A "Hands-on" Introduction to MPI

* The name "MPI" is the property of the

Tim Mattson

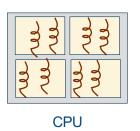
Human Learning Group.

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Hardware is diverse ... and its only getting worse!!!

Write code with TBB or OpenMP



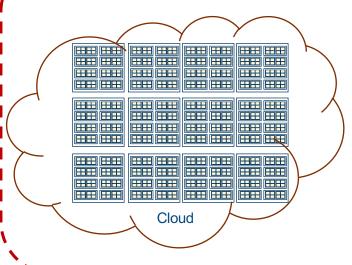
Work with the compiler to vectorize code

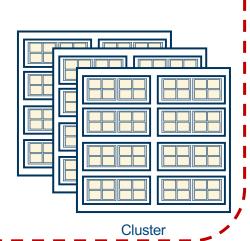


SIMD/Vector

Use a portable
API but if you
must, use CUDA.
It's all the same
model

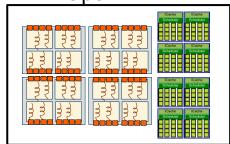
Parallelism over disjoint address-spaces MPI





OpenMP lets you "do it all".
Or combine CUDA and
OpenMP.

GPU



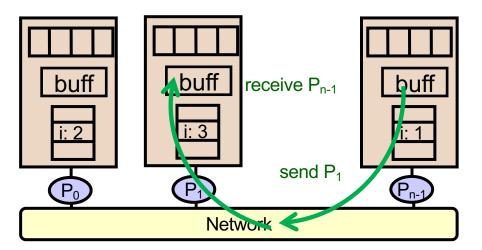
Heterogeneous node

Outline

- - MPI and distributed memory systems
 - The Bulk Synchronous Pattern and MPI collective operations
 - Introduction to message passing
 - The diversity of message passing in MPI
 - Geometric Decomposition and MPI
 - Concluding Comments

Programming Model for distributed memory systems

- Programs execute as a collection of processes.
 - Number of processes usually fixed at program startup time
 - Local address space per node -- <u>NO physically shared memory</u>.
 - **Logically** shared data is partitioned over local processes.
- Processes communicate by messages ... explicit send/receive pairs
 - Synchronization is implicit by communication events.
 - MPI (Message Passing Interface) is the most commonly used API



A collection of n MPI processes (P₀ to P_{n-1}) running on n nodes

MPI, the Message Passing Interface

MPI: An API for Writing Applications for Distributed Memory Systems

- -A library of routines to coordinate the execution of multiple processes.
- Provides point to point and collective communication in Fortran, C and C++
- -Unifies last decades of cluster computing and MPP* practice

MPI Alltoallv

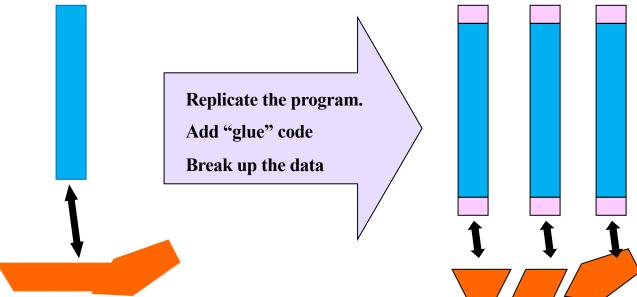
MPI Send

MPI Pack

How do people use MPI? The SPMD Design Pattern

A sequential program (blue) working on a data set (orange)

- A replicated single program working on a decomposed data set.
- Use Node ID (rank) and number of nodes to split up work between processes
- Coordinate processes by passing messages.



Running MPI programs

- MPI implementations need a way to start "P processes" on the system.
- We do this with the mpirun command:

> mpirun −n P ./a.out ←

You can test and develop code on your local system once you load MPI onto the system (mpich or openmpi).

This command will run the program locally on P processes

- On our cluster, you put mpirun inside a shell script and run through a batch queue.
- The actual nodes used are selected by the system based on the contents of the shell script

MPI uses **mpirun** or **mpiexec** (or both) to launch programs on a cluster. They are largely equivalent. Just figure out which one is preferred on the system you are using.

Exercise: Hello world part 1

- Goal
 - To confirm that you can run a program on our cluster.
- Program
 - Write a program that prints "hello world" to the screen.
 - Execute across the nodes of our cluster using mpirun inside a batch-queue shell script

```
#!/bin/bash
#SBATCH -p
sched_mit_psfc_gpu_r8
#SBATCH --reservation=cpsfr_2025
#SBATCH --ntasks=2
#SBATCH --nodes=2
#SBATCH -o job_mpi.log-%j
module load openmpi/4.1.4
mpirun a.out

Note: The sharester is it is a unix per
```

Note: The character '>' is a unix prompt

Running MPI programs

- MPI implementations need a way to start "P processes" on the system.
- We do this with the mpirun command:

> mpirun −n P ./a.out ←

Run the program locally on P processes

- To run on different nodes, use a hostfile.
 - > mpirun -hostfile hostfile -n P ./a.out 🔻

When you directly run on a cluster (i.e., not through a batch queue) you run the program as P processes on nodes from a hostfile. The hostfile has a node (a host) on each line followed by how many processes (slots) to allocated to each node. Here is an example for a typical cluster:

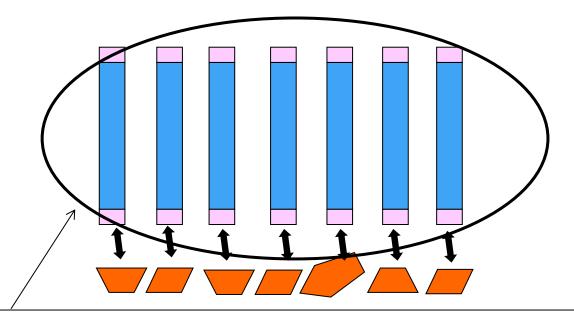
hpc-200-06-06 slots=2

hpc-200-06-17 slots=2

hpc-200-06-18 slots=2

An MPI program at runtime

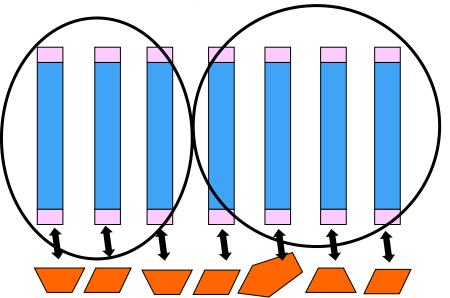
• Typically, when you run an MPI program, multiple processes all running the same program are launched ... working on their own block of data.



The collection of processes involved in a computation is called "a process group"

An MPI program at runtime

• Typically, when you run an MPI program, multiple processes all running the same program are launched ... working on their own block of data.



You can dynamically split a **<u>process group</u>** into multiple subgroups to manage how processes are mapped onto different tasks

```
#include <stdio.h>
#include <mpi.h>
int main (int argc, char **argv){
   int rank, size;
   MPI_Init (&argc, &argv);
   MPI Comm rank (MPI COMM WORLD, &rank);
   MPI Comm size (MPI COMM WORLD, &size);
   printf( "Hello from process %d of %d\n",
                               rank, size );
   MPI Finalize();
   return 0;
```

```
int MPI_Init (int* argc, char* argv[])
```

- Initializes the MPI library ... called before any other MPI functions.
- agrc and argv are the command line args passed from main()

```
#include <stdio.h>
#include <mpi.h>
int main (int argc, char **argv){
   int rank, size;
   MPI Init (&argc, &argv);
   MPI_Comm_rank (MPI_COMM_WORLD, &rank);
   MPI Comm size (MPI COMM WORLD, &size);
   printf( "Hello from process %d of %d\n",
                                rank, size );
   MPI Finalize();
                     int MPI Finalize (void)
   return 0;
                         Frees memory allocated by the MPI library ... close
                           every MPI program with a call to MPI Finalize
```

```
int MPI_Comm_size (MPI_Comm comm, int* size)
```

- MPI_Comm, an opaque data type called a communicator.
 Default context: MPI_COMM_WORLD (all processes)
- MPI_Comm_size returns the number of processes in the process group associated with the communicator

```
#include <stdio.h>
#include <mpi.h>
int main (int argc, char **argv){
   int rank, size;
   MPI Init (&argc, &argv);
   MPI_Comm_rank (MPI_COMM_WORLD, &rank);
   MPI Comm size (MPI COMM WORLD, &size);
   printf( "Hello from process %d of %d\n",
                               rank, size );
   MPI Finalize();
   return 0;
```

Communicators consist of two parts, a **context** and a **process group**.

The communicator lets one control how groups of messages interact.

Communicators support modular SW ... i.e. I can give a library module its own communicator and know that it's messages can't collide with messages originating from outside the module

```
int MPI_Comm_rank (MPI_Comm comm, int* rank)
```

- MPI_Comm, an opaque data type, a communicator. Default context:
 MPI_COMM_WORLD (all processes)
- MPI_Comm_rank An integer ranging from 0 to "(num of procs)-1"

```
#include <stdio.h>
#include <mpi.h>
int main (int argc, char **argv){
   int rank, size;
   MPI_Init (&argc, &argv);
   MPI Comm rank (MPI COMM WORLD, &rank);
   MPI Comm size (MPI COMM WORLD, &size);
   printf( "Hello from process %d of %d\n",
                               rank, size );
   MPI Finalize();
   return 0;
```

Note that other than init() and finalize(), every MPI function has a communicator.

This makes sense .. You need a context and group of processes that the MPI functions impact ... and those come from the communicator.

Compiling a program

- MPI provides a wrapper around the local compiler to create MPI programs.
- It is called mpicc or mpic++ or mpicxx ...
- The wrapper provides the libraries and anything else required to support MPI compilation and linking. Additional arguments are passed directly to the compiler.
- It is important that the compiler on the local system matches the one used by mpicc/mpic++/mpicxx

> mpicc -o complexProg -O3 -fopenmp comp.c mathyStuff.c andMore.c

Exercise: Hello world part 2

- Goal
 - To confirm that you can run an MPI program on our cluster
- Program
 - Write a program that prints "hello world" to the screen.
 - Modify it to run as an MPI program ... with each printing "hello world" and its rank

```
Compile and run MPI programs on log-in node. Load the MPI environment with the following command:
```

module load openmpi/4.1.4

Compile programs using the mpicc compiler.

```
#include <mpi.h>
int size, rank, argc; char **argv;
MPI_Init (&argc, &argv);
MPI_Comm_rank (MPI_COMM_WORLD, &rank);
MPI_Comm_size (MPI_COMM_WORLD, &size);
MPI_Finalize();
```

```
#!/bin/bash job_mpi.sh

#SBATCH -p sched_mit_psfc_gpu_r8

#SBATCH --reservation=cpsfr_2025

#SBATCH --ntasks=2

#SBATCH --nodes=2

#SBATCH -o job_mpi.log-%j

module load openmpi/4.1.4

mpirun a.out
```

> sbatch job_mpi.sh

Running the program

```
#!/bin/bash job_mpi.sh

#SBATCH -p sched_mit_psfc_gpu_r8

#SBATCH --reservation=cpsfr_2025

#SBATCH --ntasks=4

#SBATCH --nodes=4

#SBATCH -o job_mpi.log-%j

module load openmpi/4.1.4

mpirun a.out
```

```
#include <stdio.h>
#include <mpi.h>
int main (int argc, char **argv){
   int rank, size;
  MPI Init (&argc, &argv);
  MPI Comm rank (MPI COMM WORLD, &rank);
  MPI Comm size (MPI COMM WORLD, &size);
   printf( "Hello from process %d of %d\n", rank, size );
  MPI Finalize();
   return 0;
```

```
> sbatch job_mpi.sh
Submitted batch job 2695481

> cat job_mpi.log-2694870
hello from 0 of 4
hello from 2 of 4
hello from 1 of 4
hello from 3 of 4
```

Running the program (on clustered used with hostfiles)

```
On our 3 node cluster, I'd run this program (hello) as:
#include <stdio.h>
                                             > mpirun -n 3 -hostfile hosts hello
#include <mpi.h>
                                             hello from hpc-200-06-06.cr.cnaf.infn.it rank=0 of nprocs = 3
int main (int argc, char **argv){
                                              hello from hpc-200-06-18.cr.cnaf.infn.it rank=2 of nprocs = 3
   int rank, size;
                                              hello from hpc-200-06-17.cr.cnaf.infn.it rank=1 of nprocs = 3
   char name[MPI MAX PROCESSOR NAME];
   int namLen;
   MPI_Init (&argc, &argv);
   MPI Comm rank (MPI COMM WORLD, &rank);
   MPI Comm size (MPI COMM WORLD, &size);
  MPI Get processor name(name,&namLen);
   printf(" hello from %s process %d of nprocs = %d\n",name,ID, Nprocs);
   MPI Finalize();
                                       The following is the hostfile used above
   return 0;
                                        > Cat hosts
                                          hpc-200-06-06 slots=1
                                          hpc-200-06-17 slots=1
                                          hpc-200-06-18 slots=2
```

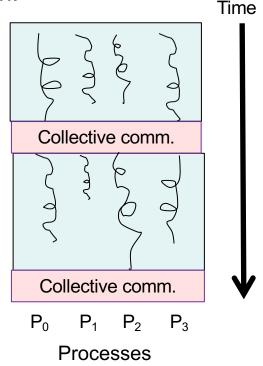
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A typical pattern with MPI Programs

- Many MPI applications directly call few (if any) message passing routines. They use the following very common pattern:
 - Use the Single Program Multiple Data pattern
 - Each process maintains a local view of the global data
 - A problem broken down into phases each of which is composed of two subphases:
 - · Compute on local view of data
 - Communicate to update global view on all processes (collective communication).
 - Continue phases until complete

This is a subset or the SPMD pattern sometimes referred to as the Bulk Synchronous pattern.



Collective Communication: Reduction

```
int MPI_Reduce (void* sendbuf,
    void* recvbuf, int count,
    MPI_Datatype datatype, MPI_Op op,
    int root, MPI_Comm comm)
```

Returns MPI_SUCCESS if there were no errors

• MPI_Reduce performs specified reduction operation (op) on the count values in sendbuf from all processes in communicator. Places result in recvbuf on the process with rank root only.

MPI Data Type*	C Data Type
MPI_CHAR	char
MPI_DOUBLE	double
MPI_FLOAT	float
MPI_INT	int
MPI_LONG	long
MPI_LONG_DOUBLE	long double
MPI_SHORT	short

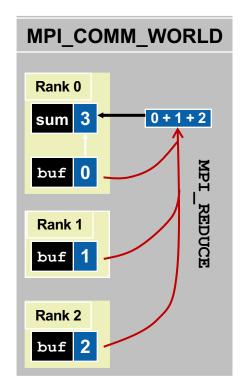
*This i	s a	subset	of	available	MPI	types
---------	-----	--------	----	-----------	-----	-------

Operation	Function
MPI_SUM	Summation
MPI_PROD	Product
MPI_MIN	Minimum value
MPI_MINLOC	Minimum value and location
MPI_MAX	Maximum value
MPI_MAXLOC	Maximum value and location
MPI_LAND	Logical AND

Operation	Function
MPI_BAND	Bitwise AND
MPI_LOR	Logical OR
MPI_BOR	Bitwise OR
MPI_LXOR	Logical exclusive OR
MPI_BXOR	Bitwise exclusive OR
User-defined	It is possible to define new reduction operations

MPI_Reduce() Example

```
#include <mpi.h>
int main(int argc, char* argv[]) {
  int buf, sum, nprocs, myrank;
 MPI Init(&argc,&argv);
 MPI Comm size(MPI COMM WORLD, &nprocs);
 MPI Comm rank(MPI COMM WORLD, &myrank);
  sum = 0;
 buf = myrank;
 MPI Reduce (&buf, &sum, 1, MPI INT,
          MPI SUM, 0, MPI COMM WORLD);
 MPI Finalize();
```



MPI_Reduce() Example

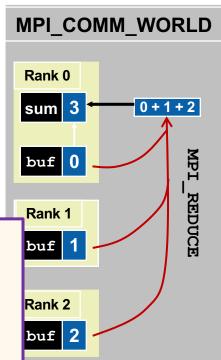
```
#include <mpi.h>
int main(int argc, char* argv[]) {
  int buf, sum, nprocs, myrank;

MPI_Init(&argc,&argv);
  MPI_Comm_size(MPI_COMM_WORLD, &nprocs);
  MPI_Comm_rank(MPI_COMM_WORLD, &myrank);

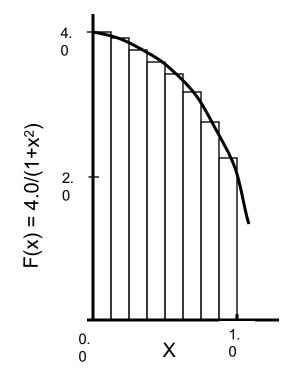
sum = 0;
```

C language comments:

- char* is a pointer to a collection of characters (a string).
- char* argv[] is the same as char **argv. They point to a collection of strings
- If you have a variable and you want its address, use the & character. C is a *call-by-value* language. If you want to pass updated values through a function argument, you need to pass in the address for that argument, for example &myrank



Example Problem: Numerical Integration



Mathematically, we know that:

$$\int_{0}^{1} \frac{4.0}{(1+x^2)} dx = \pi$$

We can approximate the integral as a sum of rectangles:

$$\sum_{i=0}^{N} F(x_i) \Delta x \approx \pi$$

Where each rectangle has width Δx and height $F(x_i)$ at the middle of interval i.

PI Program: an example

```
static long num steps = 100000;
double step;
void main ()
     int i; double x, pi, sum = 0.0;
     step = 1.0/(double) num_steps;
        x = 0.5 * step;
     for (i=0;i\leq num steps; i++)
          x+=step;
          sum += 4.0/(1.0+x*x);
     pi = step * sum;
```

Exercise: Pi Program

module load compilers/openmpi-4-1-5_gcc12.3 module load compilers/gcc-12.3 sl7

- Goal
 - To write a simple Bulk Synchronous, SPMD program
- Program
 - Start with the provided "pi program" and using an MPI reduction, write a parallel version of the program.

MPI_Op	Function
MPI_SUM	Summation

```
#include <mpi.h>
int size, rank, argc; char **argv;
MPI_Init (&argc, &argv);
MPI_Comm_rank (MPI_COMM_WORLD, &rank);
MPI_Comm_size (MPI_COMM_WORLD, &size);
MPI_Finalize();
```

MPI Data Type	C Data Type
MPI_DOUBLE	double
MPI_FLOAT	float
MPI_INT	int
MPI_LONG	long

Pi program in MPI

```
#include <mpi.h>
void main (int argc, char *argv[])
     int i, my id, numprocs; double x, pi, step, sum = 0.0;
     step = 1.0/(double) num steps;
     MPI Init(&argc, &argv);
     MPI Comm rank(MPI COMM WORLD, &my id);
     MPI Comm size(MPI COMM WORLD, &numprocs);
     my steps = num steps/numprocs;
     for (i=my id*my steps; i<(my id+1)*my steps; i++)
           x = (i+0.5)*step;
                                              Sum values in "sum" from
           sum += 4.0/(1.0+x*x);
                                              each process and place it
                                                 in "pi" on process 0
     sum *= step ;
     MPI_Reduce(&sum, &pi, 1, MPI_DOUBLE, MPI_SUM, 0, MPI_COMM_WORLD);
```

Timing MPI programs

- MPI added a function (which OpenMP copied) to time programs.
- MPI_Wtime() returns a double for the time (in seconds) for some arbitrary time in the past.
- As with omp_get_wtime(), call before and after a section of code of interest to get an elapsed time.

Exercise: Pi Program with MPI_Wtime()

- Goal
 - Time your Bulk Synchronous, SPMD program
- Program
 - Start with your parallel "pi program" and use MPI_Wtime() to explore its scalability on your system.

MPI_Op	Function
MPI_SUM	Summation

```
#include <mpi.h>
int size, rank, argc; char **argv;
MPI_Init (&argc, &argv);
MPI_Comm_rank (MPI_COMM_WORLD, &rank);
MPI_Comm_size (MPI_COMM_WORLD, &size);
double MPI_Wtime();
MPI_Finalize();
```

MPI Data Type	C Data Type
MPI_DOUBLE	double
MPI_FLOAT	float
MPI_INT	int
MPI_LONG	long

Pi program in MPI

```
#include <mpi.h>
void main (int argc, char *argv[])
     int i, my id, numprocs; double x, pi, step, sum = 0.0;
     step = 1.0/(double) num steps;
     MPI Init(&argc, &argv);
     MPI Comm rank(MPI COMM WORLD, &my id);
     MPI Comm size(MPI COMM WORLD, &numprocs);
     double init time = MPI Wtime();
     my steps = num steps/numprocs;
     for (i=my id*my steps; i<(my id+1)*my steps; i++)
           x = (i+0.5)*step;
           sum += 4.0/(1.0+x*x);
     sum *= step;
     MPI Reduce(&sum, &pi, 1, MPI DOUBLE, MPI SUM, 0, MPI COMM WORLD);
     if(my id == 0) printf(" runtime = %lf\n",MPI Wtime()-init time);
```

MPI Pi program performance (on my laptop)

```
#include <mpi.h>
void main (int argc, char *argv[])
                                                                             OpenMP
                                                                   Thread
                                                                      or
     int i, my id, numprocs; double x, pi, step, sum = 0.0;
                                                                    procs
     step = 1.0/(double) num steps;
     MPI Init(&argc, &argv);
     MPI Comm rank(MPI COMM WORLD, &my id);
                                                                      2
     MPI Comm size(MPI COMM WORLD, &numprocs);
     double init time = MPI Wtime();
                                                                      3
     my steps = num steps/numprocs;
                                                                      4
     for (i=my id*my steps; i<(my id+1)*my steps; i++)
           x = (i+0.5)*step;
           sum += 4.0/(1.0+x*x);
     sum *= step;
     MPI Reduce(&sum, &pi, 1, MPI DOUBLE, MPI SUM, 0, MPI COMM WORLD);
     if(my id == 0) printf(" runtime = %lf\n",MPI Wtime()-init time);
```

MPI

0.84

0.48

0.46

0.46

OpenMP

PI Loop

0.43

0.23

0.23

0.23

SPMD

critical

0.85

0.48

0.47

0.46

^{*}Intel compiler (icpc) with -O3 on Apple OS X 10.7.3 with a dual core (four HW thread) Intel® Core™ i5 processor at 1.7 Ghz and 4 Gbyte DDR3 memory at 1.333 Ghz.

MPI Pi program performance (on my laptop)

```
#include <mpi.h>
void main (int argc, char *argv[])
                                                                          OpenMP
                                                                                                 MPI
                                                                Thread
                                                                                     OpenMP
                                                                           SPMD
                                                                                     PI Loop
                                                                   or
    int i, my id, numprocs; double x, pi, step, sum = 0.0;
                                                                           critical
                                                                 procs
    step = 1.0/(double) num steps;
    MPI Init(&argc, &argv);
                                                                            0.85
                                                                                       0.43
                                                                                                 0.84
    MPI Comm rank(MPI COMM WORLD, &my id);
                                                                   2
                                                                            0.48
                                                                                       0.23
                                                                                                 0.48
    MPI Comm size(MPI COMM WORLD, &numprocs);
     double init time = MPI Wtime();
                                                                   3
                                                                            0.47
                                                                                       0.23
                                                                                                 0.46
    my steps = num steps/numprocs;
                                                                            0.46
                                                                                       0.23
                                                                                                 0.46
    for (i=my id*my steps; i<(my id+1)*my steps; i++)
                                         Is this a dependable way to get an elapsed time?
          x = (i+0.5)*step;
          sum += 4.0/(1.0+x*x);
                                       What if instead of a laptop, we are starting processes
                                            across a large cluster? Is this time reliable?
    sum *= step;
    MPI Reduce(&sum, &pi, 1, MPI DOUBLE, MPI SUM, 0, MPI COMM WORLD);
     if(my id == 0) printf(" runtime = %lf\n",MPI Wtime()-init time);
```

^{*}Intel compiler (icpc) with −O3 on Apple OS X 10.7.3 with a dual core (four HW thread) Intel® CoreTM i5 processor at 1.7 Ghz and 4 Gbyte DDR3 memory at 1.333 Ghz.

Synchronization in MPI

- Synchronization ... establishing ordering constraints among concurrent processes so we can establish happens-before relations.
- As we will see later ... the semantics of how messages are passed includes synchronization properties.
- For a stand-alone synchronization construct, we can use a barrier (all processes in the group associated with comm arrive before any proceed):
 - int MPI_Barrier(MPI_Comm comm)

Synchronization in MPI

- Synchronization ... establishing ordering constraints among concurrent processes so we can establish happens-before relations.
- As we will see later ... the semantics of how messages are passed includes synchronization properties.
- For a stand-alone synchronization construct, we can use a barrier (all processes in the group associated with comm arrive before any proceed):

int MPI_Barrier(MPI_Comm comm)

What is this int for? All MPI routines other than the timing routines return an int error code. Equals MPI_SUCCESS when everything is OK, other values specific to routines when errors occur. It's common to just ignore this output (which is bad practice, but "we all" do it.

Pi program in MPI

```
#include <mpi.h>
void main (int argc, char *argv[])
     int i, my id, numprocs; double x, pi, step, sum = 0.0;
     step = 1.0/(double) num steps;
     MPI Init(&argc, &argv);
     MPI Comm rank(MPI COMM WORLD, &my id);
     MPI Comm size(MPI COMM WORLD, &numprocs);
     MPI Barrier(MPI COMM WORLD);
                                                                   Use a barrier to make sure all
     if(my id ==0) double init time = MPI Wtime();
                                                                 processes have started-up before
     my steps = num steps/numprocs;
                                                                  we start timing the computation
     for (i=my id*my steps; i<(my id+1)*my steps; i++) {
           x = (i+0.5)*step;
           sum += 4.0/(1.0+x*x);
     sum *= step;
     MPI Reduce(&sum, &pi, 1, MPI DOUBLE, MPI SUM, 0, MPI COMM WORLD);
     if(my id == 0) printf(" runtime = %lf\n",MPI Wtime()-init time);
                                                            We don't need a barrier here since collective
                                                                  communication implies a barrier
```

Timing without a barrier

 Another option ... forget the barrier. Collect times for all processes and report min, max and average. This is easy to do using the operations available for use in MPI_Reduce.

```
int MPI_Reduce (void* sendbuf,
    void* recvbuf, int count,
    MPI_Datatype datatype, MPI_Op op,
    int root, MPI_Comm comm)
```

Operation	Function
MPI_SUM	Summation
MPI_PROD	Product
MPI_MIN	Minimum value
MPI_MINLOC	Minimum value and location
MPI_MAX	Maximum value
MPI_MAXLOC	Maximum value and location
MPI_LAND	Logical AND

• Plus, knowing min, max and average gives you information about how well balanced the load it. It's much more informative than a single number with barrier.

Exercise: Explore timing MPI programs with the Pi program

- Goal
 - To work with a number of reduction operators and use results to access load balancing.
- Program
 - Use MPI Wtime(), MPI Barrier() and other methods explore timing for the pi program.

```
#include <mpi.h>
int size, rank, argc; char **argv;
MPI_Init (&argc, &argv);
MPI_Comm_rank (MPI_COMM_WORLD, &rank);
MPI_Comm_size (MPI_COMM_WORLD, &size);
double MPI_Wtime();
int MPI_Barrier(MPI_COMM_WORLD);
MPI_Finalize();
```

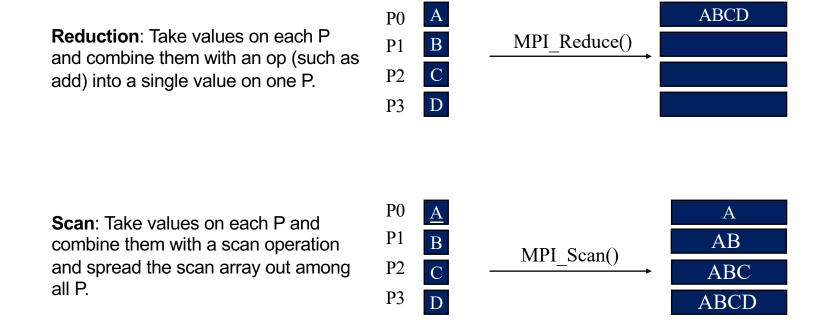
Operation	Function
MPI_SUM	Summation
MPI_PROD	Product
MPI_MIN	Minimum value
MPI_MINLOC	Minimum value and location
MPI_MAX	Maximum value
MPI_MAXLOC	Maximum value and location
MPI_LAND	Logical AND

Pi program ... return max time

```
#include <mpi.h>
void main (int argc, char *argv[])
    int i, my id, numprocs; double x, pi, step, sum = 0.0, mxtime=0.0;
     step = 1.0/(double) num steps;
     MPI Init(&argc, &argv);
     MPI Comm rank(MPI COMM WORLD, &my id);
     MPI Comm size(MPI COMM WORLD, &numprocs);
     MPI Barrier(MPI COMM WORLD);
     double init time = MPI Wtime();
     my steps = num steps/numprocs;
     for (i=my id*my steps; i<(my id+1)*my steps; i++) {
          x = (i+0.5)*step;
          sum += 4.0/(1.0+x*x);
     sum *= step;
    MPI Reduce(&sum, &pi, 1, MPI DOUBLE, MPI SUM, 0, MPI COMM WORLD);
    double wtime = MPI Wtime()-init time
     MPI Reduce(&wtime, &mxtime, 1, MPI DOUBLE, MPI MAX, 0, MPI COMM WORLD);
     if(my id == 0) printf(" maximum time = %lf",mxtime);
```

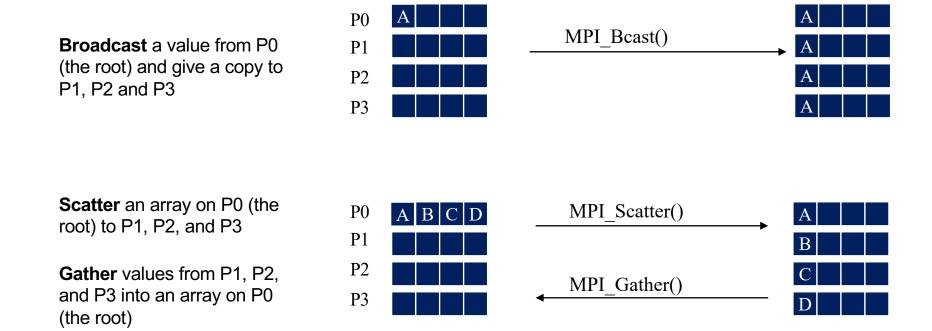
MPI defines a rich set of Collective operations

Collective Computations



int MPI_Reduce(const void *sendbuf, void *recvbuf, int count, MPI_Datatype datatype, MPI_Op op, int root, MPI_Comm comm) int MPI_Scan(const void *sendbuf, void *recvbuf, int count, MPI_Datatype datatype, MPI_Op op, MPI_Comm comm)

Collective Data Movement



int MPI_Bcast(void *buffer, int count, MPI_Datatype datatype, int root, MPI_Comm comm)
int MPI_Gather(const void *sendbuf, int sendcount, MPI_Datatype sendtype, void *recvbuf, int recvcount, MPI_Datatype recvtype, int root, MPI_Comm comm)
int MPI_Scatter(const void *sendbuf, int sendcount, MPI_Datatype sendtype, void *recvbuf, int recvcount, MPI_Datatype recvtype, int root, MPI_Comm comm)

More Collective Data Movement





int MPI_Allgather(const void *sendbuf, int sendcount, MPI_Datatype sendtype, void *recvbuf, int recvcount, MPI_Datatype recvtype, MPI_Comm comm) int MPI_Alltoall(const void *sendbuf, int sendcount, MPI_Datatype sendtype, void *recvbuf, int recvcount, MPI_Datatype recvtype, MPI_Comm comm)

MPI Collectives: Summary

- Collective communications: called by all processes in the group to create a global result and share with all participating processes.
 - Allgather, Allgatherv, Allreduce, Alltoall, Alltoallv, Bcast, Gather, Gatherv, Reduce, Reduce_scatter, Scan, Scatter, Scatterv
- Notes:
 - Allreduce, Reduce, Reduce_scatter, and Scan use the same set of built-in or userdefined combiner functions.
 - Routines with the "All" prefix deliver results to all participating processes
 - Routines with the "v" suffix allow chunks to have different sizes
- Global synchronization is available in MPI through a barrier which blocks until all the processes in the process group associated with the communicator call it.

```
- MPI Barrier ( comm )
```

Collective operations are powerful ... use them when you can

Do not implement them from scratch on your own. Think about how you'd implement, for example, a reduction.

It is MUCH harder than you might think.

Outline

- MPI and distributed memory systems
- The Bulk Synchronous Pattern and MPI collective operations
- Introduction to message passing
 - The diversity of message passing in MPI
 - Geometric Decomposition and MPI
 - Concluding Comments

Message passing: Basic ideas and jargon

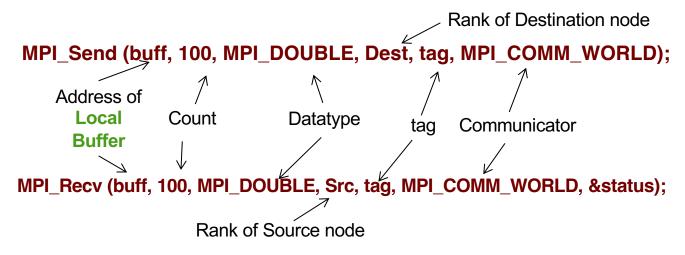
- We need to coordinate the execution of processes ... which may be spread out over a collection of independent computers
- Coordination:
 - 1. Process management (e.g., create and destroy)
 - 2. Synchronization ... timing constraints for concurrent processes)
 - 3. Communication ... Passing a buffer from one machine to another
- A message passing interface builds coordination around messages (either explicitly or implicitly).
- The fundamental (and overly simple) timing model for a message:



Network asymptotic bytes per second

Sending and receiving messages

- Pass a buffer which holds "count" values of MPI_TYPE
- The data in a message to send or receive is described by a triple:
 - (address, count, datatype)
- The receiving process identifies messages with the double :
 - (source, tag)
- Where:
 - Source is the rank of the sending process
 - Tag: a user-defined int to keep track of different messages from a single source



Sending and Receiving messages: More Details

MPI_Status is a variable that contains information about the message that is received. We can use it to find out information about the received message. The most common usage is to find out how many items were in the message:

```
MPI_Status MyStat; int count; float buff[4]; int ierr = MPI_Recv(buf, 4, MPI_FLOAT, 2, 0, MPI_COMM_WORLD, &MyStat); // receive from node=2 with message tag = 0 If(ierr == MPI_SUCCESS) MPI_Get_Count(MyStat, MPI_FLOAT, &count);
```

For messages of a known size, we typically ignore the status, in which case use the parameter MPI_STATUS_IGNORE

int ierr = MPI_Recv(&buf, 4, MPI_FLOAT, 2, 0, MPI_COMM_WORLD, MPI_STATUS_IGNORE);

Sending and Receiving messages: More Details

MPI_Status is a variable that contains information about the message that is received. The received message. The most common usage is to find out how many items were in

C language comments:

- void* says the argument can take a
 pointer to any type. The C compiler
 won't do any type checking ... it just
 needs a valid address to a block of
 memory.
- A type with a * means the function expects a pointer to that type. So I would declare a variable as MPI_Status MyStat and then put the variable in the function call with an ampersand (&) ... for example &MyStat

```
MPI_Status MyStat; int count; float buff[4]; int ierr = MPI_Recv(buf, 4, MPI_FLOAT, 2, 0, MPI_COMM_WORLD, &MyStat); // receive from node=2 with message tag = 0 If(ierr == MPI_SUCCESS) MPI_Get_Count(MyStat, MPI_FLOAT, &count);
```

For messages of a known size, we typically ignore the status, in which case use the parameter MPI_STATUS_IGNORE

int ierr = MPI_Recv(&buf, 4, MPI_FLOAT, 2, 0, MPI_COMM_WORLD, MPI_STATUS_IGNORE);

MPI Data Types for C

MPI Data Type	C Data Type
MPI_BYTE	
MPI_CHAR	signed char
MPI_DOUBLE	double
MPI_FLOAT	float
MPI_INT	int
MPI_LONG	long
MPI_LONG_DOUBLE	long double
MPI_PACKED	
MPI_SHORT	short
MPI_UNSIGNED_SHORT	unsigned short
MPI_UNSIGNED	unsigned int
MPI_UNSIGNED_LONG	unsigned long
MPI_UNSIGNED_CHAR	unsigned char

MPI defines predefined data types that must be specified when passing messages.

What about C++?

- MPI used to have a C++ interface.
- The MPI forum, however, deprecated that interface.
 - It did not add much value compared to using the C interface in C++.
 - Supporting another language in the MPI specification adds a huge amount of work.
- The major challenge in moving between C++ and C is how to handle buffers when your arrays use std::vector or std::array.
- The following should work* (I haven't fully tested these options):

```
vector<float> a(25);
MPI_Send(a.data(), 25, MPI_FLOAT, ...)
MPI_Send( &a[0], 25, MPI_FLOAT, ...)
MPI_Send( &a.front(), 25, MPI_FLOAT, ...)
```

You cannot send from an iterator Let recv determine size/capacity.

Exercise: Ping-Pong Program Time_{communication} = latency + N_{bytes}/bandwidth

Goal

Network fixed costs plus overheads

Network asymptotic bytes per second

 Measure the time to communicate a small message between nodes. Compare on-node vs between-node latencies

Program

- Write a program to bounce a messages (a single value) between a pair of processes. Bounce the message back and forth multiple times and report the average one-way communication time. Then modify it to handle larger messages and explore communication time as a function of message size.

```
int MPI Send (void* buf, int count, MPI Datatype datatype, int dest, int tag, MPI Comm comm)
int MPI Recv (void* buf, int count, MPI Datatype datatype, int source, int tag,
    MPI Comm comm, MPI Status* status)
MPI STATUS IGNORE
```

```
#include <mpi.h>
int size, rank, argc; char **argv;
MPI Init (&argc, &argv);
MPI Comm rank (MPI COMM WORLD, &rank);
MPI_Comm_size (MPI_COMM_WORLD, &size);
double MPI_Wtime();
MPI_Finalize();
```

MPI Data Type	C Data Type
MPI_DOUBLE	double
MPI_FLOAT	float
MPI_INT	int
MPI_LONG	long

Solution: Ping-Pong Program

```
#include <mpi.h>
#include <stdio.h>
#include <stdlib.h>
#define VAL 42
#define NREPS 10
#define TAG 5
int main(int argc, char **argv) {
 int rank, size;
 double t0:
 MPI_Init(&argc, &argv);
 MPI_Comm_rank(MPI_COMM_WORLD, &rank);
 MPI Comm size(MPI COMM WORLD, &size);
 int bsend = VAL;
 int brecv = 0:
 MPI Status stat;
 MPI Barrier(MPI COMM WORLD);
 if(rank == 0) t0 = MPI Wtime();
```

```
for(int i=0;i<NREPS; i++){
 if(rank == 0){
   MPI_Send(&bsend, 1, MPI_INT, 1, TAG, MPI_COMM_WORLD);
   MPI Recv(&brecv, 1, MPI INT, 1, TAG, MPI COMM WORLD, &stat);
   if(brecv != VAL)printf("error: interation %d %d != %d\n",i,brecv,VAL);
   brecv = 0:
 else if(rank == 1){
   MPI Recv(&brecv, 1, MPI INT, 0, TAG, MPI COMM WORLD, &stat);
   MPI_Send(&bsend, 1, MPI_INT, 0, TAG, MPI_COMM_WORLD);
   if(brecv != VAL)printf("error: interation %d %d != %d\n",i,brecv,VAL);
   brecv = 0:
if(rank == 0){
 double t = MPI Wtime() - t0;
 double lat = t/(2*NREPS);
 printf(" lat = %f seconds\n",(float)lat);
MPI Finalize();
```

Ping Pong for different message sizes ... but first a bit of C

• Input parameters from the command line (so you don't need to recompile for each case):

```
Argc → number of command line arguments
int main(int argc, char **argv)
                                          **argv → Pointer to a set of strings
      if (argc == 3){
                                                  Argc == 3 \rightarrow the executable Plus two args
          int msg size = atoi(*++argv);
                                                  *++argy → increment to point to next string
          int num pings = atoi(*++argv);
                                                  atoi() → converts a string to an int
      else{
          int msg size = 1;
                                       Define a default case for when skipped command line are omitted
          int num pings = 10;
```

• Allocate memory and initialize buffer (i.e., a dynamic array of doubles)

```
double *msg = (double*)malloc(msg_size*sizeof(double));
for(int i; i<msg_size; i++) msg[i] = (double) i;</pre>
```

Malloc allocates memory as a void*. Cast to the desired type

Msg is a pointer but we treat it like an array

Working with command line arguments

MPI Finalize();

- You typically need to do some processing of command line arguments before proceeding with a computation.
- The common pattern is to pick a node to do that work and then broadcast the results to the other nodes before proceeding.

```
#include <mpi.h>
int main(int argc, char **argv) {
 int rank, size, param;
 double t0:
 MPI Init(&argc, &argv);
 MPI Comm rank(MPI COMM WORLD, &rank);
 MPI Comm size(MPI COMM WORLD, &size);
 if(my ID == 0){
  if (argc == 2){
      param = atoi(*++argv);
      if(param%2 == 0) param += 1; // if odd, make param even
  else {
     param = 5;
                                                             Broadcast one
```

MPI Bcast (¶m, 1, MPI INT, 0, MPI COMM WORLD);

// now do the computation (not shown).

MPI_INT from node 0 to all other nodes

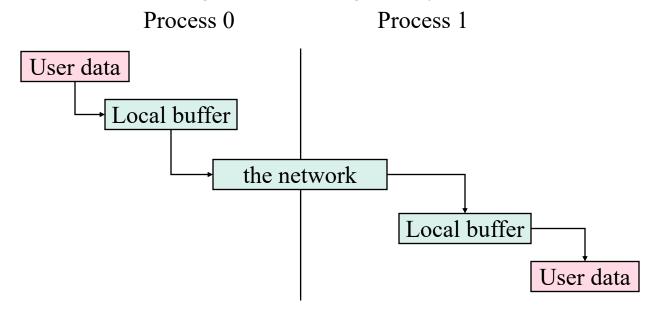
value of

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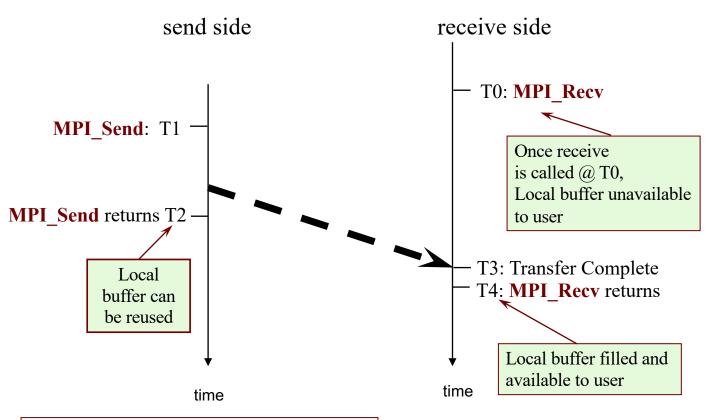
Buffers

- Message passing is straightforward, but there are subtleties
 - Buffering and deadlock
 - Deterministic execution
 - Performance
- When you send data, where does it go? The following is the typical flow:



Blocking Send-Receive Timing Diagram

(Receive before Send)



It is important to post the receive before sending, for highest performance.

Exercise: Ring program

- Start with the basic ring program we provide. Compile as:
 - > mpicc ring.c ring_naive.c
- Study the code (ring.c and ring_naive.c) and note how I manage the computation of where the message goes to and where it comes from for each node.
- Run it for a range of message sizes and notes what happens for large messages.

```
double *buff; int buff_count, to, from, tag=3; MPI_Status stat;

MPI_Recv (buff, buff_count, MPI_DOUBLE, from, tag, MPI_COMM_WORLD, &stat);
MPI_Send (buff, buff_count, MPI_DOUBLE, to, tag, MPI_COMM_WORLD);
```

Sources of Deadlocks

- Send a large message from process 0 to process 1
 - If there is insufficient storage at the destination NIC (Network Interface Unit), the send must wait for the user to provide the memory space (through a receive) to drain buffers inside the NIC
- What happens with this code?

Process 0	Process 1
Send(to 1)	Send(to 0)
Recv(from 1)	Recv(from 0)

 This code could deadlock ... it depends on the availability of system buffers in which to store the data sent until it can be received

Some Solutions to the "deadlock" Problem

• Order the operations more carefully:

Process 0	Process 1
Send(1)	Recv(0)
Recv(1)	Send(0)

• Use a collective "swap" so buffers created when the communication operation is posted:

Process 0	Process 1
Sendrecv(1)	Sendrecv(0)

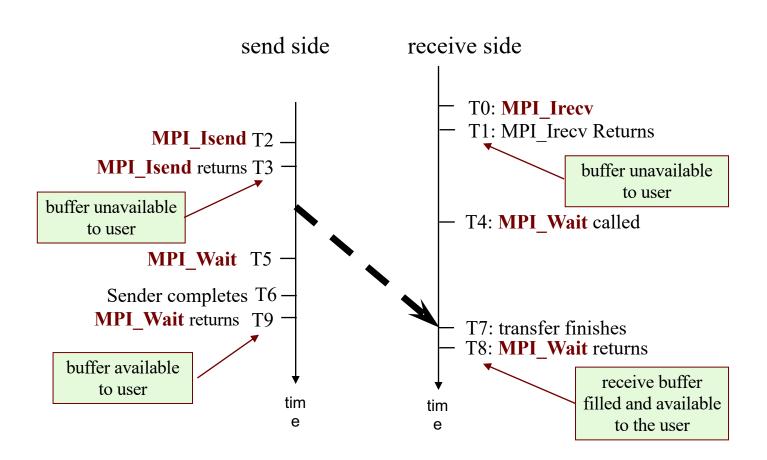
Non-Blocking Communication

- Non-blocking operations return immediately and pass "request handles" that can be waited on and queried
 - MPI_Isend(start, count, datatype, dest, tag, comm, request)
 - MPI_Irecv(start, count, datatype, src, tag, comm, request)
 - MPI_Wait(request, status)
- One can also test without waiting using MPI TEST
 - MPI_Test(request, flag, status)
- Anywhere you use MPI_Send or MPI_Recv, you can use the pair of MPI_Isend/MPI_Wait or MPI_Irecv/MPI_Wait
- Note the MPI types:

```
MPI_Status status;  // type used with the status output from recv
MPI_Request request; // the type of the handle used with isend/ircv
```

Non-blocking operations are extremely important ... they allow you to overlap computation and communication.

Non-Blocking Send-Receive Diagram



Exercise: Ring program

- Start with the basic ring program you wrote.
 - Using blocking Send/Recv, It may deadlock if the network stalls due to there being no place to put a message (i.e. no receives in place so the send blocking on when its buffer can be reused hangs).
- Make it more stable for large messages by:
 - Split-phase ... half the nodes "send than receive" while the other half "receive then send".
 - Sendrecy ... a collective communication send/receive.
 - Isend/Irecv ... nonblocking send receive

Example: shift messages around a ring (part 1 of 2)

```
#include <stdio.h>
#include <mpi.h>
int main(int argc, char **argv)
 int num, rank, size, tag, next, from;
 MPI Status status1, status2;
 MPI Request req1, req2;
 MPI Init(&argc, &argv);
 MPI Comm rank( MPI COMM WORLD, &rank);
 MPI Comm size(MPI COMM WORLD, &size);
 tag = 201;
 next = (rank+1) % size;
 from = (rank + size - 1) % size;
 if (rank == 0) {
  printf("Enter the number of times around the ring: ");
  scanf("%d", &num);
  printf("Process %d sending %d to %d\n", rank, num, next);
  MPI Isend(&num, 1, MPI INT, next, tag,
                           MPI COMM WORLD, & req1);
  MPI Wait(&reg1, &status1);
```

```
do {
 MPI Irecv(&num, 1, MPI INT, from, tag,
                           MPI COMM WORLD, &req2);
 MPI Wait(&reg2, &status2);
 if (rank == 0) {
   num--:
   printf("Process 0 decremented number\n");
 printf("Process %d sending %d to %d\n", rank, num, next);
 MPI Isend(&num, 1, MPI INT, next, tag,
                           MPI COMM WORLD, &req1);
 MPI Wait(&req1, &status1);
} while (num != 0);
if (rank == 0) {
 MPI Irecv(&num, 1, MPI INT, from, tag,
                           MPI COMM WORLD, &reg2);
 MPI Wait(&req2, &status2);
MPI Finalize();
return 0;
```

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Example: finite difference methods

- Solve the heat diffusion equation in 1 D:
 - u(x,t) describes the temperature field
 - We set the heat diffusion constant to one
 - Boundary conditions, constant u at endpoints.
 - map onto a mesh with stepsize h and k

 Central difference approximation for spatial derivative (at fixed time)

■ Time derivative at t = tⁿ⁺¹

$$\frac{\partial^2 u}{\partial x^2} = \frac{\partial u}{\partial t}$$

$$x_i = x_0 + ih \qquad t_i = t_0 + ik$$

$$\frac{\partial^2 u}{\partial x^2} = \frac{u_{j+1} - 2u_j + u_{j-1}}{h^2}$$

$$\frac{du}{dt} = \frac{u^{n+1} - u^n}{k}$$

Example: Explicit finite differences

Combining time derivative expression using spatial derivative at t = tⁿ

$$\frac{u_j^{n+1} - u_j^n}{k} = \frac{u_{j+1}^n - 2u_j^n + u_{j-1}^n}{h^2}$$

Solve for u at time n+1 and step j

$$u_{j}^{n+1} = (1-2r)u_{j}^{n} + ru_{j-1}^{n} + ru_{j+1}^{n}$$

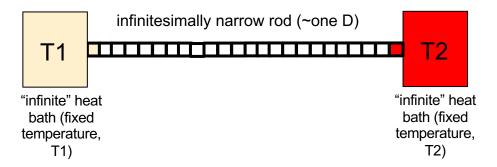
$$r = k/h^{2}$$

■ The solution at $t = t_{n+1}$ is determined explicitly from the solution at $t = t_n$ (assume u[t][0] = u[t][N] = Constant for all t).

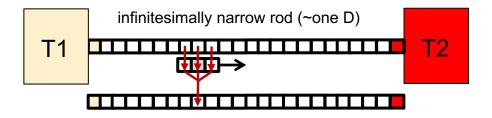
```
for (int t = 0; t < N_STEPS-1; ++t)
  for (int x = 1; x < N-1; ++x)
      u[t+1][x] = u[t][x] + r*(u[t][x+1] - 2*u[t][x] + u[t][x-1]);</pre>
```

■ Explicit methods are easy to compute ... each point updated based on nearest neighbors. Converges for r<1/2.

Heat Diffusion equation

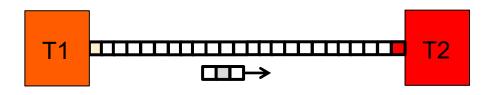


Heat Diffusion equation

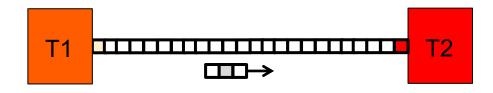


Pictorially, you are sliding a three point "stencil" across the domain (u[t]) and computing a new value of the center point (u[t+1]) at each stop.

Heat Diffusion equation



```
int main()
                                                             Note: I don't need the
                                                           intermediate "u[t]" values
   double *u = malloc (sizeof(double) * (N));
                                                         hence "u" is just indexed by x.
   double *up1 = malloc (sizeof(double) * (N));
   initialize data(uk, ukp1, N, P); // initialize, set end temperatures
   for (int t = 0; t < N_STEPS; ++t){
      for (int x = 1; x < N-1; ++x)
          up1[x] = u[x] + (k / (h*h)) * (u[x+1] - 2*u[x] + u[x-1]);
                                                   A well known trick with 2 arrays so I
      femp = up1; up1 = u; u = temp;
                                                   don't overwrite values from step k-1
                                                   as I fill in for step k
return 0;
```



```
int main()
                                                      How would you
  double *u = malloc (sizeof(double) * (N));
                                                      parallelize this program?
  double *up1 = malloc (sizeof(double) * (N));
  initialize data(uk, ukp1, N, P); // initialize, set end temperatures
  for (int t = 0; t < N_STEPS; ++t){
     for (int x = 1; x < N-1; ++x)
         up1[x] = u[x] + (k / (h*h)) * (u[x+1] - 2*u[x] + u[x-1]);
     temp = up1; up1 = u; u = temp;
return 0;
```

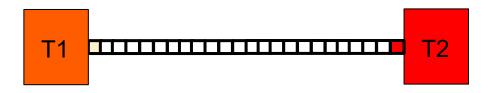
Exercise: Parallel heat diffusion

Goal

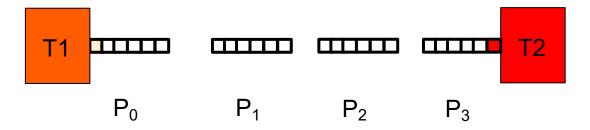
- Parallelize the heat diffusion code (MPI_Exercises/heat-eqn-seq.c) with OpenMP ... should be a quick and easy way to familiarize yourself with the code.
- As you do this, think about how you might parallelize this with MPI

```
#pragma omp parallel
#pragma omp for
#pragma omp critical
#pragma omp single
#pragma omp barrier
int omp_get_num_threads();
int omp_get_thread_num();
```

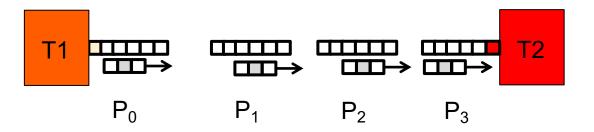
 Start with our original picture of the problem ... a one dimensional domain with end points set at a fixed temperature.



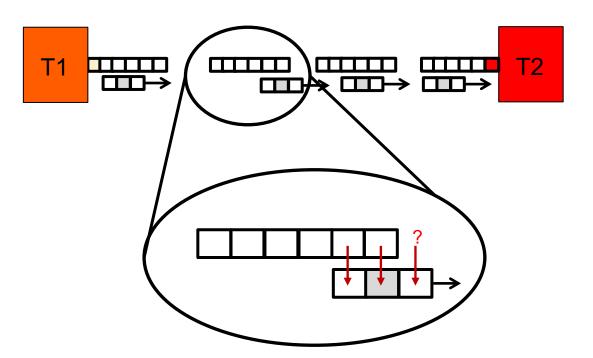
• Break it into chunks assigning one chunk to each process.

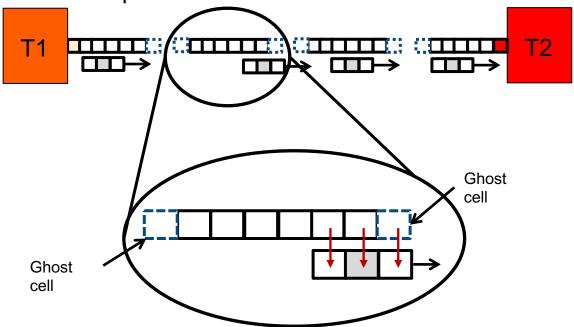


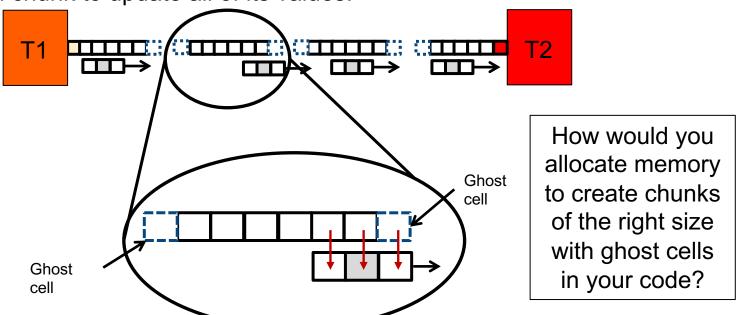
• Each process works on it's own chunk ... sliding the stencil across the domain to updates its own data.

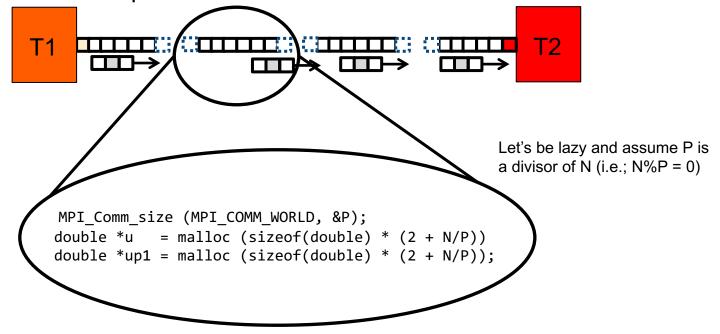


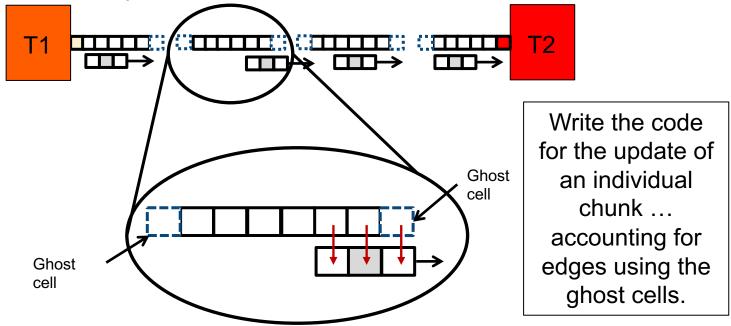
 What about the ends of each chunk ... where the stencil will run off the end and hence have missing values for the computation?











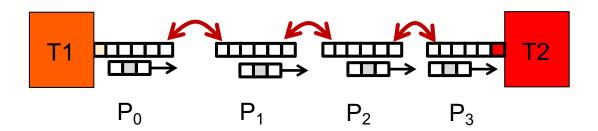
Heat Diffusion MPI Example: Updating a chunk

```
// Compute interior of each "chunk"
                                               Update array values using local data
                                                   and values from ghost cells.
  for (int x = 2; x < N/P; ++x)
    up1[x] = u[x] + (k / (h*h)) * (u[x+1] - 2*u[x] + u[x-1]);
// update edges of each chunk keeping the two far ends fixed
// (first element on Process 0 and the last element on process P-1).
  if (mvID != 0)
    up1[1] = u[1] + (k / (h*h)) * (u[1+1] - 2*u[1] + u[1-1]);
                                                                       u[0] and u[N/P+1] are
                                                                          the ghost cells
  if (myID != P-1)
    up1[N/P] = u[N/P] + (k/(h*h)) * (u[N/P+1] - 2*u[N/P] + u[N/P-1]);
// Swap pointers to prepare for next iterations
  temp = up1; up1 = u; u = temp;
                                              Note I was lazy and assumed N was
} // End of for (int t ...) loop
                                              evenly divided by P. Clearly, I'd never
                                                  do this in a "real" program.
MPI_Finalize();
```

return 0;

Heat Diffusion MPI Example: Communication

• Each process works on it's own chunk ... sliding the stencil across the domain to updates its own data.



Try to write the code for this communication pattern.

Heat Diffusion MPI Example

```
Note: the edges of domain are held at a fixed temperature.
MPI Init (&argc, &argv);

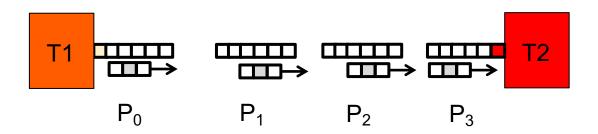
    Node 0 has no neighbor to the left

MPI Comm size (MPI COMM WORLD, &P);

    Node P has no neighbor to its right

MPI Comm rank (MPI COMM WORLD, &myID);
double *u = malloc (sizeof(double) * (2 + N/P)) // include "Ghost Cells" to hold
double *up1 = malloc (sizeof(double) * (2 + N/P)); // values from my neighbors
initialize data(uk, ukp1, N, P);
for (int t = 0; t < N STEPS; ++t){
                                                     Send my "left" boundary value to the neighbor on my "left"
  if (myID != 0) MPI_Send (&u[1], 1, MPI_DOUBLE, myID-1, 0, MPI_COMM_WORLD);
                                                     Receive my "right" ghost cell from the neighbor to my "right"
  if (myID != P-1) MPI_Recv (&u[N/P+1], 1, MPI_DOUBLE, myID+1, 0, MPI_COMM_WORLD, &status);
                                                     Send my "right" boundary value to the neighbor to my "right"
  if (myID != P-1) MPI Send (&u[N/P], 1, MPI_DOUBLE, myID+1, 0, MPI_COMM_WORLD);
                                                     Receive my "left" ghost cell from the neighbor to my "left"
  if (myID != 0) MPI Recv (&u[0], 1, MPI DOUBLE, myID-1, 0, MPI COMM WORLD, &status);
```

• Each process works on it's own chunk ... sliding the stencil across the domain to updates its own data.



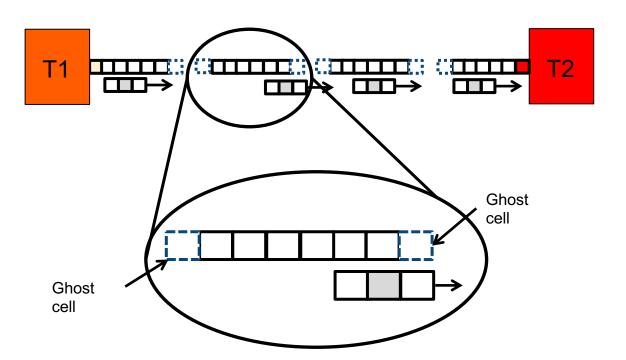
We now put all the pieces together for the full program

Heat Diffusion MPI Example

```
MPI Init (&argc, &argv);
MPI Comm size (MPI_COMM_WORLD, &P);
MPI Comm rank (MPI COMM WORLD, &myID);
double *u = malloc (sizeof(double) * (2 + N/P)) // include "Ghost Cells" to hold
double *up1 = malloc (sizeof(double) * (2 + N/P)); // values from my neighbors
initialize data(uk, ukp1, N, P);
for (int t = 0; t < N STEPS; ++t){
  if (myID != 0) MPI Send (&u[1], 1, MPI DOUBLE, myID-1, 0, MPI COMM WORLD);
  if (myID != P-1) MPI Recv (&u[N/P+1], 1, MPI DOUBLE, myID+1, 0, MPI COMM WORLD, &status);
  if (myID != P-1) MPI Send (&u[N/P], 1, MPI DOUBLE, myID+1, 0, MPI COMM WORLD);
  if (myID != 0) MPI Recv (&u[0], 1, MPI DOUBLE, myID-1, 0,MPI COMM WORLD, &status);
  for (int x = 2; x < N/P; ++x)
    up1[x] = u[x] + (k / (h*h)) * (u[x+1] - 2*u[x] + u[x-1]);
  if (myID != 0)
    up1[1] = u[1] + (k / (h*h)) * (u[1+1] - 2*u[1] + u[1-1]);
  if (myID != P-1)
    up1[N/P] = u[N/P] + (k/(h*h)) * (u[N/P+1] - 2*u[N/P] + u[N/P-1]);
 temp = up1; up1 = u; u = temp;
} // End of for (int t ...) loop
MPI Finalize();
return 0;
```

The Geometric Decomposition Pattern

This is an instance of a very important design pattern ... the Geometric decomposition pattern.



Communicating boundary data

Communicating boundary data was ugly and error prone:

```
if (myID != 0) MPI_Send (&u[1], 1, MPI_DOUBLE, myID-1, 0, MPI_COMM_WORLD);
if (myID != P-1) MPI_Recv (&u[N/P+1], 1, MPI_DOUBLE, myID+1, 0, MPI_COMM_WORLD, &status);
if (myID != P-1) MPI_Send (&u[N/P], 1, MPI_DOUBLE, myID+1, 0, MPI_COMM_WORLD);
if (myID != 0) MPI_Recv (&u[0], 1, MPI_DOUBLE, myID-1, 0, MPI_COMM_WORLD, &status);
```

 The constant MPI_PROC_NULL when used as a to/from parameter in a message passing function causes the function to return with MPI_SUCCESS as soon as it can.

```
MPI_Send (&u[1], 1, MPI_DOUBLE, MPI_PROC_NULL, 0, MPI_COMM_WORLD);
```

Partitioned Arrays

- Realistic problems are 2D or 3D; require more complex data distributions.
- We need to parallelize the computation by partitioning this index space
- Example: Consider a 2D domain over which we wish to solve a PDE using an explicit finite difference solver. The figure shows a five point stencil ... update a value based on its value and its 4 neighbors.
- Start with an array and stencil →

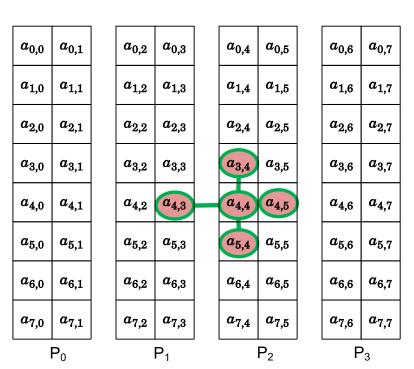
$a_{0,0}$	$a_{0,1}$	$a_{0,2}$	$a_{0,3}$	$a_{0,4}$	$a_{0,5}$	$a_{0,6}$	$a_{0,7}$
$a_{1,0}$	$a_{1,1}$	$a_{1,2}$	$a_{1,3}$	$a_{1,4}$	$a_{1,5}$	$a_{1,6}$	$a_{1,7}$
$a_{2,0}$	$a_{2,1}$	$a_{2,2}$	$a_{2,3}$	$a_{2,4}$	$a_{2,5}$	$a_{2,6}$	$a_{2,7}$
$a_{3,0}$	$a_{3,1}$	$a_{3,2}$	$a_{3,3}$	a _{3,4}	$a_{3,5}$	$a_{3,6}$	$a_{3,7}$
$a_{4,0}$	$a_{4,1}$	$a_{4,2}$	$a_{4,3}$	$a_{4,4}$	$a_{4,5}$	$a_{4,6}$	$a_{4,7}$
$a_{5,0}$	$a_{5,1}$	$a_{5,2}$	$a_{5,3}$	$a_{5,4}$	$a_{5,5}$	$a_{5,6}$	$a_{5,7}$
$a_{6,0}$	$a_{6,1}$	$a_{6,2}$	$a_{6,3}$	$a_{6,4}$	$a_{6,5}$	$a_{6,6}$	$a_{6,7}$
$a_{7,0}$	$a_{7,1}$	$a_{7,2}$	$a_{7,3}$	$a_{7,4}$	$a_{7,5}$	$a_{7,6}$	$a_{7,7}$

Partitioned Arrays: Column block distribution

- Split the non-unit-stride dimension (P-1) times to produce P chunks, assign the ith chunk to $P_{i.}$ To keep things simple, assume N%P = 0
- In a 2D finite-differencing program (exchange edges), how much do we have to communicate?
 O(N) values per processor

P is the # of processors

N is the order of our square matrix



Partitioned Arrays: Block distribution

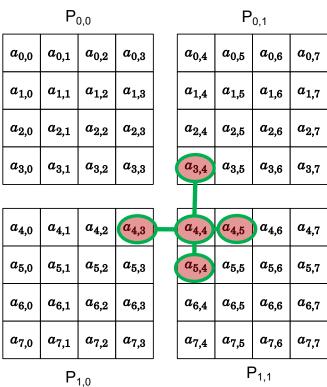
• If we parallelize in both dimensions, then we have $(N/P^{1/2})^2$ elements per processor, and we need to send $O(N/P^{1/2})$ values from each processor. Asymptotically better than O(N).

P is the # of processors

Assume a p by p square mesh ... $p=P^{1/2}$

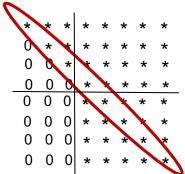
N is the order of our square matrix

Dimension of each block is N/P^{1/2}

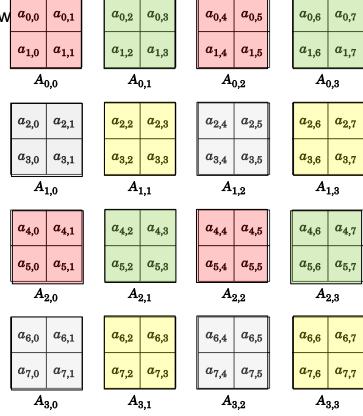


Partitioned Arrays: block cyclic distribution

LU decomposition (A= LU) .. Move down the diagonal transform rows to "zero the column" below the diagonal.

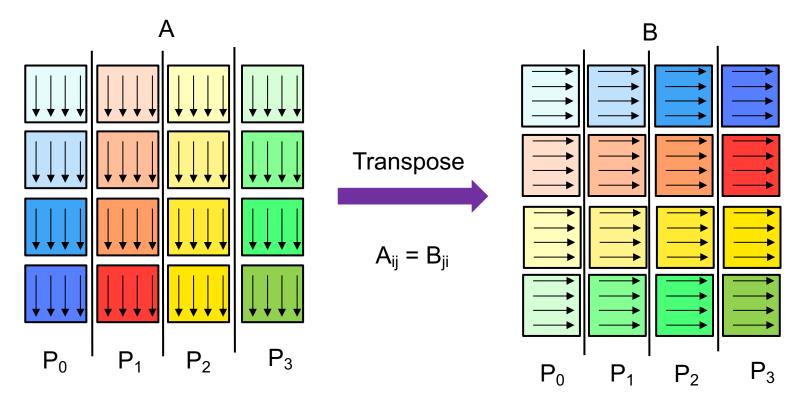


- Zeros fill in the right lower triangle of the matrix ... less work to do.
- Balance load with cyclic distribution of blocks of A mapped onto a grid of nodes (2x2 in this case ... colors show the mapping to nodes).



Matrix Transpose: Column block decomposition

You can only learn this stuff by doing it so we're going to design an algorithm to transpose a matrix using a partitioned array model based on column blocks.



Let's keep things simple. The order of A and B is N. $N = blk^*P$ where blk is the order of the square subblocks

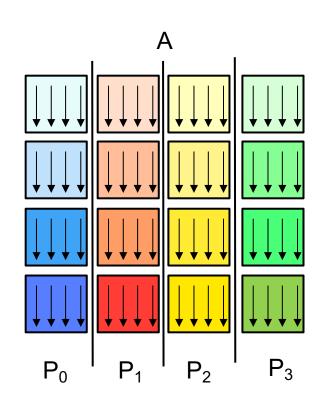
We are going to create a transpose program that uses the SPMD pattern.

That's Single Program Multiple Data.

We'll run the same program on each node.

What is the high level structure of this algorithm?

That is ... how will each Processor march through its set of blocks?



Let's keep things simple. N = blk*P where blk is the order of the square subblocks

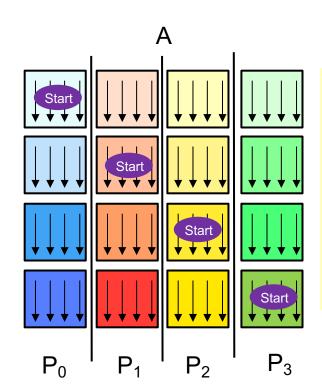
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There is more than one way to do this.

Since its an SPMD program, you want a symmetric path through the blocks on each processor.

A great approach is for everyone to start from their diagonal and shift down

Phase 0 ... transpose your diagonal

Let's keep things simple. $N = blk^*P$ where blk is the order of the square subblocks

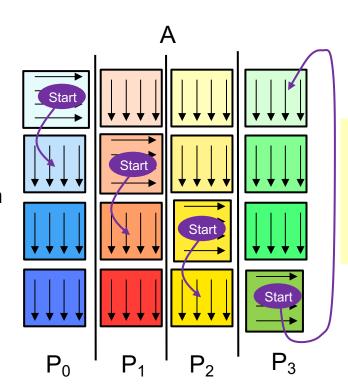
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Shift down (with a circular shift pattern ... i.e. when you run off an edge, wrap around to the opposite edge).

Phase 0 ... transpose your diagonal Phase 1 ... deal with next block "down"

Let's keep things simple. N = blk*P where blk is the order of the square subblocks

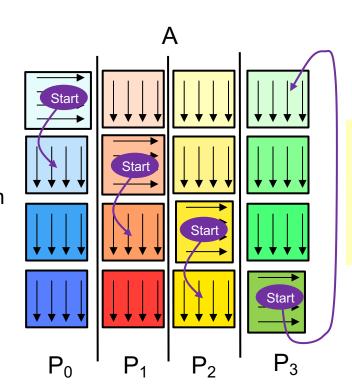
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Shift down (with a circular shift pattern ... i.e. when you run off an edge, wrap around to the opposite edge.

Phase 0 ... transpose your diagonal Phase 1 ... deal with next block "down"

We know the sender ... who receives the block?

Let's keep things simple. N = blk*P where blk is the order of the square subblocks

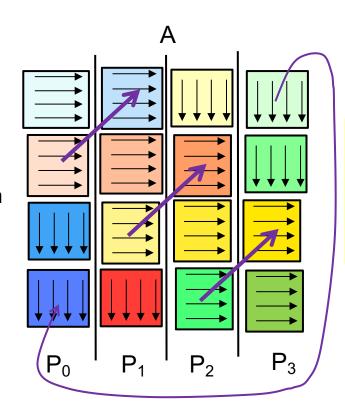
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Phase 0 ... transpose your diagonal Phase 1 ... deal with next block "down"

We know the sender ... who receives the block?

Let's keep things simple. $N = blk^*P$ where blk is the order of the square subblocks

Exercise: Matrix Transpose Program

- Start with the basic transpose program we provide (transpose.c and several trans *.c functions).
 - > mpicc transpose.c trans_utility.c trans_sendrcv.c
- Your task ... deduce a general expression for the sender and receiver (FROM and TO) for each phase.
- Go to trans_sendrcv.c and enter your definitions for the TO and FROM macros (what is there now is wrong ... I just wanted something to show how macros work).
- Test and verify correctness
- Try different message passing approaches.
- Can you overlap the local transpose and the communication between nodes?

Outline

- MPI and distributed memory systems
- The Bulk Synchronous Pattern and MPI collective operations
- Introduction to message passing
- The diversity of message passing in MPI
- Geometric Decomposition and MPI
- Concluding Comments

The 12 core functions in MPI

- MPI_Init
- MPI_Finish
- MPI_Comm_size
- MPI_Comm_rank
- MPI_Send
- MPI_Recv
- MPI_Reduce
- MPI Isend
- MPI_Irecv
- MPI_Wait
- MPI_Wtime
- MPI_Bcast

10

The 12 core functions in MPI

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Real Programmers always try to overlap communication and computation .. Post your receives using MPI_Irecv() then where appropriate, use MPI_Isend().

The 12 core functions in MPI

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- MPI Irecv
- MPI_Wait
- MPI Wtime
- MPI_Bcast

My friends on the MPI forum hate this slide.

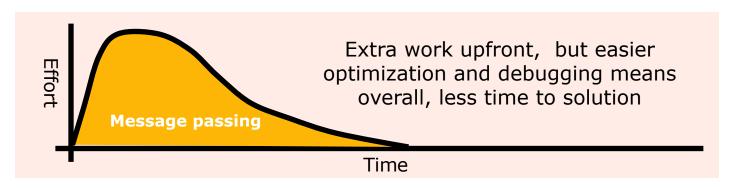
These are indeed the functions most people use, but these date back to MPI 1.5 ... The spec is currently at version 5.0

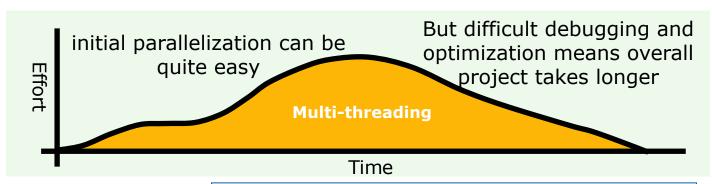
Real Programmers always try to overlap communication and computation .. Post your receives using MPI_Irecv() then where appropriate, use MPI_Isend().

Master these 12 constructs before exploring newer features in MPI. Then learn about:

- Support for mixing MPI and OpenMP
- Topologies
- One-sided communication
- User defined types
- Shared memory programming within MPI (no need for OpenMP)

Does a shared address space make programming easier?

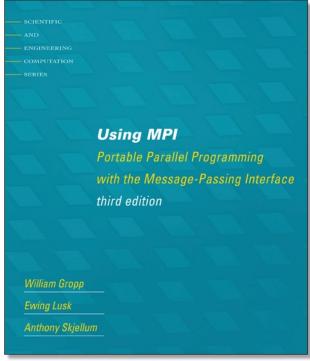


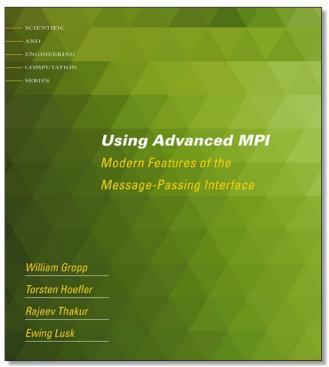


Proving that a shared address space program using semaphores is race free is an NP-complete problem*

MPI References

- The Standard itself at http://www.mpi-forum.org
- Additional tutorial information at http://www.mcs.anl.gov/mpi
- The core reference books:



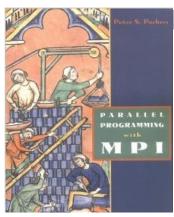


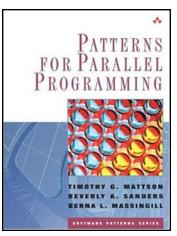
Basic MPI

Advanced MPI, including MPI-3

Additional books to help you master MPI

- Parallel Programming with MPI, by Peter Pacheco, Morgan-Kaufmann, 1997.
 - Only covers MPI 1.0 so it's out of date, but it is a very friendly and gentle introduction.
 - Peter Pacheco is a teacher first and foremost and that shows in the way he organizes the material in this book.
- Patterns for Parallel Programing, by Tim Mattson, Beverly Sanders, and Berna Massingill.
 - Only covers MPI 1.0 so it's out of date.
 - Focusses on how to use MPI, not the structure of the standard itself.
 - Shows how patterns are expressed across MPI, OpenMP, and concurrent Java



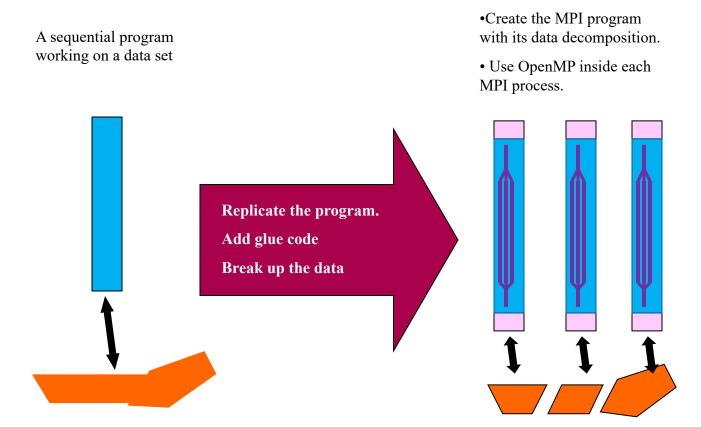


Backup Content

Mixing OpenMP and MPI

Loading MPI on your system

How do people mix MPI and OpenMP?



Pi program with MPI and OpenMP

Get the MPI

add OpenMP

makes sense

part done

first, then

pragma where it

to do so

```
#include <mpi.h>
#include "omp.h"
                                                              For many years, this was
void main (int argc, char *argv[])
                                                               all you needed to do to
                                                               make OpenMP and MPI
     int i, my id, numprocs; double x, pi, step, sum = 0.0;
                                                                    work together.
     step = 1.0/(double) num steps;
     MPI Init(&argc, &argv);
                                                               Don't put MPI calls in a
     MPI Comm Rank(MPI COMM WORLD, &my id);
                                                                 parallel region, and
     MPI Comm Size(MPI COMM WORLD, &numprocs);
                                                                everything just works.
     my steps = num steps/numprocs;
#pragma omp parallel for reduction(+:sum) private(x)
     for (i=my id*my steps; i<(m id+1)*my steps; i++)
                                                               Technically, this doesn't
                                                                   work anymore.
            x = (i+0.5)*step;
            sum += 4.0/(1.0+x*x);
     sum *= step ;
     MPI Reduce(&sum, &pi, 1, MPI DOUBLE, MPI SUM, 0, MPI COMM WORLD);
     MPI Finalize();
```

You must tell MPI at initialization about planned Thread use

• MPI includes a version of MPI_Init() that defines how to handle threads. If you are going to mix threads with MPI, you required to use this new initialization function.

int MPI_Init_thread(int *argc, char **argv, int required, int *provided)

- int *argc: number of values on the command line.
- char ***argv: Pointer to and array of pointers holding the arguments as character strings
- Int MPI threading mode that you require
- Int * provided: a pointer to an int that identifies the thread mode you got.

MPI defines four constants that represent the different thread modes

- 1. MPI_THREAD_SINGLE: Only one thread will execute.
- 2. MPI_THREAD_FUNNELED: The process may be multi-threaded, but only the initial thread will make MPI calls (all MPI calls are funneled to the initial thread).
- 3. MPI_THREAD_SERIALIZED: The process may be multi-threaded, and multiple threads may make MPI calls, but only one at a time: MPI calls are not made concurrently from two distinct threads (all MPI calls are serialized).
- 4. MPI_THREAD_MULTIPLE: Multiple threads may call MPI, with no restrictions.

The 4 constants are ordered integers of type int .. That is Multiple>Serialized>Funneled>Single

Pi program with MPI and OpenMP

```
#include <mpi.h>
#include "omp.h"
void main (int argc, char *argv[])
     int i, my id, numprocs, got; double x, pi, step, sum = 0.0;
     step = 1.0/(double) num steps;
     MPI Init thread(&argc, &argv,MPI THREAD FUNNELED, &got);
     if(got<MPI THREAD FUNNELED) MPI Abort();
                                                            Funneled has never let me
     MPI Comm Rank(MPI COMM WORLD, &my id);
     MPI Comm Size(MPI COMM WORLD, &numprocs);
                                                                      down.
     my steps = num steps/numprocs;
#pragma omp parallel for reduction(+:sum) private(x)
                                                            ... Stil, it is recommended
     for (i=my id*my steps; i<(m id+1)*my steps; i++)
                                                            that you always verify you
                                                             actually got the level of
           x = (i+0.5)*step;
                                                               thread support you
            sum += 4.0/(1.0+x*x);
                                                                    requested
     sum *= step ;
     MPI Reduce(&sum, &pi, 1, MPI DOUBLE, MPI SUM, 0, MPI COMM WORLD);
     MPI Finalize();
```

Hybrid OpenMP/MPI works, but is it worth it?

- Literature* is mixed on the hybrid model: sometimes its better, sometimes MPI alone is best.
- There is potential for benefit to the hybrid model
 - MPI algorithms often require replicated data making them less memory efficient.
 - Fewer total MPI communicating agents means fewer messages and less overhead from message conflicts.
 - Algorithms with good cache efficiency should benefit from shared caches of multi-threaded programs.
 - The model maps perfectly with clusters of SMP nodes.
- But really, it's a case by case basis and to large extent depends on the particular application.

Backup Content

Mixing OpenMP and MPI



Use homebrew to install gnu compilers on your Apple laptop

I tested this on a new (July 2023) MacBook Air with an Apple M2 CPU

Warning: by default Xcode usese the name gcc for Apple's clang compiler.

Use Homebrew to load a real, gcc compiler.

 Go to the homebrew web site (brew.sh). Cut and paste the command near the top of the page to install homebrew (in /opt/homebrew):

/bin/bash -c "\$(curl -fsSL https://raw.githubusercontent.com/Homebrew/install/HEAD/install.sh)"

Add /opt/homebrew/bin to your path. I did this by adding the following line to .zshrc

% export PATH=/opt/homebrew/bin:\$PATH

Install the latest gcc compiler

% brew install gcc

- This will install the compiler in /opt/homebrew/bin. Check /opt/homebrew/bin to see which gcc compiler was installed. In my case, it installed gcc-13
- Test the compiler (and the openmp option) with a simple hello world program

% gcc-13 -fopenmp hello.c

OpenMP and MPI on Apple Laptops: MacPorts

I have not tested this in a long time.
I greatly prefer homebrew.

But if you prefer MacPorts, this procedure should work.

- To use OpenMP and MPI on your Apple laptop:
- Download Xcode. Be sure to choose the command line tools that match your OS.
- Download and use MacPorts to install the latest gnu compilers.

sudo port selfupdate	Update to latest version of MacPorts		
sudo port install gcc14	Grab version 13 gnu compilers		
port selectlist gcc	List versions of gcc on your system		
sudo port selectset gcc mp-gcc14	Select the mp enabled version of the most recent gcc release		
sudo port install mpich-gcc14	Grab the library that matches the version of your gcc compiler.		
mpicc -fopenmp hello.c	Test the installation with a simple program		
mpiexec -n 4 ./a.out			

MPIch library on Apple Laptops: MacPorts

- To use MPI on your Apple laptop:
 - Download Xcode. Be sure to choose the command line tools that match your OS.
 - Install MacPorts (if you haven't already ... use the installer for your OS from macports.org).

sudo port selfupdate

sudo port install mpich-gcc9

mpicc hello.c
mpiexec -n 4 ./a.out

Update to latest version of MacPorts

Grab the library that matches the version of your gcc compiler.

Test the installation with a simple program