

Exercise for chapter 4 (Part 1) Automata

1 Introduction

In this exercise, we will be familiar with some basic concepts and definitions in automata: language, regular expression, finite automata and NFA (nondeterministic finite automata). Students should review the slide and related documents for chapter 4 before doing the exercises below.

2 Exercises with solution

Question 1.

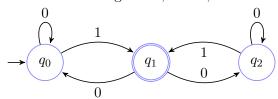
Let $\Sigma = \{a, b\}$ and $L = \{ab, aa, baa\}$.

Which of the following strings are in L^* : abaabaaabaa, aaaabaaaa, baaaaabaaaab, baaaaabaa? Solution.

abaabaaabaa, aaaabaaaa, baaaaabaa

Question 2.

Which of the strings 0001, 01001, 0000110 are accepted by the following automata:

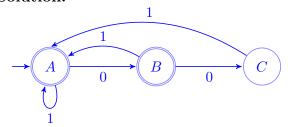


Solution.

 $0001,\,01001$

Question 3.

Consider the set of strings on $\{0,1\}$ in which every 00 is followed immediately by 1. For example 101, 0010, 0010011001 are in the language, but 0001 and 00100 are not. Construct an accepting automata. Solution.



3 Homework

Question 4.

Let $\Sigma = \{a, b\}.$

Find all strings in $L = ((a+b)^*b(a+ab)^*)$ of length less than four.

Question 5.

Let $\Sigma = \{a, b\}.$

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For which language it is true that $L = L^*$?

a)
$$L = a^n b^{n+1} : n \ge 0$$

b)
$$L = w : n_a(w) = n_b(w)$$

Question 6.

Give a finite automata for the language $L = \{a, ba, aba, bab, bbba\}$.

Question 7.

Let $\Sigma = \{a\}$. Give finite automata for the sets consisting of

- a) all strings with exactly one a.
- b) all strings with no more than three a's.

Question 8.

Let $\Sigma = \{a, b\}.$

Give finite automata for the sets consisting of

- a) all strings with exactly one a.
- b) all strings with no more than three a's.

Question 9.

Let $\Sigma = \{a, b, c\}$. Give finite automata for the sets consisting of

- a) all strings with exactly one a.
- b) all strings with no more than three a's.
- c) all strings with no more than three a's and at least one b.

Question 10.

Give an automata for the language $L = \{ab^5wb^4 : w \in \{a, b\}^*\}.$

Question 11.

Find automatas for the following languages on $\Sigma = \{a, b\}$

a)
$$L_1 = \{w : |w| \mod 3 = 0\}$$

b)
$$L_2 = \{w : |w| \mod 5 \neq 0\}$$

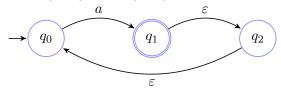
c)
$$L_3 = \{w : n_a(w) \mod 3 > 1\}$$

Question 12.

Show that the language $L = a^n : n \ge 0, n \ne 4$ is regular.

Question 13.

Find $\delta^*(q_0, a)$ and $\delta^*(q_1, \varepsilon)$ for the following automata

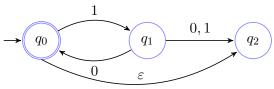


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Question 14.

For the following automata, find $\delta^*(q_0, 1010)$ and $\delta^*(q_1, 00)$.



Question 15.

Find an automata with three states that accepts the language $\{ab, abc\}^*$

Question 16.

Let $\Sigma = \{a, b, c\}$.

Give complet automatas for the sets consisting of

- a) all strings with exactly one 'a'.
- b) all strings of even length.
- c) all strings which the number of appearances of 'b' is divisible by 3.
- d) all strings ending with 'a'.
- e) all strings not ending with 'a'.
- f) all non-empty strings not ending with 'a'.
- g) all strings with at least one 'a'.
- h) all strings with at most one 'a'.
- i) all strings without any 'a'.
- i) all strings including at least one a and whose the first appearance of 'a' is not followed by a 'c'.

Complet automata: a finite automata in which from each state, it is defined precisely when receiving any event.

Question 17.

Hãy vẽ sơ đồ biểu diễn hoạt động giao dịch tại một chi nhánh ngân hàng, biết rằng các hoạt động giao dịch như sau:

- a) lấy số thứ tự hàng chờ để giao dịch hoặc nhờ một trong hai quầy tư vấn riêng $(A_1 \text{ và } A_2)$.
- b) Quầy A_1 dùng để phục vụ đóng/mở tài khoản giao dịch hoặc tài khoản thẻ cho khách hàng.
- c) Quầy A_2 dùng để xử lý sự cố, như là mất thẻ ATM, bị máy ATM nuốt thẻ, giao dịch online bị lỗi, ...
- d) Ngân hàng có 2 loại giao dịch: nội tệ và ngoại tệ.
- e) Chi nhánh có 3 quầy giao dịch nội tệ B, C, D và 1 quầy giao dịch ngoại tệ E.
- f) Người khách hàng sau khi giao dịch ngoại tệ, vẫn có thể tiếp tục giao dịch nội tệ. Trường hợp đó, anh ta sẽ được ưu tiên chuyển đến quầy giao dịch D mà không cần lấy số thứ tự lại.
- g) Khách hàng sau khi thực hiện giao dịch nội tệ và kiển tra, xác nhận giao dịch thành công, sẽ ra về. Trường hợp có trực trặc, sẽ được chuyển sang quầy đặc biệt A_2 để xử lý sự cố.

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