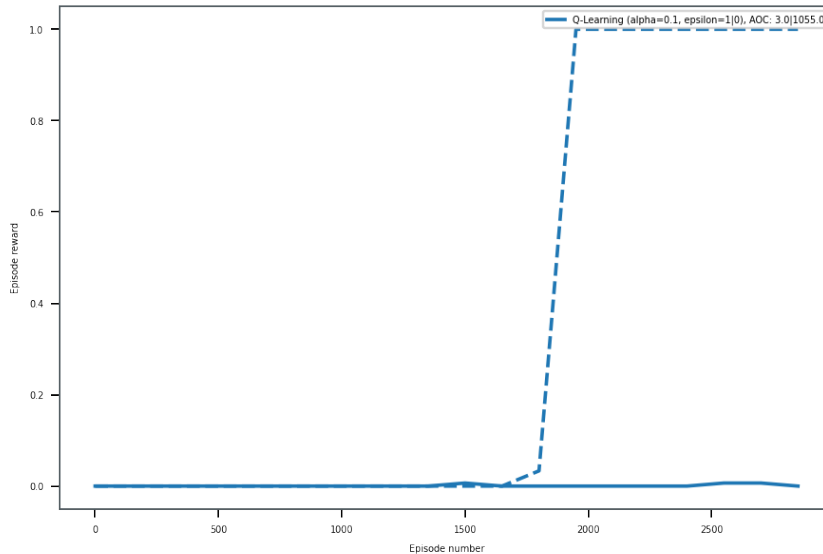
Replace the “policies” block with

[copy code](#)

```
1 # policies
2 sample_policy = QPolicy(Q, epsilon)
3 td_epsilon = 0
4 learned_policy = QPolicy(Q, td_epsilon)
5 plot_labels.append(f"Q-Learning (alpha={alpha}, epsilon={epsilon}|{td_epsilon})")
```

- Run the evaluation several times on the 4x4 and 8x8 environment. Try to get the fastest and most reliable learning by tweaking `epsilon`. How does the performance (episode reward) of the sampling policy (solid line) compare to that of the learned policy (dashed lines)? How is this different from SARSA(0)?

In SARSA(0) both policies performed equally well (up to noise). Here, the learned policy performs much better than the sampling policy. Even with a completely exploratory sampling policy, the learned policy performs optimally.



Expected TD(0) targets

The normal TD targets to estimate state-action values are computed by *sampling* from the policy π^* that is to be learned. This sampling step increases the noise in the TD error signal (in addition to the noise we already have due to sampling episodes). Instead, one can use the *expected* TD targets

$$\underbrace{\mathcal{R}_{s_t s_{t+1}}^{a_t} + \gamma \sum_{a_{t+1} \in \mathcal{A}} \pi^*(a_{t+1} | s_{t+1}) Q_{\pi^*}(s_{t+1}, a_{t+1})}_{\text{expected TD(0) target}} .$$

Exercise

- In the `q_target` replace the sampled value with an expectation over possible actions the `learned_policy` could take. *Note:* `learned_policy[next_state, a]` is giving you the probability of taking action `a` in state `next_state`.

Replace

```
1 q_target = reward + gamma * Q[next_state, next_action]
```

with

[copy code](#)

```
1 expected_Q = sum(learned_policy[next_state, a] * Q[next_state, a] for a in range(4))
2 q_target = reward + gamma * expected_Q
```

- Compare the performance when using the expected TD(0) target to using the sampled one.

There should be a slight performance gain, that is, on average the agent jumps to the optimal policy earlier. However, this could be difficult to spot due to the noise of when exactly that jump happens.

4 TD(n)

In TD(0) we do not look ahead and receiving a reward does only affect the value estimate of the current state and action. All the future expected rewards are approximated by using the current value estimates. However, we can improve on that by instead look n steps ahead (in hindsight) and taking the n next steps into account for computing TD targets. These TD(n) targets are

$$V_{\pi}(s_t) \approx \underbrace{\mathcal{R}_{s_t s_{t+1}}^{a_t} + \gamma \mathcal{R}_{s_{t+1} s_{t+2}}^{a_{t+1}} + \dots + \gamma^n \mathcal{R}_{s_{t+n} s_{t+n+1}}^{a_{t+n}}}_{\text{TD}(n) \text{ target}} + \gamma^{n+1} V_{\pi}(s_{t+n+1})$$

$$Q_{\pi^*}(s_t, a_t) \approx \underbrace{\mathcal{R}_{s_t s_{t+1}}^{a_t} + \gamma \mathcal{R}_{s_{t+1} s_{t+2}}^{a_{t+1}} + \dots + \gamma^n \mathcal{R}_{s_{t+n} s_{t+n+1}}^{a_{t+n}}}_{\text{TD}(n) \text{ target}} + \gamma^{n+1} Q_{\pi^*}(s_{t+n+1}, a_{t+n+1}) .$$

To compute them in hindsight, we have to store a trace of the last $n + 1$ transitions (including the current transition that is also used in TD(0)). The modified skeleton below is providing a trace of length $n + 1$ containing the last n steps and the current transition (for $n = 0$ this reduces to the TD(0) case of only considering the current transition).

[copy code](#)

```

1  # parameters
2  num_episodes = 3000
3  alpha = 0.1
4  gamma = 0.9
5  epsilon = 0.5
6  n = 0
7
8  Q = np.random.uniform(0, 1e-5, [env.observation_space.n, env.action_space.n]) # noisy
9  Q = np.zeros([env.observation_space.n, env.action_space.n]) # neutral
10 V = np.zeros([env.observation_space.n])
11
12 # policies
13 sample_policy = QPolicy(Q, epsilon)
14 learned_policy = sample_policy
15 plot_labels.append(f"SARSA (n={n}, alpha={alpha}, epsilon={epsilon})")
16
17 for episode in range(num_episodes):
18     state = env.reset()
19     reward_sum = 0
20     trace = np.zeros((n + 1, 4), dtype=int)
21     done_n = 0
22     # learning a policy
23     for t in itertools.count():
24         action = sample_policy.sample(state)
25         next_state, reward, done, _ = env.step(action)
26         next_action = learned_policy.sample(next_state)
27         trace[-1] = (state, action, reward, next_action)
28         if t > n:
29             # n-step targets
30             n_step_return = ... # FILL IN HERE!
31             v_target = ... # FILL IN HERE!
32             q_target = ... # FILL IN HERE!
33             # updates
34             s, a, _, _ = trace[0]
35             V[s] += alpha * (v_target - V[s])
36             Q[s, a] += alpha * (q_target - Q[s, a])
37
38         reward_sum += reward
39         done_n += done
40         if done_n > n:
41             break

```



```

42     state = next_state
43     trace = np.roll(trace, shift=-1, axis=0)
44
45     # testing the learned policy
46     state = env.reset()
47     test_reward_sum = 0
48     while True:
49         action = learned_policy.sample(state)
50         next_state, reward, done, _ = env.step(action)
51         test_reward_sum += reward
52         state = next_state
53         if done:
54             break
55
56     update_plot(int(np.ceil(num_episodes / 20)))
57
58 env.close()
59 experiment_id = next_experiment()
60 print("Sampling policy and values")
61 plot(env, v=V, policy=sample_policy, draw_vals=True)
62 print("Learned policy and optimal/max values")
63 plot(env, v=Q.max(axis=1), policy=learned_policy, draw_vals=True)

```

SARSA(n)

Exercise

- Implement SARSA(n) by filling in the `n_step_return`, `v_target` and `q_target` in the skeleton.

Answer:

[</> copy code](#)

```

1  # n-step targets
2  n_step_return = sum(gamma ** i * r for i, (_, _, r, _) in enumerate(trace))
3  v_target = n_step_return + gamma ** (n + 1) * V[next_state]
4  q_target = n_step_return + gamma ** (n + 1) * Q[next_state, next_action]

```

- Run this on the 8x8 environment and compare different values of n in terms of performance (how quickly the agent learns) and run time (roughly how fast/slow everything is running). What effects do you observe?

Generally, the larger n the better the agent's learning performance i.e. it jumps to an optimal (up to exploration) policy earlier. This is because observed rewards “travel” n steps at a time. However, larger n also considerably slow down the entire process (as longer traces have to be maintained and evaluated).

Q-Learning

For Q-Learning there is a problem because we want to evaluate a different policy (π^*) than the one used for sampling (π). That means that the n -step return was sampled with the “wrong” policy (π^* might never take some of the actions sampled from π) and so is not representative for π^* . This bias can be corrected by adding an *importance sampling* factor (a general technique in Monte Carlo methods to correct for sampling from a “wrong” distribution) to the learning rate α

$$\rho_t = \frac{\pi^*(a_t | s_t) \pi^*(a_{t+1} | s_{t+1}) \dots \pi^*(a_{t+n} | s_{t+n})}{\pi(a_t | s_t) \pi(a_{t+1} | s_{t+1}) \dots \pi(a_{t+n} | s_{t+n})} = \frac{\prod_{k=0}^n \pi^*(a_{t+k} | s_{t+k})}{\prod_{k=0}^n \pi(a_{t+k} | s_{t+k})}$$

$$\alpha_t = \alpha \rho_t .$$

Exercise

- Implement TD(n) Q-Learning by
 - computing the importance sampling factor ρ (`policy[s, a]` is giving you the probability of taking action `a` in state `s`).

- modifying the updates accordingly.

Answer:

[copy code](#)

```
1 # importance sampling factor
2 rho = np.prod([learned_policy[s, a] / sample_policy[s, a] for s, a, _, _ in trace])
3 # updates
4 s, a, _, _ = trace[0]
5 V[s] += alpha * rho * (v_target - V[s])
6 Q[s, a] += alpha * rho * (q_target - Q[s, a])
```

- Test TD(n) Q -Learning with different values for n and exploration in the sampling policy on the 8x8 environment. *Hint:* Use some small non-zero value for `epsilon` in the learned policy to make sure the importance sampling factors are not (almost) all zero. What do you observe?

TD(n) Q -Learning is less stable compared to SARSA(n). With `epsilon=1` (i.e. full exploration) in the sampling policy, even a value of $n = 1$ results in instabilities and the agent not learning a good policy. This is due to the very different probabilities between the two policies, which increases the noise in the TD targets. Additionally, full exploration does not provide many successful runs ending with a reward to learn from. Using smaller learning rates `alpha` can help increase stability.

With intermediate values (e.g. `epsilon=0.5`) in the sampling policy, learning is more reliable for small values of n . However, for larger n (≈ 10) learning success is only intermittent: it starts quickly but then degenerates again. This is again because of the noise due to the differences in the two policies. Moreover, since the sampling policy is “cheating” by using the Q values from the learned policy, it also is affected by errors due to the noise.